

Contents

CONTEXT SR0_Path	2
CONTEXT SR1_Block	3
CONTEXT SR2_Point	4
CONTEXT SR3_Signal	5
MACHINE SR_M0	6
MACHINE SR_M1	8
MACHINE SR_M2	12
MACHINE SR_M3	17

CONTEXT SR0_Path**SETS**

PATH

ROUTE

CONSTANTS

PathConflict

Route2InitPath

PathSub

NullPath

AXIOMS**axm1:** $PathConflict \in PATH \leftrightarrow PATH$ **axm2:** $\forall p \cdot p \in PATH \Rightarrow (PathConflict \cap id = \emptyset)$ **axm3:** $\forall p \cdot p \in PATH \Rightarrow (PathConflict = PathConflict^{-1})$ **axm4:** $\forall p \cdot p \in PATH \Rightarrow (finite(PATH))$ **axm5:** $Route2InitPath \in ROUTE \rightarrow PATH$ **axm6:** *(theorem)* $PathSub \in PATH \leftrightarrow PATH$ **axm7:** $\forall p \cdot p \in PATH \Rightarrow (\forall p1, p2 \cdot p1 \in PathSub[\{p2\}] \wedge p \notin PathConflict[\{p2\}] \Rightarrow p \notin PathConflict[\{p1\}])$ **axm8:** $\forall p \cdot p \in PATH \Rightarrow NullPath \in PathSub[\{p\}]$ **axm9:** $NullPath \in PATH$ **END**

CONTEXT SR1_Block

EXTENDS SR0_Path

SETS

BLOCK

CONSTANTS

Path2Block

PathReduce

PathIncrease

AXIOMS

axm1: $Path2Block \in PATH \leftrightarrow BLOCK$

axm2: $\forall p.p \in PATH \Rightarrow (\forall q.q \notin PathConflict[\{p\}] \Leftrightarrow (Path2Block[\{p\}] \cap Path2Block[\{q\}] = \emptyset))$

axm3: $PathReduce \in (PATH \setminus \{NullPath\}) \rightarrow (BLOCK \rightarrow PATH)$

axm4: $\forall p.p \in PATH \setminus \{NullPath\} \Rightarrow (\exists b.b \in BLOCK \Rightarrow PathReduce(p)(b) \in PathSub[\{p\}])$

axm5: $\forall p.p \in PATH \setminus \{NullPath\} \Rightarrow (\exists b.b \in BLOCK \Rightarrow Path2Block[\{PathReduce(p)(b)\}] = Path2Block[\{p\}] \setminus \{b\})$

axm6: $Path2Block[\{NullPath\}] = \emptyset$

axm7: $PathIncrease \in PATH \rightarrow (BLOCK \rightarrow PATH)$

axm8: $\forall p.p \in PATH \Rightarrow (\exists b.b \in BLOCK \Rightarrow p \in PathSub[\{PathIncrease(p)(b)\}])$

axm9: $\forall p.p \in PATH \Rightarrow (\exists b.b \in BLOCK \Rightarrow Path2Block[\{p\}] \cup \{b\} = Path2Block[\{PathIncrease(p)(b)\}])$

END

CONTEXT SR2_Point

EXTENDS SR1_Block

SETS

POS

ISLOCK

CONSTANTS

POINT

Point2InitPos

Route2Point2Pos

Lock

Unlock

AXIOMS

axm1: $POINT \subseteq BLOCK$

axm2: $Route2Point2Pos \in (ROUTE \leftrightarrow POINT) \rightarrow POS$

axm4: $Point2InitPos \in POINT \rightarrow POS$

axm3: $\forall pos \cdot pos \in POS \Rightarrow (finite(POS))$

axm5: $partition(ISLOCK, \{Lock\}, \{Unlock\})$

END

CONTEXT SR3_Signal

EXTENDS SR2_Point

SETS

SIGNAL

CONSTANTS

Red

Green

AXIOMS

axm1: $\text{partition}(\text{SIGNAL}, \{\text{Red}\}, \{\text{Green}\})$

END

MACHINE SR_M0**SEES** SR0_Path**VARIABLES**

Route_Req

Route_Cel

Route_Occ

Route2Path

INVARIANTS**inv1:** $Route_Req \subseteq ROUTE$ **inv2:** $Route_Cel \subseteq ROUTE$ **inv3:** $Route_Occ \subseteq ROUTE$ **inv4:** $Route2Path \in ROUTE \leftrightarrow PATH$ **inv5:** $\forall r1, r2. (r1 \neq r2 \wedge r1 \in dom(Route2Path) \wedge r2 \in dom(Route2Path)) \Rightarrow (PathConflict^{-1}[Route2Path[\{r1\}]] \cap Route2Path[\{r2\}] = \emptyset)$ **inv6:** $\forall r. r \in Route_Occ \Rightarrow (Route2Path[\{r\}] \neq \emptyset)$ **EVENTS****Initialisation****begin****act1:** $Route_Req := \emptyset$ **act2:** $Route_Cel := \emptyset$ **act3:** $Route_Occ := \emptyset$ **act4:** $Route2Path := \emptyset$ **end****Event** ATS_Request $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

where**grd1:** $r \notin Route_Req$ **then****act1:** $Route_Req := Route_Req \cup \{r\}$ **end****Event** Route_Reserve $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

where**grd1:** $r \in Route_Req$ **grd2:** $r \notin Route_Cel$ **grd3:** $r \notin dom(Route2Path)$ **grd4:** $PathConflict[Route2InitPath[\{r\}]] \cap ran(Route2Path) = \emptyset$ **then****act1:** $Route2Path := Route2Path \cup \{r \mapsto Route2InitPath(r)\}$ **end****Event** Train_Enter $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

where**grd1:** $r \in dom(Route2Path)$ **grd2:** $r \notin Route_Occ$ **then****act1:** $Route_Occ := Route_Occ \cup \{r\}$ **end****Event** Route_Sequential_Release $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

cp

sp

```

where
  grd1:  $r \in \text{Route\_Occ}$ 
  grd2:  $r \in \text{dom}(\text{Route2Path})$ 
  grd3:  $cp = \text{Route2Path}(r)$ 
  grd4:  $cp \neq \text{NullPath}$ 
  grd5:  $sp \in \text{PathSub}[\{cp\}]$ 
then
  act1:  $\text{Route2Path}(r) := sp$ 
end
Event Train_Leave  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  r
where
  grd1:  $r \in \text{Route\_Occ}$ 
  grd2:  $r \in \text{dom}(\text{Route2Path})$ 
  grd3:  $\text{Route2Path}(r) = \text{NullPath}$ 
then
  act1:  $\text{Route\_Occ} := \text{Route\_Occ} \setminus \{r\}$ 
end
Event Route_Release  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  r
where
  grd1:  $r \in \text{dom}(\text{Route2Path})$ 
  grd2:  $\text{Route2Path}(r) = \text{NullPath}$ 
  grd3:  $r \notin \text{Route\_Occ}$ 
then
  act1:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 
  act2:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
end
Event ATS_Cancel  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  r
where
  grd1:  $r \in \text{Route\_Req}$ 
then
  act1:  $\text{Route\_Cel} := \text{Route\_Cel} \cup \{r\}$ 
end
Event Route_Cancel  $\langle \text{ordinary} \rangle \hat{=}$ 
any
  r
where
  grd1:  $r \in \text{Route\_Req}$ 
  grd2:  $r \in \text{Route\_Cel}$ 
  grd3:  $r \notin \text{Route\_Occ}$ 
  grd4:  $r \in \text{dom}(\text{Route2Path})$ 
then
  act1:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
  act2:  $\text{Route\_Cel} := \text{Route\_Cel} \setminus \{r\}$ 
  act3:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 
end
END

```

MACHINE SR_M1**REFINES** SR_M0**SEES** SR1_Block**VARIABLES**

Route_Req
 Route_Cel
 Route_Occ
 Route2Path
 Block2Route
 Route2OccPath

INVARIANTS

inv1: $Block2Route \in BLOCK \leftrightarrow ROUTE$
reserve
inv2: $Route2OccPath \in ROUTE \leftrightarrow PATH$
inv3: $\forall p.p \in PATH \Rightarrow (\forall q.q \notin PathConflict[\{p\}] \Leftrightarrow (Path2Block[\{p\}] \cap Path2Block[\{q\}] = \emptyset))$

EVENTS**Initialisation** *<extended>***begin**

act1: $Route_Req := \emptyset$
act2: $Route_Cel := \emptyset$
act3: $Route_Occ := \emptyset$
act4: $Route2Path := \emptyset$
act5: $Block2Route := \emptyset$
act6: $Route2OccPath := \emptyset$

end**Event** ATS_Request *<ordinary>* $\hat{=}$ **extends** ATS_Request**any***r***where***grd1*: $r \notin Route_Req$ **then***act1*: $Route_Req := Route_Req \cup \{r\}$ **end****Event** Block_Reserve *<ordinary>* $\hat{=}$ **any***r**p***where**

grd1: $r \in Route_Req$
grd2: $r \notin Route_Cel$
grd3: $r \notin dom(Route2Path)$
grd4: $p \in PATH$
grd5: $p = Route2InitPath(r)$
grd6: $Path2Block[\{p\}] \cap dom(Block2Route) = \emptyset$

then*act1*: $Block2Route := Block2Route \cup (Path2Block[\{p\}] \times \{r\})$ **end****Event** Route_Reserve *<ordinary>* $\hat{=}$ **extends** Route_Reserve**any***r***where**

grd1: $r \in Route_Req$
grd2: $r \notin Route_Cel$
grd3: $r \notin dom(Route2Path)$


```

    grd4:  $PathConflict[Route2InitPath[\{r\}]] \cap ran(Route2Path) = \emptyset$ 
    grd5:  $Block2Route^{-1}[\{r\}] = Path2Block[\{Route2InitPath(r)\}]$ 
  then
    act1:  $Route2Path := Route2Path \cup \{r \mapsto Route2InitPath(r)\}$ 
  end
Event Train_Enter  $\langle ordinary \rangle \hat{=}$ 
extends Train_Enter
  any
    r
  where
    grd1:  $r \in dom(Route2Path)$ 
    grd2:  $r \notin Route\_Occ$ 
    grd3:  $r \notin dom(Route2OccPath)$ 
  then
    act1:  $Route\_Occ := Route\_Occ \cup \{r\}$ 
    act2:  $Route2OccPath := Route2OccPath \cup \{r \mapsto NullPath\}$ 
  end
Event Train_Head_Move  $\langle ordinary \rangle \hat{=}$ 
  any
    r
    op
    b
  where
    grd1:  $r \in Route\_Occ$ 
    grd2:  $r \in dom(Route2Path)$ 
    grd4:  $b \in Path2Block[\{Route2Path(r)\}]$ 
    grd5:  $r \in dom(Route2OccPath)$ 
    grd6:  $op = Route2OccPath(r)$ 
    grd7:  $b \notin Path2Block[\{op\}]$ 
  then
    act1:  $Route2OccPath(r) := PathIncrease(op)(b)$ 
  end
Event Train_Rear_Move  $\langle ordinary \rangle \hat{=}$ 
  any
    r
    op
    b
  where
    grd1:  $r \in Route\_Occ$ 
    grd2:  $r \in dom(Route2OccPath)$ 
    grd3:  $op = Route2OccPath(r)$ 
    grd4:  $b \in Path2Block[\{op\}]$ 
    grd5:  $op \neq NullPath$ 
  then
    act1:  $Route2OccPath(r) := PathReduce(op)(b)$ 
  end
Event Block_Release  $\langle ordinary \rangle \hat{=}$ 
extends Route_Sequential_Release
  any
    r
    cp
    sp
    b
  where
    grd1:  $r \in Route\_Occ$ 
    grd2:  $r \in dom(Route2Path)$ 
    grd3:  $cp = Route2Path(r)$ 
    grd4:  $cp \neq NullPath$ 

```

```

    grd5:  $sp \in PathSub[\{cp\}]$ 
    grd6:  $sp = PathReduce(cp)(b)$ 
    grd7:  $r \in dom(Route2OccPath)$ 
    grd8:  $b \notin Path2Block[\{Route2OccPath(r)\}]$ 
  then
    act1:  $Route2Path(r) := sp$ 
  end
Event Train_Leave  $\langle ordinary \rangle \hat{=}$ 
extends Train_Leave
  any
     $r$ 
  where
    grd1:  $r \in Route\_Occ$ 
    grd2:  $r \in dom(Route2Path)$ 
    grd3:  $Route2Path(r) = NullPath$ 
    grd4:  $Block2Route^{-1}[\{r\}] = \emptyset$ 
  then
    act1:  $Route\_Occ := Route\_Occ \setminus \{r\}$ 
  end
Event Route_Release  $\langle ordinary \rangle \hat{=}$ 
extends Route_Release
  any
     $r$ 
  where
    grd1:  $r \in dom(Route2Path)$ 
    grd2:  $Route2Path(r) = NullPath$ 
    grd3:  $r \notin Route\_Occ$ 
  then
    act1:  $Route2Path := \{r\} \triangleleft Route2Path$ 
    act2:  $Route\_Req := Route\_Req \setminus \{r\}$ 
    act3:  $Block2Route := Block2Route \triangleright \{r\}$ 
    act4:  $Route2OccPath := \{r\} \triangleleft Route2OccPath$ 
  end
Event ATS_Cancel  $\langle ordinary \rangle \hat{=}$ 
extends ATS_Cancel
  any
     $r$ 
  where
    grd1:  $r \in Route\_Req$ 
  then
    act1:  $Route\_Cel := Route\_Cel \cup \{r\}$ 
  end
Event Block_Cancel  $\langle ordinary \rangle \hat{=}$ 
  any
     $r$ 
  where
    grd1:  $r \in Route\_Cel$ 
    grd2:  $r \in ran(Block2Route)$ 
    grd3:  $r \notin Route\_Occ$ 
  then
    act1:  $Block2Route := Block2Route \triangleright \{r\}$ 
  end
Event Route_Cancel  $\langle ordinary \rangle \hat{=}$ 
extends Route_Cancel
  any
     $r$ 
  where
    grd1:  $r \in Route\_Req$ 

```

```
    grd2:  $r \in Route\_Cel$ 
    grd3:  $r \notin Route\_Occ$ 
    grd4:  $r \in dom(Route2Path)$ 
    grd5:  $Block2Route^{-1}[\{r\}] = \emptyset$ 
  then
    act1:  $Route\_Req := Route\_Req \setminus \{r\}$ 
    act2:  $Route\_Cel := Route\_Cel \setminus \{r\}$ 
    act3:  $Route2Path := \{r\} \triangleleft Route2Path$ 
  end
END
```

MACHINE SR_M2**REFINES** SR_M1**SEES** SR2_Point**VARIABLES**

Route_Req
 Route_Cel
 Route_Occ
 Route2Path
 Block2Route
 Route2OccPath
 Point2Pos
 Point2Lock

INVARIANTS

inv1: $Point2Pos \in POINT \rightarrow POS$
inv2: $Point2Lock \in POINT \rightarrow ISLOCK$
inv3: $\forall r, po \cdot po \in (Path2Block[\{Route2Path(r)\}] \cap POINT) \wedge r \in dom(Route2Path) \Rightarrow (Point2Pos(po) = Route2Point2Pos(\{r \mapsto po\}))$
inv4: $\forall r, po \cdot po \in (Path2Block[\{Route2Path(r)\}] \cap POINT) \wedge r \in dom(Route2Path) \Rightarrow (Point2Lock(po) = Lock)$

EVENTS**Initialisation** *<extended>***begin**

act1: $Route_Req := \emptyset$
act2: $Route_Cel := \emptyset$
act3: $Route_Occ := \emptyset$
act4: $Route2Path := \emptyset$
act5: $Block2Route := \emptyset$
act6: $Route2OccPath := \emptyset$
act7: $Point2Pos := Point2InitPos$
act8: $Point2Lock := POINT \times \{Unlock\}$

end**Event** ATS_Request *<ordinary>* $\hat{=}$ **extends** ATS_Request**any***r***where****grd1:** $r \notin Route_Req$ **then****act1:** $Route_Req := Route_Req \cup \{r\}$ **end****Event** Block_Reserve *<ordinary>* $\hat{=}$ **extends** Block_Reserve**any***r**p***where**

grd1: $r \in Route_Req$
grd2: $r \notin Route_Cel$
grd3: $r \notin dom(Route2Path)$
grd4: $p \in PATH$
grd5: $p = Route2InitPath(r)$
grd6: $Path2Block[\{p\}] \cap dom(Block2Route) = \emptyset$

then**act1:** $Block2Route := Block2Route \cup (Path2Block[\{p\}] \times \{r\})$ **end**

Event Point_Switch $\langle \text{ordinary} \rangle \hat{=}$

Before Route_Reserve

any

po

r

where

grd1: $r \notin \text{Route_Cel}$

grd2: $r \notin \text{dom}(\text{Route2Path})$

grd3: $po \in \text{Block2Route}^{-1}[\{r\}] \cap \text{POINT}$

grd4: $\text{Point2Pos}(po) \neq \text{Route2Point2Pos}(\{r \mapsto po\})$

grd5: $\text{Point2Lock}(po) = \text{Unlock}$

then

act1: $\text{Point2Pos}(po) := \text{Route2Point2Pos}(\{r \mapsto po\})$

end

Event Point_Lock $\langle \text{ordinary} \rangle \hat{=}$

Before Route_Reserve

any

r

po

where

grd1: $r \notin \text{Route_Cel}$

grd2: $r \notin \text{dom}(\text{Route2Path})$

grd3: $po \in \text{Block2Route}^{-1}[\{r\}] \cap \text{POINT}$

grd4: $\text{Point2Pos}(po) = \text{Route2Point2Pos}(\{r \mapsto po\})$

grd5: $\text{Point2Lock}(po) = \text{Unlock}$

then

act1: $\text{Point2Lock} := \{po \mapsto \text{Lock}\} \Leftarrow \text{Point2Lock}$

end

Event Route_Reserve $\langle \text{ordinary} \rangle \hat{=}$

extends Route_Reserve

any

r

where

grd1: $r \in \text{Route_Req}$

grd2: $r \notin \text{Route_Cel}$

grd3: $r \notin \text{dom}(\text{Route2Path})$

grd4: $\text{PathConflict}[\text{Route2InitPath}[\{r\}]] \cap \text{ran}(\text{Route2Path}) = \emptyset$

grd5: $\text{Block2Route}^{-1}[\{r\}] = \text{Path2Block}[\{\text{Route2InitPath}(r)\}]$

grd6: $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Pos}(po) = \text{Route2Point2Pos}(\{r \mapsto po\}))$

grd7: $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Lock}(po) = \text{Lock})$

then

act1: $\text{Route2Path} := \text{Route2Path} \cup \{r \mapsto \text{Route2InitPath}(r)\}$

end

Event Train_Enter $\langle \text{ordinary} \rangle \hat{=}$

extends Train_Enter

any

r

where

grd1: $r \in \text{dom}(\text{Route2Path})$

grd2: $r \notin \text{Route_Occ}$

grd3: $r \notin \text{dom}(\text{Route2OccPath})$

then

act1: $\text{Route_Occ} := \text{Route_Occ} \cup \{r\}$

act2: $\text{Route2OccPath} := \text{Route2OccPath} \cup \{r \mapsto \text{NullPath}\}$

end

Event Train_Head_Move $\langle \text{ordinary} \rangle \hat{=}$

extends Train_Head_Move

```

    any
      r
      op
      b
    where
      grd1: r ∈ Route_Occ
      grd2: r ∈ dom(Route2Path)
      grd4: b ∈ Path2Block[\{Route2Path(r)\}]
      grd5: r ∈ dom(Route2OccPath)
      grd6: op = Route2OccPath(r)
      grd7: b ∉ Path2Block[\{op\}]
    then
      act1: Route2OccPath(r) := PathIncrease(op)(b)
    end
  Event Train_Rear_Move ⟨ordinary⟩ ≐
  extends Train_Rear_Move
    any
      r
      op
      b
    where
      grd1: r ∈ Route_Occ
      grd2: r ∈ dom(Route2OccPath)
      grd3: op = Route2OccPath(r)
      grd4: b ∈ Path2Block[\{op\}]
      grd5: op ≠ NullPath
    then
      act1: Route2OccPath(r) := PathReduce(op)(b)
    end
  Event Point_Unlock_Release ⟨ordinary⟩ ≐
  Before Block_Release
    any
      r
      cp
      sp
      po
    where
      grd1: r ∈ Route_Occ
      grd2: r ∈ dom(Route2Path)
      grd3: cp = Route2Path(r)
      grd4: sp = PathReduce(cp)(po)
      grd5: r ∈ dom(Route2OccPath)
      grd7: po ∈ POINT
      grd8: po ∉ Path2Block[\{Route2Path(r)\}]
    then
      act1: Point2Lock(po) := Unlock
    end
  Event Block_Release ⟨ordinary⟩ ≐
  extends Block_Release
    any
      r
      cp
      sp
      b
    where
      grd1: r ∈ Route_Occ
      grd2: r ∈ dom(Route2Path)
      grd3: cp = Route2Path(r)
      grd4: cp ≠ NullPath

```

```

    grd5:  $sp \in PathSub[\{cp\}]$ 
    grd6:  $sp = PathReduce(cp)(b)$ 
    grd7:  $r \in dom(Route2OccPath)$ 
    grd8:  $b \notin Path2Block[\{Route2OccPath(r)\}]$ 
  then
    act1:  $Route2Path(r) := sp$ 
  end
Event Train_Leave  $\langle ordinary \rangle \hat{=}$ 
extends Train_Leave
  any
     $r$ 
  where
    grd1:  $r \in Route\_Occ$ 
    grd2:  $r \in dom(Route2Path)$ 
    grd3:  $Route2Path(r) = NullPath$ 
    grd4:  $Block2Route^{-1}[\{r\}] = \emptyset$ 
  then
    act1:  $Route\_Occ := Route\_Occ \setminus \{r\}$ 
  end
Event Route_Release  $\langle ordinary \rangle \hat{=}$ 
extends Route_Release
  any
     $r$ 
  where
    grd1:  $r \in dom(Route2Path)$ 
    grd2:  $Route2Path(r) = NullPath$ 
    grd3:  $r \notin Route\_Occ$ 
  then
    act1:  $Route2Path := \{r\} \triangleleft Route2Path$ 
    act2:  $Route\_Req := Route\_Req \setminus \{r\}$ 
    act3:  $Block2Route := Block2Route \triangleright \{r\}$ 
    act4:  $Route2OccPath := \{r\} \triangleleft Route2OccPath$ 
  end
Event ATS_Cancel  $\langle ordinary \rangle \hat{=}$ 
extends ATS_Cancel
  any
     $r$ 
  where
    grd1:  $r \in Route\_Req$ 
  then
    act1:  $Route\_Cel := Route\_Cel \cup \{r\}$ 
  end
Event Point_Unlock_Cancel  $\langle ordinary \rangle \hat{=}$ 
  Before Train_Enter
  any
     $r$ 
     $po$ 
  where
    grd1:  $r \in Route\_Cel$ 
    grd2:  $r \notin Route\_Occ$ 
    grd3:  $po \in Block2Route^{-1}[\{r\}] \cap POINT$ 
    grd4:  $Point2Lock(po) = Lock$ 
  then
    act1:  $Point2Lock := \{po \mapsto Unlock\} \triangleleft Point2Lock$ 
  end
Event Block_Cancel  $\langle ordinary \rangle \hat{=}$ 
extends Block_Cancel
  any

```

```

      r
where
  grd1: r ∈ Route_Cel
  grd2: r ∈ ran(Block2Route)
  grd3: r ∉ Route_Occ
  grd4:  $\forall po \cdot po \in \text{Block2Route}^{-1}[\{r\}] \cap \text{POINT} \Rightarrow \text{Point2Lock}(po) = \text{Unlock}$ 
then
  act1: Block2Route := Block2Route  $\triangleright \{r\}$ 
end
Event Route_Cancel  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Cancel
any
  r
where
  grd1: r ∈ Route_Req
  grd2: r ∈ Route_Cel
  grd3: r ∉ Route_Occ
  grd4: r ∈ dom(Route2Path)
  grd5:  $\text{Block2Route}^{-1}[\{r\}] = \emptyset$ 
then
  act1: Route_Req := Route_Req  $\setminus \{r\}$ 
  act2: Route_Cel := Route_Cel  $\setminus \{r\}$ 
  act3: Route2Path :=  $\{r\} \triangleleft \text{Route2Path}$ 
end
END

```


MACHINE SR_M3**REFINES** SR_M2**SEES** SR3_Signal**VARIABLES**

Route_Req
 Route_Cel
 Route_Occ
 Route2Path
 Block2Route
 Route2OccPath
 Point2Pos
 Point2Lock
 Route2Signal

INVARIANTS*inv1:* $Route2Signal \in ROUTE \rightarrow SIGNAL$ *inv2:* $\forall r. r \in dom(Route2OccPath) \wedge Route2OccPath(r) \neq NullPath \Rightarrow Route2Signal(r) = Red$ **EVENTS****Initialisation****begin**

act1: $Route_Req := \emptyset$
act2: $Route_Cel := \emptyset$
act3: $Route_Occ := \emptyset$
act4: $Route2Path := \emptyset$
act5: $Block2Route := \emptyset$
act6: $Route2OccPath := \emptyset$
act7: $Point2Pos := Point2InitPos$
act8: $Point2Lock := POINT \times \{Unlock\}$
act9: $Route2Signal := ROUTE \times \{Red\}$

end**Event** ATS_Request $\langle ordinary \rangle \hat{=}$ **extends** ATS_Request**any***r***where***grd1:* $r \notin Route_Req$ **then***act1:* $Route_Req := Route_Req \cup \{r\}$ **end****Event** Block_Reserve $\langle ordinary \rangle \hat{=}$ **extends** Block_Reserve**any***r**p***where**

grd1: $r \in Route_Req$
grd2: $r \notin Route_Cel$
grd3: $r \notin dom(Route2Path)$
grd4: $p \in PATH$
grd5: $p = Route2InitPath(r)$
grd6: $Path2Block[\{p\}] \cap dom(Block2Route) = \emptyset$

then*act1:* $Block2Route := Block2Route \cup (Path2Block[\{p\}] \times \{r\})$ **end****Event** Point_Switch $\langle ordinary \rangle \hat{=}$ **extends** Point_Switch**any**

```

    po
    r
  where
    grd1:  $r \notin \text{Route\_Cel}$ 
    grd2:  $r \notin \text{dom}(\text{Route2Path})$ 
    grd3:  $po \in \text{Block2Route}^{-1}[\{r\}] \cap \text{POINT}$ 
    grd4:  $\text{Point2Pos}(po) \neq \text{Route2Point2Pos}(\{r \mapsto po\})$ 
    grd5:  $\text{Point2Lock}(po) = \text{Unlock}$ 
  then
    act1:  $\text{Point2Pos}(po) := \text{Route2Point2Pos}(\{r \mapsto po\})$ 
  end
Event Point_Lock ⟨ordinary⟩  $\hat{=}$ 
extends Point_Lock
any
  r
  po
  where
    grd1:  $r \notin \text{Route\_Cel}$ 
    grd2:  $r \notin \text{dom}(\text{Route2Path})$ 
    grd3:  $po \in \text{Block2Route}^{-1}[\{r\}] \cap \text{POINT}$ 
    grd4:  $\text{Point2Pos}(po) = \text{Route2Point2Pos}(\{r \mapsto po\})$ 
    grd5:  $\text{Point2Lock}(po) = \text{Unlock}$ 
  then
    act1:  $\text{Point2Lock} := \{po \mapsto \text{Lock}\} \Leftarrow \text{Point2Lock}$ 
  end
Event Route_Reserve ⟨ordinary⟩  $\hat{=}$ 
extends Route_Reserve
any
  r
  where
    grd1:  $r \in \text{Route\_Req}$ 
    grd2:  $r \notin \text{Route\_Cel}$ 
    grd3:  $r \notin \text{dom}(\text{Route2Path})$ 
    grd4:  $\text{PathConflict}[\text{Route2InitPath}[\{r\}]] \cap \text{ran}(\text{Route2Path}) = \emptyset$ 
    grd5:  $\text{Block2Route}^{-1}[\{r\}] = \text{Path2Block}[\{\text{Route2InitPath}(r)\}]$ 
    grd6:  $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Pos}(po) = \text{Route2Point2Pos}(\{r \mapsto po\}))$ 
    grd7:  $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Lock}(po) = \text{Lock})$ 
  then
    act1:  $\text{Route2Path} := \text{Route2Path} \cup \{r \mapsto \text{Route2InitPath}(r)\}$ 
  end
Event Signal_Green_Reserve ⟨ordinary⟩  $\hat{=}$ 
any
  r
  where
    grd1:  $r \in \text{dom}(\text{Route2Path})$ 
    grd2:  $r \in \text{Route\_Req}$ 
    grd3:  $r \notin \text{Route\_Cel}$ 
    grd4:  $\text{Block2Route}^{-1}[\{r\}] = \text{Path2Block}[\{\text{Route2InitPath}(r)\}]$ 
    grd5:  $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Pos}(po) = \text{Route2Point2Pos}(\{r \mapsto po\}))$ 
    grd6:  $\forall po. (po \in (\text{Path2Block}[\text{Route2InitPath}[\{r\}]] \cap \text{POINT})) \Rightarrow (\text{Point2Lock}(po) = \text{Lock})$ 
    grd7:  $r \notin \text{Route\_Occ}$ 
    grd8:  $r \notin \text{dom}(\text{Route2OccPath})$ 
  then
    act1:  $\text{Route2Signal} := \{r \mapsto \text{Green}\} \Leftarrow \text{Route2Signal}$ 
  end
Event Train_Enter ⟨ordinary⟩  $\hat{=}$ 

```

```

extends Train_Enter
  any
    r
  where
    grd1: r ∈ dom(Route2Path)
    grd2: r ∉ Route_Occ
    grd3: r ∉ dom(Route2OccPath)
    grd4: Route2Signal(r) = Green
  then
    act1: Route_Occ := Route_Occ ∪ {r}
    act2: Route2OccPath := Route2OccPath ∪ {r ↦ NullPath}
  end
Event Signal_Red_Occupied ⟨ordinary⟩ ≐
  any
    r
  where
    grd1: r ∈ dom(Route2Path)
    grd2: r ∉ Route_Occ
    grd3: Route2Signal(r) = Green
    grd4: r ∈ dom(Route2OccPath)
    grd5: Route2OccPath(r) = NullPath
  then
    act1: Route2Signal(r) := Red
  end
Event Train_Head_Move ⟨ordinary⟩ ≐
extends Train_Head_Move
  any
    r
    op
    b
  where
    grd1: r ∈ Route_Occ
    grd2: r ∈ dom(Route2Path)
    grd4: b ∈ Path2Block[{Route2Path(r)}]
    grd5: r ∈ dom(Route2OccPath)
    grd6: op = Route2OccPath(r)
    grd7: b ∉ Path2Block[{op}]
    grd8: Route2Signal(r) = Red
  then
    act1: Route2OccPath(r) := PathIncrease(op)(b)
  end
Event Train_Rear_Move ⟨ordinary⟩ ≐
extends Train_Rear_Move
  any
    r
    op
    b
  where
    grd1: r ∈ Route_Occ
    grd2: r ∈ dom(Route2OccPath)
    grd3: op = Route2OccPath(r)
    grd4: b ∈ Path2Block[{op}]
    grd5: op ≠ NullPath
  then
    act1: Route2OccPath(r) := PathReduce(op)(b)
  end
Event Point_Unlock_Release ⟨ordinary⟩ ≐
extends Point_Unlock_Release

```

```

any
  r
  cp
  sp
  po
where
  grd1:  $r \in \text{Route\_Occ}$ 
  grd2:  $r \in \text{dom}(\text{Route2Path})$ 
  grd3:  $cp = \text{Route2Path}(r)$ 
  grd4:  $sp = \text{PathReduce}(cp)(po)$ 
  grd5:  $r \in \text{dom}(\text{Route2OccPath})$ 
  grd7:  $po \in \text{POINT}$ 
  grd8:  $po \notin \text{Path2Block}[\{\text{Route2Path}(r)\}]$ 
  grd9:  $\text{Route2Signal}(r) = \text{Red}$ 
then
  act1:  $\text{Point2Lock}(po) := \text{Unlock}$ 
end
Event Block_Release  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Block_Release
any
  r
  cp
  sp
  b
where
  grd1:  $r \in \text{Route\_Occ}$ 
  grd2:  $r \in \text{dom}(\text{Route2Path})$ 
  grd3:  $cp = \text{Route2Path}(r)$ 
  grd4:  $cp \neq \text{NullPath}$ 
  grd5:  $sp \in \text{PathSub}[\{cp\}]$ 
  grd6:  $sp = \text{PathReduce}(cp)(b)$ 
  grd7:  $r \in \text{dom}(\text{Route2OccPath})$ 
  grd8:  $b \notin \text{Path2Block}[\{\text{Route2OccPath}(r)\}]$ 
then
  act1:  $\text{Route2Path}(r) := sp$ 
end
Event Train_Leave  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Train_Leave
any
  r
where
  grd1:  $r \in \text{Route\_Occ}$ 
  grd2:  $r \in \text{dom}(\text{Route2Path})$ 
  grd3:  $\text{Route2Path}(r) = \text{NullPath}$ 
  grd4:  $\text{Block2Route}^{-1}[\{r\}] = \emptyset$ 
then
  act1:  $\text{Route\_Occ} := \text{Route\_Occ} \setminus \{r\}$ 
end
Event Route_Release  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Release
any
  r
where
  grd1:  $r \in \text{dom}(\text{Route2Path})$ 
  grd2:  $\text{Route2Path}(r) = \text{NullPath}$ 
  grd3:  $r \notin \text{Route\_Occ}$ 
then
  act1:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 

```

```

    act2: Route_Req := Route_Req \ {r}
    act3: Block2Route := Block2Route  $\triangleright$  {r}
    act4: Route2OccPath := {r}  $\triangleleft$  Route2OccPath
  end
Event ATSCancel  $\langle$ ordinary $\rangle \hat{=}$ 
extends ATSCancel
  any
    r
  where
    grd1: r  $\in$  Route_Req
  then
    act1: Route_Cel := Route_Cel  $\cup$  {r}
  end
Event Signal_Red_Cancel  $\langle$ ordinary $\rangle \hat{=}$ 
  any
    r
  where
    grd1: r  $\in$  Route_Cel
    grd2: Route2Signal(r) = Green
    grd3: r  $\in$  dom(Route2Path)
    grd4: r  $\notin$  Route_Occ
  then
    act1: Route2Signal := {r  $\mapsto$  Red}  $\triangleleft$  Route2Signal
  end
Event Point_Unlock_Cancel  $\langle$ ordinary $\rangle \hat{=}$ 
extends Point_Unlock_Cancel
  any
    r
    po
  where
    grd1: r  $\in$  Route_Cel
    grd2: r  $\notin$  Route_Occ
    grd3: po  $\in$  Block2Route-1{r}  $\cap$  POINT
    grd4: Point2Lock(po) = Lock
    grd5: Route2Signal(r) = Red
  then
    act1: Point2Lock := {po  $\mapsto$  Unlock}  $\triangleleft$  Point2Lock
  end
Event Block_Cancel  $\langle$ ordinary $\rangle \hat{=}$ 
extends Block_Cancel
  any
    r
  where
    grd1: r  $\in$  Route_Cel
    grd2: r  $\in$  ran(Block2Route)
    grd3: r  $\notin$  Route_Occ
    grd4:  $\forall po \cdot po \in \text{Block2Route}^{-1}\{r\} \cap \text{POINT} \Rightarrow \text{Point2Lock}(po) = \text{Unlock}$ 
  then
    act1: Block2Route := Block2Route  $\triangleright$  {r}
  end
Event Route_Cancel  $\langle$ ordinary $\rangle \hat{=}$ 
extends Route_Cancel
  any
    r
  where
    grd1: r  $\in$  Route_Req
    grd2: r  $\in$  Route_Cel
    grd3: r  $\notin$  Route_Occ

```

```
    grd4:  $r \in \text{dom}(\text{Route2Path})$ 
    grd5:  $\text{Block2Route}^{-1}[\{r\}] = \emptyset$ 
  then
    act1:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
    act2:  $\text{Route\_Cel} := \text{Route\_Cel} \setminus \{r\}$ 
    act3:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 
  end
END
```