

Assignment #2
DLD

Q1	a.	Decimal	Binary	Octal	Hexadecimal	$2^9 2^8 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0$	A 10 B 11 C 12 D 13 E 14 F 15
		12	1100	14	C	1 100 = 14	
		13	1101	15	D	1 101 = 15	
		14	1110	16	E	1 110 = 16	
		15	1111	17	F	1 111 = 17	
		16	10000	20	10	10 000 = 20	1 0000 = 10
		17	10001	21	11	10 001 = 21	1 0001 = 11
		18	10010	22	12	10 010 = 22	1 0010 = 12
		19	10011	23	13	10 011 = 23	1 0011 = 13
		20	10100	24	14	10 100 = 24	1 0100 = 14

b. i. 128k bits

$$1 \text{ K bits} = 1024 \text{ bits.}$$

$$128 \text{ K bits} = 128 \times 1024$$

$$128 \text{ K bits} = 131072 \text{ bits.}$$

ii. 32 M bytes.

$$1 \text{ byte} = 8 \text{ bits.}$$

$$32 \text{ M byte} = 8 \times 32 \text{ M}$$

$$32 \text{ M bytes} = 256 \text{ M bits.}$$

$$1 \text{ M bits} = 1048576 \text{ bits.}$$

$$256 \text{ M bits} = 256 \times 1048576.$$

$$256 \text{ M bits} = 268,435,456 \text{ bits.}$$

c.

A 10-bit register can stored $2^{10} = 1024$ possible numbers. e.g.
0 0 0 0 0 0 0 0 1, 0 0 0 0 0 0 0 1 0. etc.

d. Range of signed numbers — by a 16 bit binary number.

(i) sign-magnitude form.

We use the formula $- (2^{n-1})_{10} + (2^{n-1} - 1)$

$$\begin{aligned} & - (2^{16-1} - 1)_{10} + (2^{16-1} - 1) \\ & - (32,768 - 1)_{10} + (32,768 - 1) \\ & -32767_{10} + 32767 \end{aligned}$$

(ii) 1's complement form

$$\begin{aligned} & - (2^{n-1} - 1)_{10} + (2^{n-1} - 1) \\ & - (2^{16-1} - 1)_{10} + (2^{16-1} - 1) \\ & -32767_{10} + 32767 \end{aligned}$$

(iii) 2's complement form

$$\begin{aligned} & -2^{n-1} \text{ }_{10} + (2^{n-1} - 1) \\ & -2^{16-1} \text{ }_{10} + (2^{16-1} - 1) \\ & -12^{15} \text{ }_{10} + (2^{15} - 1) \\ & -32768 \text{ }_{10} + 32767 \end{aligned}$$

e. $((34)_r + (24)_r) * (21)_r = (1480)_r$

(Convert all the values.)

$$((3r^1 + 4r^0) + (2r^1 + 4r^0)) * (2r^1 + 1r^0) = (1r^3 + 4r^2 + 8r^1 + 0r^0)$$

$$((3r+4) + (2r+4)) * (2r+1) = r^3 + 4r^2 + 8r + 0.$$

$$(5r+8) * (2r+1) = r^3 + 4r^2 + 8r$$

$$10r^2 + 5r + 16r + 8 = r^3 + 4r^2 + 8r.$$

$$10r^2 + 21r + 8 = r^3 + 4r^2 + 8r$$

$$0 = r^3 + 4r^2 - 10r^2 + 8r - 21r - 8$$

$$0 = r^3 - 6r^2 - 13r - 8$$

Input value $r = 6$

$$0 \neq (6)^3 - 6(6)^2 - 13(6) - 8$$

$$r = 8$$

$$0 = (8)^3 - 6(8)^2 - 13(8) - 8$$

$\boxed{\text{no of roots} = 8}$

f. (i) $A5_{16} - 98_{16}$

$$\begin{array}{r} A \quad 5 \\ 1 \quad 0 \quad 5 \\ 10 \times 16^1 + 5 \times 16^0 \\ 165_{10} \end{array} \qquad \begin{array}{r} 9 \quad 8 \\ 9 \times 16^1 + 8 \times 16^0 \\ 152_{10} \end{array}$$

$$165_{10} - 152_{10} = 13_{10} = D_{16}$$

(ii) $F1_{16} - A6_{16}$

$$F \quad 1 \quad A \quad 6$$

$$15 \times 16^1 + 1 \times 16^0 \quad 10 \times 16^1 + 6 \times 16^0$$

$$241_{10} - 166_{10} = 75_{10} = 4B_{16}$$

$\Rightarrow 4B_{16}$

(iii) $653_8 - 456_8$

$$\begin{array}{r} 6 \quad 5 \quad 3 \\ 4 \quad 5 \quad 6 \end{array}$$

$$6 \times 8^2 + 5 \times 8^1 + 3 \times 8^0 - 4 \times 8^2 + 5 \times 8^1 + 6 \times 8^0$$

$$427_{10} - 302_{10} = 125_{10}$$

$$1 \times 8^2 + 2 \times 8^1 + 5 \times 8^0 = 175_8$$

a. 6248_{10}

(i) BCD.

$$\begin{array}{r} 6 \quad 2 \quad 4 \quad 8 \\ 0110 \quad 0010 \quad 0100 \quad 1000 \\ 0110 \quad 0010 \quad 0100 \quad 1000 \end{array}$$

(ii) Excess 3 code.

$$\begin{array}{r} 6 \quad 2 \quad 4 \quad 8 \\ +3 \quad +3 \quad +3 \quad +3 \\ \hline 9 \quad 5 \quad 7 \quad 11 \end{array} \qquad \begin{array}{r} 0110 \quad 0010 \\ +0011 \quad +0011 \\ \hline 1001 \end{array}$$

$1001 \quad 0101 \quad 0111 \quad 1011$

(iii) 2421 code

6	2	4	8
2421	2421	2421	2421
1100	0010	0100	1110

1100 0010 0100 1110

(iv) 6311 code

6	2	4	8
6311	6311	6311	6311
1000	0011	0101	1011

1000 0011 0101 1011

b. (i) Number in hexadecimal.

		Binary	decimal.	ASCII char	(ii) Parity.
73		0111 0011	115	s	odd
F4	15 4	1111 0100	244	ü	odd
E5	14 5	1110 0101	229	å	odd.
76		0111 0110	118	v	odd
E5	14 5	1110 0101	229	å	odd.
4A	4 10	0100 1010	74	J	odd.
EF	14 15	1110 1111	239	í	odd
62		0110 0010	98	b	odd
73		0111 0011	115	s	odd

128 64 32 16 8 4 2 1

0 1 1 1 0 0 1 1 = 115

1 1 1 1 0 1 0 0 = 244

1 1 1 0 0 1 0 1 = 229

Message: SöövääJäbs

1 byte = U+0000 to U+007F
 2 bytes = U+0080 to U+07FF

c. (i) U+0040

This is the standard.

Binary = 01000000 (1 byte)

Hexadecimal = 0100 0000

4 0
↓
40.

(ii) U+00A2

Binary = A Z C2

10 2 12 2
↓
1010 0010

1100 0010. (2 bytes)

Hexadecimal = A2 C2

(iii) U+1F66B2

Binary B2 9A 9F F0
 ↓ 11 2 9 10 9 15 15 0
 ↳ 1011 0010 1001 1100 1001 1111 1111 0.

Hexadecimal = B2 9A 9F F0.

Q3

a. (i) F_2

$F_{2,}$

A	B	D	\bar{A}	\bar{D}	$\bar{A}B$	$\bar{A}B + \bar{D}$
1	1	1	0	0	0	0
1	1	0	0	1	0	1
1	0	1	0	0	0	0
1	0	0	0	1	0	1
0	1	1	1	0	1	1
0	1	0	1	1	1	1
0	0	1	1	0	0	0
0	0	0	1	1	0	1

F₁

A	B	C	D	\bar{B}	A	$\bar{B}C$	$\bar{A}B$	$A + (\bar{B}C)$	$(\bar{A}\bar{B}) \oplus D$	F ₁
1	1	1	1	0	0	0	0	1	1	1
1	1	1	0	0	0	0	0	1	0	1
1	1	0	1	0	0	0	0	1	0	1
1	1	0	0	0	0	0	0	1	1	1
1	0	1	1	1	0	1	0	1	1	1
1	0	1	0	1	0	0	0	1	0	1
1	0	0	1	1	0	0	0	1	1	1
0	1	1	1	0	1	0	1	0	1	1
0	1	1	0	0	1	0	1	0	0	0
0	1	0	1	0	1	0	1	0	1	1
0	1	0	0	0	1	0	0	1	1	1
0	0	1	1	1	1	1	0	1	0	1
0	0	1	0	1	1	1	0	0	1	1
0	0	0	1	1	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	1	1

$$(ii) F_1 = (A + \bar{B}C) + (\bar{A}\bar{B} \oplus D)$$

$$F_2 = (\bar{A}\bar{B} + \bar{D})$$

b. 4 bit number \rightarrow 3 bit number \rightarrow giving square root

largest number
can handle
is 15

largest
number can
handle is

4 for range of 0-15 in 4 bit

so 0-15

so 0-4.

Number	a b	c d	4 bit	Square Root	After estimation	3 bit	xyz
0	00	00	0000	0	0	000	000
1	00	01	0001	1	1	001	001
2	00	10	0010	1.4	1	001	001
3	00	11	0011	1.7	2	010	010
4	01	00	0100	2	2	010	010
5	01	01	0101	2.2	2	010	010
6	01	10	0110	2.5	3	011	011
7	01	11	0111	2.6	3	011	011
8	10	00	1000	2.8	3	011	011
9	10	01	1001	3	3	011	011
10	10	10	1010	3.2	3	011	011
11	10	11	1011	3.3	3	011	011
12	11	00	1100	3.5	4	100	100
13	11	01	1101	3.6	4	100	100
14	11	10	1110	3.7	4	100	100
15	11	11	1111	3.9	4	100	100

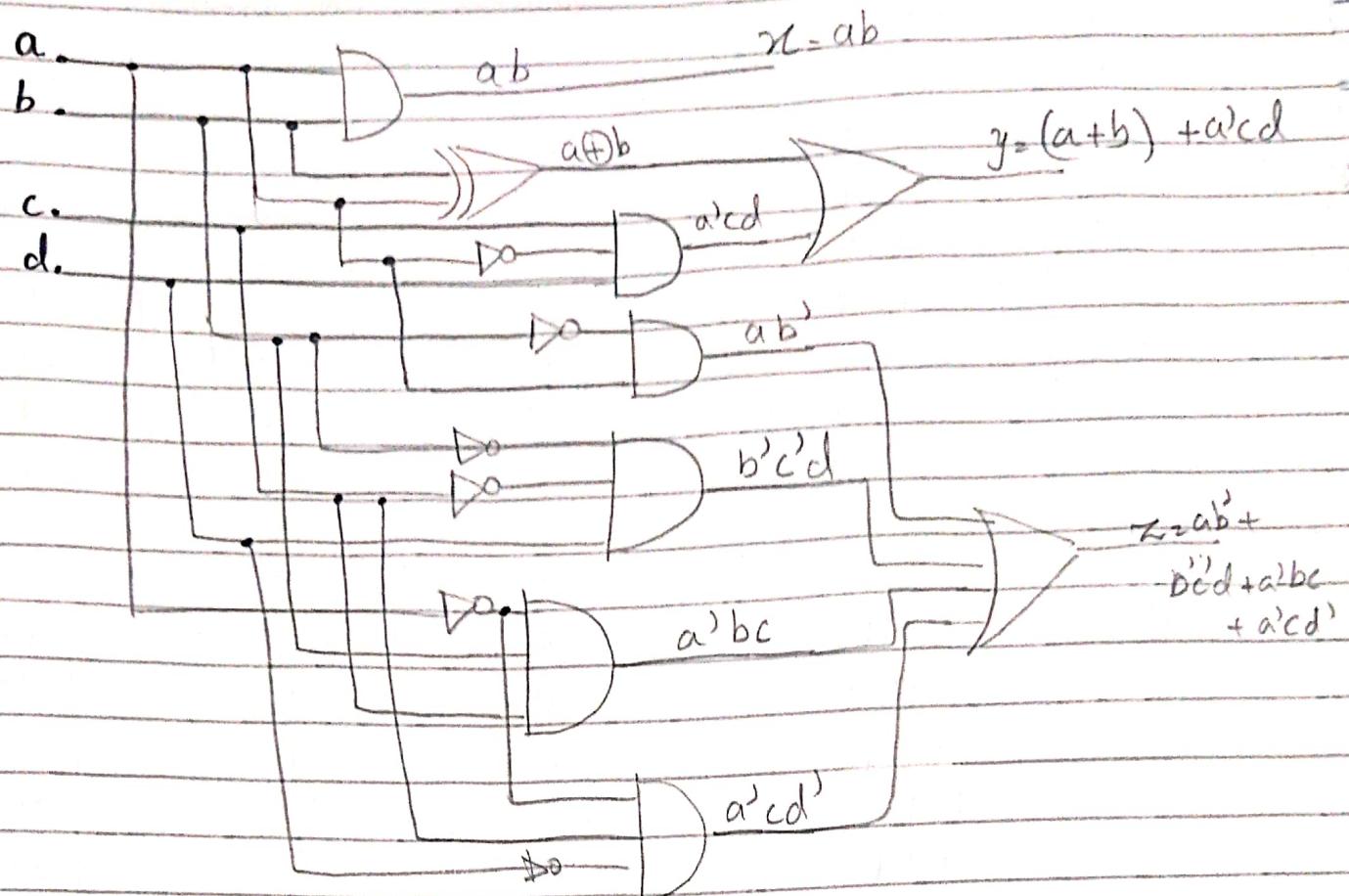
X	ab	cd	c'd'	c'd	cd	cd'	Yab	cd	00	01	11	10	Zab	cd	00	01	11	10
$\bar{a}b$	00	0	1	3	2		00	00	0	1	1	2	00	0	1	3	1	
$a'b$	01	4	5	7	6		01	1	1	1	1	1	01	4	5	1	1	
ab	11	1 ₁₂	1 ₁₃	1 ₁₅	1 ₁₄		11	12	13	15	14	11	11	2	3	15	14	
ab'	10	8	9	11	10		10	11	8	1	9	11	10	10	1	1	15	14

$$n = ab$$

$$y = ab' + a'b + a'cd$$

$$y = (a \oplus b) + a'cd$$

$$z = ab' + c'db' + a'b'c + a'c'd$$



Q4

a.	case	M	A	B	Sum	C	V
(a)	0	0 (Addition)	0111	0110	1101	0	0
(b)	0		1000	1001	0001	1	1
(c)	1		1100	1000	0100	1	0
(d)	1		0101	1010	1011	0	1
(e)	1		0000	0001	1111	0	1

(a) $M \oplus B$

$$A + B = \begin{array}{r} 0111 \\ + 0110 \\ \hline 1101 \end{array} \text{ +ve}$$

$$0 \oplus B = B$$
 ~~$0 \oplus B = B$~~

$$\text{Sum} = 1101 \text{ +ve}$$

$$\text{Carry} = 0$$

$$\text{Overflow} = 0$$

(b) $M \oplus B$

$$A + B = \begin{array}{r} 1000 \\ + 1001 \\ \hline 11001 \end{array} \text{ -ve}$$

$$0 \oplus B = B$$

$$\text{Sum} = 11001 \text{ +ve}$$

$$\text{Carry} = 1$$

$$\text{Overflow} = 1$$

$$(c) M \oplus B = 1 \oplus B = \bar{B} \quad \bar{B} = 0.111 \text{ (2's complement)}$$

$$A + 1 + \bar{B} = 1100 \quad -ve$$

$$\begin{array}{r} 0111 \\ + 1 \\ \hline \end{array} \quad +ve.$$

$$\text{Sum} = \boxed{1} 0100 \quad +ve.$$

Carry = 1 Overflow = 0

$$(d) M \oplus B = 1 \oplus B = \bar{B} \quad \bar{B}_2 = 0101$$

$$A + \bar{B} + 1 = \begin{array}{r} 0101 \\ 0101 \\ + 1 \\ \hline \end{array} \quad +ve$$

$$\text{Sum} = 1011 \quad -ve.$$

Overflow = 1

Carry = 0.

$$(e) M \oplus B = 1 \oplus B = \bar{B} \quad \bar{B}_2 = 0001 \oplus 1_2 = 1110$$

$$A + \bar{B} + 1 = \begin{array}{r} 0000 \\ 1110 \\ + 1 \\ \hline \end{array} \quad +ve$$

$$\text{Sum} = 1111 \quad -ve$$

Overflow = 1 Carry = 0

$$\text{Sum}_0 = S_0 = 1101 \quad S_1 = 0001 \quad S_2 = 0100 \quad S_3 = 1011$$

Carry = C = 0

$$\text{Overflow} = V = C_3 \oplus C_4 = 0 \oplus 0 = 0.$$

$$b. P_i = A_i + B_i \quad | \quad G_i = A_i B_i \quad |$$

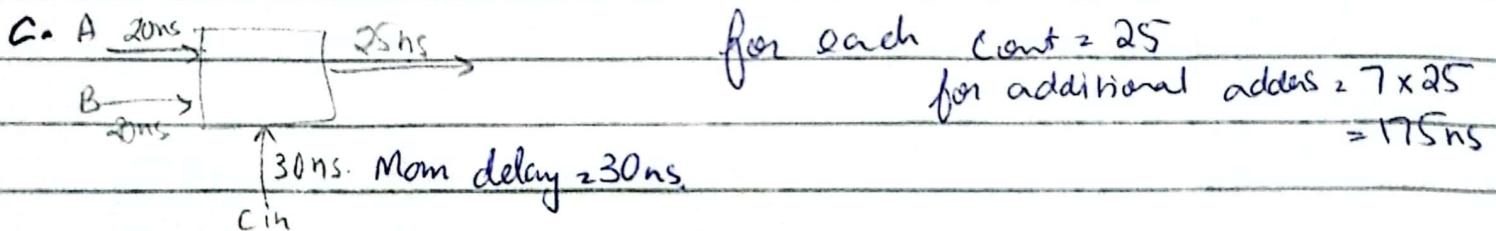
$$C_{i+1} = (C_i G_i + P_i) \quad \text{Demorgan rule.}$$

$$= (C_i^{\prime} G_i^{\prime})^{\prime} (P_i)$$

$$= (C_i + G_i) P_i = P_i C_i + P_i G_i$$

$$\begin{aligned}
 &= C_i (A_i + B_i) + (A_i + B_i) A_i B_i \\
 &= C_i (A_i + B_i) + (A_i A_i B_i + B_i B_i A_i) \quad \text{Indirectly have} \\
 &\rightarrow C_i (A_i + B_i) + (A_i B_i + B_i A_i) \\
 &= C_i (A_i + B_i) + A_i B_i \\
 C_{i+1} &= C_i P_i + G_i
 \end{aligned}$$

$$\begin{aligned}
 S_i &= (P_i G_i') \oplus C_i \\
 &= ((A_i + B_i)(A_i B_i)') \oplus C_i \\
 &= ((A_i + B_i) \cdot (A_i' + B_i')) \oplus C_i \\
 &= (A_i A_i' + A_i B_i' + B_i A_i + B_i B_i') \oplus C_i \\
 &= (0 + A_i B_i' + B_i A_i + 0) \oplus C_i \\
 &= (A_i B_i' + A_i' B_i) \oplus C_i \\
 &= (A_i \oplus B_i) \oplus C_i \\
 S_1 &= A_i \oplus B_i \oplus C_i \\
 S_i &= (P_i) \oplus C_i
 \end{aligned}$$



$$\text{Total Delay} = 30 + 175 = 205\text{ns}$$

Haven't done Q5 and Q6 Yet