

# 1 RELATIONAL ALGEBRA

- Relations are closed under relational algebra

## 1.1 Unary operators

### 1.1.1 Selection

- $\sigma_c(E)$

### 1.1.2 Projection

- $\pi_{A_1, A_2, \dots, A_n}(E)$

### 1.1.3 Rename

- $\rho_{R(A_1, A_2, \dots, A_n)}(E)$

## 1.2 Set operators

### 1.2.1 Cross product

- $E_1 \times E_2$
- $|E_1 \times E_2| = |E_1| \times |E_2|$

### 1.2.2 Difference

- $E_1 - E_2$

### 1.2.3 Union

- $E_1 \cup E_2$
- $|E_1 \cup E_2| = |E_1| + |E_1 - E_2|$

### 1.2.4 Intersection

- $E_1 \cap E_2 = E_1 - (E_1 - E_2)$

## 1.3 Join operators

### 1.3.1 $\theta$ -join

- $E_1 \bowtie_{\theta} E_2 = \sigma_{\theta}(E_1 \times E_2)$

### 1.3.2 Natural join

- $E_1 \bowtie E_2 = \pi_{\ell_1}(E_1 \bowtie_c \rho_{\ell_2}(E_2))$

## **1.4 Alternate notations**

### **1.4.1 Assignment statements**

- $c := E$
- Provides a way to modularize an expression

### **1.4.2 Expression trees**

- Similar to an AST