

Lecture 11

Recursion



QUIZ

قَالَ رَبِّ اشْرَحْ لِي صَدْرِي ۝
﴿٢٥﴾

[فَالَّذِي نَسِيَ كَهُولَ دَسَّهُ مَنْ يَرَى لَيْسَ بِمَنْ يَرَى
[فَالَّذِي نَسِيَ كَهُولَ دَسَّهُ مَنْ يَرَى لَيْسَ بِمَنْ يَرَى]

وَيَسِّرْ لِي آمْرِي ۝
﴿٢٦﴾

[وَيَسِّرْ لِي آمْرِي : مَنْ يَرَى لَيْسَ بِمَنْ يَرَى]

وَاحْلُلْ عُقْدَةً مِنْ لِسَانِي ۝
﴿٢٧﴾

[وَاحْلُلْ لِي آمْرِي : مَنْ يَرَى لَيْسَ بِمَنْ يَرَى]

يَفْقَهُوا قَوْلِي ۝
﴿٢٨﴾

[يَفْقَهُوا قَوْلِي : مَنْ يَرَى لَيْسَ بِمَنْ يَرَى]

4 QUESTIONS / FEEDBACK / CONCERNS



INFORMATION
TECHNOLOGY
UNIVERSITY

SE SECA SLIDE OF FAME

5



NO ONE
WEEK - 1



Muhammad Daniyal
Hammad (BSSE23046)
WEEK - 2



Syed Hashim Abbas
(BSSE23084)
WEEK - 3



Umar Ahmad
(BSSE23032)
WEEK - 4



YOUR NAME
WEEK - 5



YOUR NAME
WEEK - 6



YOUR NAME
WEEK - 7



YOUR NAME
WEEK - 8



YOUR NAME
WEEK - 9



YOUR NAME
WEEK - 10



YOUR NAME
MIDTERM



YOUR NAME
WEEK - 11



YOUR NAME
WEEK - 12



YOUR NAME
WEEK - 13



YOUR NAME
WEEK - 14



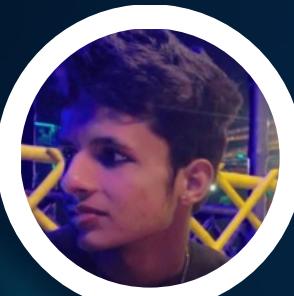
YOUR NAME
WEEK - 15

SE SEC B SLIDE OF FAME

6



Muhammad Mukarram
BSSE23029
WEEK - 1



Muhammad Abdullah
(BSSE23087)
WEEK - 2



Muhammad Abdullah
(BSSE23087)
WEEK - 3



Fasiha Rohail
(BSSE23041)
WEEK - 4



YOUR NAME
WEEK - 5



YOUR NAME
WEEK - 6



YOUR NAME
WEEK - 7



YOUR NAME
WEEK - 8



YOUR NAME
WEEK - 9



YOUR NAME
WEEK - 10



YOUR NAME
MIDTERM



YOUR NAME
WEEK - 11



YOUR NAME
WEEK - 12



YOUR NAME
WEEK - 13



YOUR NAME
WEEK - 14



YOUR NAME
WEEK - 15

RECAP

GitHub

Tools (Cygwin, IDE, GitHub)

Approach towards a word problem

Flowcharts

Flowcharts Advantages & Disadvantages

Algorithms

Pseudocode

Numbers Systems (Decimal, Binary, Octal & Hexadecimal)

Ten's Complement

Twos Complement

main function

Stream in and stream out operators

if else

Functions

Data Types

Arithmetic Operators

Relational Operators

Loops (While, for , do while)

Nested Loops

Switch cases

RECAP

Function Overloading

Scope of variables

Function Prototype and Definition

Default Value in parameters of functions

Parameters by value vs Parameters by Reference



GROUP DISCUSSIONS

Nested Loops

Nested For Loop

CODE SYNTAX

```
for ( initialization; condition; increment ) {  
    // statement(s) of outer loop  
  
    for ( initialization; condition; increment ) {  
        // statement(s) of inside loop  
    }  
  
    // statement(s) of outer loop  
}
```

Nested While Loop

CODE SYNTAX

```
while(condition) {  
    // statement(s) of outer loop  
  
    while(condition) {  
        // statement(s) of inside loop  
    }  
  
    // statement(s) of outer loop  
}
```

Nested Do-While Loop

CODE SYNTAX

```
do{  
    // statement(s) of outer loop  
    do{  
        // statement(s) of inside loop  
    }while(condition);  
  
    // statement(s) of outer loop  
}while(condition);
```

There is no rule that a loop must be nested inside its own type. In fact, there can be any type of loop nested inside any type and to any level.

Mix Nested Loop

CODE SYNTAX

```
do{  
    while(condition) {  
        for ( initialization; condition; increment ) {  
            // statement(s) of inside for loop  
        }  
        // statement(s) of inside while loop  
    }  
    // statement(s) of outer do-while loop  
}while(condition);
```

Problem

Print a calendar such that we take number of weeks from user

Week: 1

Day:1

Day:2

Day:3

Day:4

Day:5

Day:6

Day:7

Week: 2

Day:1

Day:2

Day:3

Day:4

Day:5

Day:6

Day:7

Week: 3

...

Problem

Print a calendar such that we take number of weeks from user

Week: 1

Day:2

Day:4

Day:6

Week: 2

Day:2

Day:4

Day:6

Week: 3

...

Problem

Print a calendar such that we take number of weeks from user

Week: 1

Day:2

Day:4

Day:6

Week: 2

Week: 3

Day:2

Day:4

Day:6

Week: 4

Week: 5

Day:2

Day:4

Day:6

...

Prime Factors

"Prime Factorization" is finding which prime numbers multiply together to make the original number.

$$12 = 2 \times 2 \times 3$$

Prime Factors

Can we divide 147 exactly by 2?

$$147 \div 2 = 73\frac{1}{2}$$

No it can't. The answer should be a whole number, and $73\frac{1}{2}$ is not.

Let's try the next prime number, 3:

$$147 \div 3 = 49$$

That worked, now we try factoring 49.

The next prime, 5, does not work. But 7 does, so we get:

$$49 \div 7 = 7$$

And that is as far as we need to go, because all the factors are prime numbers.

$$\mathbf{147 = 3 \times 7 \times 7}$$

Square

```
* * * * *
* * * * *
* * * * *
* * * * *
* * * * *
```

Triangle

```
*  
**  
***  
****  
*****  
*****
```

Output

....1

...22

..333

.4444

55555

Recursive Functions

$$f(n) = 1 + 2 + 3 + \dots + n$$

$$f(n) = \begin{cases} 1 & n=1 \\ n + f(n-1) & n>1 \end{cases}$$

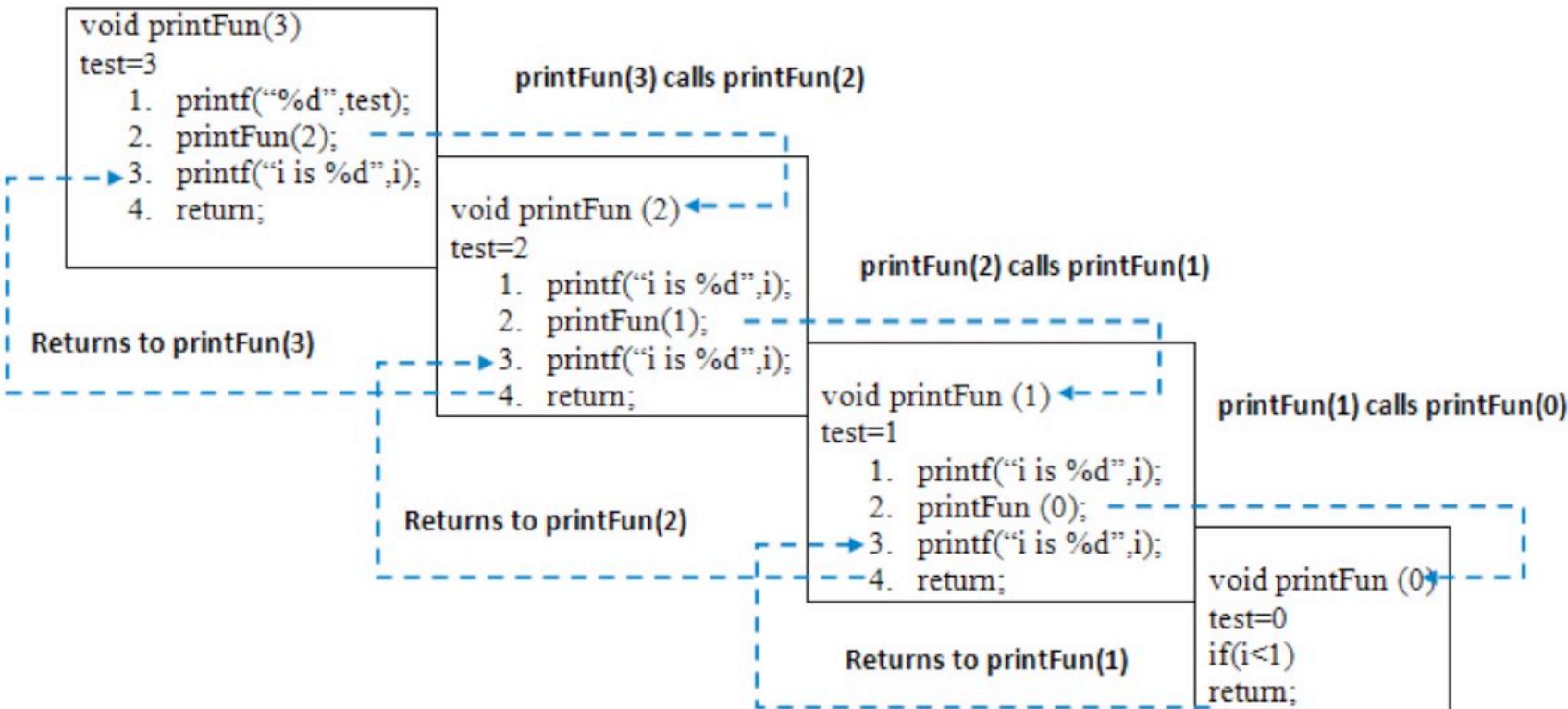
```
int f(int n)
{
    if (n == 1) // base case
        return 1;
    else
        return n+f(n-1);
}
```

```
int fact(int n)
{
    if (n <= 1) // base case
        return 1;
    else
        return n*fact(n-1);
}
```

```
#include <bits/stdc++.h>
using namespace std;

void printFun(int test)
{
    if (test < 1)
        return;
    else {
        cout << test << " ";
        printFun(test - 1); // statement 2
        cout << test << " ";
        return;
    }
}
```

3 2 1 1 2 3



Recursive Functions

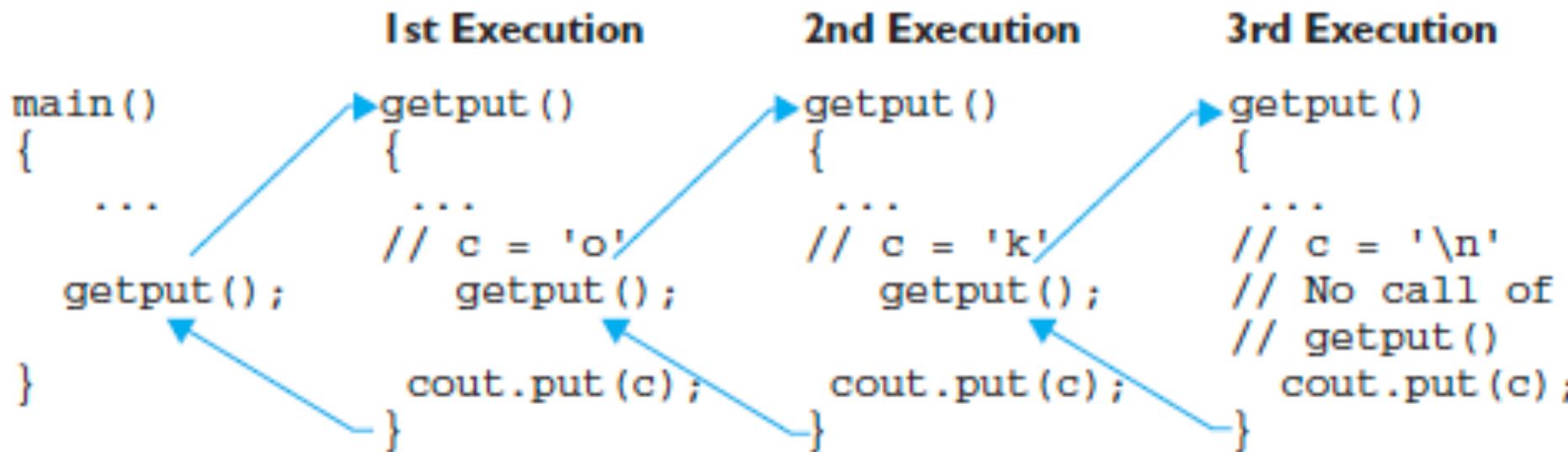
```
// recursive.cpp
// Demonstrates the principle of recursion by a
// function, which reads a line from the keyboard
// and outputs it in reverse order.
// -----
#include <iostream>
using namespace std;

void getput(void);

int main()
{
    cout << "Please enter a line of text:\n";
    getput();
    cout << "\nBye bye!" << endl;
    return 0;
}

void getput()
{
    char c;
    if( cin.get(c)  &&  c != '\n')
        getput();
    cout.put(c);
}
```

Recursive Functions



- Series

1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144

Recursion

- Functions can call themselves.
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$ can be easily expressed via a recursive implementation

```
int fibonacci(int n) {  
    if (n == 0 || n == 1) {  
        return 1;  
    } else {  
        return fibonacci(n-2) + fibonacci(n-1);  
    }  
}
```

Recursion

- Functions can call themselves.
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$ can be easily expressed via a recursive implementation

base case

```
int fibonacci(int n) {  
    if (n == 0 || n == 1)  
        return 1;  
    } else {  
        return fibonacci(n-2) + fibonacci(n-1);  
    }  
}
```

Recursion

- Functions can call themselves.
- $\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$ can be easily expressed via a recursive implementation

recursive step

```
int fibonacci(int n) {  
    if (n == 0 || n == 1) {  
        return 1;  
    } else {  
        return fibonacci(n-2) + fibonacci(n-1);  
    }  
}
```