Домашнее задание

Вариант 1:

1 .Задание 1

$$y = \log_{x}(x^{2} - x - 6)$$

$$D(f): \begin{cases} x > 0 \\ x \neq 1 \\ (x^{2} - x - 6) > 0 \end{cases} \rightarrow \begin{cases} x > 0 \\ x \neq 1 \\ (x - 3)(x + 2) > 0 \end{cases} \rightarrow \begin{cases} x > 0 \\ x \neq 1 \\ x > 3 \\ x < -2 \end{cases}$$

Ответ: x > 3

2 .Задание 2

$$y = \arccos\left(2^x - 2^{-x}\right)$$

$$: f(-x) = \arccos(2^{-x} - 2^{x})$$
$$= \arccos(-(2^{x} - 2^{-x}))$$
$$= \pi - \arccos(2^{x} - 2^{-x})$$

$$: f(-x) \neq f(x) \neq -f(x)$$

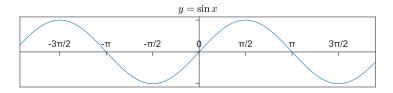
От вет: f(x) is a Nonodd noneven function.

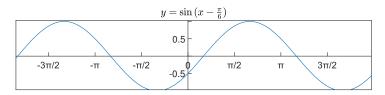
3 .Задание 3

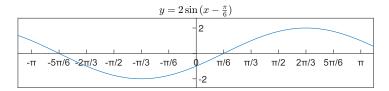
3.1 .Задание $3(\, a\,)$

$$y = 2\sin\left(x - \frac{\pi}{6}\right)$$

Function: $y = \sin x \to y = \sin \left(x - \frac{\pi}{6}\right) \to y = 2\sin \left(x - \frac{\pi}{6}\right)$





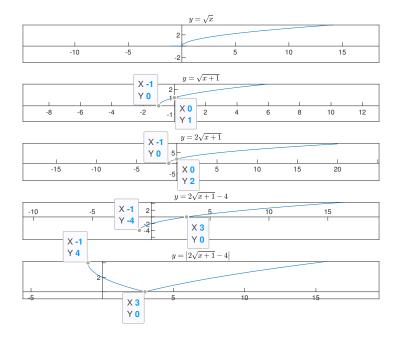


3.2 .Задание 3(б)

$$y = \left| 2\sqrt{x+1} - 4 \right|$$

$$D(f): x+1 \ge 0 \quad \Rightarrow \quad x \ge -1$$

Function: $y = \sqrt{x} \rightarrow y = \sqrt{x+1} \rightarrow y = 2\sqrt{x+1} \rightarrow y = 2\sqrt{x+1} - 4 \rightarrow y = \left|2\sqrt{x+1} - 4\right|$

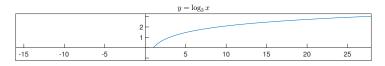


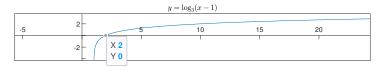
$3.3\,$.Задание $3(\,$ в $\,)$

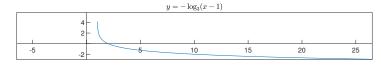
$$y = \log_3(\frac{9}{x - 1})$$

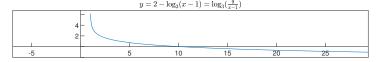
$$D(f): \frac{9}{x-1} \quad \Rightarrow \quad x-1>0 \quad \Rightarrow \quad x>1$$

Function: $y = \log_3 x \to y = \log_3(x-1) \to y = -\log_3(x-1) \to y = 2 - \log_3(x-1) = \log_3\left(\frac{9}{x-1}\right)$







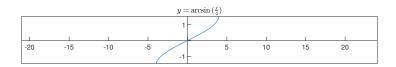


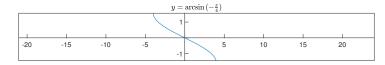
3.4 .Задание (г)

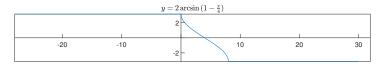
$$y = 2^{|3x+6|} - 1$$

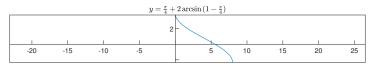
$$D(f): x \in R$$

Function: $y = 2^x \to y = 2^{3x+6} \to y = 2^{|3x+6|} \to y = 2^{|3x+6|} - 1$



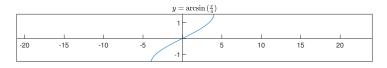


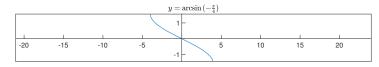


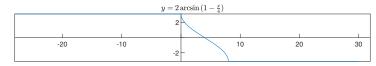


$3.5\,$.Задание (д)

$$\begin{split} y &= \frac{\pi}{4} + 2\arcsin\left(1 - \frac{x}{4}\right) \\ \text{Function: } y &= \arcsin\left(\frac{x}{4}\right) \to y = \arcsin\left(-\frac{x}{4}\right) \to y = 2\arcsin\left(1 - \frac{x}{4}\right) \\ &\to y = \frac{\pi}{4} + 2\arcsin\left(1 - \frac{x}{4}\right) \,. \end{split}$$









4 .Задание 4

$$y = \frac{2x - 3}{x^2 + 2x + 1}$$

1. Эта функция не определена в x=-1, так что эта функция имеет горизонтальную асимптоту : x=-1, и $\Delta f=f$, так мы получаем:

$$\Rightarrow \begin{cases} y = 0 \\ x = -1 \end{cases}$$

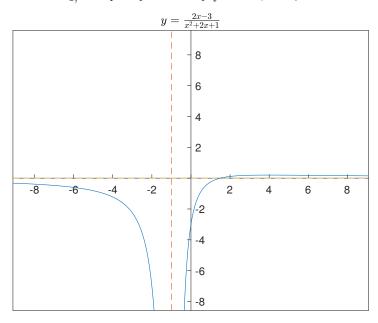
2. Точка пересеч. с осью:

$$\begin{cases} Ox: \left(\frac{3}{2}, 0\right) \\ Oy: (0, -3) \end{cases}$$

3. Знаки ф-и:

$$\begin{cases} f(x) \ge 0, & x \ge \frac{3}{2} \\ f(x) < 0, & -1 < x < \frac{3}{2} \\ f(x) < 0, & x < -1 \end{cases}$$

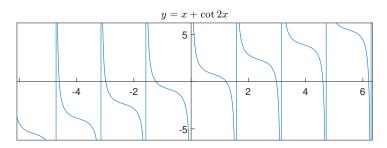
4, График функции:

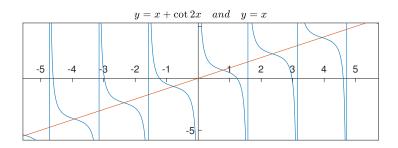


5 .Задание 5

 $y = x + \cot 2x$

1. Грайик функции y=x и $y=\cot 2x$:





2. Когда мы добавляем две функции, $\mbox{график} \quad y = \cot 2x \mbox{ идет} \quad \mbox{вверх} \quad \mbox{c} \quad y = x, \mbox{ то}$ мы получаем:

