

$$f(x) = a_0 + \sum_{n=1}^{\infty} a_n \cos n\pi x + b_n \sin n\pi x$$

$$a_0 = \frac{1}{2L} \int_{-L}^L f(x) dx = \frac{1}{2\pi} \left(\pi^2 + \frac{1}{2}\pi^2 \right) = \frac{3\pi}{4}$$

$$a_n = \frac{1}{L} \int_{-L}^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx$$

$$b_n = \frac{1}{L} \int_{-L}^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx$$

$$a_n = \frac{1}{\pi} \int_0^{\pi} x \cos(nx) dx + \frac{1}{\pi} \int_{-\pi}^0 \pi \cos(nx) dx$$

$$= \frac{1}{\pi} \left[\frac{1}{n^2} \cos(nx) - x \frac{\sin(nx)}{n} \right]_0^{\pi} + \left[\frac{\sin(nx)}{n} \right]_{-\pi}^0$$

=

$$F_c(\omega) = \int_{-\infty}^{\infty} q(\omega) e^{i\omega t} d\omega$$

$$q(\omega) = \frac{1}{2\pi} \int_0^1 v e^{i\omega v} dv$$

$$= \frac{1}{2\pi} \left. \frac{e^{i\omega v} (i\omega v - 1)}{(i\omega)^2} \right|_0^1$$