

Contents

CONTEXT SR0_Path	2
CONTEXT SR1_Block	3
CONTEXT SR2_Point	4
CONTEXT SR3_TVD	5
CONTEXT SR4_Signal	6
MACHINE SR_M0	7
MACHINE SR_M1	9

CONTEXT SR0_Path**SETS**

PATH

ROUTE

CONSTANTS

PathConflict

Route2InitPath

PathSub

NullPath

AXIOMS**assocMult_Path_conflic:** $PathConflict \in PATH \leftrightarrow PATH$ **axm1:** $\forall p \cdot p \in PATH \Rightarrow (PathConflict \cap id = \emptyset)$ **axm2:** $\forall p \cdot p \in PATH \Rightarrow (PathConflict = PathConflict^{-1})$ **axm3:** $\forall p \cdot p \in PATH \Rightarrow (finite(PATH))$ **assocRoute2Path:** $Route2InitPath \in ROUTE \rightarrow PATH$ **assocPath_SubPath:** $PathSub \in PATH \leftrightarrow PATH$ **axm4:** $\forall p \cdot p \in PATH \Rightarrow (\forall p1, p2 \cdot p1 \in PathSub[\{p2\}] \wedge p \notin PathConflict[\{p2\}] \Rightarrow p \notin PathConflict[\{p1\}])$ **axm5:** $\forall p \cdot p \in PATH \Rightarrow NullPath \in PathSub[\{p\}]$ **axm6:** $NullPath \in PATH$ **END**

CONTEXT SR1_Block

EXTENDS SR0_Path

SETS

BLOCK

CONSTANTS

Path2Block

PathReduce

AXIOMS

axm1: $Path2Block \in PATH \leftrightarrow BLOCK$

axm2: $\forall p \cdot p \in PATH \Rightarrow (\forall q \cdot q \notin PathConflict[\{p\}] \Leftrightarrow (Path2Block[\{p\}] \cap Path2Block[\{q\}] = \emptyset))$

axm3: $PathReduce \in \{PATH \setminus \{NullPath\}\} \rightarrow (BLOCK \rightarrow PATH)$

axm4: $\forall p \cdot p \in PATH \setminus \{NullPath\} \Rightarrow (\exists b \cdot b \in BLOCK \Rightarrow PathReduce(\{p\})(b) \in PathSub[\{p\}])$

axm5: $\forall p \cdot p \in PATH \setminus \{NullPath\} \Rightarrow (\exists b \cdot b \in BLOCK \Rightarrow Path2Block[\{PathReduce(\{p\})(b)\}] = Path2Block[\{p\}] \setminus \{b\})$

axm6: $Path2Block[\{NullPath\}] = \emptyset$

END

CONTEXT SR2_Point

EXTENDS SR1_Block

SETS

POS

CONSTANTS

POINT

Default_Point2Pos

Route_Point2Pos

AXIOMS

axm1: $POINT \subseteq BLOCK$

axm2: $Route_Point2Pos \in Route \rightarrow (POINT \rightarrow POS)$

axm4: $Default_Point2Pos \in POINT \rightarrow POS$

axm3: $\forall pos \cdot pos \in POS \Rightarrow (finite(POS))$

END

CONTEXT SR3_TVD

EXTENDS SR2_Point

SETS

STATUS

CONSTANTS

Vacant

Occupied

AXIOMS

axm1: $\text{partition}(\text{STATUS}, \{\text{Vacant}\}, \{\text{Occupied}\})$

END

CONTEXT SR4_Signal

EXTENDS SR3_TVD

SETS

ASPECT

CONSTANTS

Go

Stop

AXIOMS

axm1: $\text{partition}(\text{ASPECT}, \{\text{Go}\}, \{\text{Stop}\})$

END

MACHINE SR_M0**SEES** SR0_Path**VARIABLES**

Route_Req
 Route_Cel
 Route_Occ
 Route2Path

INVARIANTS

typeof_Route_Res: $Route_Req \subseteq ROUTE$
typeof_Route_Cel: $Route_Cel \subseteq ROUTE$
typeof_Route_Occ: $Route_Occ \subseteq ROUTE$
safety_Req: $\forall r1, r2. (r1 \neq r2 \wedge r1 \in Route_Occ \wedge r2 \in Route_Occ) \Rightarrow (PathConflict^{-1}[Route2Path[\{r1\}]] \cap Route2Path[\{r2\}] = \emptyset)$
typeof_CurrRoute2Path: $\langle \text{theorem} \rangle Route2Path \in ROUTE \leftrightarrow PATH$
inv1: $\forall r. r \in Route_Occ \Rightarrow (Route2Path[\{r\}] \neq \emptyset)$

EVENTS**Initialisation****begin**

act1: $Route_Req := \emptyset$
act5: $Route_Cel := \emptyset$
act2: $Route_Occ := \emptyset$
act3: $Route2Path := \emptyset$

end**Event** Route_Reserve $\langle \text{ordinary} \rangle \hat{=}$ **any****r****where**

grd1: $r \in Route_Req$
grd2: $r \notin Route_Cel$
grd3: $r \notin dom(Route2Path)$
grd4: $PathConflict[Route2InitPath[\{r\}]] \cap ran(Route2Path) = \emptyset$

then

act1: $Route2Path := Route2Path \cup \{r \mapsto Route2InitPath(r)\}$
act2: $Route_Req := Route_Req \setminus \{r\}$

end**Event** Route_Release2 $\langle \text{ordinary} \rangle \hat{=}$ **any****r****where**

grd1: $r \in dom(Route2Path)$
grd2: $\langle \text{theorem} \rangle Route2Path(r) = NullPath$
grd3: $r \notin Route_Occ$

then

act1: $Route2Path := \{r\} \triangleleft Route2Path$

end**Event** Route_Release1 $\langle \text{ordinary} \rangle \hat{=}$ **any****r****where**

grd1: $r \in Route_Req \cup dom(Route2Path)$
grd2: $r \in Route_Cel$
grd3: $r \notin Route_Occ$

then

act1: $Route_Req := Route_Req \setminus \{r\}$
act2: $Route_Cel := Route_Cel \setminus \{r\}$
act3: $Route2Path := \{r\} \triangleleft Route2Path$

```

    end
Event Train_Enter  $\langle \text{ordinary} \rangle \hat{=}$ 
    any
        r
    where
        grd1:  $r \in \text{dom}(\text{Route2Path})$ 
        grd2:  $r \notin \text{Route\_Occ}$ 
    then
        act1:  $\text{Route\_Occ} := \text{Route\_Occ} \cup \{r\}$ 
    end
Event Train_Leave  $\langle \text{ordinary} \rangle \hat{=}$ 
    any
        r
    where
        grd1:  $r \in \text{Route\_Occ}$ 
        grd2:  $r \in \text{dom}(\text{Route2Path})$ 
    then
        act1:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
        act3:  $\text{Route\_Occ} := \text{Route\_Occ} \setminus \{r\}$ 
        act2:  $\text{Route2Path}(r) := \text{NullPath}$ 
    end
Event Route_Request  $\langle \text{ordinary} \rangle \hat{=}$ 
    any
        r
    where
        grd1:  $r \in \text{ROUTE}$ 
    then
        act1:  $\text{Route\_Req} := \text{Route\_Req} \cup \{r\}$ 
    end
Event Route_Cancel  $\langle \text{ordinary} \rangle \hat{=}$ 
    any
        r
    where
        grd1:  $\langle \text{theorem} \rangle r \in \text{Route\_Req} \cup \text{dom}(\text{Route2Path})$ 
    then
        act1:  $\text{Route\_Cel} := \text{Route\_Cel} \cup \{r\}$ 
    end
END

```


MACHINE SR_M1**REFINES** SR_M0**SEES** SR1_Block**VARIABLES**

Route_Req
 Route_Cel
 Route_Occ
 Route2Path
 Block2Route

INVARIANTS**inv1:** $Block2Route \in BLOCK \leftrightarrow ROUTE$ **inv2:** $\forall p.p \in PATH \Rightarrow (\forall q.q \notin PathConflict[\{p\}] \Leftrightarrow (Path2Block[\{p\}] \cap Path2Block[\{q\}] = \emptyset))$ **EVENTS****Initialisation** $\langle \text{extended} \rangle$ **begin**

act1: $Route_Req := \emptyset$
act5: $Route_Cel := \emptyset$
act2: $Route_Occ := \emptyset$
act3: $Route2Path := \emptyset$
act4: $Block2Route := \emptyset$

end**Event** Block_Reserve $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

p

where

grd1: $r \in Route_Req$
grd3: $r \notin Route_Cel$
grd6: $r \notin Route_Occ$
grd5: $p \in PATH$
grd4: $p = Route2InitPath(r)$
grd2: $Path2Block[\{p\}] \cap dom(Block2Route) = \emptyset$

then**act1:** $Block2Route := Block2Route \cup \{Path2Block(p) \mapsto r\}$ **end****Event** Block_Release2 $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

cp

sp

b

where

grd1: $r \in Route_Occ$
grd2: $r \in dom(Route2Path)$
grd3: $cp = Route2Path(r)$
grd4: $cp \neq NullPath$
grd6: $b \in Path2Block[\{cp\}]$
grd5: $sp = PathReduce(\{cp\})(b)$

then**act1:** $Block2Route := \{b\} \triangleleft Block2Route$ **act2:** $Route2Path(r) := sp$ **end****Event** Block_Release1 $\langle \text{ordinary} \rangle \hat{=}$ **any**

r

where**grd1:** $r \in Route_Cel$

```

    grd2:  $r \in \text{dom}(\text{Route2Path})$ 
    grd3:  $\langle \text{theorem} \rangle r \notin \text{Route\_Occ}$ 
  then
    act1:  $\text{Block2Route} := \text{Block2Route} \triangleright \{r\}$ 
    act2:  $\text{Route2Path}(r) := \text{NullPath}$ 
  end
Event Route_Request  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Request
  any
     $r$ 
  where
    grd1:  $r \in \text{ROUTE}$ 
  then
    act1:  $\text{Route\_Req} := \text{Route\_Req} \cup \{r\}$ 
  end
Event Route_Cancel  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Cancel
  any
     $r$ 
  where
    grd1:  $\langle \text{theorem} \rangle r \in \text{Route\_Req} \cup \text{dom}(\text{Route2Path})$ 
  then
    act1:  $\text{Route\_Cel} := \text{Route\_Cel} \cup \{r\}$ 
  end
Event Route_Reserve  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Reserve
  any
     $r$ 
  where
    grd1:  $r \in \text{Route\_Req}$ 
    grd2:  $r \notin \text{Route\_Cel}$ 
    grd3:  $r \notin \text{dom}(\text{Route2Path})$ 
    grd4:  $\text{PathConflict}[\text{Route2InitPath}[\{r\}]] \cap \text{ran}(\text{Route2Path}) = \emptyset$ 
    grd5:  $\text{Block2Route}^{-1}(r) = \text{Path2Block}(\text{Route2InitPath}(r))$ 
  then
    act1:  $\text{Route2Path} := \text{Route2Path} \cup \{r \mapsto \text{Route2InitPath}(r)\}$ 
    act2:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
  end
Event Route_Release1  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Release1
  any
     $r$ 
  where
    grd1:  $r \in \text{Route\_Req} \cup \text{dom}(\text{Route2Path})$ 
    grd2:  $r \in \text{Route\_Cel}$ 
    grd3:  $r \notin \text{Route\_Occ}$ 
  then
    act1:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
    act2:  $\text{Route\_Cel} := \text{Route\_Cel} \setminus \{r\}$ 
    act3:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 
  end
Event Route_Release2  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Route_Release2
  any
     $r$ 
  where
    grd1:  $r \in \text{dom}(\text{Route2Path})$ 
    grd2:  $\langle \text{theorem} \rangle \text{Route2Path}(r) = \text{NullPath}$ 

```

```

    grd3:  $r \notin \text{Route\_Occ}$ 
  then
    act1:  $\text{Route2Path} := \{r\} \triangleleft \text{Route2Path}$ 
  end
Event Train_Enter  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Train_Enter
  any
     $r$ 
  where
    grd1:  $r \in \text{dom}(\text{Route2Path})$ 
    grd2:  $r \notin \text{Route\_Occ}$ 
  then
    act1:  $\text{Route\_Occ} := \text{Route\_Occ} \cup \{r\}$ 
  end
Event Train_Leave  $\langle \text{ordinary} \rangle \hat{=}$ 
extends Train_Leave
  any
     $r$ 
  where
    grd1:  $r \in \text{Route\_Occ}$ 
    grd2:  $r \in \text{dom}(\text{Route2Path})$ 
    grd3:  $\text{Block2Route}^{-1}[\{r\}] = \emptyset$ 
  then
    act1:  $\text{Route\_Req} := \text{Route\_Req} \setminus \{r\}$ 
    act3:  $\text{Route\_Occ} := \text{Route\_Occ} \setminus \{r\}$ 
    act2:  $\text{Route2Path}(r) := \text{NullPath}$ 
  end
END

```