```
# Step 1: Import Packages and classes
import sqlite3
import pandas as pd
import numpy as np
from sklearn.linear_model import LinearRegression
import matplotlib.pyplot as plt
from matplotlib import style
%matplotlib inline
# Step 2:
# Provide data from the tables
con = sqlite3.connect('cba log rv .sqlite')
# log rv Table: log realised variance (RV) of CBA
# This is the dependent variable
rv data = pd.read sql query('SELECT * FROM log rv',con)
print(rv data)
            date
                    log rv
0
      2003-01-07 -0.195388
1
      2003-01-08 -0.779210
2
      2003-01-09 -0.196713
3
      2003-01-10 0.067592
4
      2003-01-13 -0.838226
4694 2021-08-16 -0.271400
4695 2021-08-17 -0.413196
4696 2021-08-18 -0.151205
     2021-08-19 -0.295768
4697
4698 2021-08-20 -0.661106
[4699 \text{ rows } x \text{ 2 columns}]
# log rv feature: log RV based features
f_data = pd.read_sql_query('SELECT * FROM log_rv feature', con)
print(f data)
            date log rv lag1 log rv avg5 log rv avg22
log rv avg253
      2003-01-07
                    -0.741694
                                 -0.449644
                                               -0.515572
0.367086
      2003-01-08
                    -0.195388
                                 -0.545231
                                               -0.521978
0.365305
      2003-01-09
                    -0.779210
                                 -0.463997
                                               -0.551932
0.365947
      2003-01-10
                    -0.196713 -0.436124
                                               -0.567596
0.363599
      2003-01-13
                     0.067592
                                 -0.369083
                                               -0.543945
0.359683
```

```
. . .
4694 2021-08-16
                      0.017612
                                  -0.159335
                                                 -0.630536
0.297995
                     -0.271400
4695
     2021-08-17
                                  -0.149591
                                                 -0.598307
0.299752
4696 2021-08-18
                     -0.413196
                                   -0.058005
                                                 -0.583753
0.300944
4697 2021-08-19
                     -0.151205
                                  -0.162366
                                                 -0.578148
0.302293
4698 2021-08-20
                     -0.295768
                                  -0.222792
                                                 -0.581853
0.304542
      log_rv_up
0
              0
1
              0
2
              0
3
              0
4
              0
4694
              0
4695
              0
4696
              0
4697
              0
4698
              0
[4699 rows x 6 columns]
# rng feature: Range based features
rng data = pd.read sql query('SELECT * FROM rng feature', con)
print(rng data)
                 rng lag1
                                        rng avg22
                             rng avg5
                                                  rng avg253
            date
                                                                rng_up
                  0.323813
0
      2003-01-07
                             0.607873
                                         0.553536
                                                     0.703900
                                                                     0
1
      2003-01-08 0.685980 0.524683
                                         0.544489
                                                     0.705035
                                                                     0
2
      2003-01-09
                  0.398439
                             0.523289
                                         0.535820
                                                     0.704763
                                                                     0
3
      2003-01-10
                  0.795818
                             0.557333
                                         0.537353
                                                     0.705806
                                                                     0
4
      2003-01-13
                  0.614600
                             0.563730
                                         0.537039
                                                     0.706781
                                                                     0
4694
      2021-08-16 0.755281
                             0.755477
                                         0.545684
                                                     0.663862
                                                                     0
4695
      2021-08-17
                  0.788250 0.744859
                                         0.556607
                                                     0.663746
                                                                     0
4696
      2021-08-18 0.633679
                             0.782351
                                         0.563163
                                                     0.664030
                                                                     0
      2021-08-19
4697
                  0.659298
                             0.684340
                                         0.565064
                                                     0.662888
                                                                     0
4698
      2021-08-20
                  0.788937
                             0.725089
                                         0.574249
                                                     0.662476
                                                                     0
[4699 \text{ rows } \times 6 \text{ columns}]
# qtl rng feature: Quantile range based features
qtl data = pd.read sql query('SELECT * FROM qtl rng feature', con)
print(qtl data)
```

```
date qtl rng lag1 qtl rng avg5 qtl rng avg22
qtl rng avg253 \
                                 0.320090
     2003-01-07
                  0.269568
                                               0.304471
0.309980
                    0.361912
     2003-01-08
                                 0.321091
                                               0.307479
0.310409
     2003-01-09
                    0.271133
                                 0.320783
                                               0.303049
0.310296
     2003-01-10
                    0.286407
                                 0.311396
                                               0.297146
0.310441
     2003-01-13 0.434706
                                 0.324745
                                               0.304952
0.311234
                        . . .
                                     . . .
                                                   . . .
4694 2021-08-16
                    0.341765
                                 0.312585
                                               0.261822
0.312503
4695 2021-08-17
                    0.262366
                                 0.311847
                                               0.265213
0.312003
                                               0.268340
4696 2021-08-18
                    0.314158
                                 0.332025
0.311909
4697 2021-08-19 0.339382
                                 0.330446
                                               0.268275
0.311960
4698 2021-08-20
                    0.281104
                                 0.307755
                                               0.267951
0.311475
     qtl_rng_up
0
             0
1
2
3
4
             0
4694
             0
4695
             0
4696
             0
4697
             0
4698
[4699 rows \times 6 columns]
# Lets join the qtl rng feature & log rv feature & rng data
join data0 = pd.merge(qtl data, f data, on='date')
print(join data0)
           date qtl_rng_lag1 qtl_rng_avg5 qtl_rng_avg22
qtl rng avg253 \
    2003-01-07 0.269568
                                 0.320090
                                               0.304471
0.309980
     2003-01-08 0.361912
                                 0.321091
                                               0.307479
```

0.310409					
2 2003-01-09 0.310296	0.271133	0.320783	0.303049		
3 2003-01-10	0.286407	0.311396	0.297146		
0.310441 4 2003-01-13 0.311234	0.434706	0.324745	0.304952		
4694 2021-08-16	0.341765	0.312585	0.261822		
0.312503 4695 2021-08-17	0.262366	0.311847	0.265213		
0.312003 4696 2021-08-18	0.314158	0.332025	0.268340		
0.311909 4697 2021-08-19	0.339382	0.330446	0.268275		
0.311960 4698 2021-08-20 0.311475	0.281104	0.307755	0.267951		
qtl_rng_up log_rv_avg253 \	log_rv_lag1	log_rv_avg5 l	log_rv_avg22		
0 0	-0.741694	-0.449644	-0.515572	-	
0.367086 1 0	-0.195388	-0.545231	-0.521978	-	
0.365305	-0.779210	-0.463997	-0.551932	-	
0.365947 3 0	-0.196713	-0.436124	-0.567596	-	
0.363599 4 0	0.067592	-0.369083	-0.543945	-	
0.359683					
4694 0	0.017612	-0.159335	-0.630536	-	
0.297995 4695 0	-0.271400	-0.149591	-0.598307	-	
0.299752 4696 0	-0.413196	-0.058005	-0.583753	-	
0.300944 4697 0	-0.151205	-0.162366	-0.578148	-	
0.302293 4698 0	-0.295768	-0.222792	-0.581853	-	
0.304542					
log_rv_up 0 0					
1 0 2 0					
3 0					

```
4
              0
4694
              0
4695
              0
4696
              0
4697
              0
4698
              0
[4699 rows x 11 columns]
# joining the join data0 to log rv
join data1 = pd.merge(rv data, join data0, on='date')
print(join data1)
            date
                    log_rv qtl_rng_lag1 qtl_rng_avg5 qtl_rng_avg22
\
0
      2003-01-07 -0.195388
                                0.269568
                                               0.320090
                                                              0.304471
1
      2003-01-08 -0.779210
                                0.361912
                                               0.321091
                                                              0.307479
2
      2003-01-09 -0.196713
                                0.271133
                                               0.320783
                                                              0.303049
      2003-01-10 0.067592
3
                                0.286407
                                               0.311396
                                                              0.297146
4
      2003-01-13 -0.838226
                                0.434706
                                               0.324745
                                                              0.304952
                                      . . .
                                                    . . .
                                                                    . . .
4694
      2021-08-16 -0.271400
                                 0.341765
                                               0.312585
                                                              0.261822
4695
      2021-08-17 -0.413196
                                0.262366
                                               0.311847
                                                              0.265213
4696
      2021-08-18 -0.151205
                                0.314158
                                               0.332025
                                                              0.268340
      2021-08-19 -0.295768
                                0.339382
4697
                                               0.330446
                                                              0.268275
4698 2021-08-20 -0.661106
                                0.281104
                                               0.307755
                                                              0.267951
      qtl rng avg253 qtl rng up log rv lag1 log rv avg5
log_rv_avg22 \
            0.309980
                                     -0.741694
                               0
                                                  -0.449644
0.515572
            0.310409
                               0
                                     -0.195388
                                                  -0.545231
0.521978
            0.310296
                               0
                                     -0.779210
                                                  -0.463997
0.551932
            0.310441
                               0
                                     -0.196713
                                                  -0.436124
```

0.567596 4 0.543945	0.311234	1	0	0.067592	2 -0.369083	-
	• •	•	• • •	• • •		
4694 0.630536	0.312503	3	0	0.017612	-0.159335	-
4695 0.598307 4696 0.583753 4697 0.578148 4698 0.581853	0.312003	3	0	-0.271400	-0.149591	-
	0.311909	9	0	-0.413196	-0.058005	-
	0.311960	Ð	0	-0.151205	-0.162366	-
	0.31147	5	0	-0.295768	3 -0.222792	-
0 1 2 3 4	g_rv_avg253 -0.367086 -0.365305 -0.365947 -0.363599 -0.359683	log_rv_u	0 0 0 0 0			
4694 4695 4696 4697 4698	-0.297995 -0.299752 -0.300944 -0.302293 -0.304542		0 0 0 0			
[4699 rows x 12 columns]						
# Remove date						
<pre>f = join_datal.drop(['date'], axis=1) print(f)</pre>						
		_rng_lag1	qtl_	rng_avg5 d	qtl_rng_avg22	
0 -0.		0.269568		0.320090	0.304471	
	779210	0.361912		0.321091	0.307479	
	196713	0.271133		0.320783	0.303049	
0.310296 3 0.	067592	0.286407		0.311396	0.297146	

4 -0.838226 0.434706 0.324745 0.304952

... ... ... ... ...

. . .

0.310441

0.311234

4694 -0.271400 0.312503	0.341765	0.312585	0.261822		
4695 -0.413196	0.262366	0.311847	0.265213		
0.312003 4696 -0.151205	0.314158	0.332025	0.268340		
0.311909 4697 -0.295768	0.339382	0.330446	0.268275		
0.311960 4698 -0.661106 0.311475	0.281104	0.307755	0.267951		
qtl_rng_up log_rv_avg253 \	log_rv_lag1	log_rv_avg5	log_rv_avg22		
0 0	-0.741694	-0.449644	-0.515572	-	
0.367086 1 0	-0.195388	-0.545231	-0.521978	-	
0.365305 2 0	-0.779210	-0.463997	-0.551932	-	
0.365947 3 0 0.363599	-0.196713	-0.436124	-0.567596	-	
4 0	0.067592	-0.369083	-0.543945	-	
0.359683					
4694 0	0.017612	-0.159335	-0.630536	-	
0.297995 4695 0 0.299752	-0.271400	-0.149591	-0.598307	-	
4696 0	-0.413196	-0.058005	-0.583753	-	
0.300944 4697 0 0.302293	-0.151205	-0.162366	-0.578148	-	
4698 0 0.304542	-0.295768	-0.222792	-0.581853	-	
log_rv_up 0 0 1 0 2 0 3 0 4 0 4694 0 4695 0 4696 0 4697 0					
4698 0					

[4699 rows x 11 columns]

```
# Step 3:
# Relationship between variables
# Creating models and fit
def clean data(nodes):
   nodes = nodes.stack().reset index()
   nodes.columns = ['variable 1','variable 2','r']
   nodes = nodes.loc[nodes['variable 1'] != nodes['variable 2'],:]
   nodes['abs r'] = np.abs(nodes['r'])
   nodes = nodes.sort values('abs r', ascending = False)
    return (nodes)
nodes =
f.select_dtypes(include=['float64','int']).corr(method='pearson')
clean data(nodes).head(10)
                        variable 2
        variable 1
                                                 abs r
103
      log rv avg253
                    gtl rng avg253 0.981233 0.981233
53
    qtl rng avg253
                     log rv avg253 0.981233 0.981233
41
      qtl rng avg22
                      log rv avg22 0.946594 0.946594
91
       log_rv_avg22
                     qtl_rng_avg22 0.946594 0.946594
29
       qtl rng avg5
                       log rv avg5 0.920140 0.920140
79
       log rv avg5
                      qtl_rng_avg5 0.920140 0.920140
13
      qtl rng lag1
                      qtl rng avg5 0.893746 0.893746
23
      qtl rng avg5
                      qtl_rng_lag1  0.893746  0.893746
95
       log_rv_avg22
                       85
       log rv avg5
                      log rv avg22 0.893307 0.893307
x = f[['log rv lag1','log rv avg5','log rv avg22','log rv avg253']]
y = f['log rv']
model = LinearRegression().fit(x,y)
# Step 4:
# Get results
result = model.score(x, y)# obtaining R squared
print('coefficient of determination:', result)
print('intercept:', model.intercept )
print('slope:', model.coef )
coefficient of determination: 0.6061669518002699
intercept: -0.012652404429932207
slope: [0.2497617  0.4176194  0.23483427  0.05839917]
# Step 5:
# Predict Response
pred = model.intercept + np.sum(model0.coef * x, axis=1)
```

```
print('predicted response:', pred, sep='\n')
predicted response:
0
      -0.528191
1
      -0.433064
2
      -0.552027
3
      -0.398443
      -0.298649
4
     -0.240269
4694
4695
      -0.300918
4696
      -0.294737
4697 -0.271648
4698 -0.333990
Length: 4699, dtype: float64
```