

SC1238 A3

$$1. m_a - m_b = -2.5 \log(d_b^2 / d_a^2)$$

$$m_b = -2.5 \log(d_b^2 / 16 d_b^2) + 2.5 \\ = 5.51$$

$$2. a) n = \frac{M_s}{M_p} / \left( \frac{4}{3} \pi R^3 \right)$$

$$= \frac{1.989 \times 10^{33}}{10^{-24}} / \left( \frac{4}{3} \pi (6.958 \times 10^{10})^3 \right)$$

$$= 1.39 \times 10^{24} \text{ particles/cm}^3$$

$$b) \because M = 18 M \sqrt{\frac{T^3}{n}}$$

$$\therefore T = \left( \left( \frac{1}{18} \right)^2 n \right)^{\frac{1}{3}}$$

$$= 1.63 \times 10^7 \text{ K}$$

c) The actual internal core temp is  $1.5 \times 10^7 \text{ K}$ , which is a bit lower than my estimate.

3. refer to plot.