

Also, $\{0\} \subseteq U+W$ since $U+W$ is a subspace.

Thus $U+W = \{0\}$.