

Assignment # 1
DLD

Q1. Truth Tables & Boolean algebra identities.

$$a. AB\bar{C} + B\bar{C}\bar{D} + BC + \bar{C}D = B + \bar{C}D$$

LHS RHS

A	B	C	D	$\bar{C}\bar{D}$	$AB\bar{C}$	$B\bar{C}\bar{D}$	BC	$\bar{C}D$	LHS	RHS
0	0	0	0	1	0	0	0	0	0	0
0	0	0	1	1	0	0	0	1	1	1
0	0	1	0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0	0	0	0
0	1	0	0	1	1	0	1	0	1	1
0	1	0	1	1	0	0	0	1	1	1
0	1	1	0	0	1	0	1	0	1	1
0	1	1	1	0	0	0	1	0	1	1
1	0	0	0	1	1	0	0	0	0	0
1	0	0	1	1	0	0	0	1	1	1
1	0	1	0	0	1	0	0	0	0	0
1	0	1	1	0	0	0	0	0	0	0
1	1	0	0	1	1	1	1	0	1	1
1	1	0	1	1	0	1	0	1	1	1
1	1	1	0	0	1	0	0	1	1	1
1	1	1	1	0	0	0	1	0	1	1

Hence proved LHS = RHS.

$$WY + \bar{W}YZ + WZX + \bar{W}XY = WY + \bar{W}X\bar{Z} + \bar{X}Y\bar{Z} + X\bar{Y}Z$$

LHS = RHS.

w	x	y	z	w	x	y	z	wy	wyz	wxy	wxz	$\bar{w}yz$	$\bar{w}xy$	$\bar{w}xz$	$\bar{x}yz$	LHS	RHS
0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0
0	0	1	0	1	1	0	1	0	1	0	0	0	1	0	1	1	1
0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0
0	1	0	0	1	0	1	0	0	0	1	1	0	0	1	1	1	1
0	1	0	1	0	1	0	0	0	0	1	0	0	1	1	1	1	1
0	1	1	0	1	0	0	1	0	0	0	1	0	0	1	1	1	1
0	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0
1	0	0	1	0	1	1	0	0	0	0	0	0	0	0	0	0	0
1	0	1	0	0	1	0	1	0	0	0	0	0	1	0	1	1	1
1	0	1	1	0	1	0	0	1	0	0	0	0	0	0	1	1	1
1	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
1	1	0	1	0	0	0	0	0	0	1	0	0	0	1	1	1	1
1	1	1	0	0	0	0	1	0	0	0	0	0	0	0	1	1	1
1	1	1	1	0	0	0	0	1	0	1	0	0	0	0	1	1	1

Hence proved $LHS = RHS$.

$$b. -AB\bar{C} + B\bar{C}\bar{D} + BC + \bar{C}D = B + \bar{C}D$$

$$AB\bar{C} + BC + B\bar{C}\bar{D} + \bar{C}D$$

$$B(A\bar{C} + C) + \bar{C}(B\bar{D} + D)$$

$$B(A + C) + \bar{C}(B + D)$$

$$BA + BC + \bar{C}B + \bar{C}D$$

$$BA + B(C + \bar{C}) + \bar{C}D$$

$$BA + B(1) + \bar{C}D$$

$$B(A + 1) + \bar{C}D$$

$$B(1) + \bar{C}D$$

$$B + \bar{C}D.$$

Association Law.

Distributive Law

Redundancy Law.

Distributive Law.

Complement Law.

Identity Law

Identity Law

$$- WY + \bar{W}YZ + WXZ + \bar{W}X\bar{Y} = WY + \bar{W}X\bar{Z} + \bar{X}Y\bar{Z} + X\bar{Y}Z$$

$$WY + \bar{W}YZ + WXZ + \bar{W}X\bar{Y}$$

Pissoctation Law

~~$$WY + \bar{W}Z + WZ + \bar{W}X\bar{Y}$$~~

Distributive law

$$Y(W + \bar{Z}) + WZX + \bar{W}X\bar{Y}$$

Redundancy Law

$$\underline{YW} + Y\bar{Z} + WZX + \bar{W}X\bar{Y}$$

$$WY + Y\bar{Z} + WZX + \bar{W}X\bar{Y}$$

Q2

Minterms & Minterms.

a.	X	Y	Z	E	F	$m_0 M$	$m_1 M$	E minterms :- m_0, m_3, m_5, m_7
	0	0	0	0	1	m_0	m_0	E minterms :- m_1, m_2, m_4, m_6
	0	0	1	1	0	m_1	m_1	$E = \sum m(1, 2, 4, 6)$
	0	1	0	1	1	m_2	m_2	$E = \prod M(0, 3, 5, 7)$
	0	1	1	0	0	m_3	m_3	
	1	0	0	1	1	m_4	m_4	$F = \sum m(0, 2, 4, 7)$
	1	0	1	0	0	m_5	m_5	$F = \prod M(1, 3, 5, 6)$
	1	1	0	1	0	m_6	m_6	
	1	1	1	0	1	m_7	m_7	

b. $\bar{E} = \sum m(0, 3, 5, 7)$ Opposite of E's minterms. That is the minterms.
 $\bar{F} = \sum m(1, 3, 5, 6)$

c. $E + F = \sum (?)$.

$$E + F = \sum m(0, 1, 2, 4, 6, 7)$$

E	F	$E + F$	
0	1	1	m_0
1	0	1	m_1
1	1	1	m_2
0	0	0	m_4
1	1	1	m_6
0	1	1	m_7

$E \cdot f = \Sigma m(?)$

$E \cdot F = \Sigma m(2, 4)$

	E	F	E.F	
0	0	1	0	
1	1	0	0	
2	1	1	1	m_2
3	0	0	0	
4	1	1	1	m_4
5	0	0	0	
6	1	0	0	
7	0	1	0	

d. $E = \Sigma m(1, 2, 4, 6)$

m_1	001	$\bar{X}YZ$
m_2	010	$\bar{X}Y\bar{Z}$
m_4	100	$X\bar{Y}\bar{Z}$
m_6	110	$XY\bar{Z}$

$F = \Sigma m(0, 2, 4, 7)$

m_0	000	XYZ
m_2	010	$\bar{X}Y\bar{Z}$
m_4	100	$X\bar{Y}\bar{Z}$
m_7	111	XYZ

$$\bar{X}\bar{Y}Z + \bar{X}Y\bar{Z} + X\bar{Y}\bar{Z} + XY\bar{Z}$$

$$\bar{X}\bar{Y}\bar{Z} + \bar{X}Y\bar{Z} + X\bar{Y}\bar{Z} + XY\bar{Z}$$

e. $\bar{X} =$

	\bar{Z}	Z
$\bar{X}\bar{Y}$	00	1
$\bar{X}Y$	01	1
$X\bar{Y}$	11	1
$X\bar{Y}$	10	1

$$\begin{array}{l}
 XYZ \quad X\bar{Y}Z \quad XY\bar{Z} \\
 010 \quad 110 \quad 001 \\
 110 \quad 100 \quad \underline{\underline{=}}
 \end{array}$$

$$\bar{Y}\bar{Z} + X\bar{Z} + \bar{X}\bar{Y}Z$$

$X\bar{Y}Z$	0	1
00	1	
01		1
11		1
10	1	

$$\begin{array}{r}
 XYZ \quad X\bar{Y}Z \quad X\bar{Y}Z \\
 000 \quad 000 \quad 000 \\
 010 \quad 010 \quad 010 \\
 100 \quad \underline{\underline{=}} \quad \underline{\underline{=}} \\
 \bar{Y}\bar{Z} \quad X\bar{Z} \quad XYZ
 \end{array}$$

$$\bar{Y}\bar{Z} + X\bar{Z} + XY\bar{Z}$$

SOP $A=0$
 $A=1$

Q3 K-Map Simplification :=

$$a = A\bar{B} + A\bar{B}\bar{C}\bar{D} + C\bar{D} + B\bar{C}D + ABCD$$

		C D	C D	C D	C D	
		00	01	11	10	
		AB				
$\bar{A}\bar{B}$	00	0		1	2	CD
$\bar{A}B$	01	4	1	5	7	6
$A\bar{B}$	11	12	13	1	15	14
$A\bar{B}$	10	1	8	1	11	1

Ans: $\underline{\bar{A}\bar{B} + BD + CD}$

ABCD	AB CD	ABCD
1000	0101	0011
1001	1101	0111
1011	0111	1111
1010	1111	1011

$$- (\bar{A}\bar{B} + A\bar{B})(\bar{C}\bar{D} + C\bar{D})$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D}$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D}(C + \bar{C}) + A\bar{B}C\bar{D}$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} + A\bar{B}C\bar{D}$$

		C D	C D	C D	C D	
		00	01	11	10	
		AB				
$\bar{A}\bar{B}$	00	1				1
$\bar{A}B$	01					
$A\bar{B}$	11					
$A\bar{B}$	10	1			1	

Ans: $\underline{\bar{B}\bar{D}}$

$$ABCD$$

$$1000$$

$$1010$$

$$0000$$

$$0010$$

$$\bar{B}\bar{D}$$

$$F(w, x, y, z) = \sum m(2, 5, 6, 13, 15), d(w, x, y, z) = \sum m(0, 4, 8, 10, 11)$$

	wx	yz	$\bar{y}\bar{z}$	$y\bar{z}$	$\bar{y}z$
wx	00	00	01	11	10
$w\bar{x}$	00	X ₀			1 ₂
$w\bar{x}$	01	X ₄	1 ₅	7	1 ₆
wx	11	1 ₂	1 ₃	1 ₅	1 ₄
$w\bar{x}$	10	X ₈	9	X ₁₁	X ₁₀

$$\text{Ans: } \underline{\bar{w}\bar{z}} + \underline{\bar{x}\bar{y}z} + \underline{wxz}$$

ABCD	ABCD	ABCD
0000	0101	1101
0000	1101	1111
0010		
0110		
	$\bar{x}\bar{y}z$	wxz
	$\bar{w}\bar{z}$	

POS $A=1$
 $A=0$

$$b. -F(w, x, y, z) = \overline{\sum m(5, 8, 6, 12, 13, 14)}$$

	wx	yz	$\bar{y}\bar{z}$	$\bar{y}\bar{z}$	$\bar{y}z$
	00	00	01	11	10
wx	00	0	1	3	2
$w\bar{x}$	01	4	0 ₅	7	0 ₆
$\bar{w}\bar{x}$	11	0 ₁₂	0 ₁₃	15	0 ₁₄
$\bar{w}x$	10	0 ₈	9	11	10

$$\text{Ans: } \underline{(\bar{w}+y+z)} \underline{(\bar{x}+y+\bar{z})} \underline{(\bar{x}+\bar{y}+z)}$$

	$wxyz$	$wxyz$	$wxyz$
1100	0101	0110	
1000	1101	1110	$\bar{x}yz$
$\bar{w}yz$			

$$\bar{w}+y+z \quad \bar{x}+y+\bar{z} \quad \bar{x}+\bar{y}+z$$

$$- (\bar{A} + \bar{B} + D)(\bar{A} + \bar{D})(A + B + \bar{D})(A + \bar{B} + C + D)$$

	AB	CD	$\bar{C}\bar{D}$	$\bar{C}P$	$\bar{C}D$
AB	00				
$A\bar{B}$	01		0	0	
$\bar{A}\bar{B}$	11		0	0	0
$\bar{A}B$	10		0	0	

$$\text{Ans: } (\bar{B}+\bar{D}) \cdot (\bar{B}+C+D) \cdot (\bar{A}+\bar{B})$$

ABCD	ABCD	ABCD	ABCD
0001	0100	1100	
0011	1100	1101	
1001	$\bar{B}CD$	1111	
1011		1110	
$B\bar{D}$		$\bar{A}\bar{B}$	
$B+\bar{D}$	$\bar{B}+C+D$	$\bar{A}+\bar{B}$	

- $F(A, B, C, D) = \sum m(4, 6, 7, 8, 12, 15), d(A, B, C, D) = \sum m(2, 3, 5, 10, 14)$

AB	00	01	11	10
00	0	1	X	X
01	1	X	1	1
11	1	1	1	X
10	1	X	X	X

Ans: $(\bar{B}+D) \cdot (\bar{B}+\bar{C}+\bar{D}) \cdot (\bar{A}+C+D)$

ABCD	ABCD	ABCD
0100	0111	1100
1100	1111	1000
0110	$\bar{B}CD$	$A\bar{C}D$
1110		

$B\bar{D}$

$$(B\bar{D} + BCD + A\bar{C}\bar{D}) \\ (B+\bar{D}) \cdot (\bar{B}+\bar{C}+\bar{D}) \cdot (\bar{A}+C+D)$$

Q5 QM Method

$\begin{smallmatrix} 16 & 8 & 4 & 2 & 1 \\ 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \end{smallmatrix}$

$F(V, W, X, Y, Z) = \sum m(0, 2, 4, 7, 8, 10, 12, 16, 18, 20, 23, 24, 25, 26, 27, 28)$

0	00000	60	16	10000	62	27	11011
1	00010	61	18	10010	62	28	11100
4	00100	63	20	10100	62		
7	00111	63	23	10111	64		
8	01000	61	24	11000	62		
10	01010	62	25	11001	63		
12	01100	62	26	11010	63		

Group #	m	B.R		
G0	m_0	00000	G0	(0,2) 000d0
G1	m_2	00010		(0,4) 00d00
	m_4	00100		(0,8) 0d000
	m_8	01000		(0,16) d0000
	m_{16}	10000	G1	(2,10) 0d010
G2	m_{10}	01010		(2,18) d0010
	m_{12}	01100		(4,12) 0d100
	m_{18}	10010		(4,20) d0100
	m_{20}	10100		(8,10) 010d0
	m_{24}	11000		(8,12) 01d00
G3	m_7	00111		(8,24) d1000
	m_{25}	11001		(16,18) 100d0
	m_{26}	11010		(16,20) 10d00
	m_{28}	11100		(16,24) 1d000
G4	m_{23}	10111	G2	(10,26) d1010
	m_{27}	11011		(12,28) d1100
				(18,26) 1d010
				(20,28) 1d100
				(24,25) 1100d
				(24,26) 11ad0
				(24,28) 11d00
			G3	(7,23)d0111
				(25,27) 110d1
				(26,27) 1101d
			G3	(24,25,26,27) 110dd
				(24,26,25,27) 110ad

further simplifying
by taking the common
minterms out.

further simplifying
and merging terms.

VWXYZ

$\bar{X}\bar{Z}$

(0,2,8,10) dd0d0

(0,2,8,10,16,18,24,26) dd0d0

(0,4,8,12) ddd00

(0,4,8,12,16,20,24,28) ddd00

$\bar{Y}\bar{Z}$

(0,2,16,18) d00d0

(24,25,26,27) 110dd

VWX

(0,4,16,20) dd000

Rest of the minterms combined

(0,8,16,24) dd100

give the same

(2,10,18,26) dd010

(7,23) d0111

$\bar{W}XYZ$

(4,12,20,28) dd100

$\bar{X}\bar{Z}$ $\bar{Y}\bar{Z}$ VW \bar{X} $\bar{W}XYZ$

(8,10,24,28) dd0d0

0 X X

(16,18,24,26) 1d0d0

2 [X] [X]

(16,20,24,28) 1dd00

4 [X] [X]

(24,25,26,27) 110dd ✓

7 [X]

8 X X

Ans

Essential prime implicants

10 [X]

• $\bar{X}\bar{Z}$ dd0d0

12 X

• $\bar{Y}\bar{Z}$ ddd00

16 X X

• VW \bar{X} 110dd

18 [X]

• $\bar{W}XYZ$ d0111

20 [X]

$\bar{X}\bar{Z} + \bar{Y}\bar{Z} + VW\bar{X} + \bar{W}XYZ$

23 [X]

24 X X X

X

[X]

25 [X]

26 X X

X

[X]

27 [X]

28 [X]

Q4

Sets & Circles.

$$(a) F(A, B, C, D) = AB\bar{C}D + A\bar{D} + \bar{A}\bar{D}$$

a. \neg AND - NOT

$$\begin{aligned} & (AB\bar{C}D + A\bar{D} + \bar{A}\bar{D})' \\ & (AB\bar{C}D)' \cdot (\bar{A}\bar{D})' - (\bar{A}\bar{D})' \end{aligned}$$

b. \neg OR - NOT

$$\begin{aligned} & ((AB\bar{C}D + A\bar{D} + \bar{A}\bar{D})')' \\ & ((AB\bar{C}D)' \cdot (\bar{A}\bar{D})' \cdot (\bar{A}\bar{D})')' \\ & ((\bar{A} + \bar{B} + C + \bar{D}) \cdot (\bar{A} + D) \cdot (A + \bar{D}))' \\ & (\bar{A} + \bar{B} + C + \bar{D})' + (\bar{A} + D)' + (A + \bar{D})' \end{aligned}$$

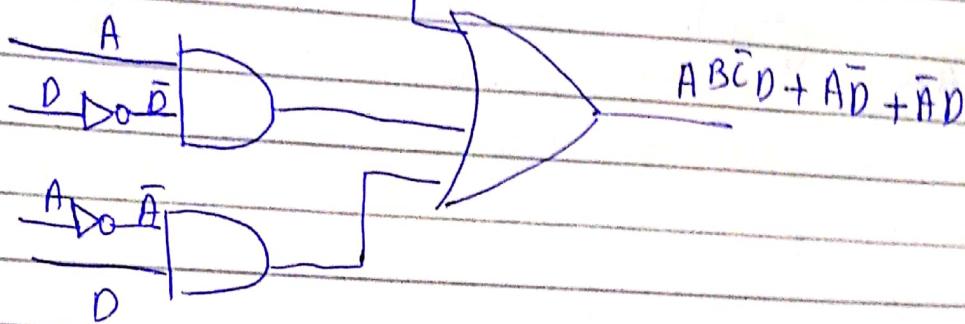
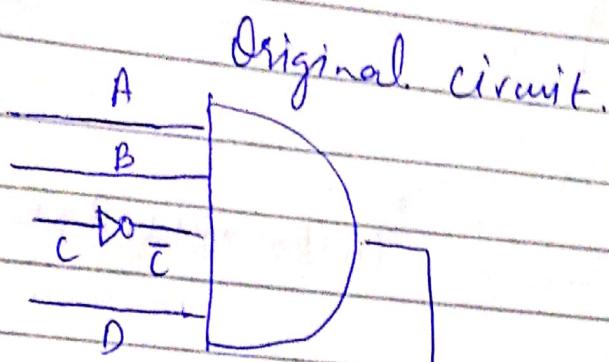
c. NAND

$$\begin{aligned} & AB\bar{C}D + A\bar{D} + \bar{A}\bar{D} \\ & (A \odot B) \odot (A \odot B) \odot ((C \oplus C) \odot B) \quad (A \odot (B \oplus D)) \odot (A \odot (D \oplus D)) \odot ((A \odot A) \odot B) \odot ((A \odot A) \odot D) \\ & \quad | \quad | \quad | \quad | \end{aligned}$$

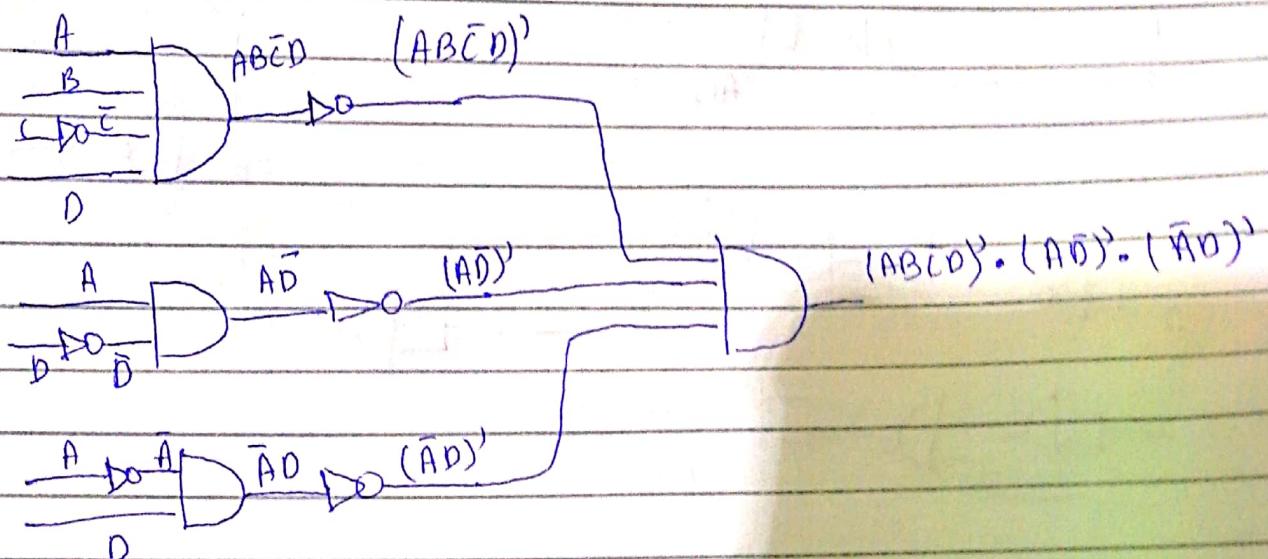
d. NOR

$$\begin{aligned} & AB\bar{C}D + A\bar{D} + \bar{A}\bar{D} \\ & (A \oplus B) \oplus (A \oplus B) \oplus ((C \oplus C) \oplus D) \oplus ((C \oplus C) \oplus D) \oplus (A \oplus (D \oplus D)) \oplus (A \oplus (D \oplus D)) \oplus \\ & \quad | \quad | \quad | \quad | \quad | \quad | \end{aligned}$$

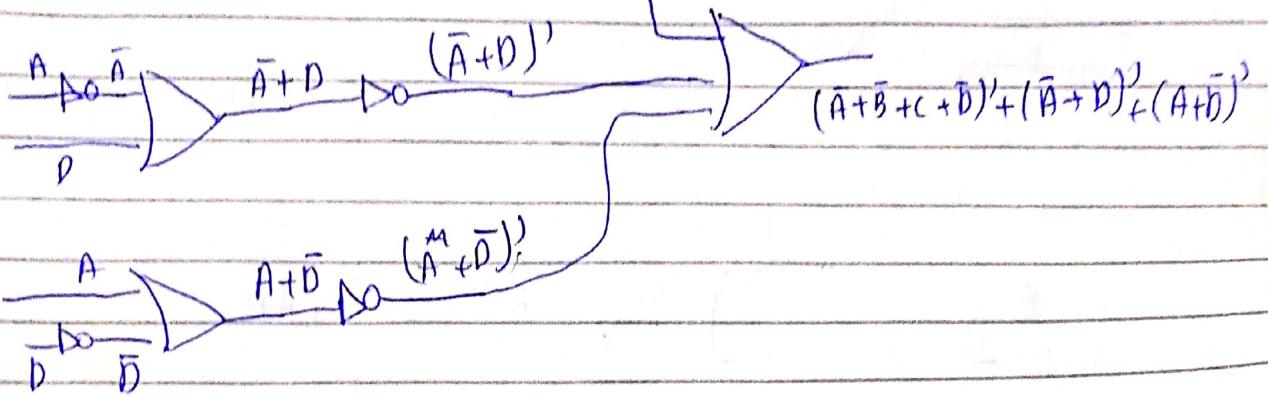
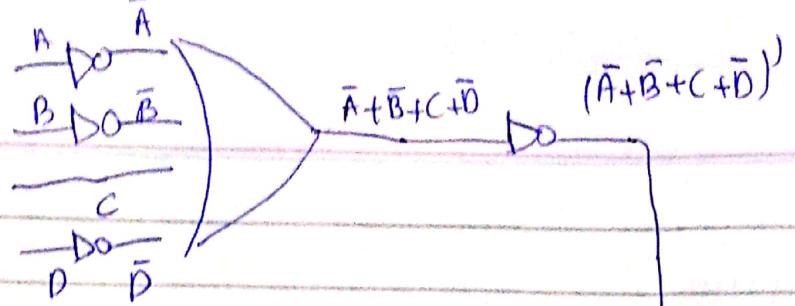
(b) Circuits.



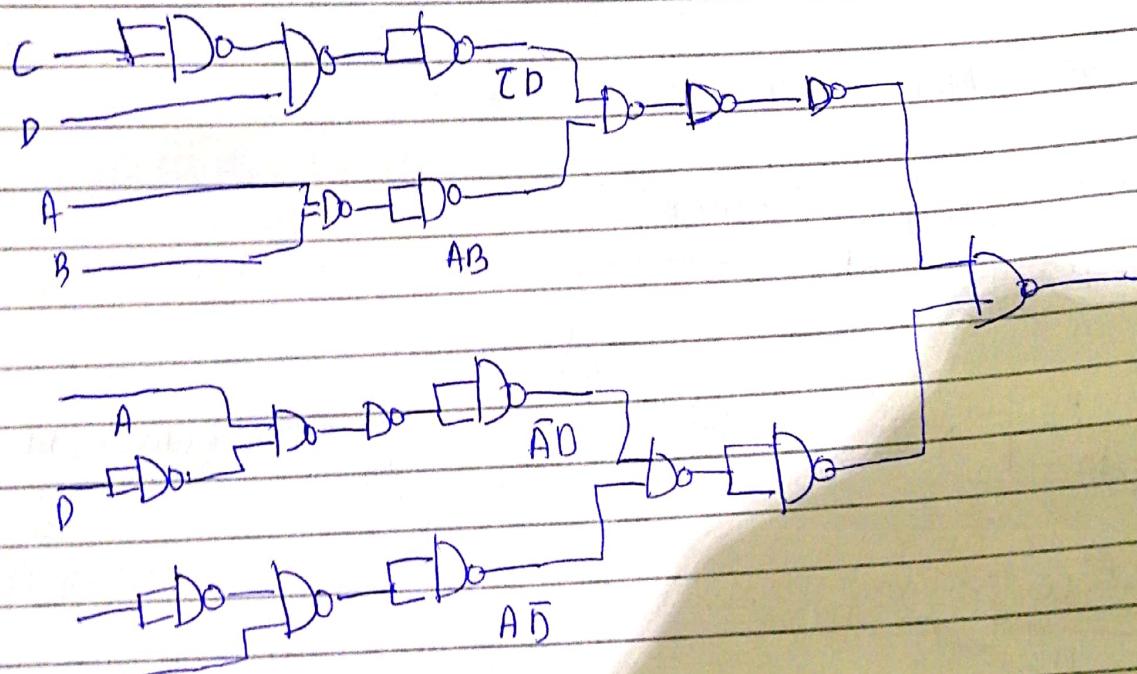
AND-NOT circuit



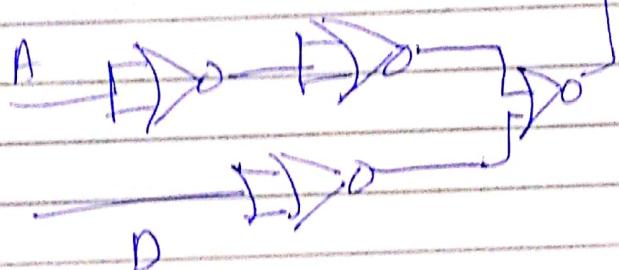
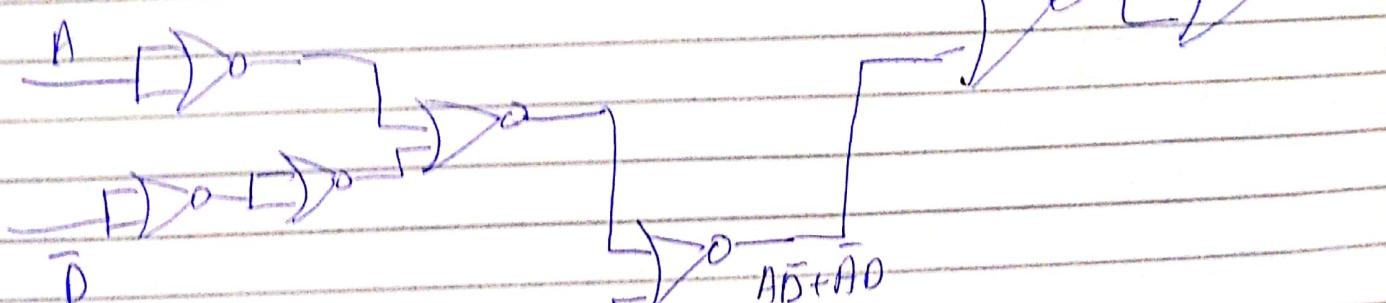
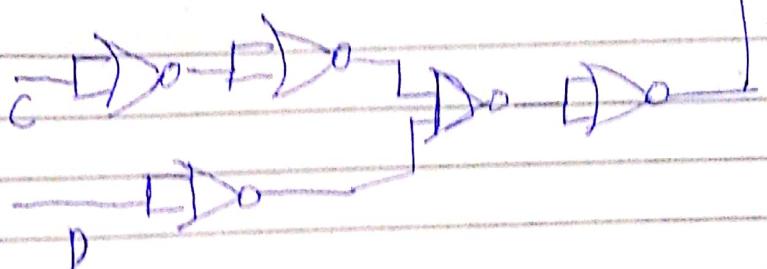
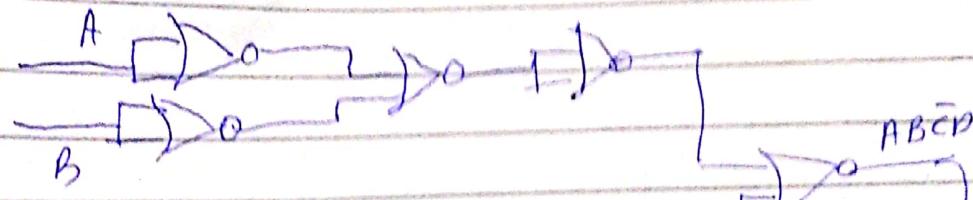
OR - NOT Circuit



NAND circuit.



NOR circuit.



c.

1. 10

2. 12

3. 13

4. 22