# **List of Symbols**

Some symbols and abbreviations which are common throughout the book are given below. They have also been explained in the text, occasionally, but not every time they occur. In addition to these symbols, several other symbols have been used in the text, and they have been explained at the places they occur. The parameters occurring in the equations could be dimensionless quantities or may have dimensions. At those places where the equations are in the dimensionless form, the method of dimensionalization has been mentioned or referred to reference indicated in the text.

For the notations used for the function spaces, the reader is referred to Appendices A–D. The same have been explained in the text, occasionally.

Standard notations have been used for the numbering of equations, figures, definitions and propositions. For example, Eq. (7.2.7) refers to the seventh equation in the second section of Chapter 7.

$c(x,t), \bar{c}(x,t)$	concentration $(kg m^{-3})$
C	specific heat $(J kg^{-1} K^{-1})$
$C_V$	specific heat at constant volume
$C_P$	specific heat at constant pressure
$\hat{C}$	heat capacity $(J K^{-1} m^{-3})$
e	specific internal energy (J $\mbox{kg}^{-1}$ ); also used for energy per unit volume (indicated in the text)
H	enthalpy (J); also enthalpy per unit volume (indicated in the text)
h	specific enthalpy (J kg <sup>-1</sup> )
$h_t$	heat transfer coefficient (W $K^{-1}$ m <sup>-2</sup> )
k	thermal diffusivity (m <sup>2</sup> s <sup>-1</sup> )
K	thermal conductivity in the isotropic case (J $\mathrm{m}^{-1}\mathrm{s}^{-1}\mathrm{K}^{-1}$ )
$K_{ij}$	thermal conductivity coefficients in an anisotropic case; $i = 1, 2, 3$ and $j = 1, 2, 3$
$\bar{K}_{C}$	mean curvature of the free boundary $(m^{-1})$
1	latent heat of fusion $(J kg^{-1})$
$l_m$	latent heat per unit mole (J kmol <sup>-1</sup> )
î	$l + (C_L - C_S)T_m$
$R^n$	$n \ge 1$ , real <i>n</i> -dimensional space, $R$ or $R^1$ used for real line
S(t)	$x = S(t) \ (x = S(y, z, t))$ , equation of the phase-change boundary in one-dimension (three-dimension)

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- $\hat{s}$  specific entropy (J kg<sup>-1</sup> K<sup>-1</sup>)
- $\hat{S}$  entropy  $(J K^{-1})$
- t real time (s)
- T temperature (K)
- $T_m$  ideal equilibrium melting/freezing temperature, also taken as 0 or 1
- $T_m^c$  equilibrium phase change temperature in supercooling/superheating
- $V_m$  molar volume (m<sup>3</sup> kmol<sup>-1</sup>)
- $\vec{n}$  unit normal vector

### Subscripts

- (L, S, M) liquid, solid and mushy regions
- i = 1, 2 quantities in the two phases

#### **Greek Symbols**

- $\rho$  density (kg m<sup>-3</sup>)
- $\sigma$  surface tension (N m<sup>-1</sup>)

#### Some Other Symbols

- differentiation with respect to the argument
- time derivative
- $\nabla f$  gradient of a scalar function
- $\nabla^2$  Laplacian operator
- Ei(x) Exponential integral
- erf(x) error function
- $\operatorname{erfc}(x)$  1  $\operatorname{erf}(x)$
- $i^n$ erfe(x) Iterated error function

#### Abbreviations

meas (A) measure of the set A

ADM Adomian decomposition method

ARIM Alternate refined heat balance integral method

CEF classical enthalpy formulation

CES classical enthalpy solution

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CODP constrained oxygen-diffusion problem

CSS classical Stefan solution

EHBIM Enthalpy heat balance integral method

HAM Homotopy analysis method
HBIM Heat balance integral method
HPM Homotopy pertubation method

HSP Hele-Shaw problem

MIM Method of integral manifold
MWR Method of weighted residual
ODP oxygen-diffusion problem
QSSP quasi steady-state problem

RHBM, RIM Refined heat balance integral method

SPF standard phase-field model SSP supercooled Stefan problem

UODP unconstrained ODP
WS weak solution