

# Can't Steal? Cont-Steal! Contrastive Stealing Attacks Against Image Encoders

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#### **Abstract**

Self-supervised representation learning techniques have been developing rapidly to make full use of unlabeled images. They encode images into rich features that are oblivious to downstream tasks. Behind their revolutionary representation power, the requirements for dedicated model designs and a massive amount of computation resources expose image encoders to the risks of potential model stealing attacks - a cheap way to mimic the well-trained encoder performance while circumventing the demanding requirements. Yet conventional attacks only target supervised classifiers given their predicted labels and/or posteriors, which leaves the vulnerability of unsupervised encoders unexplored.

In this paper, we first instantiate the conventional stealing attacks against encoders and demonstrate their severer vulnerability compared with downstream classifiers. To better leverage the rich representation of encoders, we further propose Cont-Steal, a contrastive-learning-based attack, and validate its improved stealing effectiveness in various experiment settings. As a takeaway, we appeal to our community's attention to the intellectual property protection of representation learning techniques, especially to the defenses against encoder stealing attacks like ours. <sup>1</sup>

# 1. Introduction

Recent years have witnessed the great success of applying deep learning (DL) to computer vision tasks. Different from supervised DL models, self-supervised learning which transforms unlabeled data samples into rich representations, has gained more and more popularity.

Behind its powerful representation, it is non-trivial to obtain a state-of-the-art image encoder. For instance, Sim-CLR [6] uses 128 TPU v3 cores to pre-train a ResNet-

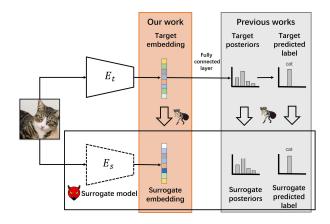


Figure 1. Model stealing attacks against classifiers (previous) v.s. model stealing attacks against encoders (ours). Previous works aim to steal a whole classifier using the predicted label or posteriors of a target model. In our work, we aim to steal the target encoder using its embeddings. The target encoder ( $E_t$ ) is pre-trained and fixed, as shown in the solid frame. The surrogate encoder ( $E_s$ ) is trainable by the adversary, as shown in the dashed frame.

50 encoder with a batch size of 4096. Therefore, many big companies provide cloud-based self-supervised learning encoder services for users. For instance, Cohere,<sup>2</sup> OpenAI,<sup>3</sup> and Clarifai<sup>4</sup> provide the embedding API of images and texts for commercial usage. There are many works [10,26,30] exploring security issues of encoder-based API. Therefore, it is a very important and urgent problem.

These kinds of service leave the possibility of *model stealing attacks* [5, 25, 28, 37, 44, 48, 50, 51]. In these attacks, the adversary aims to steal the parameters or functionalities of target models with only query access to them. A successful model stealing attack does not only threaten

<sup>&</sup>lt;sup>1</sup>See our code in https://github.com/zeyangsha/Cont-Steal.

<sup>2</sup>https://cohere.ai/

<sup>3</sup>https://beta.openai.com/docs/api-reference/ embeddings/

<sup>&</sup>lt;sup>4</sup>https://www.clarifai.com/models/general-image-embedding/

the intellectual property of the target model, but also serves as a stepping stone for further attacks such as adversarial examples [3,4,16,38,47,52], backdoor attacks [7,26,41,43], and membership inference attacks [22–24,30,33,34,40,42,45,46]. So far, model stealing attacks concentrate on the supervised classifiers, i.e., the model responses are prediction posteriors or labels for a specific downstream task. The vulnerability of unsupervised image encoders is unfortunately unexplored.

**Our Work.** To fill this gap, we pioneer the systematic investigation of model stealing attacks against image encoders. In this work, the adversary's goal is to steal the functionalities of the target model. See Figure 1 for an overview and a comparison with previous works. More specifically, we focus on encoders trained by *contrastive learning*, which is one of the most cutting-edge unsupervised representation learning strategies that unleash the information of unlabeled data.

We first instantiate the conventional stealing attacks against encoders and expose their vulnerability. Given an input image, the target encoder outputs its representation (referred to as embedding). Similar to model stealing attacks against classifiers, we consider the embedding as the "ground truth" label to guide the training procedure of a surrogate encoder on the adversary side. To measure the effectiveness of stealing attacks, we train an extra linear layer for the target and surrogate encoders towards the same downstream classification task. Preferably, the surrogate model should achieve both high classification accuracy and high agreement with the target predictions.

We evaluate our attacks on five datasets against four contrastive learning encoders. Our results demonstrate that the conventional attacks are more effective against encoders than against downstream classifiers. For instance, when we steal the downstream classifier pre-trained by SimCLR on CIFAR10 (with posteriors as its responses) using STL10 as the surrogate dataset, the adversary can only achieve an accuracy of 0.359. The accuracy, however, increases to 0.500 instead when we steal its encoder (with the embedding as its response).

Despite its encouraging performance, conventional attacks are not the most suitable ones against encoders. This is because they treat each image-embedding pair individually without interacting across pairs. Different embeddings are beneficial to each other as they can serve as anchors to better locate the position of the other embeddings in their space. Contrastive learning [6, 8, 17, 20, 27, 49, 53] is a straightforward idea to achieve this goal. It is formulated to enforce the embeddings of different augmentations of the same images closer and those of different images further.

In a similar spirit, we propose Cont-Steal, a contrastivelearning-based model stealing attack against the encoder. The goal of Cont-Steal is to enforce the surrogate embedding of an image close to its target embedding (defined as a positive pair) and also push away embeddings of different images irrespective of being generated by the target or the surrogate encoders (defined as negative pairs).

The comprehensive evaluation shows that Cont-Steal outperforms the conventional model stealing attacks to a large extent. For instance, when CIFAR10 is the target dataset, Cont-Steal achieves an accuracy of 0.714 on the SimCLR encoder pretrained on CIFAR10 with the surrogate dataset and downstream dataset being STL10, while the conventional attack only achieves 0.457 accuracy. Also, Cont-Steal is more query-efficient and dataset-independent (see Figure 9 for more details). This is because Cont-Steal leverages higher-order information across samples to mimic the functionality of the target encoder. To mitigate the attacks, we evaluate different defense mechanisms including noise, top-k, rounding, and watermark. Our evaluations show that in most cases, these mechanisms cannot effectively defend against Cont-Steal. Among them, top-k can reduce the attack performance to the largest extent. However, it also strongly limits the target model's utility.

As a takeaway, our attack further exposes the severe vulnerability of pre-trained encoders. We appeal to our community's attention to the intellectual property protection of representation learning techniques, especially to the defenses against encoder stealing attacks like ours.

# 2. Threat Model

In this work, for the encoder pre-trained with images, we consider image classification as the downstream task. We refer to the encoder as the target encoder. Then we treat both the encoder and the linear layer trained for the downstream task together as the target model. We first introduce the adversary's goal and then characterize different background knowledge that the adversary might have.

Adversary's Goal. Following previous work [25, 28, 44], we taxonomize the adversary's goal into two dimensions, i.e., theft and utility. The theft adversary aims to build a surrogate encoder that has similar performance on the downstream tasks as the target encoder. Different from the thief adversary, the goal of the utility adversary is to construct a surrogate encoder that behaves normally on different downstream tasks. In this case, the surrogate encoder not only faithfully "copies" the behaviors of the target encoder, but also serves as a stepping stone to conduct other attacks.

**Adversary's Background Knowledge.** We categorize the adversary's background knowledge into two dimensions, i.e., the knowledge of the target encoder and the distribution of the surrogate dataset.

Regarding knowledge of the target encoder, we assume that the adversary only has black-box access to it, which means that they can only query the target encoder with an input image and obtain the corresponding output, i.e., the embedding of the input image.

Regarding the surrogate dataset that is used to train the surrogate encoder, we consider two cases. First, we assume the adversary has the same training dataset as the target encoder. However, such an assumption may be hard to achieve as such datasets are usually private and protected by the model owner. In a more extreme case, we assume that the adversary has totally no information about the target encoder's training dataset, which means that they can only use a different distribution dataset to conduct the model stealing attacks. We later show that the adversary can still launch effective model stealing attacks against the target encoder given a surrogate dataset that is distributed differently compared to the target dataset.

For the model architecture that is used to train the surrogate encoder, we consider two cases. First, we assume the adversary is aware of the target encoder's architecture and can train the same architecture surrogate encoder. Then we relax our assumption that the adversary uses different architectures to train the surrogate encoder. Our evaluation shows that the choice of architecture does not have much impact on the attack performance (see Table 3), which makes the attack more realistic.

Note that we also compare our attacks against the encoders to the traditional model stealing attacks that focus on the whole classifier (which has an encoder and a linear layer). If the attack targets a whole classifier, we assume the adversary may obtain the posteriors or the predicted label for an input image.

#### 3. Model Stealing Attacks

In this section, we first describe the conventional attacks against the encoders. Then, we propose a novel contrastive stealing framework, Cont-Steal, to steal the encoders more effectively.

# 3.1. Conventional Attacks Against Encoders

The adversary takes two steps to conduct the model stealing attacks against the target encoder and one step for further evaluation.

**Obtain the Surrogate Dataset.** To conduct model stealing attacks, the adversary first needs to obtain a surrogate dataset. Based on the knowledge of the target classifier's training dataset (target dataset), we consider two cases. If the adversary has full knowledge of the target dataset, they can directly leverage the target dataset itself as the surrogate dataset. Or the adversary has no knowledge of the target dataset, which means that they can only construct the surrogate dataset, which is distributed differently from the target dataset.

**Train the Surrogate Encoder.** Slightly different from the classifier, the response of the encoder is an embedding, which is a feature vector. In this case, the adversary can still

leverage a similar loss function to optimize the surrogate encoder, which can be defined as follows:

$$L_{MS} = \sum_{k=1}^{N} l(E_T(x_k), E_S(x_k))$$
 (1)

where  $E_T(\cdot)/E_S(\cdot)$  is the target/surrogate encoder, N is the total number of samples on the surrogate dataset, and  $l(\cdot)$  is the MSE loss.

Apply the Surrogate Encoder to Downstream Tasks. To evaluate the effectiveness of model stealing attacks against the encoder, the adversary can leverage the same downstream task to both the target and surrogate encoders. Concretely, the adversary trains an extra linear layer for the target and surrogate encoders, respectively. Note that we refer to the target/surrogate encoder and the extra linear layer as the target/surrogate classifiers. Then, the adversary quantifies the attack effectiveness by measuring the performance of the target/surrogate classifier on the downstream tasks.

# 3.2. Cont-Steal Attacks Against Encoders

To better leverage the rich information from the embeddings, we propose Cont-Steal, a contrastive learning-based model stealing attacks against encoders, which leverages contrastive learning to enhance the stealing performance. Concretely, Cont-Steal aims to enforce the surrogate embedding of an image to get close to its target embedding (defined as a positive pair), and also push away embeddings of different images regardless of being generated by the target or the surrogate encoders (defined as negative pairs). There are three steps for the adversary to conduct contrastive stealing attacks against encoders and one step for further evaluation.

**Obtain the Surrogate Dataset.** The adversary follows the same strategy as Section 3.1 to obtain the surrogate dataset. **Data Augmentation.** Our proposed Cont-Steal leverages data augmentation to transform an input image into its two augmented views. In this paper, we leverage RandAugment [11] as the augmentation method, which is made up of a group of advanced augmentation operations. Concretely, we set n=2 and m=14 following Cubuk et al. [11] where n denotes the number of transformations to a given sample and m represents the magnitude of global distortion.

**Train the Surrogate Encoder.** Instead of querying the encoders with the original images, the adversary queries the encoders with the augmented views of them. Concretely, for an input image  $x_i$ , we generate two augmented views of it, i.e.,  $\widetilde{x}_{i,s}$  and  $\widetilde{x}_{i,t}$ , where  $\widetilde{x}_{i,s}/\widetilde{x}_{i,t}$  is used to query the surrogate/target encoder. We consider  $(\widetilde{x}_{i,s},\widetilde{x}_{j,t})$  as a positive pair if i=j, and otherwise a negative pair.

Given a mini-batch of N samples, we generate N augmented views as the input of the target encoder and another N augmented views as the input of the surrogate encoders.

Concretely, the loss of Cont-Steal can be formulated as follows:

$$D_{encoder}^{+}(i) = exp(sim(E_S(\widetilde{x}_{i,s}), E_T(\widetilde{x}_{i,t}))/\tau)), \tag{2}$$

$$D_{encoder}^{-}(i) = \sum_{k=1}^{N} (exp(sim(E_S(\widetilde{x}_{i,s}), E_T(\widetilde{x}_{k,t}))/\tau)), \quad (3)$$

$$D_{self}^{-}(i) = \sum_{k=1}^{N} \mathbb{1}_{[k \neq i]}(exp(sim(E_S(\widetilde{x}_{i,s}), E_S(\widetilde{x}_{k,s}))/\tau)),$$
(4)

$$l(i) = -log \frac{D_{encoder}^{+}(i)}{D_{encoder}^{-}(i) + D_{self}^{-}(i)},$$
(5)

$$L_{Cont-Steal} = \frac{\sum_{k=1}^{N} l(k)}{N},$$
(6)

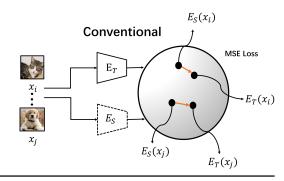
where  $E_S(\cdot)$  and  $E_T(\cdot)$  denotes the surrogate and target encoder,  $sim(u,v) = u^T v/||u||||v||$  represents the cosine similarity between u and v, and  $\tau$  is parameter to control the temperature.

As illustrated in Figure 2, the conventional attack treats each embedding individually without interacting across pairs. However, different embeddings are beneficial to each other as they can serve as anchors to better locate the position of the other embeddings in their space. Cont-Steal maximizes the similarity of embeddings generated from the target and surrogate encoders for a positive pair  $(\widetilde{x}_{i,s}, \widetilde{x}_{i,t})$ (orange arrows in Figure 2). For the embedding generated from the target and surrogate encoders for any pair  $(\widetilde{x}_{i,s},\widetilde{x}_{i,t})$ , contrastive stealing aims to make them more distant (green arrows in Figure 2). Besides, as pointed out by Chen et al. [6], contrastive learning benefits larger negative samples. To achieve this goal, we also consider the embeddings generated from the surrogate encoder for augmented views of different images, i.e.,  $(\tilde{x}_{i,s}, \tilde{x}_{j,s})$ , as negative pairs minimize their similarity (blue arrows in Figure 2). We later show that such design can enhance the performance of contrastive stealing (see Table 5).

**Apply the Surrogate Encoder to Downstream Tasks.** We follow Section 3.1 to evaluate the effectiveness of model stealing on downstream tasks.

#### 4. Experiments

In this section, we first describe the experimental setup in Section 4.1. Then we show the performance of the target encoders on the downstream tasks. Next, we summarize the performance of conventional attacks against classifiers and encoders in Section 4.2. Lastly, we evaluate the performance of Cont-Steal and conduct ablation studies to demonstrate its effectiveness under different settings in Section 4.3.



#### Cont-Steal

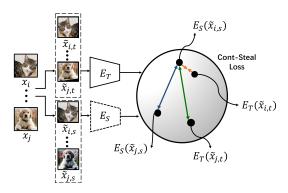


Figure 2. Conventional attack (top) vs. Cont-Steal (bottom) against encoders. Conventional attack applies MSE loss to approximate target embeddings for each sample individually. Cont-Steal (bottom) introduces data augmentation and interacts across multiple samples: associating target/surrogate embeddings of the same images closer and repulsing those of different images farther away. The target encoder  $(E_t)$  is pre-trained and fixed, as shown in the solid frame. The surrogate encoder  $(E_s)$  is trainable by the adversary, as shown in the dashed frame.

#### 4.1. Experimental Setup

Our encoders are pre-trained on CIFAR10 [1], and ImageNet [12]. We use four different kinds of contrastive methods: SimCLR [6], MoCo [20], BYOL [17] and SimSiam [8] to train a ResNet18 [21] as our target encoders. Our implementation is based on a PyTorch framework of contrastive learning.<sup>5</sup> Then, these well pre-trained encoders will be applied to train downstream classifiers on CIFAR10 [1], STL10 [9], Fashion-MNIST [54], and SVHN [35]. In the experiments in the model stealing section, we use CIFAR10, STL10, Fashion-MNIST, and SVHN to conduct the attack.

Agreement and accuracy are used as metrics to evaluate the model stealing attack's performance. The agreement will evaluate the similarity of surrogate encoders and target encoders in downstream tasks. The accuracy will evaluate

<sup>5</sup>https://github.com/vturrisi/solo-learn/

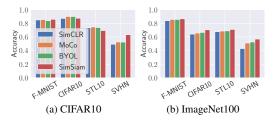


Figure 3. The performance of target classifiers composed by target encoder and an extra linear layer. The encoders are pre-trained on CIFAR10 (a) and ImageNet100 (b). The x-axis represents different downstream datasets for the target encoder and classifier. The y-axis represents the target model's accuracy on downstream tasks.

the utility of surrogate models on downstream tasks. For each metric, a larger value is more desirable. During the stealing process, we set the batch size as 128 and the learning rate as 0.001. We show more results on the impact of hyperparameters in Supplementary Material in Section A.2

# 4.2. Performance of Conventional Attacks

We first show the target encoder's performance in various downstream tasks. The results are summarized in Figure 3. We conduct our experiments to explore whether the encoders are more vulnerable to model stealing attacks. We show our results of target encoders and downstream classifiers both trained on CIFAR10 in Figure 4. In all cases, the adversary can get better attack performance by stealing encoders rather than classifiers. This gap becomes especially apparent when the adversary has absolutely no knowledge of the train data. This is because the rich information in embeddings can better facilitate the learning process of surrogate encoders. For instance, when the surrogate dataset is CIFAR10 (the same as the target downstream dataset), stealing SimCLR's embeddings can achieve 0.785 agreement, while stealing predicted labels can achieve 0.712 agreement. However, when the surrogate dataset is totally different from the downstream target dataset, e.g., SVHN, stealing embeddings from SimCLR can still achieve 0.507 agreement while the agreement of stealing predicted labels drops to 0.192. We show more results in Supplementary Material Section A.4 due to the page limitation.

We also find that all model stealing attacks' accuracy and agreement are highly correlated. As shown in Figure 5, the agreement is highly correlated with the accuracy. This indicates that besides accuracy, the agreement can also be used as a metric to evaluate the performance of model stealing attacks. We show the result on Figure 5. It can be obviously seen that agreement is highly related to accuracy. We use the linear regression method to describe the relationship between agreement and accuracy and find that the relation function is y=0.940 \* x.

#### 4.3. Performance of Cont-Steal

As shown in Section 4.2, encoders are more vulnerable to model stealing attacks since the embedding usually contains richer information compared to the predicted label or posteriors. We then show that our proposed Cont-Steal can achieve better attack performance by making deeper use of embeddings' information.

Figure 7 shows the attack performance when the target pre-training dataset is CIFAR10. Note that we also show the attack performance on other settings in the appendix. We discover that compared to conventional attacks against encoders, Cont-Steal can consistently achieve better performance. For instance, as shown in Figure 7d, when the target encoder is MoCo trained on CIFAR10, if the adversary uses STL10 to conduct model stealing attacks against encoders, the surrogate encoder can achieve 0.841 agreement in CIFAR10 downstream tasks with the Cont-Steal but only 0.479 with conventional attacks. Another finding is that compared to the same distribution surrogate dataset, our Cont-Steal can better enhance the performance when the surrogate dataset comes from a different distribution from the pre-trained dataset. For instance, when the target encoder is SimCLR trained on CIFAR10, Cont-Steal outperforms conventional attack by 0.055 agreement when the surrogate dataset is also CIFAR10, while the improvement increases to 0.207 and 0.214 when the surrogate dataset is STL10. We show more comparing results in Supplementary Material Section A.5. Note that our Cont-Steal also has great performance on other recent state-of-the-art visual models (ViT [13], MAE [19], and CLIP [39]), as we show in Section A.6, and can have better performance than other recent similar attacks [14, 31] shown in Section A.7.

To better understand why Cont-Steal can always achieve better performance, we extract samples' embeddings generated by different encoders, i.e., the target encoder, surrogate encoder trained with the conventional attack, and surrogate encoder trained with the Cont-Steal, and project them into a 2-dimensional space using t-SNE. From the results summarized in Figure 6, we find that Cont-Steal can effectively mimic the pattern of the embeddings as the target encoder. However, the conventional attack fails to capture such patterns for a number of input samples, e.g., the outer circle in Figure 8c. This further demonstrates that Cont-Steal benefits from jointly considering different embeddings as they can serve as anchors to better locate the position of the other embeddings in their space. We also show some ablation study results on Supplementary Material Section A.2 to show that with the less surrogate dataset, less training epoch, and different model architecture, Cont-Steal can still achieve much better results than conventional steal. Also, we show further attacks based on the stole models on Supplementary Material Section A.3 to show that Cont-Steal can be used as a springboard for other attacks.

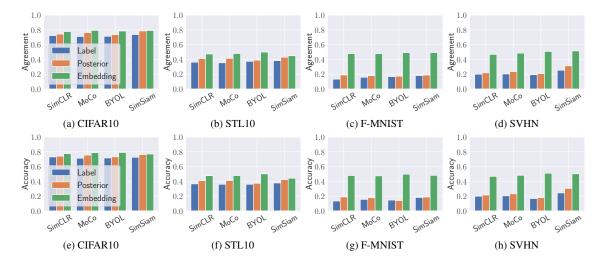


Figure 4. The performance of model stealing attack against target encoders and downstream classifiers both trained on CIFAR10. Target models can output predicted labels, posteriors, or embeddings. The adversary uses CIFAR10, STL10, Fashion-MNIST (F-MNIST), and SVHN to conduct model stealing attacks. The x-axis represents different kinds of target models. The first line's y-axis represents the agreement of the model stealing attack. The second line's y-axis represents the accuracy of the model stealing attack.

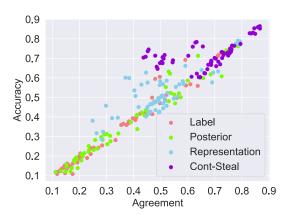


Figure 5. The relationship between accuracy and agreement. The x-axis is the agreement number, and the y-axis is the accuracy number.



Figure 6. The t-SNE projection of 1,000 randomly selected samples' embeddings from target encoder, surrogate encoder under Cont-Steal, and surrogate encoder under the conventional attack, respectively. Note that the target encoder is pre-trained by Sim-CLR on CIFAR10.

Table 1. The monetary and (training) time costs for normal training and Cont-Steal attack. Cont-Steal's monetary cost contains two parts: query cost and training cost. Note that we ignore the query time cost of Cont-Steal as it normally has a smaller value than the training time cost.

	Monetary Cost		Time Cost	
Model	Normal (\$)	Cont-Steal (\$)	Normal (h)	Cont-Steal (h)
SimCLR	58.68	11.83 (1.83 + 10)	20.01	0.62
МоСо	54.83	12.13 (2.13 + 10)	18.69	0.73
BYOL	61.46	12.08 (2.08 + 10)	20.96	0.71
SimSiam	57.14	12.00 (2.00 + 10)	19.46	0.68

#### 4.4. Cost Analysis

As we mentioned before, pre-train a state-of-the-art encoder is time-consuming and resource-demanding. We wonder if the model stealing attacks can steal the functionality of the encoder with much less cost. To this end, we evaluate the time and monetary cost of training an encoder from scratch or stealing a pre-trained encoder via Cont-Steal. The monetary cost of model stealing includes querying the target model and training the surrogate model. We refer to the query price as \$1 for 1,000 queries based on AWS.<sup>6</sup> Our experiment is conducted on 1 NVIDIA A100 whose price is \$2.934 per hour based on google cloud.<sup>7</sup>

The monetary and time cost is shown in Table 1. We observe that Cont-Steal can obtain a surrogate encoder with much less money and time cost than training the encoder from scratch. For instance, a ResNet18 trained by SimCLR

<sup>6</sup>https://aws.amazon.com/rekognition/pricing/

<sup>7</sup>https://cloud.google.com/compute/gpus-pricing/

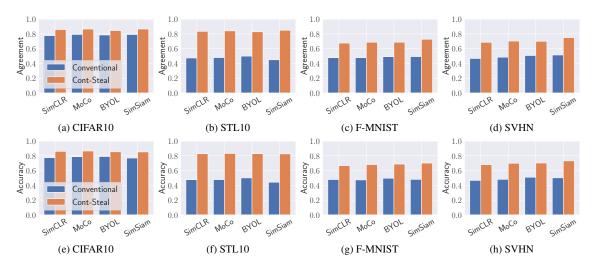


Figure 7. The performance of Cont-Steal and conventional attack against target encoders trained on CIFAR10. The adversary uses CIFAR10, STL10, F-MNIST, and SVHN to conduct model stealing attacks. The adversary uses CIFAR10 as the downstream task to evaluate the attack performance. The x-axis represents different kinds of the target model. The first line's y-axis represents the agreement of the model stealing attack. The second line's y-axis represents the accuracy of the model stealing attack.

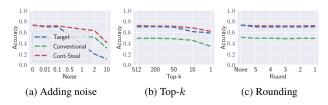


Figure 8. The performance of different defense methods. Target encoders are trained on CIFAR10. The downstream dataset and surrogate dataset are both STL10. The x-axis represents different defense levels. The y-axis represents the model's accuracy.

on CIFAR10 takes 20.01 hours and 58.68\$ on 1 NVIDIA A100 GPU, while Cont-Steal only takes 0.62 hours and 11.83\$ to steal an encoder that performs similarly on downstream tasks. The results demonstrate that Cont-Steal is able to construct surrogate encoders that perform similarly to the target encoders but with much less time and monetary cost.

#### 4.5. Defenses

In this section, we will consider different defenses against model stealing attacks on encoders to evaluate the robustness of our proposed attack. We divided all defenses into three categories: perturbation-based defense [37] and watermark-based defense [2].

**Perturbation-based Defense.** In this defense setting, the defender aims to perturb the output of the target model to limit the information the adversary can obtain. The common practice of this kind of defense includes adding noise [37], top-k [37], and feature rounding [48].

Adding noise means that the defender will introduce noise value to the original output of the model. In our case, we consider adding Gaussian noise to the embeddings generated by the target encoder. We set the mean value to 0, and different noise levels represent different standard deviations of the Gaussian distribution. For Top-k, the defender will only output the first k largest number of each embedding (and set the rest as 0). In this way, the high-dimensional information of the image contained in embeddings can be appropriately reduced. Regarding feature rounding, the defender will truncate the values in the embedding to a specific digit. As a case study, we consider a ResNet18 encoder pre-trained on CIFAR10 with SimCLR and take STL10 to train its downstream classifier. The experimental results are summarized in Figure 8. We can observe that while adding noise and top-k can reduce the model stealing attacks' performance, it may also degrade the target model performance to a large extent. For instance, when the noise increases from 0 to 10, the attack performance of Cont-Steal decreases from 0.729 to 0.410, while the target encoder's performance drops from 0.734 to 0.098. On the other hand, rounding only has a limited effect on both target model performance and attack performance. This indicates that perturbation-based defense cannot defend against the encoder's model stealing attack effectively since they cannot reach a good trade-off between attack performance and model utility.

Watermark-based Defense. Watermark-based defense is also one of the most popular defense methods against model stealing attacks [2]. Watermark provides copyright protection by adding some specific identification to the target model. If the surrogate model is stolen from the watermarked target model, then ideally, it will contain the same watermark as well. Adi et al. [2] show that back-

Table 2. Watermark defense. Pretrain dataset and surrogate dataset are both CIFAR10. Watermark leverages a watermark rate (wr) to verify the ownership of target models. A higher wr denotes a better verification performance.

Dataset	Target model (acc/wr)	Cont-Steal (acc/wr)	Baseline (acc/wr)
CIFAR10	0.864 / 0.998	0.769 / 0.130	0.871 / 0.095
STL10	0.721 / 0.999	0.702 / 0.034	0.733 / 0.111
SVHN	0.501 / 0.999	0.535 / 0.303	0.492 / 0.103
F-MNIST	0.857 / 0.999	0.813 / 0.061	0.850 / 0.099

door technology can be used as the watermark to protect the model. In that sense, BadEncoder [26], a backdoor mechanism against the encoder, can be leveraged as a watermarking technology for our target encoder as well. The defenders first will train the watermarked (backdoored) encoder, where images with a certain trigger will cause misclassification. Then, if they find the surrogate model can also misclassify images with the same trigger, the defenders can claim ownership of the surrogate model.

In our experiments, we leverage BadEncoder to watermark the encoder pre-trained on CIFAR10 by SimCLR, and leverage different downstream datasets to perform different tasks. We assume a strong adversary that has the same downstream dataset as the surrogate dataset. Also, we consider the baseline cases where the trigger samples are fed into the clean model to calculate the watermark rate (wr). As shown in Table 2), the watermark cannot be preserved as the surrogate models constructed by Cont-Steal have similar wr as the baseline model. For instance, when the downstream dataset is CIFAR10, Cont-Steal builds a surrogate model with 0.769 accuracy while only 0.130 wr, which is close to the baseline model. This indicates that Cont-Steal can bypass the watermarking technique as it can reach similar utility while reducing the wr to a large extent. Note that there is also another work to protect contrastive learning models from model stealing attacks using dataset inference [15]. We show in Supplementary Material in Section A.8 that this kind of defense can be easily bypassed by Cont-Steal.

# 5. Related Work

Contrastive Learning. Contrastive learning is one of the most popular methods to train encoders. Current works [6, 8, 17, 20, 49, 53] propose different advanced contrastive learning algorithms. SimCLR, MoCo, BYOL, SimSiam are currently the mainstream frameworks of contrastive learning. Thus, we concentrate on them in this paper. There are many works on evaluating the security and privacy risks of contrastive learning. Previous works [23, 26, 30] propose membership inference attacks, attribution inference attacks, and backdoor attacks on contrastive learning. All proposed attacks show that contrastive-based models are vulnerable

to popular attacks. Therefore, the security issues of selfsupervised learning deserve more attention.

**Model Stealing Attack.** In model stealing, the adversary's goal is to steal part of the target model. Tramèr et al. [48] proposed the first model stealing attack against black-box machine learning API to steal its parameters. Wang et al. [50] proposed the first hyperparameter stealing attacks against ML models. Oh et al. [36] also tried to steal machine learning model's architectures and hyperparameters. Orekondy et al. [37] proposed knockoff nets, which aim at stealing the functionality of black-box models. Krishna et al. [28] formulated a model stealing attack against BERTbased API. Besides, Wu et al. [51] and Shen et al. [44] perform model stealing attacks against Graph Neural Networks. These works often have relatively strong assumptions, such as the model family is known and the victim's data is partly available while we conduct model stealing attacks against encoders and relax the above assumption.

#### 6. Conclusion

In this paper, we conduct the first model stealing risk assessment towards image encoders. Our evaluation shows that the encoder is more vulnerable to model stealing attacks compared to the classifier. This is because the embedding provided by the encoder contains richer information than the posteriors or predicted labels from whole classifiers.

To better unleash the power from the embeddings, we propose Cont-Steal, a contrastive learning-based model stealing method against encoders. Concretely, Cont-Steal introduces different types of negative pairs as "anchors" to better navigate the surrogate encoder and learn the functionality of the target encoder. Extensive evaluations show that Cont-Steal consistently performs better than conventional attacks against encoders. And such an advantage is further amplified when the adversary has no information on the target dataset, a limited amount of data, and restricted query budgets. Our work points out that the threat of model stealing attacks against encoders is largely underestimated, which prompts the need for more effective intellectual property protection of representation learning techniques.

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