

Name:

Score:      /8

Math 1321      Week 12 Lab      Due Thursday 12/4

1. **(2 points)** Let  $W$  be the solid bounded by the planes  $x = 0$ ,  $y = 0$ , and  $z = 2$ , and the surface  $z = x^2 + y^2$ . Compute  $\iiint_W x dx dy dz$ .
2. **(1 points)** Determine the area of the region bounded by two hyperbolas  $xy = 1$ ,  $xy = 2$  and two lines  $y = 2x$  and  $y = \frac{1}{2}x$  in the first quadrant.

3. **(1 point)** Determine the volume of the solid bounded by the cone  $z = 2 - \sqrt{x^2 + y^2}$  and the paraboloid  $z = x^2 + y^2$ .

4. **(2 point)** Determine the volume of the solid bounded by the circular cylinder  $(x - a)^2 + y^2 = a^2$ , the cone  $z = x^2 + y^2$  and the plane  $z = 0$ .

5. **(2 point)** Let  $\Omega$  be the region bounded by the sphere  $x^2 + y^2 + z^2 = 1$  and the plane  $z = 0$ . Compute  $\iiint_{\Omega} \frac{1}{x^2 + y^2 + z^2 + 1} dx dy dz$ .

6. **(2 point)** Determine the center of mass for the solid bounded by the paraboloid  $z = 4 - x^2 - y^2$  and  $z = 0$  with density function  $\rho(x, y, z) \equiv 1$ .