

# CEE263B Final Project Report Source Code for Fortran90-based Program

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### 1. Regionalmodel.f90

```
! regionalmodel
! usage: generate a basic regional
! model that solves the equations of
! atompheric dynamics.
! Yun Zhang 04/24/2015
! @stanford
! MODEL DESCRIPTION
! The purpose of this project is to
! develop a basic regional- or global-scale
! model that solves the equations of atmospheric
! dynamics, except for the water-vapor continuity
! equation. Diabatic energy sources and sinks and
! eddy diffusion are ignored. Winds are driven
! primarily by pressure gradients.
program regionalmodel
  use iso fortran env
  use allocate_variable
  use phys
  use output
  implicit none
  integer:: nt
  real(dp):: tstart,tend
  ! initialize lat and long
  call initialize_lat_long_coriolis(lat_c,long_c,lat_uface,long_uface,lat_vface,long_vface,f_c)
  ! part 1)
  ! calculate dsigma
  ! assume mean surface altitude 0m
  ! from table B.1
  call initialize_vertical_sigima(zbot_test,pa_test,sigma_bot,dsigma)
  ! part 2)
  ! calculate initial surface pressure
  call initialize_air_pressure_surf(Pa_surf)
  ! calculate initial column pressure
initialize_pressure_system(pi_c,pi_c_new,pi_c_tminus1,Pa_bot,P_bot,P_c,Pa_c,Pa_surf,sigma_bo
```

```
! part 3)
  ! initialize water mass mixing ratio
  call initialize_watermass_mixingratio(qv_c,qv_c_new,Qqv)
  ! initialize temperature for each cell
  call initialize_temperature_system(Temp_c,Pa_c,qv_c,PVT_c,PVT_c_new,P_c,P_bot,Qheat)
  ! initialize gas concentration for each cell
  if(gasmodel==1)
                                                                                               call
initialize_gas_concentration(gas_c,gas_c_new,Pa_c,P_c,P_bot,lat_c,long_c,Qgas)
  ! part 4) initialize air density for each cell center
  call calculate_air_density(rhoa_c,Pa_c,qv_c,Temp_c)
  ! part 5) initialize velocity field, zero everywhere
  call initialize_velocity_field(u,u_new,v,v_new,w_sigma,w_sigma_new,lat_uface,lat_vface,&
     long_uface,long_vface)
  ! part 6) initialize turbulence term
  call calculate_eddy_viscousity_diffusivity(nu_t,K_t)
  ! part 7) initialize heat source
  if(heatsource==1) call calculate heat source(Pa c,Qheat,lat c,long c,0)
  ! initialize specific humidity source
  if(qvsource==1) call calculate_qv_source(Pa_c,Qqv,lat_c,long_c,nt)
  ! gas source
  if(gasmodel==1) call calculate_gas_source(Pa_c,Qgas,lat_c,long_c,0)
  ! part 8) initialize geopotential
calculate_geopotential(geopot_bot,geopot_c,geopot_c_tminus1,P_c,P_bot,PVT_c,lat_c,long_c,0)
  print *, "The initialization process is finished!"
  ! store cpu time
  call cpu_time(tstart)
  ! main loop for physical function
  do nt=1,Ndt
```

```
! calculate column pressure at flux face
     call calculate_fluxface_column_pressure(pi_c,pi_uface,pi_vface)
     ! calcualte flux sum for each cell each layer
     call
calculate_fluxsum(fluxsum,flux_uface,flux_vface,u,v,pi_uface,pi_vface,lat_c,lat_vface,dsigma)
     ! update column pressure for each cell center
     call calculate column pressure(pi c,pi c new,lat c,fluxsum)
     ! update w sigma
     call calculate_w_sigma(w_sigma_new,pi_c,pi_c_new,lat_c,fluxsum,sigma_bot,dsigma)
     if(qvmodel==1) then
       ! calculate qv at flux face
       call calculate fluxface qv(qv c,qv uface,qv vface,qv bot,P c,P bot,&
         lat_uface,long_uface,lat_vface,long_vface,nt)
       ! update specific humidity
       call calculate_scalar_field(qv_c, qv_c_new, qv_bot, &
         pi c,pi c new,qv uface, qv vface,flux uface,flux vface,lat c, rhoa c,&
         dsigma, w_sigma_new,K_t,Pa_c,Qqv)
     endif
     if(PVTmodel==1) then
       ! calculate PVT at flux face
       call calculate_fluxface_PVT(PVT_c,PVT_uface,PVT_vface,PVT_bot,&
         P_c,P_bot,lat_uface,long_uface,lat_vface,long_vface,nt)
       ! update potential temperature
       call calculate scalar field(PVT c, PVT c new, PVT bot, &
         pi_c,pi_c_new,PVT_uface, PVT_vface,flux_uface,flux_vface,lat_c, rhoa_c,&
         dsigma, w sigma new, K t, Pa c, Qheat)
     endif
     if(gasmodel==1) then
       ! calculate gas at flux face
       call calculate fluxface gas(gas c,gas uface,gas vface,gas bot,&
         P_c,P_bot,lat_uface,long_uface,lat_vface,long_vface,nt)
       ! update potential temperature
       call calculate_scalar_field(gas_c, gas_c_new, gas_bot, &
         pi_c,pi_c_new,gas_uface, gas_vface,flux_uface,flux_vface,lat_c, rhoa_c,&
         dsigma, w_sigma_new,K_t,Pa_c,Qgas)
     endif
```

```
! update velocity field
    call calculate_velocity_field(pi_c,pi_c_new,pi_c,pi_c_tminus1,lat_c, lat_vface,&
       u,u_new,u,v,v_new,v,flux_uface,flux_vface,dsigma,&
       sigma_bot,w_sigma_new,f_c,geopot_c,geopot_c_tminus1,&
       PVT c,P bot,P c,nu t,rhoa c)
    ! update air pressure
    call calculate_pressure_field(pi_c_new,Pa_c_new,Pa_bot_new,&
       P c new,P bot new,sigma bot)
    ! update air temperature
    call calculate_air_temperature(PVT_c_new,Temp_c_new,qv_c_new,Pa_c_new)
    ! update air density
    call calculate_air_density(rhoa_c_new,Pa_c_new,qv_c_new,Temp_c_new)
    ! update eddy diffusivity and viscousity
    if(turbmodel==1) then
       call calculate_eddy_viscousity_diffusivity(nu_t,K_t)
    endif
    ! update geopotential
    call calculate_geopotential(geopot_bot,geopot_c,geopot_c_tminus1,P_c_new,P_bot_new,&
       PVT_c_new,lat_c,long_c,nt)
    ! for Matsuno method
    if(matsuno==1) then
       ! calculate column pressure at flux face
       call calculate_fluxface_column_pressure(pi_c_new,pi_uface,pi_vface)
       ! calcualte flux sum for each cell each layer
       call
calculate_fluxsum(fluxsum,flux_uface,flux_vface,u_new,v_new,pi_uface,pi_vface,lat_c,lat_vface,
dsigma)
       ! store the first calculation of pi for velocity calculation
       pi_c_tmp=pi_c_new
       ! update column pressure for each cell center
       call calculate column pressure(pi c,pi c new,lat c,fluxsum)
       ! update w_sigma
       call calculate_w_sigma(w_sigma_new,pi_c,pi_c_new,lat_c,fluxsum,sigma_bot,dsigma)
       if(qvmodel==1) then
        ! calculate qv at flux face
        call calculate_fluxface_qv(qv_c_new,qv_uface,qv_vface,qv_bot,P_c_new,P_bot_new,&
```

```
lat_uface,long_uface,lat_vface,long_vface,nt)
 ! update specific humidity
 call calculate_scalar_field(qv_c, qv_c_new, qv_bot, &
  pi_c,pi_c_new,qv_uface, qv_vface,flux_uface,flux_vface,lat_c, rhoa_c_new,&
  dsigma, w_sigma_new,K_t,Pa_c_new,Qqv)
endif
if(PVTmodel==1) then
  ! calculate PVT at flux face
  call calculate_fluxface_PVT(PVT_c_new,PVT_uface,PVT_vface,PVT_bot,&
    P c new,P bot new,lat uface,long uface,lat vface,long vface,nt)
  ! store the first calculation of pVT for velocity calculation
  PVT_c_tmp=PVT_c_new
  ! update potential temperature
  call calculate_scalar_field(PVT_c, PVT_c_new, PVT_bot, &
    pi c,pi c new,PVT uface, PVT vface,flux uface,flux vface,lat c, rhoa c new,&
    dsigma, w_sigma_new,K_t,Pa_c_new,Qheat)
endif
if(gasmodel==1) then
  ! calculate PVT at flux face
  call calculate_fluxface_gas(gas_c_new,gas_uface,gas_vface,gas_bot,&
    P_c_new,P_bot_new,lat_uface,long_uface,lat_vface,long_vface,nt)
  ! update potential temperature
  call calculate scalar field(gas c, gas c new, gas bot, &
    pi_c,pi_c_new,gas_uface, gas_vface,flux_uface,flux_vface,lat_c, rhoa_c_new,&
    dsigma, w_sigma_new,K_t,Pa_c_new,Qgas)
endif
! update velocity field
call calculate_velocity_field(pi_c,pi_c_new,pi_c_tmp,pi_c_tminus1,lat_c, lat_vface,&
  u,u new,u new,v,v new,v new,flux uface,flux vface,dsigma,&
  sigma_bot,w_sigma_new,f_c,geopot_c,geopot_c_tminus1,&
  PVT_c_tmp,P_bot_new,P_c_new,nu_t,rhoa_c_new)
! update air pressure
call calculate pressure field(pi c new,Pa c new,Pa bot new,&
  P_c_new,P_bot_new,sigma_bot)
! update air temperature
call calculate_air_temperature(PVT_c_new,Temp_c_new,qv_c_new,Pa_c_new)
! update eddy diffusivity and viscousity
if(turbmodel==1) then
```

```
call calculate_eddy_viscousity_diffusivity(nu_t,K_t)
       endif
       ! update geopotential
       call
calculate_geopotential(geopot_bot,geopot_c,geopot_c_tminus1,P_c_new,P_bot_new,&
         PVT_c_new,lat_c,long_c,nt)
    endif
    ! update heat source
    if(heatsource==1) call calculate_heat_source(Pa_c_new,Qheat,lat_c,long_c,nt)
    ! update specific humidity source
    if(qvsource==1) call calculate_qv_source(Pa_c,Qqv,lat_c,long_c,nt)
    ! update gas source
    if(gasmodel==1) call calculate_gas_source(Pa_c,Qgas,lat_c,long_c,nt)
    ! replace all variable with the new variables
    ! column pressure
    pi_c_tminus1=pi_c
    pi_c=pi_c_new
    ! pressure variable
    Pa bot=Pa bot new
    P_bot=P_bot_new
    Pa_c=Pa_c_new
    Pa_bot=Pa_bot_new
    ! temperature
    Temp_c=Temp_c_new
    PVT_c=PVT_c_new
    gas c=gas c new
    ! specific humidity
    qv_c=qv_c_new
    ! air density
    rhoa_c=rhoa_c_new
    ! velocity field
    w_sigma=w_sigma_new
    u=u_new
    v=v_new
    ! output results: pi_c,Pa_c,PTV_c,u,v,w_sigma,nu_t,K_t,geobot_c, Temp_c, rha_c, qv
    ! at first time step open all file
    if(outputswitch==1) then
```

```
if(nt==1) call output_open_txt_files()
  if(nt==1 .or. mod(nt,Nout)==0) then
      call output_all_variables()
  endif
  if(nt==Ndt) call output_close_files()
  endif
enddo

! calculate runtime
 call cpu_time(tend)
 print *, 'The program has been finished. The runtime is ',(tend-tstart),'sec'
end program regionalmodel
```

#### 2. allocatevariable.f90

```
! regional model module - allocate_variable
! usage: allocate all variables in the program
! Yun Zhang 04/24/2015
! @stanford
! unit clarification
! pressure: hpa
! temperature: K
! latitude,longitude: degree
! density: kg/m^3
! altitude, length: m
! gravity: m/s/s
module allocate_variable
  use constant_parameter
  implicit none
  ! Initialize parameter
  ! lat and long for each cell
  real(dp),dimension(NLAT,NLONG):: lat_c, long_c ! latitude and longitude
  real(dp),dimension(NLAT,NLONG):: f_c ! coriolis coefficient
  real(dp),dimension(NLAT+1,NLONG):: lat vface, long vface! latitude at v flux face
  real(dp),dimension(NLAT,NLONG+1):: lat_uface, long_uface! longtitude at u flux face
  ! part 1)
  ! test column to calculate dsigma
  real(dp), dimension(0:NVERT):: zbot_test! layer bottom elevation at test column
  real(dp), dimension(0:NVERT):: pa_test! layer bottom pressure at test column
  real(dp), dimension(0:NVERT):: sigma bot! sigma value at each column, constant for all time
step
  real(dp), dimension(NVERT):: dsigma! sigma(k+1)-sigma(k)
  ! part 2) pressure setup
  ! initialize surface pressure
  real(dp), dimension(NLAT,NLONG):: Pa_surf! surface pressure
  real(dp), dimension(NLAT,NLONG):: pi_c_new, pi_c, pi_c_tminus1, pi_c_tmp! column pressure
at t+1 t t-1
  real(dp), dimension(NLAT+1,NLONG):: pi_vface! column pressure at v face
  real(dp), dimension(NLAT,NLONG+1):: pi_uface! column pressure at u face
  ! calculate all pressure at different layers for different cells
  real(dp), dimension(NLAT,NLONG,0:NVERT):: Pa_bot, Pa_bot_new! layer bottom air pressure
```

```
at each layer at t t+1
  real(dp), dimension(NLAT,NLONG,0:NVERT):: P_bot, P_bot_new! layer bottom P at each layer
at t t+!
  real(dp), dimension(NLAT,NLONG,NVERT):: Pa_c, Pa_c_new! cell center air pressure at t t+1
  real(dp), dimension(NLAT,NLONG,NVERT):: P_c, P_c_new ! cell center P at t t+1
  ! part 3) initialize temperature, humidity and gas
  real(dp), dimension(NLAT,NLONG,NVERT):: Temp_c, Temp_c_new! cell center Temperature
at t + 1
  real(dp), dimension(NLAT,NLONG,NVERT):: PVT_c, PVT_c_new, PVT_c_tmp! cell center
potential virtual temperature at t t+1
  real(dp), dimension(NLAT,NLONG,0:NVERT):: PVT_bot, qv_bot, gas_bot! layer bottom
potential virtual temperature and specific humidity
  real(dp), dimension(NLAT,NLONG,NVERT):: qv_c, qv_c_new !cell center specific humidity at
t t+1
  real(dp), dimension(NLAT,NLONG,NVERT):: gas_c, gas_c_new !cell center gas concentration
at t t+1
  real(dp), dimension(NLAT+1,NLONG,NVERT):: PVT vface, qv vface, gas vface! v face
potential virtual temperature and specific humidity
  real(dp), dimension(NLAT,NLONG+1,NVERT):: PVT_uface, qv_uface, gas_uface ! u face
potential virtual temperature and specific humidity
  ! part 4) initialize air density
  real(dp), dimension(NLAT,NLONG,NVERT):: rhoa_c, rhoa_c_new! cell center air density at t
t+1
  ! part 5) initialize velocity field
  real(dp), dimension(NLAT,NLONG+1,NVERT):: u, u_new ! u at t t+1
  real(dp), dimension(NLAT+1,NLONG,NVERT):: v, v_new! v at t t+1
  real(dp), dimension(NLAT,NLONG,0:NVERT):: w sigma, w sigma new! w sigma at t t+!
  ! part 6) calculate column pressure at flux face
  real(dp), dimension(NLAT,NLONG,NVERT):: fluxsum! fluxsum(i,j,k) means the sum of flux
from layer 1 to k at cell i,i
  real(dp), dimension(NLAT,NLONG+1,NVERT):: flux_uface! the sum of flux from u direction
at each layer
  real(dp), dimension(NLAT+1,NLONG,NVERT):: flux_vface! the sum of flux from v direction
at each layer
  ! part 7) turbulence variable
  real(dp),dimension(NLAT,NLONG,NVERT):: nu_t,K_t ! cell center eddy viscousity and
diffusity
```

```
! part 8) heat/gas source variable
real(dp),dimension(NLAT,NLONG,NVERT):: Qheat ! cell center heat source
real(dp),dimension(NLAT,NLONG,NVERT):: Qgas ! cell center gas source
real(dp),dimension(NLAT,NLONG,NVERT):: Qqv ! cell center specific source
! part 9) geopotential
real(dp), dimension(NLAT,NLONG,NVERT):: geopot_c,geopot_c_tminus1 ! geopotential at t t-

real(dp), dimension(NLAT,NLONG,0:NVERT)::geopot_bot ! geopotential at layer bottom
end module allocate_variable
```

```
3. basic_state.f90
! regional model module - basic_state
! usage: external procedure for all air
! state equation to transfer air, temp
! pressure, density and other related
! aspects
! Yun Zhang 04/24/2015
! @stanford
module basic state
  use constant_parameter
  implicit none
contains
! standard_atmophere_interp
! usage: use table B.1 to interpolate pressure, altitude,
! gravity, temperature, air density
! input: a vertical array for horizontal cell
! output: get the relevant data based on input
! input_mode: 'z'=altitude, 'p'=pressure, 'g'=gravity
! 'T'=temperature,'rho'=density
! output mode is same as input mode
! Yun Zhang @Stanford
! 04/25/2015
function standard_atmophere_interp(input,N,input_mode,output_mode) result(output)
  integer, intent(in)::N
  real(dp), dimension(1:N),intent(in)::input
  real(dp), dimension(1:N)::output
  character, intent(in)::input_mode,output_mode
  real(dp), dimension(5):: tmp_data
  real(dp), dimension(79):: alt, p, g, T, rho, basedata, outdata
  integer:: i,j,k,order1,order2
  ! read tableb1
  open (unit=99, file='tableb1.txt', status='old', action='read')
  do i=1,79
    read(99,*) tmp_data
    alt(i)=tmp_data(1)*1000
    p(i)=tmp_data(3)
```

 $g(i)=tmp_data(2)$ 

```
T(i)=tmp_data(4)
  rho(i)=tmp\_data(5)
enddo
close(99)
order1=1
order2=-1
select case(input_mode)
  case ('z')
     basedata=alt
     order1=-1
     order2=-1
  case ('p')
     basedata=p
  case ('g')
     basedata=g
  case ('T')
     basedata=T
  case ('rho')
     basedata=rho
end select
select case(output_mode)
  case ('z')
     outdata=alt
  case ('p')
     outdata=p
  case ('g')
     outdata=g
  case ('T')
     outdata=T
  case ('rho')
     outdata=rho
end select
! find section no. at basedata for each value in input data
! then interpolate data based on the section number
k=79
do i=1,N
  do j=1,k
     if((input(i)*order1)>(basedata(j)*order1)) then
       output(i) = outdata(j + order2*1) + (input(i) - basedata(j + order2*1)) &
          /(basedata(j)-basedata(j+order2*1))*(outdata(j)-outdata(j+order2*1))
       !print
                                input_mode,
                                                  input(i),
                                                               basedata(j),basedata(j+order2*1),
                         į,
```

```
outdata(j),outdata(j+order2*1), output(i)

exit
endif
enddo
enddo
end function standard_atmophere_interp
end module basic_state
```

## 4. boundary.f90 ! regional model module - boundary ! usage: include all the functions and ! subroutines to define boundary condition ! Yun Zhang 04/30/2015 ! @stanford module boundary use constant\_parameter implicit none contains ! boundary\_potential\_virtual\_temp ! usage: provide the PVT value at domain ! boundary ! Yun Zhang 04/30/2015 ! @stanford function boundary\_potential\_virtual\_temp(lat,long,nlayer,t) result(output) real(dp),intent(in)::lat,long,t integer, intent(in):: nlayer real(dp)::output ! change boundary condition for differnt problem output=1.0\_dp end function boundary potential virtual temp ! boundary\_specific\_humidity ! usage: provide the qv value at domain ! boundary ! Yun Zhang 05/02/2015 ! @stanford function boundary\_specific\_humidity(lat,long,nlayer,t) result(output) real(dp),intent(in)::lat,long,t integer, intent(in):: nlayer real(dp)::output

! change boundary condition for differnt problem

```
output=1.0_dp
end function boundary_specific_humidity
! boundary_gas
! usage: provide the gas concentration value at domain
! boundary
! Yun Zhang 05/02/2015
! @stanford
function boundary_gas(lat,long,nlayer,t) result(output)
 real(dp),intent(in)::lat,long,t
 integer, intent(in):: nlayer
 real(dp)::output
  ! change boundary condition for differnt problem
 output=1.0_dp
end function boundary_gas
! boundary_surf_geopotential
! usage: provide the geopotential boundary
! value at the surface layer
! Yun Zhang 04/30/2015
! @stanford
function boundary_surf_geopotential(lat,long,t) result(output)
 real(dp),intent(in)::lat,long,t
 real(dp)::output
  ! change boundary condition for differnt problem
 output=0.0_dp
end function boundary_surf_geopotential
```

end module boundary

```
5. constant_parameter.f90
! regional model module - constant_parameter
! usage: define all the paramter and
! precision setup
! Yun Zhang 04/24/2015
! @stanford
! unit clarification
! pressure: hpa
! temperature: K
! latitude,longitude: rad
! density: kg/m<sup>3</sup>
! altitude, length: m
! gravity: m/s/s
module constant parameter
  use iso_fortran_env, only: real32, real64, int64
  ! basic setup
  integer, parameter:: sp=real32
  integer, parameter:: dp=real64
  integer, parameter:: li=int64
  real(dp), parameter:: pi = 4.0_dp*atan(1.0_dp) ! pi
  real(dp), parameter:: k therm=0.286 dp
  real(dp), parameter:: R_prime=2.8704_dp !m^3 hpa kg^-1 K^-1
  real(dp), parameter:: Cp d=1004.67 ! J kg^-1 K^-1
  real(dp), parameter:: Omega=7.2921e-5! rad/s rotation frequency for earth
  real(dp), parameter:: Re=6371000.0_dp! Earth radius use unit in million of meters
  ! switch
  integer, parameter:: PVTmodel=1! whether the air is dry (0) or not(1)
  integer, parameter:: PTVbound=0! whether set exact boundary condition (1) or not (0)
  integer, parameter:: heatsource=0! whether there is heat source or sink in each cell
  integer, parameter:: gasmodel=1! whether to simulation passive gas transport
  integer, parameter:: gasbound=0! whether to use specified boundary condition
  integer, parameter:: gassource=0! whether there is a gas source within the domain
  integer, parameter:: qvmodel=1! whether the air is dry (0) or not(1)
  integer, parameter:: qvbound=0! whether set exact boundary condition (1) or not (0)
  integer, parameter:: qvsource=0! whether there is a specific humidity source within the domain
  integer, parameter:: turbmodel=0! whether to turn on turbulence
  integer, parameter:: outputswitch=1! whether output results or not
  integer, parameter:: periodicBC=0! whether to use periodic boundary condition
  integer, parameter:: matsuno=1! whether to use matsuno scheme
  integer, parameter:: coriolis=1! whether to consider coriolis effects
```

```
! numerical parameter
  integer, parameter:: Ndt=500! the numbers of time steps
  integer, parameter:: Nout=50! how often to output results
  integer, parameter:: Nrep=1! how often to report progress
  real(dp), parameter:: dt=5.0_dp! time step0
  ! grid parameter
  real(dp), parameter:: lat_0=-1/180*pi! southwest corner latitude
  real(dp), parameter:: long 0=-1/180*pi! southwest corner longitude
  integer, parameter:: NLAT=40! the numbers of latitude cells
  integer, parameter:: NLONG=40! the numbers of longitude cells
  integer, parameter:: NVERT=15! the number of vertical layers
  real(dp), parameter:: dlamda_e=0.05/180*pi! differential longitude to represent cell size
  real(dp), parameter:: dphi=0.05/180*pi! differential latitude to represent cell size
  real(dp), parameter:: phi_center=lat_0+((NLAT-1)/2+DBLE(mod((NLAT-1),2))/2)*dphi ! the
latitude center in the domain
                                  lamda_center=long_0+((NLONG-1)/2+DBLE(mod((NLONG-
  real(dp),
                 parameter::
1),2))/2)*dlamda_e! the longitude center in the domain
  real(dp), parameter:: z_surf=0.0_dp! surface elevation
  ! Phys parameter
  real(dp), parameter:: Pa_top=250_dp ! top pressure constant
  real(dp),
            parameter:: Pa below=265 dp, rhoa below=0.414 dp, g below=9.7764 dp,
z_below=10000_dp! values from table B.1
  real(dp), parameter:: ztop_test=z_below+(Pa_below-Pa_top)*100/rhoa_below/g_below ! top
elevation for test column
  real(dp), parameter:: Pa_base=1000.0_dp, dpa_peak=10.0_dp
  ! output results: pi_c,Pa_c,PTV_c,u,v,w_sigma,nu_t,K_t,geobot_c, Temp_c, rhoa_c
  ! output file names
  character(*),
                                      resultfolder="/Users/zyaj/Documents/atomsphere-regional-
                    parameter::
model/results/"
  character(*), parameter:: pi_file="pi.txt"! file for column pressure results
  character(*), parameter:: pi_format="(1xf9.4)"
  integer, parameter:: pi_file_no=1
  character(*), parameter:: Pa_file="Pa.txt"! file for air pressure results
  character(*), parameter:: Pa_format="(1xf9.4)"
  integer, parameter:: Pa_file_no=2
  character(*), parameter:: PTV_file="PVT.txt"! file for potential virtual temperature results
  integer, parameter:: PVT_file_no=3
  character(*), parameter:: PVT_format="(1xf9.4)"
  character(*), parameter:: u_file="u.txt"! file for u results
```

```
integer, parameter:: u_file_no=4
  character(*), parameter:: u_format="(1xf9.6)"
  character(*), parameter:: v_file="v.txt"! file for v results
  integer, parameter:: v file no=5
  character(*), parameter:: v_format="(1xf9.6)"
  character(*), parameter:: w_file="w.txt" ! file for w_sigma results
  integer, parameter:: w_file_no=6
  character(*), parameter:: w_format="(1xf9.6)"
  character(*), parameter:: nu file="nu.txt"! file for eddy viscousity results
  integer, parameter:: nu_file_no=7
  character(*), parameter:: nu_t_format="(1xf9.4)"
  character(*), parameter:: K_t_file="K_t.txt"! file for eddy diffusivity results
  integer, parameter:: K_t_file_no=8
  character(*), parameter:: K t format="(1xf9.4)"
  character(*), parameter:: geopot_file="geopot.txt" ! file for geopotential results
  integer, parameter:: geopot_file_no=9
  character(*), parameter:: geopot_format="(1xf12.4)"
  character(*), parameter:: Temp file="temp.txt"! file for temperature results
  integer, parameter:: Temp_file_no=10
  character(*), parameter:: Temp_format="(1xf9.4)"
  character(*), parameter:: rhoa_file="rhoa.txt"! file for air density results
  integer, parameter:: rhoa_file_no=11
  character(*), parameter:: rhoa_format="(1xf6.4)"
  character(*), parameter:: qv_file="qv.txt"! file for specific humidity results
  integer, parameter:: qv file no=12
  character(*), parameter:: qv_format="(1xf6.4)"
  character(*), parameter:: gas_file="gas.txt"! file for potential virtual temperature results
  integer, parameter:: gas_file_no=13
  character(*), parameter:: gas_format="(1xf10.8)"
end module constant parameter
```

#### 6. initialization.f90

```
! regional model module - initialization
! usage: initialize all the variables
! Yun Zhang 04/29/2015
! @stanford
module initialization
  use constant_parameter
 use basic_state
 implicit none
contains
! initialize_lat_long
! usage: initialize all lat and long for cell center and flux face
! Yun Zhang @Stanford
! 04/25/2015
subroutine initialize_lat_long_coriolis(lat_c,long_c,lat_uface,long_uface,lat_vface,long_vface,f_c)
 integer::i,j,k
 real(dp),dimension(NLAT,NLONG),intent(inout):: lat_c, long_c,f_c
 real(dp),dimension(NLAT+1,NLONG),intent(inout):: lat_vface, long_vface
 real(dp),dimension(NLAT,NLONG+1),intent(inout):: lat_uface, long_uface
  ! calculate lat and long tidu for all cell
 do i=1,NLAT
    do j=1,NLONG
      lat_c(i,j)=lat_0+(i-1)*dphi
      long_c(i,j)=long_0+(j-1)*dlamda_e
    enddo
 enddo
  ! coriolis efficients
 if(coriolis==1) then
    f_c=2*Omega*sin(lat_c)
 else
    f_c=0.0_dp
 endif
  ! uface
 lat_uface(:,1:NLONG)=lat_c
 lat_uface(:,NLONG+1)=lat_c(:,NLONG)
 long_uface(:,1:NLONG)=long_c-0.5*dlamda_e
 long_uface(:,NLONG+1)=long_c(:,NLONG)+0.5*dlamda_e
```

```
! vface
 lat_vface(1:NLAT,:)=lat_c-0.5*dphi
 lat vface(NLAT+1,:)=lat c(NLAT,:)+0.5*dphi
 long_vface(1:NLAT,:)=long_c
 long_vface(NLAT+1,:)=long_c(NLAT,:)
end subroutine initialize_lat_long_coriolis
! initialize_vertical_sigima
! usage: calculate and initialize sigma grid for test column
! Yun Zhang @Stanford
! 04/25/2015
subroutine initialize_vertical_sigima(zbot_test,pa_test,sigma_bot,dsigma)
  integer::i,j,k
 real(dp), dimension(0:NVERT),intent(inout):: zbot test, pa test, sigma bot! from layer 0
 real(dp), dimension(NVERT),intent(inout):: dsigma
 do i=0,NVERT
    zbot_test(i)=z_surf+(ztop_test-z_surf)*(1-DBLE(i)/NVERT)
 enddo
  ! calculate pa_test
  pa test=standard atmophere interp(zbot test,NVERT+1,'z','p')
 pa_test(0)=Pa_top
  ! calculate sigma_bot
 sigma_bot=(pa_test-Pa_top)/(pa_test(NVERT)-Pa_top)
 dsigma=sigma_bot(1:NVERT)-sigma_bot(0:(NVERT-1))
end subroutine initialize vertical sigima
! initialize_air_pressure_surf
! usage: initialize the air pressure at surface for each cell
! Yun Zhang @stanford
! 05/01/2015
subroutine initialize_air_pressure_surf(Pa_surf)
 real(dp), dimension(NLAT, NLONG), intent(inout) :: Pa\_surf
 integer::i,j
 real(dp)::tmp
 do i=1,NLAT
    do j=1,NLONG
      tmp=((Re/1000000*cos((lat_0+(i-1)*dphi+phi_center)/2)*(long_0+(j-1)*dlamda_e-
```

```
lamda_center))**2)/2
      tmp=tmp+((Re/1000000*(lat 0+(i-1)*dphi-phi center))**2)/2
      Pa_surf(i,j)=Pa_base+dpa_peak*exp(-tmp)
    enddo
  enddo
end subroutine initialize_air_pressure_surf
! initialize pressure system
! usage: initialize the column pressure, air pressure
! at the bottom and center for each layer at each cell
! Yun Zhang @stanford
! 05/01/2015
subroutine
initialize_pressure_system(pi_c_old,pi_c_new,pi_c_tminus1,Pa_bot,P_bot,P_c,Pa_c,Pa_surf,sigm
a_bot)
  real(dp),dimension(NLAT,NLONG),intent(inout)::pi c old,pi c new,pi c tminus1
  real(dp),dimension(NLAT,NLONG,0:NVERT),intent(inout)::Pa_bot,P_bot
  real(dp),dimension(0:NVERT),intent(in)::sigma_bot
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::Pa_c,P_c
  real(dp),dimension(NLAT,NLONG),intent(in)::Pa_surf
  integer::i,j
  pi c old=Pa surf-Pa top
  pi_c_tminus1=pi_c_old
  ! provide approximate value for pi_timus1 at boundaries
  pi_c_tminus1(1,:)=pi_c_old(1,:)+(pi_c_old(1,:)-pi_c_old(2,:))
  pi\_c\_tminus1(NLAT,:) = pi\_c\_old(NLAT,:) + (pi\_c\_old(NLAT,:) - pi\_c\_old(NLAT-1,:))
  pi c tminus1(:,1)=pi c old(:,1)+(pi c old(:,1)-pi c old(:,2))
  pi\_c\_tminus1(:,NLONG) = pi\_c\_old(:,NLONG) + (pi\_c\_old(:,NLONG) - pi\_c\_old(:,NLONG-1))
  pi_c_new=pi_c_old
  ! calculate pressure at different vertical layer
  ! layer bottom
  do i=1,NLAT
    do j=1,NLONG
      Pa\_bot(i,j,:)=sigma\_bot*pi\_c\_old(i,j)+Pa\_top
      P_{bot(i,j,:)}=(Pa_{bot(i,j,:)}/1000)**k_{therm}
    enddo
  enddo
  ! layer center
  do i=1,NLAT
```

```
do j=1,NLONG
               P_c(i,j,:)=1/(1+k_t)*(P_bot(i,j,1:NVERT)*Pa_bot(i,j,1:NVERT)-
Pa_bot(i,j,0:(NVERT-1))*P_bot(i,j,0:(NVERT-1)))
               P_c(i,j,:)=P_c(i,j,:)/(Pa_bot(i,j,1:NVERT)-Pa_bot(i,j,0:NVERT-1))
               Pa_c(i,j,:)=1000*(P_c(i,j,:)**(1/k_therm))
          enddo
    enddo
end subroutine initialize pressure system
! initialize_watermass_mixingratio
! usage: initialize qv for each cell each layer
! Yun Zhang 05/02/2015
! @stanford
subroutine initialize_watermass_mixingratio(qv_c,qv_c_new,Qqv)
    real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::qv c
    real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::qv_c_new, Qqv
    qv_c=0.0_dp
    qv_c_new=qv_c
     Qqv=0.0_dp
end subroutine initialize watermass mixingratio
! initialize_temperature_system
! usage: first initial the southwest corner of the domain
! then set all the value for all cells and layers
! Yun Zhang @stanford
! 05/01/2015
subroutine
initialize_temperature_system(Temp_c,Pa_c,qv_c,PVT_c_old,PVT_c_new,P_c,P_bot,Qheat)
real(dp), dimension(NLAT, NLONG, NVERT), intent(inout):: Temp\_c, PVT\_c\_old, PVT\_c\_new, Qhear and the property of the propert
t
    real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::qv_c,Pa_c,P_c
    real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::P_bot
    real(dp)::tmp
    integer::i,j,k
     ! first choose one corner use the southwest cornder (1,1,:)
    Temp_c(1,1,:)=standard_atmophere_interp(Pa_c(1,1,:),NVERT,'p','T')
     ! set all other cells temperature and potential virtual temperature
```

```
do i=1,NLAT
           do j=1,NLONG
                 Temp_c(i,j,:)=Temp_c(1,1,:)
           enddo
     enddo
     ! set potential temperature at cell center
     PVT_c_old=Temp_c*(1+0.608*qv_c)*((1000/Pa_c)**k_therm)
     PVT c new=PVT c old
     Qheat=0.0_dp
end subroutine initialize_temperature_system
! initialize gas concentration
! usage: set the initial value for passive gas concentration
! Yun Zhang @stanford
! 05/01/2015
subroutine initialize_gas_concentration(gas_c_old,gas_c_new,Pa_c,P_c,P_bot,lat_c,long_c,Qgas)
     real(dp), dimension(NLAT, NLONG, NVERT), intent(inout):: gas\_c\_old, gas\_c\_new, Qgas\_outless and the property of the control of the property 
     real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::Pa_c,P_c
     real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::P_bot
     real(dp),dimension(NLAT,NLONG),intent(in)::lat_c,long_c
     real(dp)::tmp
     integer::i,j,k
     ! set all other cells temperature and potential virtual temperature
     do i=1,NLAT
           do j=1,NLONG
                 if(j>18 .and. j<22 .and. i>18 .and. i<22) then
                       gas_c_old(i,j,:)=1.0_dp
                 else
                       gas_c_old(i,j,:)=0.0_dp !Temp_c(1,1,:)
                 endif
           enddo
     enddo
     ! set potential temperature at cell center
     gas_c_new=gas_c_old
     Qgas=0.0_dp
end subroutine initialize_gas_concentration
! initialize_velocity_field
! usage: initialize field velocity field
```

```
! Yun Zhang @stanford
! 05/01/2015
subroutine
initialize\_velocity\_field(u,u\_new,v,v\_new,w\_sigma\_old,w\_sigma\_new,lat\_uface,lat\_vface,long\_u
face,long_vface)
  real(dp), dimension(NLAT,NLONG+1,NVERT),intent(inout):: u,u_new
  real(dp), dimension(NLAT+1,NLONG,NVERT),intent(inout):: v,v_new
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(inout):: w_sigma_old, w_sigma_new
  real(dp), dimension(NLAT,NLONG+1),intent(in)::lat_uface,long_uface
  real(dp), dimension(NLAT+1,NLONG),intent(in)::long_vface,lat_vface
  u = 0.0_dp
  v = 0.0_dp
  u_new=u
  v_new=v
  w_sigma_old=0.0_dp
  w_sigma_new=0.0_dp
end subroutine initialize_velocity_field
```

end module initialization

```
7. output.f90
! regional model module - output
! usage: output all results
! Yun Zhang 05/03/2015
! @stanford
module output
  use allocate variable
  use constant_parameter
  implicit none
contains
!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
! output_open_files
! usage: open all output files for output
! Yun Zhang 05/03/2015
! @stanford
!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
subroutine output_open_bin_files()
  open (unit = pi_file_no, file = resultfolder//pi_file, status='new',form='unformatted',recl=2*10)
  open (unit = Pa_file_no, file = resultfolder//Pa_file, status='new',form='unformatted',recl=2*10)
  if(PVTmodel==1)
                       open
                                (unit
                                        =
                                             PVT file no,
                                                             file
                                                                         resultfolder//PTV file,
status='new',form='unformatted',recl=2*10)
  open (unit = u file no, file = resultfolder//u file, status='new', form='unformatted', recl=2*10)
  open (unit = v_file_no, file = resultfolder//v_file, status='new',form='unformatted',recl=2*10)
  open (unit = w_file_no, file = resultfolder//w_file, status='new',form='unformatted',recl=2*10)
  open (unit = nu_file_no, file = resultfolder//nu_file, status='new',form='unformatted',recl=2*10)
              (unit
  open
                                   K_t_file_no,
                                                       file
                                                                          resultfolder//K_t_file,
status='new',form='unformatted',recl=2*10)
             (unit
                        =
                                geopot_file_no,
                                                      file
                                                                       resultfolder//geopot_file,
  open
                                                               =
status='new',form='unformatted',recl=2*10)
  if(PVTmodel==1)
                                                                        resultfolder//Temp_file,
                       open
                               (unit
                                      = Temp_file_no,
                                                             file
status='new',form='unformatted',recl=2*10)
  open
              (unit
                                  rhoa_file_no,
                                                       file
                                                                          resultfolder//rhoa_file,
status='new',form='unformatted',recl=2*10)
  if(qvmodel==1)
                      open
                               (unit
                                              qv_file_no,
                                                              file
                                                                            resultfolder//qv_file,
status='new',form='unformatted',recl=2*10)
  if(gasmodel==1)
                       open
                                                                            resultfolder//qv_file,
                                (unit
                                              gas_file_no,
                                                              file
status='new',form='unformatted',recl=2*10)
```

end subroutine output\_open\_bin\_files

```
! output open files
! usage: open all output files for output
! Yun Zhang 05/03/2015
! @stanford
subroutine output_open_txt_files()
  open (unit = pi_file_no, file = resultfolder//pi_file)
  open (unit = Pa file no, file = resultfolder//Pa file)
  if(PVTmodel==1) open (unit = PVT_file_no, file = resultfolder//PTV_file)
  open (unit = u_file_no, file = resultfolder//u_file)
  open (unit = v_file_no, file = resultfolder//v_file)
  open (unit = w_file_no, file = resultfolder//w_file)
  open (unit = nu file no, file = resultfolder//nu file)
  open (unit = K_t_file_no, file = resultfolder//K_t_file)
  open (unit = geopot_file_no, file = resultfolder//geopot_file)
  if(PVTmodel==1) open (unit = Temp_file_no, file = resultfolder//Temp_file)
  open (unit = rhoa file no, file = resultfolder//rhoa file)
  if(qvmodel==1) open (unit = qv_file_no, file = resultfolder//qv_file)
  if(gasmodel==1) open (unit = gas_file_no, file = resultfolder//gas_file)
end subroutine output_open_txt_files
! output_all_variables
! usage: output all variables
! Yun Zhang 05/03/2015
! @stanford
subroutine output_all_variables()
  ! column pressure
  call output_2Dcellcenter_variables(pi_c,pi_file_no,pi_format)
  ! air pressure
  call output_3Dcellcenter_variables(Pa_c,Pa_file_no,Pa_format)
  ! u
  call output_3Duface_variables(u,u_file_no,u_format)
  ! v
  call output_3Dvface_variables(v,v_file_no,v_format)
  ! w_sigma
  call output_3Dvertical_variables(w_sigma,w_file_no,w_format)
```

```
! eddy viscousity
  call output_3Dcellcenter_variables(nu_t,nu_file_no,nu_t_format)
  ! eddy diffusivity
  call output_3Dcellcenter_variables(K_t,K_t_file_no,K_t_format)
  ! geopotential
  call output_3Dcellcenter_variables(geopot_c,geopot_file_no,geopot_format)
  if(PVTmodel==1) then
    ! Temperature
    call output_3Dcellcenter_variables(Temp_c,Temp_file_no,Temp_format)
    ! potential virtual temperature
    call output_3Dcellcenter_variables(PVT_c,PVT_file_no,PVT_format)
  endif
  ! air density
  call output_3Dcellcenter_variables(rhoa_c,rhoa_file_no,rhoa_format)
  ! specific humidity
  if(qvmodel==1) call output_3Dcellcenter_variables(qv_c,qv_file_no,qv_format)
  ! gas concentration
  if(gasmodel==1) call output_3Dcellcenter_variables(gas_c,gas_file_no,gas_format)
end subroutine output_all_variables
! output 3Dcellcenter variables
! usage: output 3D cellcenter all variables
! Yun Zhang 05/03/2015
! @stanford
subroutine output_3Dcellcenter_variables(Value,file_no,format)
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT
    do j=1,NLONG
      do k=1,NVERT-1
         write(file_no, format, iostat=ios, advance="no") Value(i,j,k)
      enddo
```

```
write(file_no, format, iostat=ios) Value(i,j,NVERT)
       if ( ios = 0 ) then
        print *,file_no
        stop "Write error in output file"
       endif
    enddo
  enddo
end subroutine output_3Dcellcenter_variables
! output_3Duface_variables
! usage: output 3D variables at u flux face
! Yun Zhang 05/03/2015
! @stanford
subroutine output_3Duface_variables(Value,file_no,format)
  real(dp),dimension(NLAT,NLONG+1,NVERT),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT
    do j=1,NLONG+1
       do k=1,NVERT-1
         write(file_no, format, iostat=ios,advance="no") Value(i,j,k)
       enddo
       write(file_no, format, iostat=ios) Value(i,j,NVERT)
       if ( ios = 0 ) then
        print *,file_no
        stop "Write error in output file"
       endif
    enddo
  enddo
end subroutine output_3Duface_variables
!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
! output_3Duface_variables
! usage: output 3D variables at v flux face
! Yun Zhang 05/03/2015
! @stanford
!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
subroutine output_3Dvface_variables(Value,file_no,format)
  real(dp), dimension(NLAT+1, NLONG, NVERT), intent(in) :: Value \\
  integer, intent(in):: file_no
  integer:: i,j,k,ios
```

```
character(*), intent(in)::format
  do i=1,NLAT+1
    do j=1,NLONG
      do k=1,NVERT-1
         write(file_no, format, iostat=ios,advance="no") Value(i,j,k)
      write(file_no, format, iostat=ios) Value(i,j,NVERT)
      if ( ios = 0 ) then
        print *,file_no
       stop "Write error in output file"
      endif
    enddo
  enddo
end subroutine output_3Dvface_variables
! output_3Dvertical_variables
! usage: output 3D variables at vertical face layer top-bottom
! Yun Zhang 05/03/2015
! @stanford
subroutine output_3Dvertical_variables(Value,file_no,format)
  real(dp),dimension(NLAT,NLONG,0:NVERT),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT
    do j=1,NLONG
      do k=0,NVERT-1
         write(file_no, format, iostat=ios,advance="no") Value(i,j,k)
      write(file_no, format, iostat=ios) Value(i,j,NVERT)
      if ( ios = 0 ) then
       print *,file_no
       stop "Write error in output file"
      endif
      enddo
  enddo
end subroutine output_3Dvertical_variables
```

```
! output_2Dcellcenter_variables
! usage: output 2D cellcenter all variables
! Yun Zhang 05/03/2015
! @stanford
subroutine output_2Dcellcenter_variables(Value,file_no,format)
  real(dp),dimension(NLAT,NLONG),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT
    do j=1,NLONG-1
       write(file_no, format, iostat=ios, advance="no") Value(i,j)
    enddo
    write(file_no, format, iostat=ios) Value(i,NLONG)
    if ( ios = 0 ) then
     print *,file_no
     stop "Write error in output file"
    endif
  enddo
end subroutine output 2Dcellcenter variables
! output_2Duface_variables
! usage: output 2D cellcenter at uface
! Yun Zhang 05/03/2015
! @stanford
!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
subroutine output_2Duface_variables(Value,file_no,format)
  real(dp),dimension(NLAT,NLONG+1),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT
    do j=1,NLONG
       write(file_no, format, iostat=ios,advance="no") Value(i,j)
    enddo
    write(file_no, format, iostat=ios) Value(i,NLONG+1)
    if ( ios = 0 ) then
       print *,file_no
       stop "Write error in output file"
```

```
endif
  enddo
end subroutine output_2Duface_variables
! output_2Dvface_variables
! usage: output 2D cellcenter at v flux face
! Yun Zhang 05/03/2015
! @stanford
subroutine output_2Dvface_variables(Value,file_no,format)
  real(dp),dimension(NLAT+1,NLONG),intent(in):: Value
  integer, intent(in):: file_no
  integer:: i,j,k,ios
  character(*), intent(in)::format
  do i=1,NLAT+1
    do j=1,NLONG-1
      write(file no, format, iostat=ios,advance="no") Value(i,j)
    enddo
    write(file_no, format, iostat=ios) Value(i,NLONG)
    if ( ios = 0 ) then
     print *,file_no
     stop "Write error in output file"
    endif
  enddo
end subroutine output_2Dvface_variables
! output_close_files
! usage: close all output files for output
! Yun Zhang 05/03/2015
! @stanford
subroutine output_close_files()
  close (pi_file_no)
  close (Pa_file_no)
  close (PVT_file_no)
  close (u_file_no)
  close (v_file_no)
  close (w_file_no)
  close (nu_file_no)
  close (K_t_file_no)
  close (geopot_file_no)
  close (Temp_file_no)
```

close (rhoa\_file\_no)
 close (qv\_file\_no)
end subroutine output\_close\_files

end module output

```
8. phys.f90
! regional model module - phys
! usage: include all the subroutines
! and functions to calculate physical equations
! Yun Zhang 04/29/2015
! @stanford
module phys
 use constant_parameter
 use boundary
 use turbulence
 use source
 use initialization
 implicit none
contains
! calculate_air_density
! usage: calculate air density for each cell
! each layer
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate_air_density(rhoa_c,Pa_c,qv_c,Temp_c)
 real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::Pa_c,qv_c,Temp_c
 real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::rhoa_c
 rhoa_c=Pa_c/R_prime/(1+0.608*qv_c)/Temp_c
end subroutine calculate_air_density
! calculate_mass_weighed_P
! usage: calculate P_c P_bot
! each layer
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate_mass_weighed_P(Pa_bot,P_bot,P_c)
 real(dp),dimension(NLAT,NLONG,0:NVERT),intent(in)::Pa_bot
 real(dp),dimension(NLAT,NLONG,0:NVERT),intent(inout)::P_bot
 real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::P_c
 integer::i,j,k
 do i=1,NLAT
```

do j=1,NLONG

```
P_{bot(i,j,:)}=(Pa_{bot(i,j,:)}/1000)**k_{therm}
      P_c(i,j,:)=1.0_dp/(1+k_t)*(P_bot(i,j,1:NVERT)*Pa_bot(i,j,1:NVERT)-
Pa\_bot(i,j,0:(NVERT-1))*Pa\_bot(i,j,0:(NVERT-1)))
      P_c(i,j,:)=P_c(i,j,:)/(Pa_bot(i,j,1:NVERT)-Pa_bot(i,j,0:NVERT-1))
    enddo
  enddo
end subroutine calculate_mass_weighed_P
! calculate_fluxface_column_pressure
! usage: calculate column pressure at each edge
! of each cell. The values will be used to calculate
! cell-centered column pressure
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate fluxface column pressure(pi c old,pi uface,pi vface)
  integer::i,j
  real(dp), dimension(NLAT,NLONG), intent(in)::pi_c_old
  real(dp), dimension(NLAT,NLONG+1), intent(inout):: pi_uface
  real(dp), dimension(NLAT+1,NLONG), intent(inout):: pi_vface
  ! calculate uface
  ! use central differencing
  do i=1,NLAT
    if(periodicBC==1) then
      pi\_uface(i,1)=0.5*(pi\_c\_old(i,1)+pi\_c\_old(i,NLONG))
      pi\_uface(i,NLONG+1)=0.5*(pi\_c\_old(i,1)+pi\_c\_old(i,NLONG))
    else
      pi_uface(i,1)=pi_c_old(i,1)
      pi_uface(i,NLONG+1)=pi_c_old(i,NLONG)
    pi\_uface(i,2:NLONG) = 0.5*(pi\_c\_old(i,1:(NLONG-1)) + pi\_c\_old(i,2:NLONG))
  enddo
  ! calculate vface
  ! use central differencing
  do i=1,NLONG
    if(periodicBC==1) then
      pi_vface(1,i)=0.5*(pi_c_old(1,i)+pi_c_old(NLAT,i))
      pi_vface(NLAT+1,i)=0.5*(pi_c_old(1,i)+pi_c_old(NLAT,i))
    else
      pi_vface(1,i)=pi_c_old(1,i)
```

```
pi_vface(NLAT+1,i)=pi_c_old(NLAT,i)
    endif
    pi_vface(2:NLAT,i)=0.5*(pi_c_old(1:(NLAT-1),NLONG)+pi_c_old(2:NLAT,NLONG))
end subroutine calculate_fluxface_column_pressure
! calculate_fluxsum
! usage:calculate fluxsum for each cell and each layer
! fluxsum(i,j,k) means the sum of flux of 4 edges
! from layer 1 to layer k at cell i,j
! and also calculate flux_uface and flux_vface
! Yun Zhang 04/30/2015
! @stanford
subroutine
calculate_fluxsum(fluxsum,flux_uface,flux_vface,u,v,pi_uface,pi_vface,lat_c,lat_vface,dsigma)
  integer:: k
  real(dp), dimension(NVERT),intent(in):: dsigma
  real(dp), dimension(NLAT,NLONG,NVERT),intent(inout):: fluxsum
  real(dp), dimension(NLAT,NLONG+1,NVERT), intent(in):: u
  real(dp), dimension(NLAT+1,NLONG,NVERT), intent(in):: v
  real(dp), dimension(NLAT,NLONG+1), intent(in):: pi uface
  real(dp), dimension(NLAT+1,NLONG), intent(in):: pi_vface,lat_vface
  real(dp), dimension(NLAT,NLONG),intent(in):: lat c
  real(dp), dimension(NLAT,NLONG+1,NVERT),intent(inout):: flux_uface
  real(dp), dimension(NLAT+1,NLONG,NVERT),intent(inout):: flux_vface
  ! reset all flux as zero
  fluxsum=0.0 dp
  flux_vface=0.0_dp
  flux_uface=0.0_dp
  ! set for the first layer 7.15 7.16
  do k=1,NVERT
    flux_uface(:,:,k)=u(:,:,k)*pi_uface*Re*dphi
    flux_vface(:,:,k)=v(:,:,k)*pi_vface*Re*dlamda_e*cos(lat_vface)
  enddo
  k=1
  fluxsum(:,:,k)=(flux_uface(:,2:(NLONG+1),k)-flux_uface(:,1:NLONG,k))*dsigma(k)
  fluxsum(:,:,k) = fluxsum(:,:,k) + (flux_vface(2:(NLAT+1),:,k) - flux_vface(1:NLAT,:,k)) * dsigma(k)
  ! for other layers
```

```
do k=2,NVERT
    fluxsum(:,:,k)=fluxsum(:,:,k-1)+(flux uface(:,2:(NLONG+1),k)-
flux_uface(:,1:NLONG,k))*dsigma(k)
    fluxsum(:,:,k)=fluxsum(:,:,k)+(flux vface(2:(NLAT+1),:,k)-
flux_vface(1:NLAT,:,k))*dsigma(k)
  enddo
  !print
fluxsum(1,1,NVERT),flux\_uface(1,1,1),flux\_uface(1,2,1),flux\_vface(1,1,1),flux\_vface(2,1,1)
end subroutine calculate fluxsum
! calculate_column_pressure
! usage: update column pressure for each cell
! and call by regional model every time step
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate column pressure(pi c old,pi c new,lat c,fluxsum)
  integer:: i,j,k
  real(dp), dimension(NLAT,NLONG,NVERT),intent(in):: fluxsum
  real(dp), dimension(NLAT,NLONG),intent(inout):: pi_c_new
  real(dp), dimension(NLAT,NLONG),intent(in):: pi_c_old
  real(dp), dimension(NLAT,NLONG),intent(in):: lat_c
  ! calculate new column pressure
  pi_c_new=pi_c_old-dt/(Re**2)/dphi/dlamda_e/cos(lat_c)*fluxsum(:,:,NVERT)
end subroutine calculate_column_pressure
! calculate w sigma
! usage: update w_sigma after each time step
! for each layer using continuity equation for
! each layer
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate_w_sigma(w_sigma, pi_c_old,pi_c_new,lat_c,fluxsum,sigma_bot,dsigma)
  integer:: i,j,k
  real(dp),dimension(NLAT,NLONG,0:NVERT),intent(inout)::w_sigma
  real(dp),dimension(NLAT,NLONG),intent(in):: pi_c_old,pi_c_new,lat_c
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: fluxsum
  real(dp),dimension(NVERT),intent(in):: dsigma
  real(dp),dimension(0:NVERT),intent(in):: sigma_bot
```

```
w_sigma(:,:,0)=0.0_dp
  w_sigma(:,:,NVERT)=0.0_dp
  ! calculate interior layers boundaries 7.21
  do i=1,NLAT
    do i=1,NLONG
      w_sigma(i,j,1:NVERT)=-
1.0 dp/(pi c new(i,j)*Re*Re*cos(lat c(i,j))*dlamda e*dphi)*fluxsum(i,j,1:NVERT)
      w_sigma(i,j,1:NVERT)=w_sigma(i,j,1:NVERT)-sigma_bot(1:NVERT)*(pi_c_new(i,j)&
        -pi_cold(i,j)/dt/pi_c_new(i,j)
    enddo
  enddo
end subroutine calculate_w_sigma
! calculate fluxface PVT
! usage: calculate the potential virtual temperature
! at flux face
! Yun Zhang 05/01/2015
! @STANFORD
subroutine calculate_fluxface_PVT(PVT_c_old,PVT_uface,PVT_vface,PVT_bot,&
  P c,P bot,lat uface,long uface,lat vface,long vface,nt)
  integer::i,j,k
  integer,intent(in):: nt
  real(dp), dimension(NLAT,NLONG,NVERT), intent(in):: PVT_c_old
  real(dp), dimension(NLAT,NLONG+1,NVERT), intent(inout):: PVT_uface
  real(dp), dimension(NLAT+1,NLONG,NVERT), intent(inout):: PVT vface
  real(dp),dimension(NLAT,NLONG,0:NVERT),intent(inout)::PVT_bot
  real(dp),dimension(NLAT+1,NLONG),intent(in):: lat_vface, long_vface
  real(dp),dimension(NLAT,NLONG+1),intent(in):: lat_uface, long_uface
  real(dp), dimension(NLAT,NLONG,NVERT),intent(in)::P_c
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in)::P_bot
  ! calculate uface
  ! use central differencing
  do i=1,NLAT
    do k=1,NVERT
      if(periodicBC==1) then
        PVT\_uface(i,1,k)=0.5*(PVT\_c\_old(i,1,k)+PVT\_c\_old(i,NLONG,k))
        PVT\_uface(i,NLONG+1,k)=0.5*(PVT\_c\_old(i,1,k)+PVT\_c\_old(i,NLONG,k))
      else
        PVT\_uface(i,1,k)=PVT\_c\_old(i,1,k)
```

! assume the top and bottom w\_sigma=0

```
PVT_uface(i,NLONG+1,k)=PVT_c_old(i,NLONG,k)
      endif
      PVT_uface(i,2:NLONG,k)=0.5*(PVT_c_old(i,1:(NLONG-
1),k)+PVT c old(i,2:NLONG,k))
    enddo
  enddo
  ! calculate vface
  ! use central differencing
  do i=1,NLONG
    do k=1,NVERT
      if(periodicBC==1) then
         PVT\_vface(1,i,k) = 0.5*(PVT\_c\_old(1,i,k) + PVT\_c\_old(NLAT,i,k))
         PVT\_vface(NLAT+1,i,k) = 0.5*(PVT\_c\_old(1,i,k) + PVT\_c\_old(NLAT,i,k))
      else
         PVT\_vface(1,i,k)=PVT\_c\_old(1,i,k)
         PVT_vface(NLAT+1,i,k)=PVT_c_old(NLAT,i,k)
      endif
      PVT_vface(2:NLAT,i,k)=0.5*(PVT_c_old(1:(NLAT-1),i,k)+PVT_c_old(2:NLAT,i,k))
    enddo
  enddo
  ! set boundary PTV value
  if(PTVbound==1) then
    ! vface value
    do j=1,NLONG
      do k=1,NVERT
PVT_vface(1,j,k)=boundary_potential_virtual_temp(lat_vface(1,j),long_vface(1,j),k,nt*dt)
PVT_vface(NLAT+1,j,k)=boundary_potential_virtual_temp(lat_vface(NLAT+1,j),long_vface(NL
AT+1,j,k,nt*dt
      enddo
    enddo
    ! uface value
    do i=1,NLAT
      do k=1,NVERT
PVT\_uface(i,1,k) = boundary\_potential\_virtual\_temp(lat\_vface(i,1),long\_uface(i,1),k,nt*dt)
PVT_uface(i,NLONG+1,k)=boundary_potential_virtual_temp(lat_uface(i,NLONG+1),long_uface
(i,NLONG+1),k,nt*dt)
      enddo
    enddo
```

```
endif
```

```
! layer bottom eqn 7.11
  do i=1,NLAT
    do j=1,NLONG
      ! for zero 0, P_bot(i,j,0) = P_c(i,j,0)
      PVT_bot(i,j,0)=PVT_c_old(i,j,1)
      PVT\_bot(i,j,1:(NVERT-1))=(P\_bot(i,j,1:(NVERT-1))-P\_c(i,j,1:(NVERT-1))
1)))*PVT_c_old(i,j,1:(NVERT-1))
      PVT\_bot(i,j,1:(NVERT-1))=PVT\_bot(i,j,1:(NVERT-1))+(P\_c(i,j,2:NVERT)-1)
P_bot(i,j,1:(NVERT-1)))*PVT_c_old(i,j,2:NVERT)
      PVT_bot(i,j,1:(NVERT-1))=PVT_bot(i,j,1:(NVERT-1))/(P_c(i,j,2:NVERT)-
P_c(i,j,1:(NVERT-1)))
      PVT_bot(i,j,NVERT)=PVT_c_old(i,j,NVERT)
    enddo
  enddo
end subroutine calculate fluxface PVT
! calculate_fluxface_qv
! usage: calculate specific humidity
! at flux face
! Yun Zhang 05/01/2015
! @STANFORD
subroutine calculate_fluxface_qv(qv_c_old,qv_uface,qv_vface,qv_bot,P_c,P_bot,&
  lat_uface,long_uface,lat_vface,long_vface,nt)
  integer::i,j,k
  integer,intent(in):: nt
  real(dp), dimension(NLAT,NLONG,NVERT), intent(in):: qv_c_old
  real(dp), dimension(NLAT,NLONG+1,NVERT), intent(inout):: qv_uface
  real(dp), dimension(NLAT+1,NLONG,NVERT), intent(inout):: qv_vface
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(inout)::qv_bot
  real(dp), dimension(NLAT+1,NLONG),intent(in):: lat_vface, long_vface
  real(dp), dimension(NLAT,NLONG+1),intent(in):: lat_uface, long_uface
  real(dp), dimension(NLAT,NLONG,NVERT),intent(in)::P_c
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in)::P_bot
  ! calculate uface
  ! use central differencing
  do i=1,NLAT
    do k=1,NVERT
      if(periodicBC==1) then
```

```
qv\_uface(i,1,k)=0.5*(qv\_c\_old(i,1,k)+qv\_c\_old(i,NLONG,k))
         qv\_uface(i,NLONG+1,k)=0.5*(qv\_c\_old(i,1,k)+qv\_c\_old(i,NLONG,k))
       else
         qv\_uface(i,1,k)=qv\_c\_old(i,1,k)
         qv_uface(i,NLONG+1,k)=qv_c_old(i,NLONG,k)
       qv\_uface(i,2:NLONG,k) = 0.5*(qv\_c\_old(i,1:(NLONG-1),k) + qv\_c\_old(i,2:NLONG,k))
    enddo
  enddo
  ! calculate vface
  ! use central differencing
  do i=1,NLONG
    do k=1,NVERT
       if(periodicBC==1) then
         qv\_vface(1,i,k)=0.5*(qv\_c\_old(1,i,k)+qv\_c\_old(NLAT,i,k))
         qv\_vface(NLAT+1,i,k)=0.5*(qv\_c\_old(1,i,k)+qv\_c\_old(NLAT,i,k))
       else
         qv_vface(1,i,k)=qv_c_old(1,i,k)
         qv_vface(NLAT+1,i,k)=qv_c_old(NLAT,i,k)
       endif
       qv_vface(2:NLAT,i,k)=0.5*(qv_c_old(1:(NLAT-1),i,k)+qv_c_old(2:NLAT,i,k))
    enddo
  enddo
  ! set boundary PTV value
  if(qvbound==1) then
    ! vface value
    do j=1,NLONG
       do k=1,NVERT
         qv_vface(1,j,k)=boundary_specific_humidity(lat_vface(1,j),long_vface(1,j),k,nt*dt)
qv_vface(NLAT+1,j,k)=boundary_specific_humidity(lat_vface(NLAT+1,j),long_vface(NLAT+1,j)
),k,nt*dt)
       enddo
    enddo
    ! uface value
    do i=1,NLAT
       do k=1,NVERT
         qv_uface(i,1,k)=boundary_specific_humidity(lat_vface(i,1),long_uface(i,1),k,nt*dt)
qv_uface(i,NLONG+1,k)=boundary_specific_humidity(lat_uface(i,NLONG+1),long_uface(i,NL
ONG+1),k,nt*dt)
       enddo
```

```
enddo
  endif
  ! layer bottom 7.25
  do i=1,NLAT
    do j=1,NLONG
      ! for zero 0, P_bot(i,j,0) = P_c(i,j,0)
      qv_bot(i,j,0)=qv_c_old(i,j,1)
      do k=1,(NVERT-1)
         if(qv_c_old(i,j,k)==qv_c_old(i,j,k+1)) then
           qv_bot(i,j,k)=qv_c_old(i,j,k)
         else if(qv_c_old(i,j,k)==0 .or. qv_c_old(i,j,k+1)==0) then
           qv_bot(i,j,k)=0.5*(qv_c_old(i,j,k)+qv_c_old(i,j,k+1))
         else
           qv\_bot(i,j,k) = (log(qv\_c\_old(i,j,k)) - log(qv\_c\_old(i,j,k+1))) \&
             /(1/qv_c_old(i,j,k+1)-1/qv_c_old(i,j,k))
         endif
      enddo
      qv_bot(i,j,NVERT)=qv_c_old(i,j,NVERT)
    enddo
  enddo
end subroutine calculate fluxface qv
! calculate_fluxface_gas
! usage: calculate gas concentration
! at flux face
! Yun Zhang 05/01/2015
! @STANFORD
subroutine calculate_fluxface_gas(gas_c_old,gas_uface,gas_vface,gas_bot,P_c,P_bot,&
  lat_uface,long_uface,lat_vface,long_vface,nt)
  integer::i,j,k
  integer,intent(in):: nt
  real(dp), dimension(NLAT,NLONG,NVERT), intent(in):: gas_c_old
  real(dp), dimension(NLAT,NLONG+1,NVERT), intent(inout):: gas_uface
  real(dp), dimension(NLAT+1,NLONG,NVERT), intent(inout):: gas_vface
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(inout)::gas_bot
  real(dp), dimension(NLAT+1,NLONG),intent(in):: lat_vface, long_vface
  real(dp), dimension(NLAT,NLONG+1),intent(in):: lat_uface, long_uface
  real(dp), dimension(NLAT,NLONG,NVERT),intent(in)::P_c
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in)::P_bot
```

```
! calculate uface
  ! use central differencing
  do i=1,NLAT
    do k=1,NVERT
       if(periodicBC==1) then
         gas\_uface(i,1,k)=0.5*(gas\_c\_old(i,1,k)+gas\_c\_old(i,NLONG,k))
         gas\_uface(i,NLONG+1,k)=0.5*(gas\_c\_old(i,1,k)+gas\_c\_old(i,NLONG,k))
       else
         gas\_uface(i,1,k)=gas\_c\_old(i,1,k)
         gas_uface(i,NLONG+1,k)=gas_c_old(i,NLONG,k)
       gas_uface(i,2:NLONG,k)=0.5*(gas_c_old(i,1:(NLONG-1),k)+gas_c_old(i,2:NLONG,k))
    enddo
  enddo
  ! calculate vface
  ! use central differencing
  do i=1,NLONG
    do k=1,NVERT
       if(periodicBC==1) then
         gas\_vface(1,i,k)=0.5*(gas\_c\_old(1,i,k)+gas\_c\_old(NLAT,i,k))
         gas\_vface(NLAT+1,i,k)=0.5*(gas\_c\_old(1,i,k)+gas\_c\_old(NLAT,i,k))
       else
         gas_vface(1,i,k)=gas_c_old(1,i,k)
         gas_vface(NLAT+1,i,k)=gas_c_old(NLAT,i,k)
       gas_vface(2:NLAT,i,k)=0.5*(gas_c_old(1:(NLAT-1),i,k)+gas_c_old(2:NLAT,i,k))
    enddo
  enddo
  ! set boundary PTV value
  if(gasbound==1) then
    ! vface value
    do j=1,NLONG
       do k=1,NVERT
         gas_vface(1,j,k)=boundary_gas(lat_vface(1,j),long_vface(1,j),k,nt*dt)
gas_vface(NLAT+1,j,k)=boundary_gas(lat_vface(NLAT+1,j),long_vface(NLAT+1,j),k,nt*dt)
       enddo
    enddo
    ! uface value
    do i=1,NLAT
       do k=1,NVERT
         gas_uface(i,1,k)=boundary_gas(lat_vface(i,1),long_uface(i,1),k,nt*dt)
```

```
gas_uface(i,NLONG+1,k)=boundary_gas(lat_uface(i,NLONG+1),long_uface(i,NLONG+1),k,nt*
dt)
      enddo
    enddo
  endif
  ! layer bottom 7.25
  do i=1.NLAT
    do j=1,NLONG
      gas\_bot(i,j,0)=gas\_c\_old(i,j,1)
      gas_bot(i,j,NVERT)=gas_c_old(i,j,NVERT)
      do k=1,(NVERT-1)
        gas_bot(i,j,k)=0.5*(gas_c_old(i,j,k)+gas_c_old(i,j,k+1))
      enddo
    enddo
  enddo
end subroutine calculate_fluxface_gas
! calculate heat source
! usage: calculate heat source value for each time
! step for each cell at each layer
! the heat source is treated as explicit
! and defined in the heat_source function
! in source.f90
! Yun Zhang 05/01/2015
! @stanford
subroutine calculate_heat_source(Pa_c,Q,lat_c,long_c,nt)
  real(dp),dimension(NLAT,NLONG),intent(in)::lat_c,long_c
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout):: Q
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: Pa_c
  integer, intent(in):: nt
  integer:: i,j,k
  do i=1,NLAT
    do j=1,NLONG
      do k=1,NVERT
        Q(i,j,k)=heat_source(lat_c(i,j),long_c(i,j),k,nt*dt)
        Q(i,j,k)=((1000/Pa_c(i,j,k))**k_therm)/Cp_d*Q(i,j,k)
      enddo
    enddo
```

```
enddo end subroutine calculate heat source
```

```
! calculate_gas_source
! usage: calculate gas source value for each time
! step for each cell at each layer
! the heat source is treated as explicit
! and defined in the heat_source function
! in source.f90
! Yun Zhang 05/01/2015
! @stanford
subroutine calculate_gas_source(Pa_c,Q,lat_c,long_c,nt)
  real(dp),dimension(NLAT,NLONG),intent(in)::lat_c,long_c
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout):: Q
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: Pa_c
  integer, intent(in):: nt
  integer:: i,j,k
  do i=1,NLAT
    do j=1,NLONG
      do k=1,NVERT
        Q(i,j,k)=gas\_source(lat\_c(i,j),long\_c(i,j),k,nt*dt)
      enddo
    enddo
  enddo
end subroutine calculate_gas_source
! calculate_gas_source
! usage: calculate gas source value for each time
! step for each cell at each layer
! the heat source is treated as explicit
! and defined in the heat_source function
! in source.f90
! Yun Zhang 05/01/2015
! @stanford
subroutine calculate_qv_source(Pa_c,Q,lat_c,long_c,nt)
  real(dp),dimension(NLAT,NLONG),intent(in)::lat_c,long_c
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout):: Q
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: Pa_c
  integer, intent(in):: nt
```

```
integer:: i,j,k
  do i=1,NLAT
    do j=1,NLONG
      do k=1,NVERT
        Q(i,j,k)=qv\_source(lat\_c(i,j),long\_c(i,j),k,nt*dt)
      enddo
    enddo
  enddo
end subroutine calculate qv source
! calculate_scalar_field
! usage: update scalar transport for each cell
! at every time step
! eqn 7.24 7.27
! use for PTV, qv and other components
! code use PTV as example
! Yun Zhang 04/30/2015
! @stanford
subroutine calculate_scalar_field(PVT_c_old, PVT_c_new, PVT_bot, &
  pi_c_old,pi_c_new,PVT_uface, PVT_vface,flux_uface,flux_vface,lat_c, rhoa_c,&
  dsigma, w sigma new, K t, Pa c, Q)
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in):: PVT_c_old, K_t, Q
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout):: PVT c new
  real(dp),dimension(NLAT,NLONG),intent(in)::pi_c_old, pi_c_new, lat_c
  real(dp), dimension(NLAT+1,NLONG,NVERT),intent(in):: PVT_vface, flux_vface
  real(dp), dimension(NLAT,NLONG+1,NVERT),intent(in):: PVT_uface, flux_uface
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in):: w_sigma_new
  real(dp), dimension(NVERT),intent(in):: dsigma
  real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in):: PVT_bot
  real(dp), dimension(NLAT,NLONG,NVERT),intent(in):: Pa_c, rhoa_c
  integer:: i,j,k
  ! old value
  do k=1,NVERT
    PVT_c_new(:,:,k)=pi_c_old*PVT_c_old(:,:,k)/pi_c_new
  enddo
  ! horizontal flux at boundary
  do k=1,NVERT
    PVT\_c\_new(:,:,k) = PVT\_c\_new(:,:,k) + dt/(pi\_c\_new*Re*Re*cos(lat\_c)*dlamda\_e*dphi)\&
    *(flux_uface(:,1:NLONG,k)*PVT_uface(:,1:NLONG,k)-
flux_uface(:,2:(NLONG+1),k)*PVT_uface(:,2:(NLONG+1),k)&
      +flux_vface(1:NLAT,:,k)*PVT_vface(1:NLAT,:,k)-
```

```
flux_vface(2:(NLAT+1),:,k)*PVT_vface(2:(NLAT+1),:,k))
     enddo
     ! vertical flux
     do k=1,NVERT
           PVT_c_new(:,:,k)=PVT_c_new(:,:,k)+dt/dsigma(k)*(w_sigma_new(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_bot(:,:,k-1)*PVT_b
1)&
                 -w_sigma_new(:,:,k)*PVT_bot(:,:,k))
     enddo
      ! turbulence vertical flux
     ! not finished
     if(turbmodel==1) then
           do k=1,NVERT
                 PVT_c_new(:,:,k)=PVT_c_new(:,:,k)
           enddo
     endif
     ! heat source
     if(heatsource==1) then
           do k=1,NVERT
                 PVT_c_new(:,:,k)=PVT_c_new(:,:,k)+dt*pi_c_old/pi_c_new*Q(:,:,k)
           enddo
     endif
end subroutine calculate_scalar_field
! calculate_geopotential
! usage: calculate geopotential for each cell center
! and layer bottom
! need to specify the boundary geopotential at bottom
! use boundary_surf_geopotential
! Yun 05/02/2015
! @stanford
subroutine
calculate_geopotential(geopot_bot,geopot_c,geopot_c_tminus1,P_c,P_bot,PVT_c_old,lat_c,long_
c,nt)
     real(dp), dimension(NLAT,NLONG,NVERT),intent(in)::P_c,PVT_c_old
     real(dp), dimension(NLAT,NLONG,NVERT),intent(inout)::geopot_c,geopot_c_tminus1
     real(dp), dimension(NLAT,NLONG,0:NVERT),intent(inout):: geopot_bot
     real(dp), dimension(NLAT,NLONG,0:NVERT),intent(in):: P_bot
     real(dp), dimension(NLAT,NLONG), intent(in):: lat_c,long_c
```

```
integer,intent(in):: nt
  integer::i,j,k
  if(nt>0) geopot_c_tminus1=geopot_c
  do i=1,NLAT
    do j=1,NLONG
      geopot_bot(i,j,NVERT)=boundary_surf_geopotential(lat_c(i,j),long_c(i,j),nt*dt)
      geopot_c(i,j,NVERT)=geopot_bot(i,j,NVERT)-
Cp d*(PVT c old(i,j,NVERT)*(P c(i,j,NVERT)-P bot(i,j,NVERT)))
      do k=NVERT-1,0,-1
         geopot\_bot(i,j,k)=geopot\_c(i,j,k+1)-Cp\_d*(PVT\_c\_old(i,j,k+1)*(P\_bot(i,j,k)-i,k+1))
P_c(i,j,k+1)))
         if(k/=0) then
           geopot\_c(i,j,k)=geopot\_bot(i,j,k)-Cp\_d*(PVT\_c\_old(i,j,k)*(P\_c(i,j,k)-P\_bot(i,j,k)))
        endif
      enddo
    enddo
  enddo
  if(nt==0) geopot_c_tminus1=geopot_c
end subroutine calculate_geopotential
! calculate_velocity_field
! usage: update velocity field for each flux face
! Yun Zhang 05/02/2015
! @stanford
subroutine calculate_velocity_field(pi_c_old,pi_c_new,pi_c_tmp,pi_c_tminus1,lat_c,lat_vface,&
  u old, u new, u tmp, v old, v new, v tmp, flux uface, flux vface, dsigma, &
  sigma_bot,w_sigma_new,f_c,geopot_c,geopot_c_tminus1,&
  PVT_c_old,P_bot,P_c,nu_t,rhoa_c)
real(dp),dimension(NLAT,NLONG),intent(in)::pi_c_old,pi_c_new,pi_c_tmp,pi_c_tminus1,lat_c,f
_c
  real(dp),dimension(NLAT,NLONG+1,NVERT),intent(in)::u_old,flux_uface,u_tmp
  real(dp),dimension(NLAT,NLONG+1,NVERT),intent(inout)::u_new
  real(dp), dimension(NLAT+1, NLONG, NVERT), intent(in) :: v\_old, flux\_vface, v\_tmp
  real(dp),dimension(NLAT+1,NLONG,NVERT),intent(inout)::v_new
  real(dp),dimension(0:NVERT),intent(in)::sigma_bot
  real(dp),dimension(NVERT),intent(in)::dsigma
  real(dp), dimension(NLAT, NLONG, 0: NVERT), intent(in):: w\_sigma\_new, P\_bot
real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::geopot_c,geopot_c_tminus1,PVT_c_old,P
```

```
_c,nu_t,rhoa_c
 real(dp),dimension(NLAT+1,NLONG),intent(in)::lat_vface
 real(dp),dimension(NLAT,NLONG+1,0:NVERT)::u_bot_old
 real(dp),dimension(NLAT+1,NLONG,0:NVERT)::v bot old
 ! u field
 real(dp),dimension(NLAT,NLONG+1)::A_old,A_new
 real(dp),dimension(NLAT,NLONG+1,0:NVERT)::F
 real(dp),dimension(NLAT,0:NLONG+1,NVERT)::B
 real(dp),dimension(NLAT+1,NLONG+1,NVERT)::C
 real(dp),dimension(NLAT+1,0:NLONG+1,NVERT)::D,E
 ! v field
 real(dp),dimension(NLAT+1,NLONG)::P old,P new
 real(dp),dimension(NLAT+1,NLONG,0:NVERT)::O
 real(dp),dimension(0:NLAT+1,NLONG,NVERT)::R
 real(dp),dimension(NLAT+1,NLONG+1,NVERT)::Q
 real(dp),dimension(0:NLAT+1,NLONG+1,NVERT)::S,T
 integer::i,j,k
 ! prepare for the boundary values
  ! use new virtual matrix to calculate velocity to simplify equation
 real(dp),dimension(0:NLAT+1,0:NLONG+1)::v_f_c,v_pi_c_new,v_pi_c_old,v_lat_c
 real(dp),dimension(0:NLAT+1,0:NLONG+1,0:NVERT)::v F new
 real(dp),dimension(0:NLAT+1,0:NLONG+1,0:NVERT)::v_w_sigma_new
  !real(dp),dimension(0:NLAT+1,0:NLONG+1,NVERT):: v_PVT_c_old, v_P_c, v_geopot_c
  !real(dp),dimension(0:NLAT+1,0:NLONG+1,0:NVERT):: v_P_bot
 real(dp),dimension(0:NLAT+1,0:NLONG+2,NVERT)::v_u_old, v_flux_uface
 real(dp),dimension(0:NLAT+2,0:NLONG+1,NVERT)::v v old, v flux vface
 v_f_c(1:NLAT,1:NLONG)=f_c
 v_pi_c_old(1:NLAT,1:NLONG)=pi_c_old
 v_pi_c_new(1:NLAT,1:NLONG)=pi_c_new
 v_lat_c(1:NLAT,1:NLONG)=lat_c
 v_w_sigma_new(1:NLAT,1:NLONG,0:NVERT)=w_sigma_new
 if(periodicBC==1) then
    v_pi_c_old(0,1:NLONG)=pi_c_old(NLAT,:)
    v_pi_c_old(NLAT+1,1:NLONG)=pi_c_old(1,:)
    v_pi_c_old(1:NLAT,0)=pi_c_old(:,NLONG)
    v_pi_c_old(1:NLAT,NLONG+1)=pi_c_old(:,1)
    v_{pi}_cold(0,0)=0.5*(pi_cold(1,NLONG)+pi_cold(NLAT,1))
    v_pi_c_old(NLAT,0)=0.5*(pi_c_old(1,NLONG)+pi_c_old(1,1))
```

```
v_{pi_cold}(0,NLONG+1)=0.5*(pi_c_old(1,1)+pi_c_old(NLAT,NLONG))
  v_pi_c_old(NLAT,NLONG+1)=0.5*(pi_c_old(1,NLONG)+pi_c_old(NLAT,1))
else
  v_pi_cold(0,1:NLONG)=pi_cold(1,:)
  v_pi_c_old(NLAT+1,1:NLONG)=pi_c_old(NLAT,:)
  v_pi_c_old(:,0)=v_pi_c_old(:,1)
  v_pi_c_old(:,NLONG+1)=v_pi_c_old(:,NLONG)
endif
if(periodicBC==1) then
  v_pi_c_new(0,1:NLONG)=pi_c_new(NLAT,:)
  v_pi_c_new(NLAT+1,1:NLONG)=pi_c_new(1,:)
  v_pi_c_new(1:NLAT,0)=pi_c_new(:,NLONG)
  v pi c new(1:NLAT,NLONG+1)=pi c new(:,1)
  v_pi_c_new(0,0)=0.5*(pi_c_new(1,NLONG)+pi_c_new(NLAT,1))
  v_pi_c_new(NLAT,0)=0.5*(pi_c_new(1,NLONG)+pi_c_new(1,1))
  v_pi_c_new(0,NLONG+1)=0.5*(pi_c_new(1,1)+pi_c_new(NLAT,NLONG))
  v_pi_c_new(NLAT,NLONG+1)=0.5*(pi_c_new(1,NLONG)+pi_c_new(NLAT,1))
else
  v_pi_c_new(0,1:NLONG)=pi_c_new(1,:)
  v_pi_c_new(NLAT+1,1:NLONG)=pi_c_new(NLAT,:)
  v_pi_c_new(:,0)=v_pi_c_new(:,1)
  v_pi_c_new(:,NLONG+1)=v_pi_c_new(:,NLONG)
endif
v_{at_c(0,:)=lat_c(1,1)-dphi
v_{lat_c(NLAT+1,:)=lat_c(NLAT,1)+dphi}
v_{lat_c(1:NLAT,0)=lat_c(1:NLAT,1)}
v_lat_c(1:NLAT,NLONG+1)=lat_c(1:NLAT,NLONG)
if(coriolis==1) then
  v_f_c=2*Omega*sin(v_lat_c)
else
  v_f_c=0.0_dp
endif
if(periodicBC==1) then
  v_w_sigma_new(0,1:NLONG,:)=w_sigma_new(NLAT,:,:)
  v_w_sigma_new(NLAT+1,1:NLONG,:)=w_sigma_new(1,:,:)
  v_w_sigma_new(1:NLAT,0,:)=w_sigma_new(:,NLONG,:)
  v_w_sigma_new(1:NLAT,NLONG+1,:)=w_sigma_new(:,1,:)
  v_w_{sigma_new(0,0,:)}=0.5*(w_{sigma_new(1,NLONG,:)}+w_{sigma_new(NLAT,1,:)})
  v_w_{sigma_new}(NLAT,0,:)=0.5*(w_{sigma_new}(1,NLONG,:)+w_{sigma_new}(1,1,:))
```

```
v_w_sigma_new(0,NLONG+1,:)=0.5*(w_sigma_new(1,1,:)+w_sigma_new(NLAT,NLONG,:))
v_w_sigma_new(NLAT,NLONG+1,:)=0.5*(w_sigma_new(1,NLONG,:)+w_sigma_new(NLAT,1,
:))
  else
    v_w_sigma_new(0,1:NLONG,:)=w_sigma_new(1,:,:)
    v_w_sigma_new(NLAT+1,1:NLONG,:)=w_sigma_new(NLAT,:,:)
    v w sigma new(:,0,:)=v w sigma new(:,1,:)
    v_w_sigma_new(:,NLONG+1,:)=v_w_sigma_new(:,NLONG,:)
  endif
  v_u_old(1:NLAT,1:NLONG+1,:)=u_tmp
  v flux uface(1:NLAT,1:NLONG+1,:)=flux uface
  v_v_old(1:NLAT+1,1:NLONG,:)=v_tmp
  v_flux_vface(1:NLAT+1,1:NLONG,:)=flux_vface
  v_u_old(0,1:NLONG+1,:)=u_tmp(1,:,:)
  v_u_old(NLAT+1,1:NLONG+1,:)=u_tmp(NLAT,:,:)
  v_u_old(:,0,:)=v_u_old(:,1,:)
  v_u_old(:,NLONG+2,:)=v_u_old(:,NLONG+1,:)
  v_flux_uface(0,1:NLONG+1,:)=flux_uface(1,:,:)
  v_flux_uface(NLAT+1,1:NLONG+1,:)=flux_uface(NLAT,:,:)
  v flux uface(:,0,:)=v flux uface(:,1,:)
  v_flux_uface(:,NLONG+2,:)=v_flux_uface(:,NLONG+1,:)
  v_v_old(1:NLAT+1,0,:)=v_tmp(:,1,:)
  v_v_old(1:NLAT+1,NLONG+1,:)=v_tmp(:,NLONG,:)
  v \ v \ old(0,:,:)=v \ v \ old(1,:,:)
  v_v_old(NLAT+2,:,:)=v_v_old(NLAT+1,:,:)
  v_flux_vface(1:NLAT+1,0,:)=flux_vface(:,1,:)
  v_flux_vface(1:NLAT+1,NLONG+1,:)=flux_vface(:,NLONG,:)
  v_flux_vface(0,:,:)=v_flux_vface(1,:,:)
  v_flux_vface(NLAT+2,:,:)=v_flux_vface(NLAT+1,:,:)
  ! Update u field
  ! calculate column pressure multiplied by grid-cell area 7.38
  ! interior points
A\_old=1.0\_dp/8.0\_dp*Re*Re*dphi*dlamda\_e*(v\_pi\_c\_old(2:NLAT+1,0:NLONG)*cos(v\_lat\_c(1))
2:NLAT+1,0:NLONG))&
```

```
+v_{pi}_{cold}(2:NLAT+1,1:NLONG+1)*cos(v_{lat_{c}(2:NLAT+1,1:NLONG+1))+2*v_{pi}_{cold}(1:v_{lat_{c}(2:NLAT+1,1:NLONG+1))+2*v_{lat_{c}(2:NLAT+1,1:NLONG+1))}
NLAT,0:NLONG)*cos(v_lat_c(1:NLAT,0:NLONG))&
+2*v\_pi\_c\_old(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)) + v\_pi\_c\_old(0:NLAT-1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)) + v\_pi\_c\_old(0:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)) + v\_pi\_c\_old(0:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)) + v\_pi\_c\_old(0:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_lat\_c(1:NLAT,1:NLONG+1)*cos(v\_
1,0:NLONG)*cos(v_lat_c(0:NLAT-1,0:NLONG))&
         +v_pi_cold(0:NLAT-1,1:NLONG+1)*cos(v_lat_c(0:NLAT-1,1:NLONG+1)))
A_new=1.0_dp/8.0_dp*Re*Re*dphi*dlamda_e*(v_pi_c_new(2:NLAT+1,0:NLONG)*cos(v_lat_c
(2:NLAT+1,0:NLONG))&
         +v_pi_c_new(2:NLAT+1,1:NLONG+1)*cos(v_lat_c(2:NLAT+1,1:NLONG+1))&
         +2*v_pi_c_new(1:NLAT,0:NLONG)*cos(v_lat_c(1:NLAT,0:NLONG))&
         +2*v_pi_c_new(1:NLAT,1:NLONG+1)*cos(v_lat_c(1:NLAT,1:NLONG+1))&
         +v pi c new(0:NLAT-1,0:NLONG)*cos(v lat c(0:NLAT-1,0:NLONG))&
         +v_pi_c_new(0:NLAT-1,1:NLONG+1)*cos(v_lat_c(0:NLAT-1,1:NLONG+1)))
    ! equation 7.41
    B=1.0 dp/12.0 dp*(v flux uface(0:NLAT-1,0:NLONG+1,:)+v flux uface(0:NLAT-
1,1:NLONG+2,:)&
         +2*v_flux_uface(1:NLAT,0:NLONG+1,:)+2*v_flux_uface(1:NLAT,1:NLONG+2,:)&
         +v_flux_uface(2:NLAT+1,0:NLONG+1,:)+v_flux_uface(2:NLAT+1,1:NLONG+2,:))
    ! equation 7.42
C=1.0 dp/12.0 dp*(v flux vface(0:NLAT,0:NLONG,:)+v flux vface(0:NLAT,1:NLONG+1,:)&
         +2*v_flux_vface(1:NLAT+1,0:NLONG,:)+2*v_flux_vface(1:NLAT+1,1:NLONG+1,:)&
         +v_flux_vface(2:NLAT+2,0:NLONG,:)+v_flux_vface(2:NLAT+2,1:NLONG+1,:))
    ! equation 7.43
D=1.0_dp/24.0_dp*(v_flux_vface(0:NLAT,0:NLONG+1,:)+2*v_flux_vface(1:NLAT+1,0:NLON
G+1,:)+v_flux_vface(2:NLAT+2,0:NLONG+1,:)&
+v_flux_uface(0:NLAT,0:NLONG+1,:)+v_flux_uface(1:NLAT+1,0:NLONG+1,:)+v_flux_uface(
0:NLAT,1:NLONG+2,:)&
         +v_flux_uface(1:NLAT+1,1:NLONG+2,:))
    ! equation 7.44
E=1.0_dp/24.0_dp*(v_flux_vface(0:NLAT,0:NLONG+1,:)+2*v_flux_vface(1:NLAT+1,0:NLON
G+1,:)+v_flux_vface(2:NLAT+2,0:NLONG+1,:)&
         -v_flux_uface(0:NLAT,0:NLONG+1,:)-v_flux_uface(1:NLAT+1,0:NLONG+1,:)-
v_flux_uface(0:NLAT,1:NLONG+2,:)&
         -v_flux_uface(1:NLAT+1,1:NLONG+2,:))
```

```
! equation 7.45 get velocity at layer bottom
     ! the top most and bottom most u_bot are not important because w_sigma is zero
     do i=1,NLAT
          do j=1,NLONG+1
                u_bot_old(i,j,1:NVERT-1)=(u_tmp(i,j,1:NVERT-1)*dsigma(1:NVERT-
1)+u_tmp(i,j,2:NVERT)*dsigma(2:NVERT))&
                /(dsigma(1:NVERT-1)+dsigma(2:NVERT))
                u\_bot\_old(i,j,0)=u\_tmp(i,j,1)
                u_bot_old(i,j,NVERT)=u_tmp(i,j,NVERT)
     enddo
     ! equation 7.40
     do i=0,NLAT+1
          do j=0,NLONG+1
v_F_{new(i,j)}:=v_pi_c_{new(i,j)}*Re*Re*dphi*dlamda_e*cos(v_lat_c(i,j))*v_w_sigma_new(i,j,:)
          enddo
     enddo
     F=1.0_dp/8.0_dp*(v_F_new(2:NLAT+1,0:NLONG,:)+v_F_new(2:NLAT+1,1:NLONG+1,:)&
          +2*v F new(1:NLAT,0:NLONG,:)+2*v F new(1:NLAT,1:NLONG+1,:)&
          +v_F_new(0:NLAT-1,0:NLONG,:)+v_F_new(0:NLAT-1,1:NLONG+1,:))
     ! equation 7.32 time difference term
     do k=1,NVERT
          u_new(:,:,k)=A_old/A_new*u_old(:,:,k)
     enddo
     ! equation 7.33 horizontal advection B
     do k=1,NVERT
          u_new(:,:,k)=u_new(:,:,k)+dt/A_new*(B(:,0:NLONG,k)\&
                *0.5*(v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,1:NLONG+1,k))&
B(:,1:NLONG+1,k)*0.5*(v\_u\_old(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)))\\
     enddo
     ! equation 7.33 horizontal advection C
     do k=1,NVERT
          u_new(:,:,k)=u_new(:,:,k)+dt/A_new*(C(1:NLAT,1:NLONG+1,k)&
                *0.5*(v_u_old(0:NLAT-1,1:NLONG+1,k)+v_u_old(1:NLAT,1:NLONG+1,k))&
C(2:NLAT+1,1:NLONG+1,k)*0.5*(v_u_old(1:NLAT,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_u_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLONG+1,k)+v_old(2:NLAT+1,1:NLAT
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ONG+1,k)))
               enddo
               ! equation 7.33 horizontal advection D
               do k=1,NVERT
                              u_new(:,:,k)=u_new(:,:,k)+dt/A_new*(D(1:NLAT,0:NLONG,k)\&
                                              *0.5*(v_u_old(0:NLAT-1,0:NLONG,k)+v_u_old(1:NLAT,1:NLONG+1,k))&
D(2:NLAT+1,1:NLONG+1,k)*0.5*(v\_u\_old(1:NLAT,1:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v\_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old(2:NLAT+1,2:NLONG+1,k)+v_u\_old
ONG+2,k)))
              enddo
               ! equation 7.33 horizontal advection E
               do k=1,NVERT
                              u_new(:,:,k)=u_new(:,:,k)+dt/A_new*(E(1:NLAT,1:NLONG+1,k)&
                                             *0.5*(v_u_old(0:NLAT-1,2:NLONG+2,k)+v_u_old(1:NLAT,1:NLONG+1,k))&
E(2:NLAT+1,0:NLONG,k)*0.5*(v u old(1:NLAT,1:NLONG+1,k)+v u old(2:NLAT+1,0:NLON
G,k)))
               enddo
               ! equation 7.34 vertical transport F
              do k=1,NVERT
                              u_new(:,:,k)=u_new(:,:,k)+dt/A_new/dsigma(k)*(F(:,:,k-1)*u_bot_old(:,:,k-1)&
                                             -F(:,:,k)*u bot old(:,:,k))
              enddo
               ! equation 7.35 coriolis and sperical grid conversion
              do k=1,NVERT
                               u_new(:,:,k)=u_new(:,:,k)+0.5*dt/A_new*Re*dlamda_e*dphi&
 *(v_pi_c_old(1:NLAT,0:NLONG)*0.5*(v_v_old(1:NLAT,0:NLONG,k)+v_v_old(2:NLAT+1,0:N
LONG,k))&
                                              *(v_f_c(1:NLAT,0:NLONG)*Re*cos(v_lat_c(1:NLAT,0:NLONG))&
+0.5*(v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,1:NLONG+1,k))*sin(v\_lat\_c(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u\_old(1:NLAT,0:NLONG,k)+v\_u_old(1:NLAT,0:NLONG,k)+v\_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u_old(1:NLAT,0:NLONG,k)+v_u
NLONG)))&
+v_pi_cold(1:NLAT,1:NLONG+1)*0.5*(v_vold(1:NLAT,1:NLONG+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(2:NLAT+1,k)+v_vold(
1:NLONG+1,k))&
                                              *(v_f_c(1:NLAT,1:NLONG+1)*Re*cos(v_lat_c(1:NLAT,1:NLONG+1))&
+0.5*(v\_u\_old(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k))*sin(v\_lat\_c(1:NLAT,1:NLONG+1,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u\_old(1:NLAT,2:NLONG+2,k)+v\_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLAT,2:NLONG+2,k)+v_u_old(1:NLA
 1:NLONG+1))))
```

```
! equation 7.36 pressure gradient
     do k=1,NVERT
           u_new(:,2:NLONG,k)=u_new(:,2:NLONG,k)
dt/A_new(:,2:NLONG)*Re*dphi*((geopot_c(:,2:NLONG,k)&
                -geopot_c(:,1:NLONG-1,k))*0.5*(pi_c_tmp(:,1:NLONG-1)+pi_c_tmp(:,2:NLONG))&
                +0.5*(-pi\_c\_tmp(:,1:NLONG-1)+pi\_c\_tmp(:,2:NLONG))*Cp\_d\&
                *(PVT_c_old(:,1:NLONG-1,k)/dsigma(k)*(sigma_bot(k)&
                *(P_bot(:,1:NLONG-1,k)-P_c(:,1:NLONG-1,k))+sigma_bot(k-1)&
                *(P_c(:,1:NLONG-1,k)-P_bot(:,1:NLONG-1,k-
1)))+PVT_c_old(:,2:NLONG,k)/dsigma(k)&
                *(sigma\_bot(k)*(P\_bot(:,2:NLONG,k)-P\_c(:,2:NLONG,k))&
                +sigma\_bot(k-1)*(P\_c(:,2:NLONG,k)-P\_bot(:,2:NLONG,k-1)))))
           ! west boundary
           u_new(:,1,k)=u_new(:,1,k)-dt/A_new(:,1)*Re*dphi*((-
geopot\_c\_tminus1(:,1,k)+geopot\_c(:,1,k))*pi\_c\_tmp(:,1)&
                +(-
pi\_c\_tminus1(:,1) + pi\_c\_tmp(:,1)) * Cp\_d * (PVT\_c\_old(:,1,k)/dsigma(k) * (sigma\_bot(k) * (P\_bot(:,1,k)/dsigma(k) * (sigma\_bot(k) * (P\_bot(i,1,k)/dsigma(k) * (sigma\_bot(k) * (P\_bot(i,1,k)/dsigma(k) * (P
k)&
                -P_c(:,1,k)+sigma_bot(k-1)*(P_c(:,1,k)-P_bot(:,1,k-1))))
           ! east boundary
          if(periodicBC==1) then
                u_new(:,NLONG+1,k)=u_new(:,1,k);
                u_new(:,NLONG+1,k)=u_new(:,NLONG+1,k)-
dt/A\_new(:,NLONG+1)*Re*dphi*((geopot\_c\_tminus1(:,NLONG,k)\&
                     -geopot_c(:,NLONG,k))*pi_c_tmp(:,NLONG)&
                     +(pi_c_tminus1(:,NLONG)-
pi_c_tmp(:,NLONG))*Cp_d*(PVT_c_old(:,NLONG,k)/dsigma(k)*(sigma_bot(k)*(P_bot(:,NLO
NG,k)&
                     -P_c(:,NLONG,k))+sigma\_bot(k-1)*(P_c(:,NLONG,k)-P_bot(:,NLONG,k-1)))))
          endif
     enddo
     ! equation 7.37 eddy vicousity not finished!
     if(turbmodel==1) then
          do k=1,NVERT
                u_new(:,:,k)=u_new(:,:,k)
          enddo
     endif
```

```
! column pressure multiplied by the area eqn 7.53
P\_old=1.0\_dp/8.0\_dp*Re*Re*dphi*dlamda\_e*(v\_pi\_c\_old(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat\_c(0:NLAT,2:NLONG+1)*cos(v\_lat_c(0:NLAT,2:NLONG+1)*cos(v\_lat_c(0:NLAT,2:NLONG+1)*cos(v\_lat_c(0:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NLAT,2:NL
:NLAT,2:NLONG+1))&
              +v_pi_cold(1:NLAT+1,2:NLONG+1)*cos(v_lat_c(1:NLAT+1,2:NLONG+1))&
              +2*v_pi_c_old(0:NLAT,1:NLONG)*cos(v_lat_c(0:NLAT,1:NLONG))&
              +2*v_pi_c_old(1:NLAT+1,1:NLONG)*cos(v_lat_c(1:NLAT+1,1:NLONG))&
              +v pi c old(0:NLAT,0:NLONG-1)*cos(v lat c(0:NLAT,0:NLONG-1))&
              +v_pi_c_old(1:NLAT+1,0:NLONG-1)*cos(v_lat_c(1:NLAT+1,0:NLONG-1)))
P\_new = 1.0\_dp/8.0\_dp*Re*Re*dphi*dlamda\_e*(v\_pi\_c\_new(0:NLAT,2:NLONG+1)*cos(v\_lat\_c) + (v\_pi\_c\_new(0:NLAT,2:NLONG+1)*cos(v\_lat\_c) + (v\_pi\_c\_new(0:NLAT,2:NLONG+1)*cos(v\_pi\_c) + (v\_pi\_c) + (
(0:NLAT,2:NLONG+1))&
              +v_pi_c_new(1:NLAT+1,2:NLONG+1)*cos(v_lat_c(1:NLAT+1,2:NLONG+1))&
              +2*v_pi_c_new(0:NLAT,1:NLONG)*cos(v_lat_c(0:NLAT,1:NLONG))&
              +2*v_pi_c_new(1:NLAT+1,1:NLONG)*cos(v_lat_c(1:NLAT+1,1:NLONG))&
              +v pi c new(0:NLAT,0:NLONG-1)*cos(v lat c(0:NLAT,0:NLONG-1))&
             +v_pi_c_new(1:NLAT+1,0:NLONG-1)*cos(v_lat_c(1:NLAT+1,0:NLONG-1)))
           ! equation 7.56
       R=1.0\_dp/12.0\_dp*(v\_flux\_vface(0:NLAT+1,0:NLONG-1))
1,:)+v flux vface(1:NLAT+2,0:NLONG-1,:)&
              +2*v_flux_vface(0:NLAT+1,1:NLONG,:)+2*v_flux_vface(1:NLAT+2,1:NLONG,:)&
              +v flux vface(0:NLAT+1,2:NLONG+1,:)+v flux vface(1:NLAT+2,2:NLONG+1,:))
       ! equation 7.55
Q=1.0_dp/12.0_dp*(v_flux_uface(0:NLAT,0:NLONG,:)+v_flux_uface(1:NLAT+1,0:NLONG,:)&
              +2*v flux uface(0:NLAT,1:NLONG+1,:)+2*v flux uface(1:NLAT+1,1:NLONG+1,:)&
              +v_flux_uface(0:NLAT,2:NLONG+2,:)+v_flux_uface(1:NLAT+1,2:NLONG+2,:))
       ! equation 7.57
S=1.0_dp/24.0_dp*(v_flux_uface(0:NLAT+1,0:NLONG,:)+2*v_flux_uface(0:NLAT+1,1:NLON
G+1,:)+v_flux_uface(0:NLAT+1,2:NLONG+2,:)&
+v_flux_vface(0:NLAT+1,0:NLONG,:)+v_flux_vface(0:NLAT+1,1:NLONG+1,:)+v_flux_vface(
1:NLAT+2,0:NLONG,:)&
              +v_flux_vface(1:NLAT+2,1:NLONG+1,:))
       ! equation 7.58
      T=1.0_dp/24.0_dp*(-v_flux_uface(0:NLAT+1,0:NLONG,:)-
2*v_flux_uface(0:NLAT+1,1:NLONG+1,:)-v_flux_uface(0:NLAT+1,2:NLONG+2,:)&
```

! Update v field

```
+v flux vface(0:NLAT+1,0:NLONG,:)+v flux vface(0:NLAT+1,1:NLONG+1,:)+v flux vface(
1:NLAT+2,0:NLONG,:)&
           +v flux vface(1:NLAT+2,1:NLONG+1,:))
     ! equation 7.54
     O=1.0_dp/8.0_dp*(v_F_new(0:NLAT,2:NLONG+1,:)+v_F_new(1:NLAT+1,2:NLONG+1,:)&
           +2*v_F_new(0:NLAT,1:NLONG,:)+2*v_F_new(1:NLAT+1,1:NLONG,:)&
          +v F new(0:NLAT,0:NLONG-1,:)+v F new(1:NLAT+1,0:NLONG-1,:))
     ! equation 7.45 get velocity at layer bottom
     ! the top most and bottom most u_bot are not important because w_sigma is zero
     do i=1,NLAT+1
           do j=1,NLONG
                v_bot_old(i,j,1:NVERT-1)=(v_tmp(i,j,1:NVERT-1)*dsigma(1:NVERT-
1)+v_tmp(i,j,2:NVERT)*dsigma(2:NVERT))&
                /(dsigma(1:NVERT-1)+dsigma(2:NVERT))
                v_bot_old(i,j,0)=v_tmp(i,j,1)
                v_bot_old(i,j,NVERT)=v_tmp(i,j,NVERT)
           enddo
     enddo
     ! equation 7.47 time difference term
     do k=1,NVERT
           v \text{ new}(:,:,k)=P \text{ old/}P \text{ new*}v \text{ old}(:,:,k)
     enddo
     ! equation 7.48 horizontal advection R
     do k=1,NVERT
           v \text{ new}(:,:,k)=v \text{ new}(:,:,k)+dt/P \text{ new}*(R(0:NLAT,:,k)\&
                *0.5*(v_v_old(0:NLAT,1:NLONG,k)+v_v_old(1:NLAT+1,1:NLONG,k))&
R(1:NLAT+1,:,k)*0.5*(v_v_old(1:NLAT+1,1:NLONG,k)+v_v_old(2:NLAT+2,1:NLONG,k)))
     enddo
     ! equation 7.48 horizontal advection Q
     do k=1,NVERT
           v_{new}(:,:,k)=v_{new}(:,:,k)+dt/P_{new}*(Q(1:NLAT+1,1:NLONG,k)\&
                *0.5*(v\_v\_old(1:NLAT+1,0:NLONG-1,k)+v\_v\_old(1:NLAT+1,1:NLONG,k))\&
Q(1:NLAT+1,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v\_old(1:NLAT+1,2:NLONG,k)+v\_v_old(1:NLAT+1,2:NLONG,k)+v\_v_old(1:NLAT+1,2:NLONG,k)+v_old(1:NLAT+1,2:NLONG,k)+v_old(1:NLAT+1,2:NLONG,k)+v_old(1:NLAT+1,2:NLONG,k)+v_old(1:NLAT+1,2:NLONG,k)+v_old(1:NLAT+1,2:NLONG,k)+v_old(1:N
ONG+1,k)))
     enddo
```

```
! equation 7.48 horizontal advection S
               do k=1.NVERT
                              v_new(:,:,k)=v_new(:,:,k)+dt/P_new*(S(0:NLAT,1:NLONG,k)&
                                              *0.5*(v_v_old(0:NLAT,0:NLONG-1,k)+v_v_old(1:NLAT+1,1:NLONG,k))&
S(1:NLAT+1,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG,k)+v\_v\_old(2:NLAT+2,2:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLAT+1,1:NLONG+1,k)*0.5*(v\_v\_old(1:NLA
ONG+1,k)))
             enddo
               ! equation 7.48 horizontal advection T
             do k=1,NVERT
                              v_new(:,:,k)=v_new(:,:,k)+dt/P_new*(-T(1:NLAT+1,1:NLONG,k)&
                                              *0.5*(v_v_old(2:NLAT+2,0:NLONG-1,k)+v_v_old(1:NLAT+1,1:NLONG,k))&
+T(0:NLAT,2:NLONG+1,k)*0.5*(v_v_old(1:NLAT+1,1:NLONG,k)+v_v_old(0:NLAT,2:NLON
G+1,k)))
             enddo
               ! equation 7.49 vertical transport O
             do k=1,NVERT
                              v_{new}(:,:,k) = v_{new}(:,:,k) + dt/P_{new}/dsigma(k)*(O(:,:,k-1)*v_{bot}_{old}(:,:,k-1)&
                                             -O(:,:,k)*v\_bot\_old(:,:,k))
             enddo
               ! equation 7.50 coriolis and sperical grid conversion
             do k=1,NVERT
                              v_new(:,:,k)=v_new(:,:,k)-0.5*dt/P_new*Re*dlamda_e*dphi&
 *(v\_pi\_c\_old(0:NLAT,1:NLONG)*0.5*(v\_u\_old(0:NLAT,1:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u\_old(0:NLAT,2:NLONG,k)+v\_u_old(0:NLAT,2:NLONG,k)+v\_u_old(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG,k)+v_u_old(
NG+1,k)
                                              *(v_f_c(0:NLAT,1:NLONG)*Re*cos(v_lat_c(0:NLAT,1:NLONG))&
+0.5*(v_u_old(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,1:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG,k)+v_u_old(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat_c(0:NLAT,2:NLONG+1,k))*sin(v_lat
NLONG)))&
,2:NLONG+1,k))&
                                             *(v_f_c(1:NLAT+1,1:NLONG)*Re*cos(v_lat_c(1:NLAT+1,1:NLONG))&
+0.5*(v\_u\_old(1:NLAT+1,1:NLONG,k)+v\_u\_old(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,1:NLONG,k)+v\_u\_old(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,1:NLONG,k)+v\_u\_old(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,1:NLONG,k)+v\_u\_old(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLONG+1,k))*sin(v\_lat\_c(1:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1,2:NLAT+1
AT+1,1:NLONG))))
             enddo
                ! equation 7.51 pressure gradient
```

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do k=1,NVERT
                 v new(2:NLAT,:,k)=v new(2:NLAT,:,k)-
dt/P_new(2:NLAT,:)*Re*dlamda_e*cos(lat_vface(2:NLAT,:))&
                         *((geopot_c(2:NLAT,:,k)-geopot_c(1:NLAT-1,:,k))*0.5*(pi_c_old(1:NLAT-1,:,k))
1,:)+pi_c_old(2:NLAT,:))&
                         +0.5*(-pi_c_old(1:NLAT-1,:)+pi_c_old(2:NLAT,:))*Cp_d&
                         *(PVT_c_old(1:NLAT-1,:,k)/dsigma(k)*(sigma_bot(k)&
                         *(P_bot(1:NLAT-1,:,k)-P_c(1:NLAT-1,:,k))+sigma_bot(k-1)&
                         *(P c(1:NLAT-1,:,k)-P bot(1:NLAT-1,:,k-1)))+PVT c old(2:NLAT,:,k)/dsigma(k)&
                         *(sigma\_bot(k)*(P\_bot(2:NLAT,:,k)-P\_c(2:NLAT,:,k))&
                         +sigma_bot(k-1)*(P_c(2:NLAT,:,k)-P_bot(2:NLAT,:,k-1))))
                 ! south boundary
                 v new(1,:,k)=v new(1,:,k)-dt/P new(1,:)*Re*dlamda e*cos(lat vface<math>(1,:))&
                         *((-geopot_c_tminus1(1,:,k)+geopot_c(1,:,k))*pi_c_old(1,:)&
pi\_c\_tminus1(1,:) + pi\_c\_old(1,:)) * Cp\_d * (PVT\_c\_old(1,:,k)/dsigma(k) * (sigma\_bot(k) * (P\_bot(1,:,k)/dsigma(k) * (sigma\_bot(k) * (sigma\_bot(k
k)&
                         -P_c(1,:,k)+sigma_bot(k-1)*(P_c(1,:,k)-P_bot(1,:,k-1))))
                 ! north boundary
                if(periodicBC==1) then
                         v_new(NLAT+1,:,k)=v_new(1,:,k)
                else
                         v_new(NLAT+1,:,k)=v_new(NLAT+1,:,k)-
dt/P new(NLAT+1,:)*Re*dlamda e*cos(lat vface(NLAT+1,:))&
                                  *((geopot_c_tminus1(NLAT,:,k)-geopot_c(NLAT,:,k))*pi_c_old(NLAT,:)&
                                 +(pi_c_tminus1(NLAT,:)-
pi\_c\_old(NLAT,:))*Cp\_d*(PVT\_c\_old(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(P\_bot(NLAT,:,k)\& and bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(p\_bot(NLAT,:,k)/dsigma(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sigma\_bot(k)*(sig
                                 -P\_c(NLAT,:,k)) + sigma\_bot(k-1)*(P\_c(NLAT,:,k)-P\_bot(NLAT,:,k-1)))))\\
                endif
       enddo
        ! equation 7.52 eddy vicousity not finished!
        if(turbmodel==1) then
                do k=1,NVERT
                         v_new(:,:,k)=v_new(:,:,k)
                enddo
       endif
end subroutine calculate_velocity_field
! calculate_pressure_field
! usage: update pressure field using pi_c_new
```

```
! Yun Zhang 05/02/2015
! @stanford
subroutine calculate_pressure_field(pi_c,Pa_c,Pa_bot,P_c,P_bot,sigma_bot)
  real(dp),dimension(NLAT,NLONG),intent(in)::pi_c
  real(dp), dimension(NLAT, NLONG, 0: NVERT), intent(inout):: Pa\_bot, P\_bot
  real(dp),dimension(0:NVERT),intent(in)::sigma_bot
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::Pa_c,P_c
  integer::i,j
  ! calculate pressure at different vertical layer
  ! layer bottom
  do i=1,NLAT
    do j=1,NLONG
      Pa\_bot(i,j,:)=sigma\_bot*pi\_c(i,j)+Pa\_top
      P_{bot(i,j,:)}=(Pa_{bot(i,j,:)}/1000)**k_{therm}
    enddo
  enddo
  ! layer center
  do i=1,NLAT
    do j=1,NLONG
      P_c(i,j,:)=1.0_dp/(1+k_t)*(P_bot(i,j,1:NVERT)*Pa_bot(i,j,1:NVERT)-
P_bot(i,j,0:(NVERT-1))*Pa_bot(i,j,0:(NVERT-1)))
      P_c(i,j,:)=P_c(i,j,:)/(Pa_bot(i,j,1:NVERT)-Pa_bot(i,j,0:NVERT-1))
      Pa_c(i,j,:)=1000*(P_c(i,j,:)**(1/k_therm))
    enddo
  enddo
end subroutine calculate pressure field
! calculate_air_temperature
! usage: update air temperature with the new
! Potential virtual temperature
! Yun Zhang 05/03/2015
! @stanford
subroutine calculate_air_temperature(PVT_c,Temp_c,qv_c,Pa_c)
  real(dp),dimension(NLAT,NLONG,NVERT),intent(in)::PVT_c,qv_c,Pa_c
  real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::Temp_c
  Temp_c=PVT_c/(1+0.608*qv_c)*((Pa_c/1000)**k_therm)
end subroutine calculate_air_temperature
```

```
! calculate_horizontal_bottom_value
! usage: calculate the horizontal value (u,v)
! at the layer bottom of each edege
! Yun Zhang 05/22/2015
! @stanford
subroutine calculate_horizontal_bottom_value(u,u_bot,N1,N2,dsigma)
     real(dp),dimension(N1,N2,NVERT),intent(in)::u
     real(dp),dimension(N1,N2,0:NVERT),intent(inout)::u_bot
     integer,intent(in)::N1,N2
     real(dp),dimension(NVERT),intent(in)::dsigma
     integer:: i,j
     do i=1,N1
           do i=1,N2
                u\_bot(i,j,1:NVERT-1)=(u(i,j,1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(1:NVERT-1)*dsigma(
1)+u(i,j,2:NVERT)*dsigma(2:NVERT))&
                /(dsigma(1:NVERT-1)+dsigma(2:NVERT))
                u\_bot(i,j,0)=u(i,j,1)
                u_bot(i,j,NVERT)=u(i,j,NVERT)
           enddo
     enddo
end subroutine calculate_horizontal_bottom_value
! calculate_horizontal_center_value
! usage: calculate the horizontal value (u,v)
! at the layer bottom of each edege
! Yun Zhang 05/22/2015
! @stanford
subroutine calculate_horizontal_center_value(u,u_c,N1,N2)
     integer,intent(in)::N1,N2
     real(dp),dimension(N1,N2,NVERT),intent(in)::u
     real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::u_c
     if(N2>NLONG) u_c=0.5*(u(:,1:NLONG,:)+u(:,2:NLONG+1,:))
     if(N1>NLAT) u_c=0.5*(u(1:NLAT,:,:)+u(2:NLAT+1,:,:))
end subroutine calculate_horizontal_center_value
end module phys
```

## 9. source.f90 ! regional model module - source ! usage: include all the functions and ! subroutines to define source and sinks ! for heat, momentum and scalar ! Yun Zhang 04/30/2015 ! @stanford module source use constant\_parameter implicit none contains ! heat\_source ! usage: provide the value of heat sinks ! and source to calculate potential virtual ! temperature ! Yun Zhang 04/30/2015 ! @stanford function heat\_source(lat,long,nlayer,t) result(output) real(dp),intent(in)::lat,long,t integer, intent(in):: nlayer real(dp)::output output=0.0\_dp end function heat\_source ! gas\_source ! usage: provide the value of gas sinks ! and source to calculate gas concentration ! Yun Zhang 04/30/2015 ! @stanford function qv\_source(lat,long,nlayer,t) result(output) real(dp),intent(in)::lat,long,t integer, intent(in):: nlayer real(dp)::output output=0.0\_dp

end function qv\_source

end function gas\_source end module source

## 

module turbulence
use constant\_parameter
implicit none

! not finished assume Kb is zero contains

! usage: use turbulence model to calculate

! eddy diffusivty and viscousity for momentum

! and transport equations

! Yun Zhang 05/02/2015

! @stanford

 $subroutine\ calculate\_eddy\_viscousity\_diffusivity(nu\_t,K\_t)\\ real(dp),dimension(NLAT,NLONG,NVERT),intent(inout)::\ nu\_t,K\_t\\ nu\_t=0.0\_dp\\ K\_t=0.0\_dp$ 

end subroutine calculate\_eddy\_viscousity\_diffusivity end module turbulence

```
11. Makefile
FC = gfortran
LD = gfortran
#LDFLAGS = -framework Accelerate
LDFLAGS = -lblas
FFLAGS = -O
.PHONY: clean
%.o: %.f90
    $(FC) $(FFLAGS) -c $<
%.mod: %.f90
    $(FC) $(FFLAGS) -c $<
EXE0 = regional model
MOD0 = constant_parameter.mod allocate_variable.mod basic_state.mod \
      initialization.mod boundary.mod turbulence.mod source.mod output.mod phys.mod
OBJ0 = regionalmodel.o constant_parameter.o allocate_variable.o \
      basic_state.o initialization.o boundary.o turbulence.o source.o output.o phys.o
$(EXE0): $(MOD0) $(OBJ0)
    $(LD) $(OBJ0) $(LDFLAGS) -o $@
ALLEXE = \$(EXE0)
all: $(ALLEXE)
cleanall:
    rm -f $(ALLEXE) *.mod *.o
    rm -rf results
clean:
    rm -f $(ALLEXE) *.mod *.o
    rm -f results/*.bin results/*.txt
test:
    ./$(ALLEXE)
```

## 12. Matlab Library

```
% ReadResult.m
% usage: read the results from the output
% of regional model for cee263B
% save as result.mat which can be used for
% further discussion
% Yun Zhang 05/06/2015
% @Stanford
% result directory
datadir='../results';
NLAT=40;
NLONG=40;
NVERT=15;
lat 0=-1;
long_0=-1;
dlat=0.05;
dlong=0.05;
Pa_top=250;
for i=1:NLAT
   for j=1:NLONG
       lat(i,j)=lat_0+(i-1)*dlat;
       long(i,j)=long_0+(j-1)*dlong;
   end
end
latuface=zeros(NLAT,NLONG+1);
longuface=zeros(NLAT,NLONG+1);
latuface(:,1:NLONG)=lat;
latuface(:,NLONG+1)=lat(:,1);
longuface(:,1:NLONG)=long-0.5*dlong;
longuface(:,NLONG+1)=long(:,NLONG)+0.5*dlong;
latvface=zeros(NLAT+1,NLONG);
longvface=zeros(NLAT+1,NLONG);
longvface(1:NLAT,:)=long;
longvface(NLAT+1,:)=long(NLAT,:);
latvface(1:NLAT,:)=lat-0.5*dlong;
latvface(NLAT+1,:)=lat(NLAT,:)+0.5*dlong;
% load in all results
```

```
filename=[datadir,'/pi.txt'];
pi_tmp=load(filename);
filename=[datadir,'/Pa.txt'];
Pa_tmp=load(filename);
filename=[datadir,'/geopot.txt'];
geopot_tmp=load(filename);
filename=[datadir,'/K_t.txt'];
K_t_tmp=load(filename);
filename=[datadir,'/nu.txt'];
nu_t_tmp=load(filename);
filename=[datadir,'/PVT.txt'];
PVT_tmp=load(filename);
filename=[datadir,'/u.txt'];
u_tmp=load(filename);
filename=[datadir,'/v.txt'];
v_tmp=load(filename);
filename=[datadir,'/w.txt'];
w_tmp=load(filename);
filename=[datadir,'/qv.txt'];
qv_tmp=load(filename);
filename=[datadir,'/temp.txt'];
temp_tmp=load(filename);
filename=[datadir,'/rhoa.txt'];
rhoa_tmp=load(filename);
filename=[datadir,'/gas.txt'];
gas_tmp=load(filename);
% get Nt from output
Nt=length(pi_tmp')/NLAT;
% seperate different time step
for i=1:Nt
```

```
base1=(i-1)*NLAT;
 base2=(i-1)*NLAT*NLONG;
 base3=(i-1)*(NLAT+1)*NLONG;
 base4=(i-1)*(NLONG+1)*NLAT;
 pi\{i\}=pi\_tmp((base1+1):(base1+NLAT),:);
 Pa\{i\}=Pa\_tmp((base2+1):(base2+NLAT*NLONG),:);
  geopot{i}=geopot_tmp((base2+1):(base2+NLAT*NLONG),:);
  K_t\{i\}=K_t_m((base2+1):(base2+NLAT*NLONG),:);
 nu_t\{i\}=nu_t_t(base2+1):(base2+NLAT*NLONG),:);
 PVT{i}=PVT_tmp((base2+1):(base2+NLAT*NLONG),:);
 u\{i\}=u_tmp((base4+1):(base4+NLAT*(NLONG+1)),:);
 v\{i\}=v_tmp((base3+1):(base3+(NLAT+1)*NLONG),:);
  w\{i\}=w_tmp((base2+1):(base2+NLAT*NLONG),:);
 qv{i}=qv_tmp((base2+1):(base2+NLAT*NLONG),:);
 temp{i}=temp_tmp((base2+1):(base2+NLAT*NLONG),:);
 rhoa{i}=rhoa_tmp((base2+1):(base2+NLAT*NLONG),:);
  gas{i}=gas_tmp((base2+1):(base2+NLAT*NLONG),:);
end
% save results
save('results.mat');
% plotvelocityquiver.m
% usage: plot velocity quiver for specific layer
% Yun Zhang 05/07/2015
% @Stanford
function plotvelocityquiver(u,v,k,x,y,xtype,ytype,titleinfo)
[a,b]=size(x);
uu=reshape(u(:,k),b+1,a);
vv = reshape(v(:,k),b,a+1);
vv=vv';
uu=uu';
uc = (uu(:,1:b)+uu(:,2:b+1))/2;
vc = (vv(1:a,:) + vv(2:a+1,:))/2;
quiver(x,y,uc,vc,1.4)
xlabel(xtype);
ylabel(ytype);
title(titleinfo);
end
```

```
% plot3Dsliceresults.m
% usage: plot 3D results for a specific layer from regional model
% Yun Zhang 05/07/2015
% @Stanford
function plot3Dsliceresults(input,k,x,y,xtype,ytype,titleinfo)
[a,b]=size(x);
plotdata=reshape(input(:,k),b,a);
plotdata=plotdata';
pcolor(x,y,plotdata)
xlabel(xtype);
ylabel(ytype);
title(titleinfo);
colorbar;
colormap('Jet');
end
% plot2Dresults.m
% usage: plot 2D results from regional model
% only for cell centered 2D data
% Yun Zhang 05/07/2015
% @Stanford
function plot2Dresults(input,x,y,xtype,ytype,titleinfo)
pcolor(x,y,input)
xlabel(xtype);
ylabel(ytype);
title(titleinfo);
colorbar;
colormap('Jet');
end
```