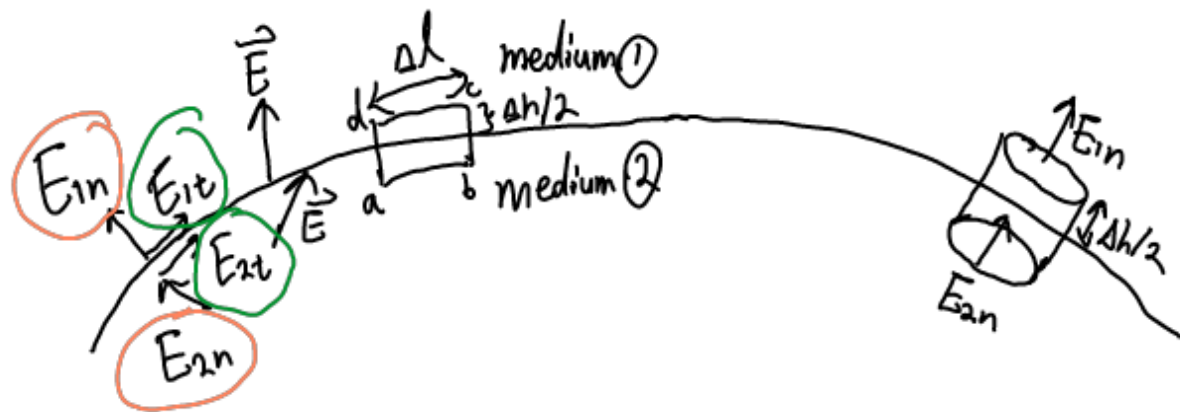


# Boundary Conditions

## Electrostatic B.C.

normal  
tangentia



$$\oint_{\text{path}} \vec{E} \cdot d\vec{l} = 0$$

$$= \int_a^b + \int_b^c + \int_c^d + \int_d^a$$

$$= E_{2t} \Delta l + 0 + (-E_{1t} \Delta l) + 0 = 0$$

$$\therefore E_{2t} = E_{1t}$$

btw  
 $\vec{D} = \epsilon \vec{E}$

## Gauss' Law

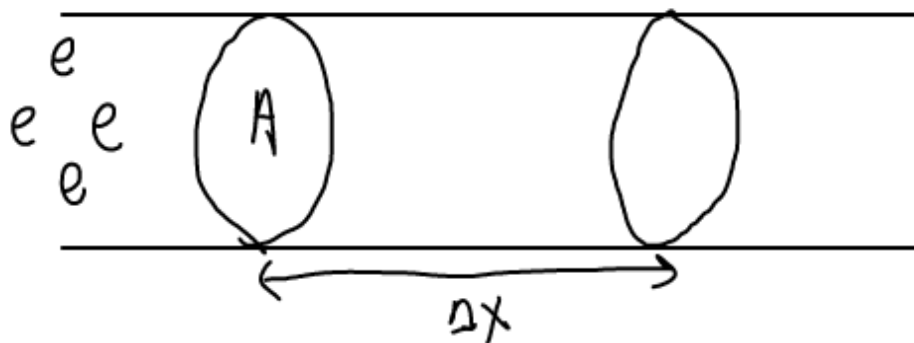
$$\oint_{\text{closed } S} \vec{E} \cdot d\vec{s} = \frac{Q}{\epsilon_0}$$

$$Q = \rho_s A$$

$$\Rightarrow E_{1n} A - E_{2n} A = \frac{\rho_s A}{\epsilon_0}$$

$$E_{1n} - E_{2n} = \frac{\rho_s}{\epsilon_0}$$

\*The normal components are disconnected by  $\rho_s / \epsilon_0$ . \* maybe



$i_e \equiv$  electron current  $\frac{1}{\text{sec}}$

$N_e \equiv$  # electrons passing through A in  $\Delta t$ .

$$V_d = \frac{\Delta x}{\Delta t}$$

$n_e \equiv$  # density of e  $\left( \frac{\text{electron}}{\text{m}^3} \right)$

$$N_e = n_e (\text{Volume}) = n_e A \Delta x = n_e A V_d \Delta t$$

$$N_e = i_e \Delta t \Rightarrow \boxed{i_e = n_e A V_d}$$

$$I = e i_e \frac{\text{Coulomb}}{\text{sec}}$$

$$\boxed{\begin{array}{c} \uparrow \\ J \equiv \frac{I}{A} = \frac{e n_e A V_d}{A} = e n_e V_d \end{array}}$$

current density

$$\boxed{J = \sigma E}$$