

► Define  $W = \text{span}\{v_1, \dots, v_m\}$ . \*\*

► We want to show  $v_1, \dots, v_m$  is basis of  $W$ ; ie  $v_1, \dots, v_m$  is linearly indep.

Suppose there exists  $a_1, \dots, a_m$

not all are zero such that

$$a_1 v_1 + \dots + a_m v_m = 0,$$

then

$$a_1 v_1 + U + \dots + a_m v_m + U$$

$$= (a_1 v_1 + \dots + a_m v_m) + U$$

$$= 0 + U$$

$$= 0_{U/U}$$