Project 1 function

YL

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Intro

This is an R Markdown document for project 1: http://utdallas.edu/~ammann/stat6341/node10.html.

Question 1

Setup:

```
p = c(0.5,0.3,0.2)
alpha = 0.05
sampleSizeVector=c(500,1000,1500)
# parameter for method 1
m=3
M = m*(m-1)/2
cv = qchisq(1-alpha/M,M-1) ### critical value
print(cv)

## [1] 8.188689
# parameter for method 2
x = seq(1,4,length=1000)
y = 1 - 2*(1 - pnorm(x)) - 4*(m-2)*(1-pnorm(x*sqrt(2)))
a = min(x[y >= 1 - alpha]) ### a value
print(a)

## [1] 2.036036
```

Generate simulation

Generate 2 simulated data, for example:

```
set.seed(321)
df = rbind(rmultinom(2, size = sampleSizeVector[1], prob = p),trialID = 1:2)
df

##     [,1] [,2]
##     252    259
##     144    145
##     104    96
## trialID     1    2
```

Each column is one poll. You can see the distribution is about 0.5, 0.3, 0.2. Then a function is designed to compute the confidence interval using method 1 and method 2. This function is going to be the importance one, because it is the most basic part for confidence interval computation regardless what's the distribution or whether it is mixed or not.

```
## singleSample: the one single column you want to calculate
## type: the character string to record the pair difference
## i,j : the locations of the pair elements: p1 means the first element in p,namely p[1]
```

```
## a dataframe is returned with complete result
confiFun <- function(singleSample,type,i,j){</pre>
  N = sum(singleSample[1:3])
                               #the column sum; sample size
  phat_i = singleSample[i] / N # the estimated p_i
  phat_j = singleSample[j] / N # the estimated p_j
  delta = phat_i- phat_j
                               #Differences Between Multinomial Proportions
  d_ij = phat_i + phat_j - delta^2 # d_ij for method 1
  # each vector has results from method 1 and method 2
  confiLower = c(delta - sqrt( cv * d_ij /N), delta - a/sqrt(N))
  confiUpper = c(delta + sqrt( cv * d_ij /N), delta + a/sqrt(N))
  ## return a dataframe that named column
  return(data.frame(confiLower = round(confiLower,4),confiUpper = round(confiUpper,4),
                    type=type,method=c(1L,2L),trueValue = p[i]-p[j],
                    trialID = singleSample[[4]]))
}
```

Let's apply this function to our data. Suppose we want to calculate the delta_12, which is p1-p2.

```
delta_12 = apply(df, 2,confiFun,type="p1-p2",i=1,j=2)
delta_12
```

```
## [[1]]
##
     confiLower confiUpper type method trueValue trialID
## 1
                      0.3265 p1-p2
          0.1055
                                          1
                                                  0.2
## 2
          0.1249
                      0.3071 p1-p2
                                          2
                                                  0.2
                                                              1
##
## [[2]]
     \verb|confilower| confilOper | type method trueValue trialID| \\
## 1
                      0.3393 p1-p2
         0.1167
                                          1
                                                  0.2
## 2
          0.1369
                      0.3191 p1-p2
                                          2
                                                  0.2
                                                             2
```

Since we have two column, the result is the length 2 list, where each element is a dataframe. Looks good. Then we have to try different sample size, which can be done using a function. And we can embed all 3 pair difference to one sampleSize. Check the **apply** build-in function. Check the **Reduce** build-in function.

```
confiDataFun <- function(sampleSize,nrep=2){
    set.seed(321)
    df = rbind(rmultinom(nrep, size = sampleSizeVector[1], prob = p),trialID = 1:nrep)

    delta_12 = apply(df, 2,confiFun,type="p1-p2",i=1,j=2)
    delta_13 = apply(df, 2,confiFun,type="p1-p3",i=1,j=3)
    delta_23 = apply(df, 2,confiFun,type="p2-p3",i=2,j=3)

    res = Reduce(rbind,c(delta_12,delta_13,delta_23)) # rbind all dataframe
    res$sampleSize = sampleSize # record the sampleSize
    return(res)
}</pre>
```

Use this function to repeat what we just did.

confiDataFun(sampleSize = 500,nrep=2)

```
confiLower confiUpper type method trueValue trialID sampleSize
##
## 1
          0.1055
                      0.3265 p1-p2
                                          1
                                                  0.2
                                                             1
                                                                       500
                                          2
## 2
          0.1249
                      0.3071 p1-p2
                                                  0.2
                                                             1
                                                                       500
## 3
          0.1167
                      0.3393 p1-p2
                                          1
                                                  0.2
                                                             2
                                                                       500
## 4
          0.1369
                      0.3191 p1-p2
                                          2
                                                  0.2
                                                             2
                                                                       500
                                          1
                                                  0.3
                                                             1
## 5
          0.1949
                      0.3971 p1-p3
                                                                       500
## 6
          0.2049
                      0.3871 p1-p3
                                          2
                                                  0.3
                                                             1
                                                                       500
                                                             2
## 7
          0.2266
                      0.4254 p1-p3
                                          1
                                                  0.3
                                                                       500
## 8
          0.2349
                      0.4171 p1-p3
                                          2
                                                  0.3
                                                             2
                                                                       500
## 9
         -0.0095
                      0.1695 p2-p3
                                          1
                                                  0.1
                                                             1
                                                                       500
                                          2
## 10
         -0.0111
                      0.1711 p2-p3
                                                  0.1
                                                             1
                                                                       500
                                                             2
## 11
          0.0100
                      0.1860 p2-p3
                                          1
                                                  0.1
                                                                       500
## 12
          0.0069
                                          2
                                                  0.1
                                                             2
                                                                       500
                      0.1891 p2-p3
```

Then we have all three pair difference in one shot. The sampleSize column is to distinguish the result from different sampleSize. Let's try two sample size: 500, 1000,1500. Check the **lapply** build-in function.

```
confiList = lapply(sampleSizeVector, confiDataFun)
confiList
```

[[1]]

```
confiLower confiUpper type method trueValue trialID sampleSize
##
## 1
          0.1055
                      0.3265 p1-p2
                                         1
                                                  0.2
                                                             1
                                                                       500
## 2
                                          2
                                                  0.2
          0.1249
                      0.3071 p1-p2
                                                             1
                                                                       500
## 3
                                                  0.2
                                                             2
                                                                       500
          0.1167
                      0.3393 p1-p2
                                         1
                                                             2
## 4
          0.1369
                      0.3191 p1-p2
                                         2
                                                  0.2
                                                                       500
                                                  0.3
                                                             1
## 5
          0.1949
                      0.3971 p1-p3
                                         1
                                                                       500
## 6
          0.2049
                      0.3871 p1-p3
                                          2
                                                  0.3
                                                             1
                                                                       500
## 7
          0.2266
                                         1
                                                  0.3
                                                             2
                                                                       500
                      0.4254 p1-p3
                      0.4171 p1-p3
## 8
          0.2349
                                          2
                                                  0.3
                                                             2
                                                                       500
## 9
         -0.0095
                                                  0.1
                      0.1695 p2-p3
                                         1
                                                             1
                                                                       500
         -0.0111
                                          2
                                                  0.1
                                                             1
## 10
                      0.1711 p2-p3
                                                                       500
## 11
          0.0100
                      0.1860 p2-p3
                                         1
                                                  0.1
                                                             2
                                                                       500
## 12
          0.0069
                      0.1891 p2-p3
                                          2
                                                  0.1
                                                             2
                                                                       500
##
## [[2]]
##
      confiLower confiUpper type method trueValue trialID sampleSize
## 1
          0.1055
                      0.3265 p1-p2
                                         1
                                                  0.2
                                                             1
                                                                      1000
## 2
          0.1249
                      0.3071 p1-p2
                                          2
                                                  0.2
                                                             1
                                                                      1000
## 3
                      0.3393 p1-p2
                                         1
                                                  0.2
                                                             2
                                                                      1000
          0.1167
                                          2
                                                             2
## 4
          0.1369
                      0.3191 p1-p2
                                                  0.2
                                                                      1000
                                                  0.3
## 5
          0.1949
                      0.3971 p1-p3
                                         1
                                                             1
                                                                      1000
                                         2
## 6
          0.2049
                      0.3871 p1-p3
                                                  0.3
                                                             1
                                                                      1000
## 7
          0.2266
                      0.4254 p1-p3
                                         1
                                                  0.3
                                                             2
                                                                      1000
## 8
          0.2349
                      0.4171 p1-p3
                                         2
                                                  0.3
                                                             2
                                                                      1000
## 9
         -0.0095
                      0.1695 p2-p3
                                         1
                                                  0.1
                                                             1
                                                                      1000
## 10
         -0.0111
                                          2
                                                  0.1
                                                             1
                                                                      1000
                      0.1711 p2-p3
                                                             2
## 11
          0.0100
                      0.1860 p2-p3
                                          1
                                                  0.1
                                                                      1000
## 12
          0.0069
                      0.1891 p2-p3
                                          2
                                                  0.1
                                                             2
                                                                      1000
##
## [[3]]
##
      confiLower confiUpper type method trueValue trialID sampleSize
## 1
          0.1055
                      0.3265 p1-p2
                                          1
                                                  0.2
                                                             1
                                                                      1500
```

```
## 2
          0.1249
                     0.3071 p1-p2
                                                0.2
                                                           1
                                                                    1500
## 3
                     0.3393 p1-p2
                                        1
                                                0.2
                                                           2
                                                                    1500
          0.1167
## 4
          0.1369
                     0.3191 p1-p2
                                        2
                                                0.2
                                                           2
                                                                   1500
## 5
          0.1949
                     0.3971 p1-p3
                                        1
                                                0.3
                                                           1
                                                                   1500
                     0.3871 p1-p3
                                        2
## 6
          0.2049
                                                0.3
                                                           1
                                                                   1500
## 7
          0.2266
                     0.4254 p1-p3
                                        1
                                                0.3
                                                           2
                                                                   1500
                     0.4171 p1-p3
                                        2
                                                           2
## 8
          0.2349
                                                0.3
                                                                   1500
                     0.1695 p2-p3
## 9
         -0.0095
                                        1
                                                0.1
                                                           1
                                                                   1500
## 10
         -0.0111
                     0.1711 p2-p3
                                        2
                                                0.1
                                                           1
                                                                    1500
                                                                   1500
## 11
          0.0100
                     0.1860 p2-p3
                                        1
                                                0.1
                                                           2
## 12
          0.0069
                     0.1891 p2-p3
                                        2
                                                0.1
                                                           2
                                                                   1500
```

Therefore, we get the result for one specific distribution. Combine them into one dataframe and save it for plotting.

confiData = Reduce(rbind,confiList)
confiData

##		${\tt confiLower}$	confiUpper	type	method	trueValue	${\tt trialID}$	sampleSize
##	1	0.1055	0.3265	p1-p2	1	0.2	1	500
##	2	0.1249	0.3071	p1-p2	2	0.2	1	500
##	3	0.1167	0.3393	p1-p2	1	0.2	2	500
##	4	0.1369	0.3191	p1-p2	2	0.2	2	500
##	5	0.1949	0.3971	p1-p3	1	0.3	1	500
##	6	0.2049	0.3871	p1-p3	2	0.3	1	500
##	7	0.2266	0.4254	p1-p3	1	0.3	2	500
##	8	0.2349	0.4171	p1-p3	2	0.3	2	500
##	9	-0.0095	0.1695	p2-p3	1	0.1	1	500
##	10	-0.0111	0.1711	p2-p3	2	0.1	1	500
##	11	0.0100	0.1860	p2-p3	1	0.1	2	500
##	12	0.0069	0.1891	p2-p3	2	0.1	2	500
##	13	0.1055	0.3265		1	0.2	1	1000
##	14	0.1249	0.3071		2	0.2	1	1000
##	15	0.1167	0.3393	p1-p2	1	0.2	2	1000
##	16	0.1369	0.3191		2	0.2	2	1000
##	17	0.1949	0.3971	p1-p3	1	0.3	1	1000
##	18	0.2049	0.3871	p1-p3	2	0.3	1	1000
##	19	0.2266	0.4254	p1-p3	1	0.3	2	1000
##	20	0.2349	0.4171	p1-p3	2	0.3	2	1000
##	21	-0.0095	0.1695	p2-p3	1	0.1	1	1000
##	22	-0.0111	0.1711		2	0.1	1	1000
##	23	0.0100	0.1860		1	0.1	2	1000
##	24	0.0069	0.1891	p2-p3	2	0.1	2	1000
##	25	0.1055	0.3265	p1-p2	1	0.2	1	1500
##	26	0.1249	0.3071	p1-p2	2	0.2	1	1500
##	27	0.1167	0.3393	p1-p2	1	0.2	2	1500
##	28	0.1369	0.3191		2	0.2	2	1500
##	29	0.1949	0.3971		1	0.3	1	1500
##	30	0.2049	0.3871	p1-p3	2	0.3	1	1500
##	31	0.2266	0.4254		1	0.3	2	1500
##	32	0.2349	0.4171		2	0.3	2	1500
##	33	-0.0095	0.1695		1	0.1	1	1500
##	34	-0.0111	0.1711		2	0.1	1	1500
##	35	0.0100	0.1860		1	0.1	2	1500
##	36	0.0069	0.1891	p2-p3	2	0.1	2	1500

```
saveRDS(confiData,"YL_Q1a_example.rds") ## R format data type
```

Question 2

Generating data

```
q = 0.1 # mixing probabilities
p = c(0.46, 0.44, 0.1)
r = c(0.34, 0.33, 0.33)
df
##
           [,1] [,2]
##
            252 259
##
            144 145
##
            104
                   96
## trialID
              1
                    2
Back to our earlier example. The sample size is 500. (Column sum). nrep=2. (Column number)
sampleSize = 500
nrep = 2
sampleSize_NV = rbinom(nrep, sampleSize, q)
sampleSize_NV # the number of people not going to vote, for column 1 and column 2
## [1] 57 48
sampleSize_V = sampleSize - sampleSize_NV
sampleSize_V # the number of people going to vote, for column 1 and column 2
## [1] 443 452
Then, we want to generate data according to each sample size (each column would have different sample size
for people vote and not vote)
VList = lapply(sampleSize_V,function(x){
  rmultinom(1, size = x, prob = p)
})
Vmat = Reduce(cbind, VList) # transfer to matrix format
Vmat #the exact number for people vote for p1 p2 p3
##
        [,1] [,2]
        216 184
## [1,]
## [2,]
         185
              222
## [3,]
          42
               46
NVList = lapply(sampleSize_NV,function(x){
 rmultinom(1, size = x, prob = r)
})
NVmat = Reduce(cbind, NVList) #transfer to matrix format
NVmat #the exact number for people not vote but said would vote for p1 p2 p3
##
        [,1] [,2]
## [1,]
          16
               18
## [2,]
          22
                22
## [3,]
          19
                8
```

Add these two matrix together gives us the mixed data. Each column sum is still 500

```
dfmix = Vmat+ NVmat
dfmix

## [,1] [,2]
## [1,] 232 202
## [2,] 207 244
## [3,] 61 54

colSums(dfmix)
```

```
## [1] 500 500
```

Once we have the similar data at question 1. We can just simply apply the defined functions.

```
dfmix = rbind(dfmix,trialID=1:2) # add trial id as last row
tmp = apply(dfmix, 2,confiFun,type="p1-p2",i=1,j=2)
tmp
```

```
## [[1]]
     confiLower confiUpper type method trueValue trialID
                    0.1697 p1-p2
                                              0.02
## 1
        -0.0697
                                       1
## 2
        -0.0411
                    0.1411 p1-p2
                                       2
                                              0.02
##
## [[2]]
     confiLower confiUpper type method trueValue trialID
##
## 1
        -0.2044
                    0.0364 p1-p2
                                       1
                                              0.02
## 2
        -0.1751
                                              0.02
                                                          2
                    0.0071 p1-p2
                                       2
```

Then we can design a function that generate mix data and calucate the pair difference, which is similar to confiDataFun.

```
confiMixDataFun <- function(sampleSize,q,r = c(0.34,0.33,0.33),nrep=2){</pre>
  set.seed(321)
  sampleSize_NV = rbinom(nrep, sampleSize, q)
  sampleSize_V = sampleSize - sampleSize_NV
  VList = lapply(sampleSize_V,function(x){
   rmultinom(1, size = x, prob = p)
  })
  Vmat = Reduce(cbind, VList) # transfer to matrix format
  NVList = lapply(sampleSize_NV,function(x){
   rmultinom(1, size = x, prob = r)
  })
  NVmat = Reduce(cbind, NVList)
  dfmix = Vmat+ NVmat
  dfmix = rbind(dfmix,trialID=1:nrep)
  delta_12 = apply(dfmix, 2,confiFun,type="p1-p2",i=1,j=2)
  delta_13 = apply(dfmix, 2,confiFun,type="p1-p3",i=1,j=3)
  delta_23 = apply(dfmix, 2,confiFun,type="p2-p3",i=2,j=3)
  res = Reduce(rbind,c(delta_12,delta_13,delta_23))
  res$sampleSize = sampleSize
  return(res)
```

```
}
confiMixDataFun(sampleSize = 500,q=0.1)
##
      confiLower confiUpper type method trueValue trialID sampleSize
## 1
         -0.0885
                      0.1525 p1-p2
                                          1
                                                 0.02
                                                              1
## 2
         -0.0591
                      0.1231 p1-p2
                                          2
                                                  0.02
                                                              1
                                                                       500
                                                              2
## 3
         -0.0888
                      0.1488 p1-p2
                                          1
                                                  0.02
                                                                       500
## 4
         -0.0611
                      0.1211 p1-p2
                                          2
                                                  0.02
                                                              2
                                                                       500
## 5
          0.2621
                      0.4339 p1-p3
                                          1
                                                  0.36
                                                              1
                                                                       500
## 6
          0.2569
                      0.4391 p1-p3
                                          2
                                                 0.36
                                                              1
                                                                       500
## 7
          0.2185
                      0.3975 p1-p3
                                          1
                                                  0.36
                                                              2
                                                                       500
                                                              2
## 8
          0.2169
                      0.3991 p1-p3
                                          2
                                                 0.36
                                                                       500
## 9
          0.2311
                      0.4009 p2-p3
                                          1
                                                  0.34
                                                              1
                                                                       500
## 10
                                          2
                                                                       500
          0.2249
                      0.4071 p2-p3
                                                 0.34
                                                              1
## 11
          0.1896
                      0.3664 p2-p3
                                          1
                                                  0.34
                                                              2
                                                                       500
## 12
          0.1869
                      0.3691 p2-p3
                                          2
                                                  0.34
                                                              2
                                                                       500
Apply to different sampleSize and q
resMix = lapply(seq(0.1,0.5,by=0.1), function(q){
  resList = lapply(sampleSizeVector, confiMixDataFun,q=q)
  resDF = Reduce(rbind,resList)
  resDF$mixRatio = q # Record q
  return(resDF)
})
resMix
## [[1]]
##
      confiLower confiUpper type method trueValue trialID sampleSize
## 1
         -0.0885
                      0.1525 p1-p2
                                                  0.02
                                          1
## 2
         -0.0591
                      0.1231 p1-p2
                                          2
                                                  0.02
                                                                       500
                                                              1
                      0.1488 p1-p2
## 3
         -0.0888
                                          1
                                                  0.02
                                                              2
                                                                       500
## 4
         -0.0611
                      0.1211 p1-p2
                                          2
                                                 0.02
                                                              2
                                                                       500
## 5
          0.2621
                      0.4339 p1-p3
                                          1
                                                  0.36
                                                              1
                                                                       500
                                          2
## 6
          0.2569
                      0.4391 p1-p3
                                                 0.36
                                                              1
                                                                       500
## 7
                                                              2
          0.2185
                      0.3975 p1-p3
                                          1
                                                  0.36
                                                                       500
                                                              2
## 8
                                          2
                                                                       500
          0.2169
                      0.3991 p1-p3
                                                  0.36
## 9
          0.2311
                      0.4009 p2-p3
                                          1
                                                  0.34
                                                              1
                                                                       500
## 10
          0.2249
                      0.4071 p2-p3
                                          2
                                                  0.34
                                                              1
                                                                       500
## 11
          0.1896
                      0.3664 p2-p3
                                                  0.34
                                                              2
                                                                       500
                                          1
                                                              2
## 12
          0.1869
                      0.3691 p2-p3
                                          2
                                                  0.34
                                                                       500
                                                 0.02
## 13
         -0.0362
                      0.1322 p1-p2
                                          1
                                                              1
                                                                      1000
                                          2
## 14
         -0.0164
                      0.1124 p1-p2
                                                  0.02
                                                              1
                                                                      1000
## 15
         -0.0916
                      0.0796 p1-p2
                                          1
                                                 0.02
                                                              2
                                                                      1000
## 16
         -0.0704
                      0.0584 p1-p2
                                          2
                                                  0.02
                                                              2
                                                                      1000
## 17
          0.2631
                      0.3889 p1-p3
                                          1
                                                 0.36
                                                              1
                                                                      1000
                      0.3904 p1-p3
## 18
          0.2616
                                          2
                                                  0.36
                                                              1
                                                                      1000
                                                              2
## 19
          0.2783
                      0.3977 p1-p3
                                          1
                                                 0.36
                                                                      1000
## 20
          0.2736
                      0.4024 p1-p3
                                          2
                                                  0.36
                                                              2
                                                                      1000
## 21
          0.2163
                      0.3397 p2-p3
                                          1
                                                 0.34
                                                              1
                                                                      1000
## 22
                                          2
                                                  0.34
                                                              1
                                                                      1000
          0.2136
                      0.3424 p2-p3
                      0.4039 p2-p3
                                                              2
## 23
          0.2841
                                          1
                                                  0.34
                                                                      1000
                                          2
                                                              2
## 24
          0.2796
                      0.4084 p2-p3
                                                  0.34
                                                                      1000
```

```
## 25
          -0.0274
                       0.1101 p1-p2
                                                  0.02
                                                                       1500
                                          1
                                                              1
## 26
         -0.0112
                                                  0.02
                                                                       1500
                       0.0939 p1-p2
                                          2
                                                              1
## 27
         -0.0675
                       0.0715 p1-p2
                                                  0.02
                                                              2
                                                                       1500
                                          1
## 28
         -0.0506
                       0.0546 p1-p2
                                          2
                                                  0.02
                                                              2
                                                                       1500
## 29
          0.2713
                       0.3740 p1-p3
                                          1
                                                  0.36
                                                              1
                                                                       1500
## 30
          0.2701
                       0.3752 p1-p3
                                          2
                                                  0.36
                                                              1
                                                                       1500
## 31
          0.2805
                       0.3795 p1-p3
                                          1
                                                  0.36
                                                              2
                                                                       1500
## 32
                       0.3826 p1-p3
                                          2
                                                              2
          0.2774
                                                  0.36
                                                                       1500
## 33
          0.2309
                       0.3318 p2-p3
                                          1
                                                  0.34
                                                              1
                                                                       1500
## 34
          0.2288
                       0.3339 p2-p3
                                          2
                                                  0.34
                                                              1
                                                                       1500
## 35
           0.2785
                       0.3775 p2-p3
                                          1
                                                  0.34
                                                              2
                                                                       1500
## 36
           0.2754
                       0.3806 p2-p3
                                          2
                                                  0.34
                                                              2
                                                                       1500
##
      mixRatio
## 1
            0.1
## 2
            0.1
## 3
            0.1
## 4
            0.1
## 5
            0.1
## 6
            0.1
## 7
            0.1
## 8
            0.1
## 9
            0.1
## 10
            0.1
## 11
            0.1
## 12
            0.1
## 13
            0.1
           0.1
## 14
## 15
            0.1
## 16
            0.1
## 17
            0.1
## 18
            0.1
## 19
            0.1
## 20
            0.1
## 21
            0.1
## 22
            0.1
## 23
            0.1
## 24
            0.1
## 25
            0.1
## 26
            0.1
## 27
            0.1
## 28
            0.1
## 29
            0.1
## 30
            0.1
## 31
            0.1
## 32
            0.1
## 33
           0.1
## 34
            0.1
## 35
            0.1
## 36
            0.1
##
## [[2]]
      confiLower confiUpper type method trueValue trialID sampleSize
##
         -0.0987
                       0.1387 p1-p2
                                                  0.02
## 1
                                          1
                                                              1
                                                                        500
## 2
          -0.0711
                       0.1111 p1-p2
                                          2
                                                  0.02
                                                              1
                                                                        500
```

	_						
##		-0.0638	0.1718 p1-p2	1	0.02	2	500
##	4	-0.0371	0.1451 p1-p2	2	0.02	2	500
##	5	0.2104	0.3896 p1-p3	1	0.36	1	500
##	6	0.2089	0.3911 p1-p3	2	0.36	1	500
##	7	0.2105	0.3935 p1-p3	1	0.36	2	500
##	8	0.2109	0.3931 p1-p3	2	0.36	2	500
##		0.1912	0.3688 p2-p3	1	0.34	1	500
	10	0.1889	0.3711 p2-p3	2	0.34	1	500
##		0.1587	0.3373 p2-p3	1	0.34	2	500
	12	0.1569	0.3391 p2-p3	2	0.34	2	500
	13	-0.0503	0.1163 p1-p2	1	0.02	1	1000
##	14	-0.0314	0.0974 p1-p2	2	0.02	1	1000
##	15	-0.0300	0.1360 p1-p2	1	0.02	2	1000
##	16	-0.0114	0.1174 p1-p2	2	0.02	2	1000
##	17	0.2255	0.3545 p1-p3	1	0.36	1	1000
##	18	0.2256	0.3544 p1-p3	2	0.36	1	1000
##	19	0.2289	0.3591 p1-p3	1	0.36	2	1000
##	20	0.2296	0.3584 p1-p3	2	0.36	2	1000
##		0.1935	0.3205 p2-p3	1	0.34	1	1000
	22	0.1926	0.3214 p2-p3	2	0.34	1	1000
	23	0.1775	0.3045 p2-p3	1	0.34	2	1000
	24	0.1766	0.3054 p2-p3	2	0.34	2	1000
	25	-0.0448	0.0914 p1-p2	1	0.02	1	1500
##		-0.0292	0.0759 p1-p2	2	0.02	1	1500
	27	-0.0286	0.1073 p1-p2	1	0.02	2	1500
##		-0.0132	0.0919 p1-p2	2	0.02	2	1500
	29	0.2342	0.3391 p1-p3	1	0.36	1	1500
##		0.2341	0.3392 p1-p3	2	0.36	1	1500
##	31	0.2378	0.3435 p1-p3	1	0.36	2	1500
##	32	0.2381	0.3432 p1-p3	2	0.36	2	1500
##	33	0.2114	0.3153 p2-p3	1	0.34	1	1500
##	34	0.2108	0.3159 p2-p3	2	0.34	1	1500
##	35	0.1994	0.3032 p2-p3	1	0.34	2	1500
	36	0.1988	0.3039 p2-p3	2	0.34	2	1500
##		mixRatio	1 1				
##	1	0.2					
##		0.2					
##		0.2					
##		0.2					
##		0.2					
##		0.2					
##		0.2					
##		0.2					
##		0.2					
	10	0.2					
	11	0.2					
##	12	0.2					
##	13	0.2					
##	14	0.2					
	15	0.2					
	16	0.2					
##		0.2					
##		0.2					
##		0.2					
##	19	0.2					

```
## 20
            0.2
## 21
            0.2
## 22
            0.2
## 23
            0.2
## 24
            0.2
## 25
            0.2
## 26
            0.2
## 27
            0.2
## 28
            0.2
## 29
            0.2
## 30
            0.2
## 31
            0.2
##
  32
            0.2
## 33
            0.2
## 34
            0.2
## 35
            0.2
## 36
            0.2
##
##
   [[3]]
##
       confiLower confiUpper type method trueValue trialID sampleSize
## 1
          -0.1026
                       0.1306 p1-p2
                                           1
                                                   0.02
                                                               1
                                                                         500
## 2
          -0.0771
                       0.1051 p1-p2
                                           2
                                                   0.02
                                                               1
                                                                         500
## 3
          -0.0457
                                                   0.02
                                                               2
                       0.1857 p1-p2
                                                                         500
                                           1
                       0.1611 p1-p2
## 4
          -0.0211
                                           2
                                                   0.02
                                                               2
                                                                         500
## 5
                                                   0.36
                                                               1
                                                                         500
           0.1590
                       0.3450 p1-p3
                                           1
                       0.3431 p1-p3
## 6
           0.1609
                                           2
                                                   0.36
                                                               1
                                                                         500
## 7
           0.1729
                       0.3631 p1-p3
                                           1
                                                   0.36
                                                               2
                                                                         500
## 8
                                           2
                                                   0.36
                                                               2
                                                                         500
           0.1769
                       0.3591 p1-p3
## 9
                       0.3304 p2-p3
                                           1
                                                   0.34
                                                               1
                                                                         500
           0.1456
                                           2
## 10
           0.1469
                       0.3291 p2-p3
                                                   0.34
                                                               1
                                                                         500
                                                               2
## 11
           0.1062
                       0.2898 p2-p3
                                           1
                                                   0.34
                                                                         500
## 12
           0.1069
                       0.2891 p2-p3
                                           2
                                                   0.34
                                                               2
                                                                         500
## 13
                                                   0.02
          -0.0621
                       0.1021 p1-p2
                                           1
                                                               1
                                                                        1000
## 14
          -0.0444
                       0.0844 p1-p2
                                           2
                                                   0.02
                                                               1
                                                                        1000
                       0.1248 p1-p2
                                                               2
## 15
          -0.0388
                                           1
                                                   0.02
                                                                        1000
## 16
          -0.0214
                       0.1074 p1-p2
                                           2
                                                   0.02
                                                               2
                                                                        1000
## 17
           0.1797
                       0.3123 p1-p3
                                           1
                                                   0.36
                                                               1
                                                                        1000
## 18
           0.1816
                       0.3104 p1-p3
                                           2
                                                   0.36
                                                               1
                                                                        1000
                                                               2
## 19
           0.1829
                       0.3171 p1-p3
                                           1
                                                   0.36
                                                                        1000
## 20
                       0.3144 p1-p3
                                                               2
           0.1856
                                           2
                                                   0.36
                                                                        1000
                       0.2917 p2-p3
## 21
           0.1603
                                           1
                                                   0.34
                                                               1
                                                                        1000
                       0.2904 p2-p3
## 22
           0.1616
                                           2
                                                   0.34
                                                               1
                                                                        1000
## 23
           0.1414
                       0.2726 p2-p3
                                           1
                                                   0.34
                                                               2
                                                                        1000
## 24
                                           2
                                                               2
           0.1426
                       0.2714 p2-p3
                                                   0.34
                                                                        1000
## 25
          -0.0125
                                                   0.02
                                                               1
                                                                        1500
                       0.1218 p1-p2
                                           1
## 26
                                           2
           0.0021
                       0.1072 p1-p2
                                                   0.02
                                                               1
                                                                        1500
## 27
                                                   0.02
                                                               2
          -0.0426
                       0.0906 p1-p2
                                           1
                                                                        1500
## 28
          -0.0286
                                           2
                                                   0.02
                                                               2
                       0.0766 p1-p2
                                                                        1500
## 29
           0.2171
                       0.3256 p1-p3
                                           1
                                                   0.36
                                                               1
                                                                        1500
## 30
                                           2
           0.2188
                       0.3239 p1-p3
                                                   0.36
                                                               1
                                                                        1500
                       0.2869 p1-p3
## 31
                                                   0.36
                                                               2
                                                                        1500
           0.1771
                                           1
                                                               2
## 32
                                           2
           0.1794
                       0.2846 p1-p3
                                                   0.36
                                                                        1500
## 33
           0.1638
                       0.2695 p2-p3
                                           1
                                                   0.34
                                                               1
                                                                        1500
## 34
           0.1641
                       0.2692 p2-p3
                                           2
                                                   0.34
                                                               1
                                                                        1500
```

```
0.1538
                      0.2622 p2-p3
                                                 0.34
                                                             2
                                                                      1500
                                         1
## 36
                      0.2606 p2-p3
                                                             2
          0.1554
                                         2
                                                 0.34
                                                                      1500
##
      mixRatio
## 1
           0.3
## 2
           0.3
## 3
           0.3
## 4
           0.3
## 5
           0.3
## 6
           0.3
           0.3
## 7
## 8
           0.3
## 9
           0.3
## 10
           0.3
## 11
           0.3
           0.3
## 12
## 13
           0.3
## 14
           0.3
## 15
           0.3
## 16
           0.3
## 17
           0.3
## 18
           0.3
## 19
           0.3
## 20
           0.3
## 21
           0.3
## 22
           0.3
## 23
           0.3
## 24
           0.3
## 25
           0.3
## 26
           0.3
## 27
           0.3
## 28
           0.3
## 29
           0.3
## 30
           0.3
## 31
           0.3
## 32
           0.3
## 33
           0.3
## 34
           0.3
## 35
           0.3
## 36
           0.3
##
## [[4]]
      confiLower confiUpper type method trueValue trialID sampleSize
##
## 1
         -0.0918
                      0.1398 p1-p2
                                         1
                                                 0.02
                                                             1
                                                                       500
## 2
         -0.0671
                      0.1151 p1-p2
                                         2
                                                 0.02
                                                             1
                                                                       500
## 3
         -0.1229
                      0.1109 p1-p2
                                         1
                                                 0.02
                                                             2
                                                                       500
                                                             2
## 4
         -0.0971
                                         2
                                                 0.02
                                                                       500
                      0.0851 p1-p2
                      0.3363 p1-p3
## 5
          0.1477
                                         1
                                                 0.36
                                                             1
                                                                       500
## 6
          0.1509
                      0.3331 p1-p3
                                         2
                                                 0.36
                                                             1
                                                                      500
## 7
                                                 0.36
                                                             2
                                                                      500
          0.1559
                      0.3401 p1-p3
                                         1
## 8
          0.1569
                      0.3391 p1-p3
                                         2
                                                 0.36
                                                             2
                                                                      500
## 9
          0.1248
                      0.3112 p2-p3
                                         1
                                                 0.34
                                                             1
                                                                      500
## 10
                      0.3091 p2-p3
          0.1269
                                         2
                                                 0.34
                                                             1
                                                                      500
## 11
                                                 0.34
                                                             2
          0.1616
                      0.3464 p2-p3
                                         1
                                                                      500
## 12
          0.1629
                      0.3451 p2-p3
                                         2
                                                 0.34
                                                             2
                                                                      500
```

```
-0.0276
                       0.1336 p1-p2
                                                   0.02
                                                                        1000
## 13
                                           1
                                                               1
## 14
          -0.0114
                       0.1174 p1-p2
                                           2
                                                   0.02
                                                               1
                                                                        1000
## 15
          -0.0900
                       0.0720 p1-p2
                                                   0.02
                                                               2
                                                                        1000
                                           1
## 16
          -0.0734
                       0.0554 p1-p2
                                           2
                                                   0.02
                                                               2
                                                                        1000
## 17
           0.1532
                       0.2908 p1-p3
                                           1
                                                   0.36
                                                               1
                                                                        1000
                       0.2864 p1-p3
## 18
           0.1576
                                           2
                                                   0.36
                                                               1
                                                                        1000
## 19
           0.1295
                       0.2645 p1-p3
                                           1
                                                   0.36
                                                               2
                                                                        1000
                       0.2614 p1-p3
                                                               2
## 20
           0.1326
                                           2
                                                   0.36
                                                                        1000
## 21
           0.1021
                       0.2359 p2-p3
                                           1
                                                   0.34
                                                               1
                                                                        1000
## 22
           0.1046
                       0.2334 p2-p3
                                           2
                                                   0.34
                                                               1
                                                                        1000
                       0.2738 p2-p3
## 23
           0.1382
                                           1
                                                   0.34
                                                               2
                                                                        1000
## 24
                                           2
                                                               2
                                                                        1000
           0.1416
                       0.2704 p2-p3
                                                   0.34
                       0.0868 p1-p2
## 25
          -0.0468
                                                   0.02
                                                               1
                                                                        1500
                                           1
                                           2
## 26
          -0.0326
                       0.0726 p1-p2
                                                   0.02
                                                               1
                                                                        1500
## 27
          -0.0474
                       0.0860 p1-p2
                                           1
                                                   0.02
                                                               2
                                                                        1500
## 28
                                                               2
          -0.0332
                       0.0719 p1-p2
                                           2
                                                   0.02
                                                                        1500
## 29
           0.1835
                       0.2925 p1-p3
                                                   0.36
                                                               1
                                                                        1500
                                           1
                       0.2906 p1-p3
## 30
                                                   0.36
           0.1854
                                           2
                                                               1
                                                                        1500
## 31
           0.1780
                       0.2874 p1-p3
                                           1
                                                   0.36
                                                               2
                                                                        1500
## 32
                                           2
                                                               2
           0.1801
                       0.2852 p1-p3
                                                   0.36
                                                                        1500
## 33
           0.1641
                       0.2719 p2-p3
                                           1
                                                   0.34
                                                               1
                                                                        1500
## 34
           0.1654
                       0.2706 p2-p3
                                           2
                                                   0.34
                                                               1
                                                                        1500
           0.1592
                       0.2675 p2-p3
                                                   0.34
                                                               2
                                                                        1500
## 35
                                           1
                                                               2
## 36
           0.1608
                       0.2659 p2-p3
                                           2
                                                   0.34
                                                                        1500
##
      mixRatio
## 1
            0.4
## 2
            0.4
## 3
            0.4
## 4
            0.4
## 5
            0.4
## 6
            0.4
## 7
            0.4
## 8
            0.4
## 9
            0.4
## 10
            0.4
## 11
            0.4
## 12
            0.4
## 13
            0.4
## 14
            0.4
## 15
            0.4
## 16
            0.4
            0.4
## 17
## 18
            0.4
## 19
            0.4
## 20
            0.4
## 21
            0.4
## 22
            0.4
## 23
            0.4
## 24
            0.4
## 25
            0.4
## 26
            0.4
## 27
            0.4
## 28
            0.4
## 29
            0.4
```

```
## 30
            0.4
## 31
            0.4
## 32
            0.4
## 33
            0.4
  34
##
            0.4
## 35
            0.4
## 36
            0.4
##
## [[5]]
##
      confiLower confiUpper type method trueValue trialID sampleSize
## 1
          -0.0466
                       0.1786 p1-p2
                                           1
                                                   0.02
                                                               1
## 2
          -0.0251
                       0.1571 p1-p2
                                           2
                                                   0.02
                                                                         500
                                                               1
                       0.1290 p1-p2
## 3
          -0.0970
                                                               2
                                                                         500
                                           1
                                                   0.02
                                                               2
## 4
          -0.0751
                       0.1071 p1-p2
                                           2
                                                   0.02
                                                                         500
## 5
           0.1005
                       0.2995 p1-p3
                                                   0.36
                                                               1
                                                                         500
                                           1
## 6
           0.1089
                       0.2911 p1-p3
                                           2
                                                   0.36
                                                               1
                                                                         500
## 7
           0.0800
                       0.2760 p1-p3
                                                   0.36
                                                               2
                                                                         500
                                           1
## 8
                                                               2
           0.0869
                       0.2691 p1-p3
                                           2
                                                   0.36
                                                                         500
## 9
           0.0382
                       0.2298 p2-p3
                                                   0.34
                                                               1
                                                                         500
                                           1
## 10
           0.0429
                       0.2251 p2-p3
                                           2
                                                   0.34
                                                               1
                                                                         500
## 11
           0.0649
                       0.2591 p2-p3
                                           1
                                                   0.34
                                                               2
                                                                         500
## 12
           0.0709
                       0.2531 p2-p3
                                           2
                                                   0.34
                                                               2
                                                                         500
                       0.0858 p1-p2
## 13
          -0.0778
                                                   0.02
                                                               1
                                                                        1000
                                           1
                       0.0684 p1-p2
## 14
          -0.0604
                                           2
                                                   0.02
                                                               1
                                                                        1000
                       0.0656 p1-p2
                                                               2
## 15
          -0.0936
                                                   0.02
                                           1
                                                                        1000
                       0.0504 p1-p2
                                                                        1000
## 16
          -0.0784
                                           2
                                                   0.02
                                                               2
## 17
           0.1625
                       0.2955 p1-p3
                                           1
                                                   0.36
                                                               1
                                                                        1000
## 18
                       0.2934 p1-p3
                                           2
                                                   0.36
                                                               1
                                                                        1000
           0.1646
## 19
                                                               2
           0.0849
                       0.2231 p1-p3
                                                   0.36
                                                                        1000
                                           1
## 20
                                                               2
           0.0896
                       0.2184 p1-p3
                                           2
                                                   0.36
                                                                        1000
## 21
           0.1586
                       0.2914 p2-p3
                                           1
                                                   0.34
                                                               1
                                                                        1000
## 22
           0.1606
                       0.2894 p2-p3
                                           2
                                                   0.34
                                                               1
                                                                        1000
## 23
                       0.2376 p2-p3
                                                   0.34
                                                               2
           0.0984
                                           1
                                                                        1000
                                                                        1000
## 24
           0.1036
                       0.2324 p2-p3
                                           2
                                                   0.34
                                                               2
## 25
          -0.0512
                       0.0806 p1-p2
                                           1
                                                   0.02
                                                               1
                                                                        1500
## 26
          -0.0379
                       0.0672 p1-p2
                                           2
                                                   0.02
                                                               1
                                                                        1500
## 27
          -0.0430
                       0.0883 p1-p2
                                           1
                                                   0.02
                                                               2
                                                                        1500
## 28
          -0.0299
                       0.0752 p1-p2
                                           2
                                                   0.02
                                                               2
                                                                        1500
## 29
           0.1456
                       0.2571 p1-p3
                                           1
                                                   0.36
                                                               1
                                                                        1500
## 30
           0.1488
                       0.2539 p1-p3
                                           2
                                                   0.36
                                                               1
                                                                        1500
                       0.2535 p1-p3
##
  31
           0.1412
                                           1
                                                   0.36
                                                               2
                                                                        1500
## 32
           0.1448
                       0.2499 p1-p3
                                           2
                                                   0.36
                                                               2
                                                                        1500
                       0.2419 p2-p3
##
   33
                                                   0.34
                                                               1
           0.1314
                                           1
                                                                        1500
## 34
                       0.2392 p2-p3
                                           2
           0.1341
                                                   0.34
                                                               1
                                                                        1500
                       0.2301 p2-p3
## 35
           0.1192
                                                   0.34
                                                               2
                                                                        1500
                                           1
                                                               2
                       0.2272 p2-p3
                                           2
                                                   0.34
                                                                        1500
## 36
           0.1221
      mixRatio
##
## 1
            0.5
## 2
            0.5
## 3
            0.5
## 4
            0.5
## 5
            0.5
## 6
            0.5
## 7
            0.5
```

```
## 8
           0.5
## 9
           0.5
## 10
           0.5
## 11
           0.5
## 12
           0.5
## 13
           0.5
## 14
           0.5
## 15
           0.5
## 16
           0.5
## 17
           0.5
## 18
           0.5
## 19
           0.5
## 20
           0.5
## 21
           0.5
## 22
           0.5
## 23
           0.5
## 24
           0.5
## 25
           0.5
## 26
           0.5
## 27
           0.5
## 28
           0.5
## 29
           0.5
## 30
           0.5
## 31
           0.5
## 32
           0.5
## 33
           0.5
## 34
           0.5
## 35
           0.5
## 36
           0.5
```

Combine and save

```
saveRDS(Reduce(rbind,resMix),'YL_Q2_example.rds')
```