

b) Recall:

From Q9. suppose  $v_1, \dots, v_n$  is basis of  $V$ ,

and  $\varphi_1, \dots, \varphi_n$  is dual basis. then for any

$\psi \in V'$ ,

$$\psi = \psi(v_1)\varphi_1 + \dots + \psi(v_n)\varphi_n$$

► Analogously,  $e_1, e_2, e_3$  is a basis of  $\mathbb{R}^3$ ,

and  $\psi_1, \psi_2, \psi_3$  is the dual basis. Then

for  $T'(\varphi_1), T'(\varphi_2) \in (\mathbb{R}^3)'$ , ( $T': \mathbb{R}^3 \rightarrow \mathbb{R}^3$ )

$$T'(\varphi_1) = T'(\varphi_1)(e_1)\psi_1 + T'(\varphi_1)(e_2)\psi_2 + T'(\varphi_1)(e_3)\psi_3$$

①

$$T'(\varphi_2) = T'(\varphi_2)(e_1)\psi_1 + T'(\varphi_2)(e_2)\psi_2 + T'(\varphi_2)(e_3)\psi_3$$

②