# 8.23-9.5 周报

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# 1 写在前面

这个双周主要完成了 cs231n 课程的 Lecture 1 至 Lecture 6, 主要内容包括距离函数、KNN、SVM、损失函数及优化、BP 算法、CNN 架构、非线性激活函数以及神经网络的参数优化等,并完成 cs231n assignment1。课程概要笔记及 assignment 将在https://github.com/zxh991103/cs231NOTE持续跟踪。

# 2 Lec 1-6 课程概要

## 2.1 距离函数

 $L_1$  Distance

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$

 $L_2$  Distance

$$d_2(I_1, I_2) = \sqrt{\sum_p (I_1^p - I_2^p)^2}$$

#### 2.2 KNN

计算测试样本与所有训练集样本之间的距离值,并根据 K 值投票选举出最相似的标签。

## 2.3 SVM

计算能够划分训练集样本且距离最大的超平面。

$$w\cdot x+b=0$$

# 2.4 损失函数

损失函数评估模型预测值与模型真实值之间的差异性,我们要将其最小化。对于给定的训练集  $(x_i, y_i)_{i=1}^N$  ,我们有损失函数:

$$L = \frac{1}{N} \sum_{i} L_i(f(x_i, W), y_i)$$

对于 Multi-SVM, 我们有损失函数, 即 hinge loss:

$$s = f(x_i, W)$$

$$L_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1)$$

对于 softmax loss:

$$L_i = -log(\frac{e^{s_{y_i}}}{\sum_j e^{s_j}})$$

# 2.5 正则化

根据奥卡姆剃刀原则,模型越简单越符合实际,所以我们将正则惩罚项 加在损失函数上。

$$L = \frac{1}{N} \sum_{i} L_i(f(x_i, W), y_i) + R(W)$$

L1

$$R(W) = \sum_{k} \sum_{l} |W_{k,l}|$$

L2

$$R(W) = \sum_{k} \sum_{l} W_{k,l}^2$$

Elastic

$$R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^2 + |W_{k,l}|$$

## 2.6 BP 算法

链式法则:

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial y}$$

故在计算损失函数对于参数的梯度值时,我们应当将本地梯度值与上 游回传梯度值相乘。

此时,我们也可以发现 Relu 函数,即 max gate 中只有前向传播计算中的正值能影响下游。

A vectorized example:

$$f(x, W) = ||W x||^2 = \sum_{i=1}^{n} (W x)_i^2$$
$$q = W \cdot x$$
$$\nabla_W f = 2q \cdot x^T$$

#### 2.7 NN

假设我们将神经网络的计算图表示为:

$$f = Softmax(W_2Relu(W_1x))$$

神经元 A 拥有  $W_1$ ,能够具有识别出来 100 种特征的功能,比如识别出马的左脸或者右脸、车头或者车位。而神经元 B 拥有  $W_2$ ,其功能就在于将马的左脸或右脸合并为马的特征,将车头或车尾合并成车的特征,从而进行识别。

#### 2.8 CNN

卷积层:

假设有 32\*32\*3 的图片,卷积核 w 5\*5\*3 ,以及偏置 b,卷积后我们获得 28\*28\*1 的矩阵,其中 1 时卷积核的数量。卷积公式为(每位相乘再求和):

$$f[x,y] * g[x,y] = \sum_{n_1 = -\infty}^{\infty} \sum_{n_2 = -\infty}^{\infty} f[x,y] * g[x - n_1, y - n_2]$$

步长 (stride):

假设我们有 7\*7 的输入,3\*3 的卷积核,2 的步长,最后的输出为 3\*3。 此时 outputsize =  $\frac{(N-F)}{stride}+1$ 

填充 (Pad):

图像四周补充 0,来防止在深层卷积时张量过小。此时,outputsize =  $\frac{(N-F+2P)}{stride}+1$ 。

Example:

input volume 32\*32\*3,10 5\*5 filters (include 3 depth), stride 1 ,pad 2 ,wo have 760 parameters ( 10 \*( 5 \* 5 \*3 +1 bias)=760)

pooling layer: 相当于下采样。

maxpooling:

一般,每一个池化 filter 具有和步长相同的大小以避免 overlap.

例如,

我们使用 2\*2 的 filter 和 2 的 stride,maxpooling 后变为:

# 2.9 激活函数

若全部线性连接则等同于一个线性连接,所以网络中需要非线性的激 活函数变换。

sigmod

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

tanh

Relu

LeakyRelu

$$\max(0.1x,x)$$

Maxout

$$\max (w_1^T x + b_1, w_2^T x + b_2)$$

Elu

$$\begin{cases} x & x \ge 0 \\ \alpha (e^x - 1) & x < 0 \end{cases}$$

SELU

$$f(x) = \begin{cases} \lambda x & \text{if } x > 0\\ \lambda \alpha (e^x - 1) & \text{otherwise} \end{cases}$$

softmax 的问题:

- x 过大或过小,本地梯度接近 0,使得与上游梯度乘积也接近于 0,更新缓慢。
- x 的值恒正或恒负,本地梯度总是大于 0 的,造成 w 的移动时锯齿状的,接近最优点放缓。

relu 的问题:

• 若 $w \cdot x + b$  总是负的,则本地梯度为0,造成参数不更新。

## 2.10 数据处理

```
1 # ZERO-CENTER
2 X -= np.mean(X,axis = 0)
3 # normalize
4 X /= np.std(X,axis = 0)
```

Listing 1: normalization

## 2.11 参数初始化

Naive: 为参数初始化小随机数。但是随着网络深度的增加,本地梯度与上游梯度相乘之后接近零,学习十分缓慢。

Xavier:

1 W = np.random.randn(dim\_in,dim\_out)/np.sqrt(dim\_in)

Listing 2: Xavier

原因:

we want  $Var(y) = Var(x_i)$ , and we have

$$y = \sum_{i=1}^{Din} x_i w_i$$

and we assume that every x has same var. so we have

$$var(y) = Din \times var(x) \times var(w_i)$$

and obviously initial  $w_i \ N(0,1)$  , we make  $\frac{w_i}{\sqrt{Din}}$  to achieve the var is  $\frac{1}{Din}$ 

Kaiming/MSRA:

W = np.random.randn(dim\_in,dim\_out)\*np.sqrt(2/dim\_in)

Listing 3: MSRA

#### 2.12 Batch Normalization

we have the input x like  $N \times D$ 

$$\widehat{x}^{(k)} = \frac{x^{(k)} - \operatorname{E}\left[x^{(k)}\right]}{\sqrt{\operatorname{Var}\left[x^{(k)}\right]}}$$

so that we have:

$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \varepsilon}}$$

the net is supposed to learn  $\gamma \in \mathbb{R}^D$  and  $\beta \in \mathbb{R}^D$ 

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

BN 层经常用于全连接或卷积层后。

#### 2.13 Norm For Conv.

batch norm , 对于每一个 batch 中的每个 channel 取平均得到  $(1 \times 1 \times C)$ 

layer norm , 对于所有的 batch 我们取一个平均的图片  $(H \times W \times C)$  instance norm , 对于所有的 batch 我们将取一个平均的单通道图片  $(H \times W \times I)$ 

group norm , 对于所有 batch , 我们将 channel 分为 k 个组 , 在每个组 山上取平均值得到  $(H \times W \times k)$ 

# 3 Assignment1

## 3.1 KNN

双循环实现距离矩阵:

```
num_test = X.shape[0]
num_train = self.X_train.shape[0]
dists = np.zeros((num_test, num_train))
for i in range(num_test):
for j in range(num_train):
t1 = X[i]
```

```
t2 = self.X_train[j]

t = t1 - t2

t = t*t

t = t.sum()

t = t**0.5

dists[i][j] = t
```

Listing 4: KNN 双循环实现距离矩阵

#### 单循环实现距离矩阵:

```
num_test = X.shape[0]
num_train = self.X_train.shape[0]
dists = np.zeros((num_test, num_train))
for i in range(num_test):
    dists[i,:] = np.sum((X[i,:]-self.X_train)**2,axis = 1)
```

Listing 5: KNN 单循环实现距离矩阵

向量操作实现距离矩阵 (矩阵下的完全平方公式):

```
M = np.dot(X, self.X_train.T)
nrow=M.shape[0]
ncol=M.shape[1]
te = np.diag(np.dot(X,X.T))
tr = np.diag(np.dot(self.X_train,self.X_train.T))
te= np.reshape(np.repeat(te,ncol),M.shape)
tr = np.reshape(np.repeat(tr, nrow), M.T.shape)
sq=-2 * M +te+tr.T
dists = np.sqrt(sq)
```

Listing 6: KNN 向量操作实现距离矩阵

## KNN 预测:

Listing 7: KNN 预测

#### 3.2 SVM

计算 SVM loss、dW(naive):

```
dW = np.zeros(W.shape) # initialize the gradient as zero
      # compute the loss and the gradient
      num_classes = W.shape[1]
      num_train = X.shape[0]
      loss = 0.0
      for i in range(num_train):
          scores = X[i].dot(W)
          correct_class_score = scores[y[i]]
          for j in range(num_classes):
10
              if j == y[i]:
12
                   continue
               margin = scores[j] - correct_class_score + 1 # note delta = 1
13
               if margin > 0:
14
                  loss += margin
      loss /= num_train
16
17
       # Add regularization to the loss.
18
      loss += reg * np.sum(W * W)
19
20
      for i in range(num_train):
21
           scores = X[i].dot(W)
           correct_class_score = scores[y[i]]
          for j in range(num_classes):
24
               if j == y[i]:
25
                   continue
26
27
               margin = scores[j] - correct_class_score + 1 # note delta = 1
28
               if margin > 0:
                  dW[:,j] += X[i]
                   dW[:,y[i]] -= X[i]
      dW /= num_train
31
      dW += reg * W * 2
32
```

Listing 8: SVM(naive)

## 计算 SVM loss、dW(vectorized):

```
1    loss = 0.0
2    dW = np.zeros(W.shape) # initialize the gradient as zero
3    N = X.shape[0]
4    scores = X.dot(W)
5    score_yi = scores[range(N),y].reshape(-1,1)
6    t = scores - score_yi + 1
7    t[range(N),y] = 0
8    condition = (t>0).astype(int)
9    t = condition*t
10    t = t.sum() / N
11    loss = t + 2 * reg * np.sum(W * W)
```

```
condition[range(N), y] = - np.sum(condition, axis = 1)
dW += np.dot(X.T,condition)/N + 2 * reg * W
```

Listing 9: SVM(vectorized)

## 训练线性分类器 (batch):

```
num_train, dim = X.shape
      num_classes = (
          np.max(y) + 1
      ) # assume y takes values 0...K-1 where K is number of classes
      if self.W is None:
          # lazily initialize W
          self.W = 0.001 * np.random.randn(dim, num_classes)
       # Run stochastic gradient descent to optimize W
      loss_history = []
10
      for it in range(num_iters):
          X_batch = None
          y_batch = None
13
          indices = np.random.choice(num_train,batch_size)
14
          X_batch = X[indices]
16
          y_batch = y[indices]
17
           # evaluate loss and gradient
18
19
          loss, grad = self.loss(X_batch, y_batch, reg)
          loss_history.append(loss)
20
21
           # perform parameter update
22
           self.W -= learning_rate*grad
```

Listing 10: 训练线性分类器

## SVM 预测:

```
y_pred = np.argmax(np.dot(X,self.W),axis = 1)
```

Listing 11: SVM 预测

#### SVM grid search:

```
best_val = y_val_acc
best_svm = svm
```

Listing 12: SVM grid search

#### 3.3 softmax

Softmax loss, dW(Naive):

```
loss = 0.0
      dW = np.zeros_like(W)
      N , D = X.shape
      C = W.shape[1]
      for i in range(N):
         f = np.dot(X[i],W)
         f -= np.max(f) # avoid overflow
         loss = loss + np.log(np.sum(np.exp(f))) - f[y[i]]
10
          dW[:, y[i]] -= X[i]
          s = np.exp(f).sum()
          for j in range(C):
              dW[:, j] += np.exp(f[j]) / s * X[i]
14
     loss = loss / N + reg * np.sum(W * W)
    dW = dW / N + 2*reg * W
```

Listing 13: Softmax(Naive)

Softmax loss, dW(vectorized):

```
N , D = X.shape
C = W.shape[1]
score = np.dot(X,W)
t = np.max(score,axis = 1).reshape(N,1)
score -= t
s = np.exp(score).sum(axis = 1)
loss = - score[range(N),y].sum() + np.log(s).sum()
counts = np.exp(score) / s.reshape(N, 1)
counts[range(N),y] -= 1
dW = np.dot(X.T,counts)

loss = loss/N + reg * np.sum(W * W)

dW = dW/N + reg *W
```

Listing 14: Softmax(vectorized)

$$Loss = -\log(\frac{e^{s_{y_i}}}{\sum_{j} e^{s_j}}) = -s_{y_i} + \log \sum_{j} e^{s_j}$$
$$\frac{dL}{dW} = -\frac{ds_{y_i}}{dW} + \frac{1}{\sum_{j} e^{s_j}} \cdot (\sum_{j} (e^{s_j} \frac{dS_j}{dW}))$$

## softmax grid search:

```
from cs231n.classifiers.linear_classifier import Softmax
      for lr in learning_rates:
3
      for rs in regularization_strengths:
          softmax = Softmax()
          softmax.train(X_train, y_train, learning_rate = lr, reg=rs,
      num_iters = 1500,
                       verbose = True)
          y_pred_train = softmax.predict(X_train)
          acc_train = np.mean(y_pred_train == y_train)
10
          y_pred_val = softmax.predict(X_val)
13
          acc_val = np.mean(y_pred_val == y_val)
          results[(lr, rs)] = (acc_train, acc_val)
14
          if acc_val > best_val:
16
17
              best_val = acc_val
              best_softmax = softmax
```

Listing 15: softmax grid search

#### 3.4 FC Net

## FC 单层向后传播:

```
N = x.shape[0]
D = x[0].reshape(-1,1).shape[0]

M = b.shape[0]

print(N,D,M)

out = np.zeros((N,M))

for i in range(N):
    t = x[i].reshape(-1,1)

print(w.shape,t.shape)

t = np.dot(w.T,t) + b.reshape(-1,1)

out[i:,] = t.T
```

Listing 16: FC 单层前向传播

## FC 单层向后传播:

```
N = x.shape[0]
t = x.shape
D = x[0].reshape(-1,1).shape[0]

M = b.shape[0]

x = x.reshape(N,D)
dx = np.dot(dout,w.T).reshape(t)
dw = np.dot(x.T,dout)
```

```
9 db = dout.sum(axis=0)
```

Listing 17: FC 单层向后传播

Relu 向前传播:

```
condition = (x>0).astype(int)

out = condition * x
```

Listing 18: Relu 向前传播

Relu 向后传播:

```
dx = (x > 0).astype(int) * dout
```

Listing 19: Relu 向后传播

SVM loss, dx

```
N,C = x.shape
      scores = x
      score_yi = scores[range(N),y].reshape(-1,1)
      t = scores - score_yi + 1
      t[range(N),y] = 0
6
      condition = (t>0).astype(int)
      t = condition*t
      t = t.sum() / N
     loss = t
11
      condition[range(N), y] = - np.sum(condition, axis = 1)
12
       print(condition.shape)
13 #
      dx = condition/N
```

Listing 20: SVM loss, dx

Softmax loss , dx

```
N,C = x.shape
score = x - np.max(x,axis = 1).reshape(N,1)
s = np.exp(score).sum(axis = 1).reshape(N,1)
score_yi = score[range(N),y].reshape(N,1)
loss = (-score_yi + np.log(s)).sum() /N

expscore = np.exp(score)

dx = (expscore / s).reshape(N,C)

dx[range(N),y] -=1

dx /= N
```

Listing 21: Softmax loss, dx

#### Two Layer Net Loss:

```
scores = None
      N = X.shape[0]
      D = X.reshape(N,-1).shape[1]
      C = self.C
      X_new = X.reshape(N,D)
      # layer 1
      cp = X.reshape(N,D)
      cp = np.dot(cp,self.params['W1'])
10
      cp = cp + self.params['b1']
      h = cp
12
13
14
      # relu
15
      condition1 = (cp>0).astype(int)
      cp = condition1 * cp
16
      h1 = cp
17
      # layer 2
18
      cp = np.dot(cp,self.params['W2'])
      cp = cp + self.params['b2']
20
      # softmax
21
      scores = cp
22
23
24
      if y is None:
26
          return scores
27
28
      loss, grads = 0, {}
29
30
      scoresmax = np.max(scores,axis = 1).reshape(N,1)
      scores = scores - scoresmax
32
      expscores = np.exp(scores)
33
      t = expscores.sum(axis =1).reshape(N,1)
34
       expscores = expscores / t
35
       scores_yi = expscores[range(0,N),y]
      loss = -np.log(scores_yi).sum() /N+ 0.5*self.reg * (self.params['W1'] *
       self.params['W1']).sum() + 0.5*self.reg * (self.params['W2'] *self.
       params['W2']).sum()
38
            print(loss)
39 #
40
       '''gradient'''
41
      # Loss
42
      dscore = (expscores).reshape(N,C)
43
      dscore[range(N),y] -= 1
44
      dscore /= N
45
46
      # f2
```

```
48
49
       dw2 = np.dot(h1.T , dscore)
50
       db2 = np.sum(dscore,axis = 0)
51
       dh1 = np.dot(dscore, self.params['W2'].T)
52
       # relu
53
54
       dh = (h>0).astype(int)
55
56
      dh = dh * dh1
57
       # f1
58
59
       dw1 = np.dot(X_new.T,dh)
60
       db1 = np.sum(dh,axis = 0)
61
62
63 #
             dw1 = dw1.reshape(self.params['W1'].shape)
64 #
             dw2 = dw2.reshape(self.params['W2'].shape)
       dw1 += self.reg * self.params['W1']
65
       dw2 += self.reg * self.params['W2']
66
67
       grads['W1']=dw1
       grads['b1']=db1
69
       grads['W2']=dw2
70
       grads['b2']=db2
71
```

Listing 22: Two Layer Net Loss

```
sgd
w -= config['learning_rate'] * dw
```

Listing 23: sgd

## FC Net grid search:

```
input_size = 32 * 32 * 3
      num_classes = 10
3
      best_acc =-1
      for bs in [200, 400]:
4
          for lr in [1e-3, 1e-4, 1e-5]:
              for hidden_size in [50, 100, 200]:
6
                   net = TwoLayerNet(input_size, hidden_size, num_classes)
                   solver = Solver(net, data,
                       num_train_samples=100,
                       lr_decay=0.9,
                       num_epochs=20,
11
12
                       print_every=50000,
                       batch_size = bs,
13
                       optim_config={
14
                           'learning_rate': lr,
15
                       }
16
```

```
solver.train()

# Predict on the validation set

val_acc = solver.check_accuracy(data['X_val'],data['y_val'])

print ('batch_size = %d, lr = %f, hidden size = %f,

Valid_accuracy: %f' %(bs, lr, hidden_size,val_acc))

if val_acc > best_acc:

best_acc = val_acc

best_model = net
```

Listing 24: FC Net grid search

# 3.5 Feature Extract

Listing 25: FC Net grid search