

## Problem 1:

(1)

```
method1(int[ ] a) // returns integer
    x = 0;
    y = 0;
    for (i=1; i<n; i++) { // n is the number of elements in array a
        if (a[i] == a[i-1]) {
            x = x + 1;
        }
        else {
            y = y + 1;
        }
    }
    return (x - y);
```

**O(n) linear,**

One for loop so  $f(n) = n+1$

(2)

```
method2(int[ ] a, int[ ] b) // assume equal-length arrays
    x = 0;
    i = 0;
    while (i < n) { // n is the number of elements in each array
        y = 0;
        j = 0;
        while (j < n) {
            k = 0
            while (k <= j) {
                y = y + a[k];
                k = k + 1;
            }
            j = j + 1;
        }
        if (b[i] == y) {
            x++;
        }
        i = i + 1;
    }
    return x;
```

**O(n<sup>3</sup>) cubic,**

Three while loop that add one at a time so its  $n^3$

(3)

```
// n is the length of array a
// p is an array of integers of length 2
// initial call: method3(a, n-1, p)
// initially p[0] = 0, p[1] = 0
method3(int[] a, int i, int[] p)
```

---

```
if (i == 0) {
    p[0] = a[0];
    p[1] = a[0];
}
else {
    method3(a, i-1, p);
    if (a[i] < p[0]) {
        p[0] = a[i];
    }
    if (a[i] > p[1]) {
        p[1] = a[i];
    }
}
```

**O(n) linear,**

Recursion method3, i-1 one at a time so its linear

(4)

```
// initial call: method4(a, 0, n-1) // n is the length of array a
public static int method4(int[] a, int x, int y)
    if (x >= y) {return a[x];}
    else {
        z = (x + y) / 2; // integer division
        u = method4(a, x, z);
        v = method4(a, z+1, y);
        if (u < v) return u;
        else return v;
    }
}
```

**O(n) linear,**

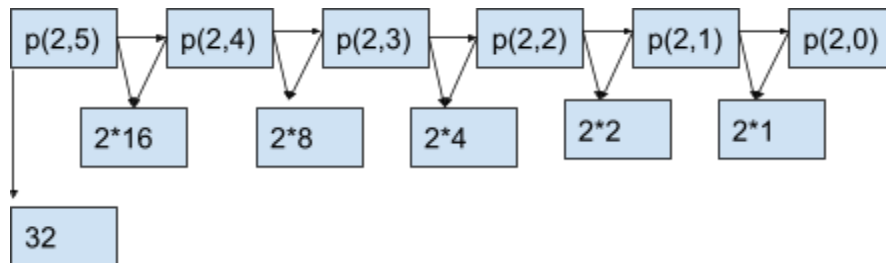
Am I seems like a very confusing Loop but it's actually a linear function because that inside the method4 its will call method 4 two times, so its  $n*2$  but it is still linear

## Problem 2:

(1)

```
Public static double power(double x, int n){
    if (n==0)
        Return 1;
    else
        Return x * power(x, n-1)
}
```

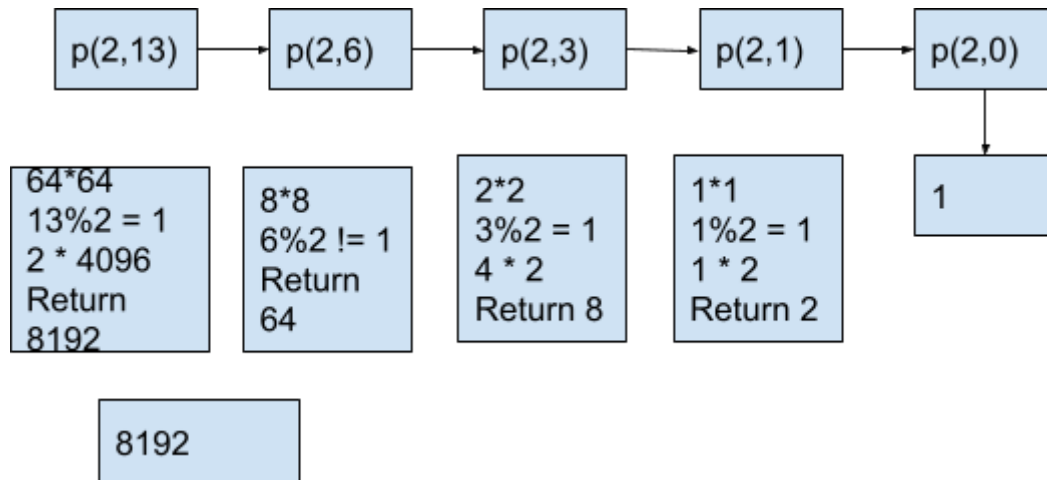
power(2, 5)



(2)

```
Public static double power(double x, int n){
    if (n==0)
        Return 1;
    else
        Double partial = power(x, n/2);
        Double result = partial * partial;
        If (n%2==1)
            Result *= x;
        Return result
}
```

power(2, 13)



### Problem 3:

(1)

operation	Return value	Stack contents
push(10)	-	(10)
pop()	10	()
push(12)	-	(12)
push(20)	-	(12,20)
size()	2	(12,20)
push(7)	-	(12,20,7)
pop()	7	(12,20)
top()	20	(12,20)
pop()	20	(12)
pop()	12	()
push(35)	-	(35)
isEmpty()	false	(35)

(2)

operation	Return value	Queue Contents (first $\leftarrow$ Q $\leftarrow$ last)
enqueue(7)	-	(7)
dequeue( )	7	()
enqueue(15)	-	(15)
enqueue(3)	-	(15,3)
first()	15	(15,3)
dequeue( )	15	(3)
dequeue( )	3	()

first()	null	()
enqueue(11)	-	(11)
dequeue( )	11	()
isEmpty()	true	()
enqueue(5)	-	(5)