

Date: \_\_\_\_\_

# Assignment #1

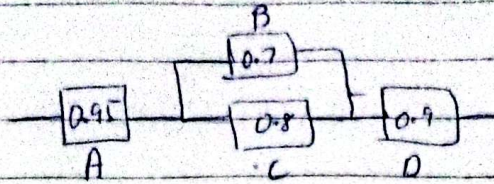
## Probability & Statistics

Day: \_\_\_\_\_

BSSE23058

Section A.

Q2.92



$$P(A) = 0.95 \quad P(B) = 0.7 \quad P(C) = 0.8 \quad P(D) = 0.9$$

Assume the component fail independently means system will work if

- ① component A works
- ② either B or C (or both works) as in parallel
- ③ D works

$$P(\text{system works}) = ?$$

$$\begin{aligned}
 P(\text{system works}) &= P(A \cap (B \cup C) \cap D) \\
 &= P(A) \cdot P(B \cup C) \cdot P(D) \text{ as independent.} \\
 &= 0.95 \cdot P(B \cup C) \cdot 0.9
 \end{aligned}$$

$$P(B \cup C) = ?$$

$$P(B \cup C) \Rightarrow$$



$$\begin{aligned}
 P(B \cup C) &= 1 - P(B' \cap C') \Rightarrow \\
 &= 1 - P(B') \cdot P(C') \\
 &= 1 - (1 - P(B)) \cdot (1 - P(C)) \\
 &= 1 - (1 - 0.7) \cdot (1 - 0.8) \\
 &= 1 - (0.3) \cdot (0.2) \\
 &= 1 - 0.06 \\
 &= 0.94
 \end{aligned}$$

$$\begin{aligned}
 P(\text{system works}) &= P(A) \cdot P(B \cup C) \cdot P(D) \\
 &= 0.95 \cdot 0.94 \cdot 0.9 \\
 &= 0.8037 \\
 &\approx 0.804
 \end{aligned}$$