

Q1 Convert each of the final following expressions into sum of products and product of sums

a) $(u+xw)(x+\bar{u}v)$

$$(u+xw)(x+\bar{u}v)$$

$$ux + u\bar{u}v + xw + xw\bar{u}v$$

$$ux + 0 + xw(1+\bar{u}v)$$

$$ux + xw \rightarrow \text{sum of products}$$

$$x(u+w) \rightarrow \text{product of sums}$$

b) $\bar{x} + x(x+\bar{y})(y+\bar{z})$

$$\bar{x} + x(x+\bar{y})(y+\bar{z})$$

$$(\bar{x}+x)[\bar{x} + (x+\bar{y})(y+\bar{z})]$$

$$(\bar{x}+x+\bar{y})(\bar{x}+y+\bar{z})$$

\rightarrow product of sums

$$\bar{x} + y + \bar{z} \rightarrow \text{sum of products}$$

Q2: 19F0228

Complete and design BCD to 7
segment Display circuit.

UNUSED COMBINATION GIVE E FOR ERROR. from
10 to 15

a
f | g | b
e | d | c

□ 1 2 3 4 5 6 7 8 9

Solution:

Truth table

A	B	C	D	a	b	c	d	e	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	0	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1
1	0	1	0	1	0	0	1	1	1	1
1	0	1	1	1	0	0	1	1	1	1
1	1	0	0	1	0	0	1	1	1	1
1	1	0	1	1	0	0	1	1	1	1
1	1	1	0	1	0	0	1	1	1	1
1	1	1	1	1	0	0	1	1	1	1

K-maps

AB \ CD	00	01	11	10
00	1	0	1	1
01	0	1	1	1
11	x	x	x	x
10	1	1	x	x

$$F(A,B,C,D) = BD + A + C + \bar{B}\bar{D}$$

AB \ CD	00	01	11	10
00	1	1	1	1
01	1	0	1	0
11	0	0	0	0
10	1	1	0	0

$$F = \bar{A}\bar{B} + \bar{B}\bar{C} + \bar{A}\bar{C}\bar{D} + \bar{A}CD$$

AB \ CD	00	01	11	10
00	1	1	1	0
01	1	1	1	1
11	0	0	0	0
10	1	1	0	0

$$F = \bar{A}D + \bar{A}B + \bar{B}\bar{C}$$

AB \ CD	00	01	11	10
00	1	0	1	1
01	0	1	0	1
11	1	1	1	1
10	1	1	1	1

$$F = A + C\bar{D} + \bar{B}\bar{C}D + \bar{B}\bar{C} + \bar{B}\bar{D}$$

AB \ CD	00	01	11	10
00	1	0	0	1
01	0	0	0	1
11	1	1	1	1
10	1	0	1	1

$$F = AB + C\bar{D} + AC + \bar{B}\bar{D}$$

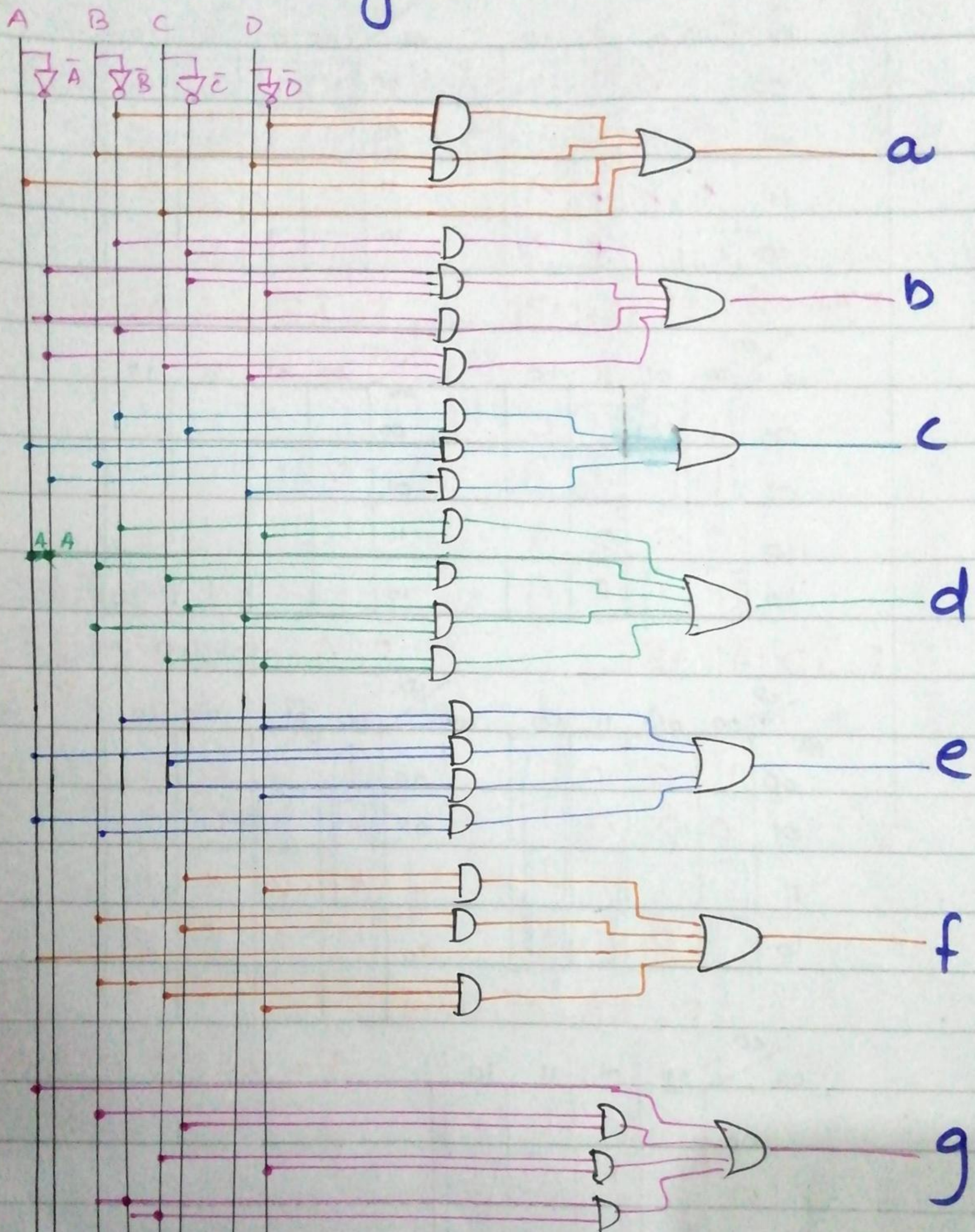
AB \ CD	00	01	11	10
00	1	0	0	0
01	1	1	0	1
11	x	x	x	x
10	1	1	x	x

$$F = A + \bar{C}\bar{D} + \bar{B}\bar{C} + \bar{B}\bar{D}$$

AB \ CD	00	01	11	10
00	0	0	1	1
01	1	1	0	1
11	1	1	1	1
10	1	1	1	1

$$\bar{F} = A + C\bar{D} + \bar{B}\bar{C} + \bar{B}\bar{C}$$

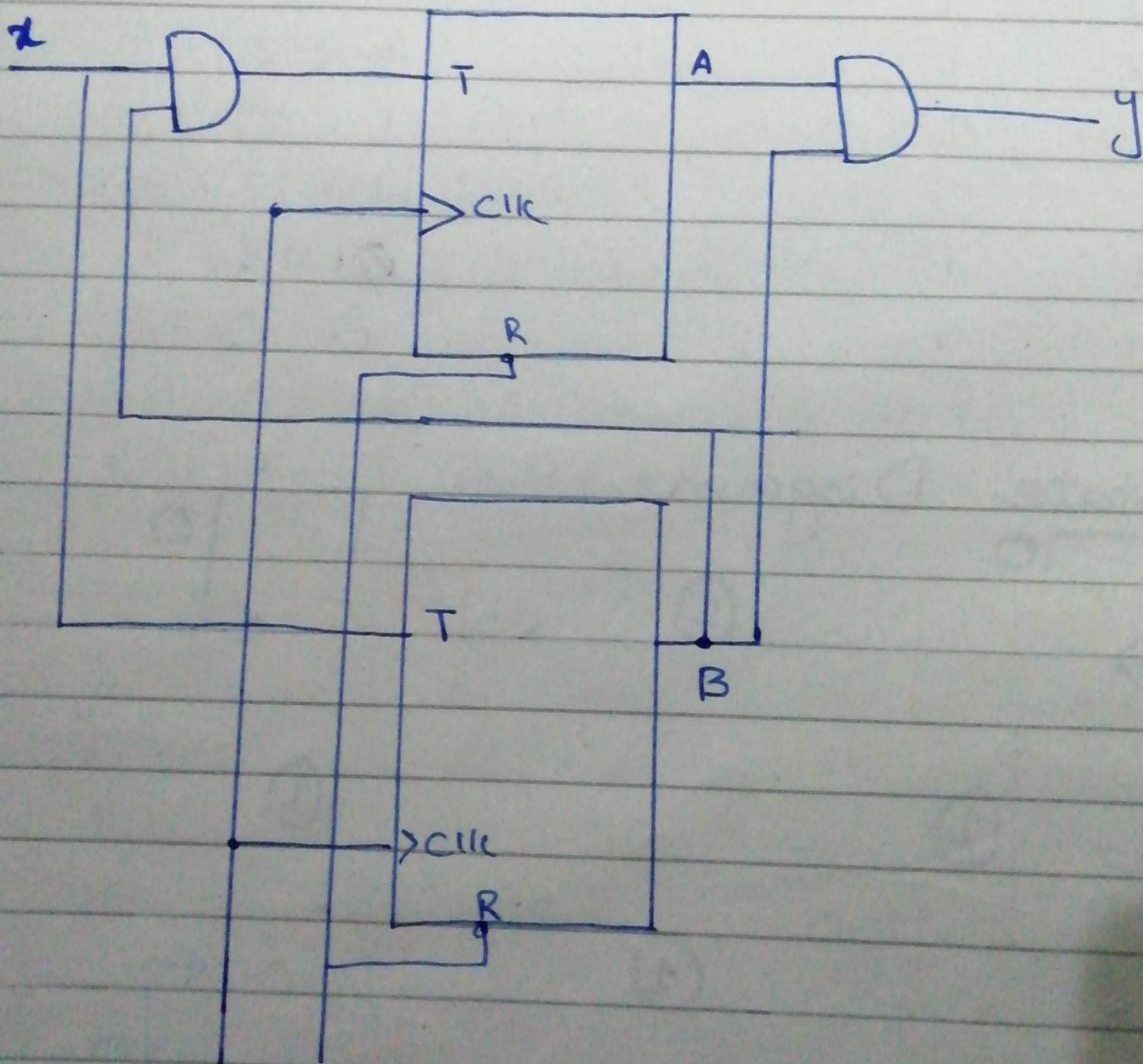
Circuit Diagram.



19F-0228

Q3

Analysis of clocked sequential circuit
to write state table form, second
form also draw state diagram.



Clock reset

State Equations:

$$T_A = B \cdot x$$

$$T_B = x$$

$$Y = AB$$

$A(t+1)$, $(B(t+1))$ equation is

$$\begin{aligned} A(t+1) &= T_A \oplus A = Bx \oplus A = Bx \oplus A \\ &= (Bx)' \cdot A + (Bx) \cdot \bar{A} \end{aligned}$$

$$A(t+1) = A\bar{B} + A\bar{x} + \bar{A} \cdot B \cdot x$$

$$B(t+1) = T_B \oplus B = x \oplus B$$

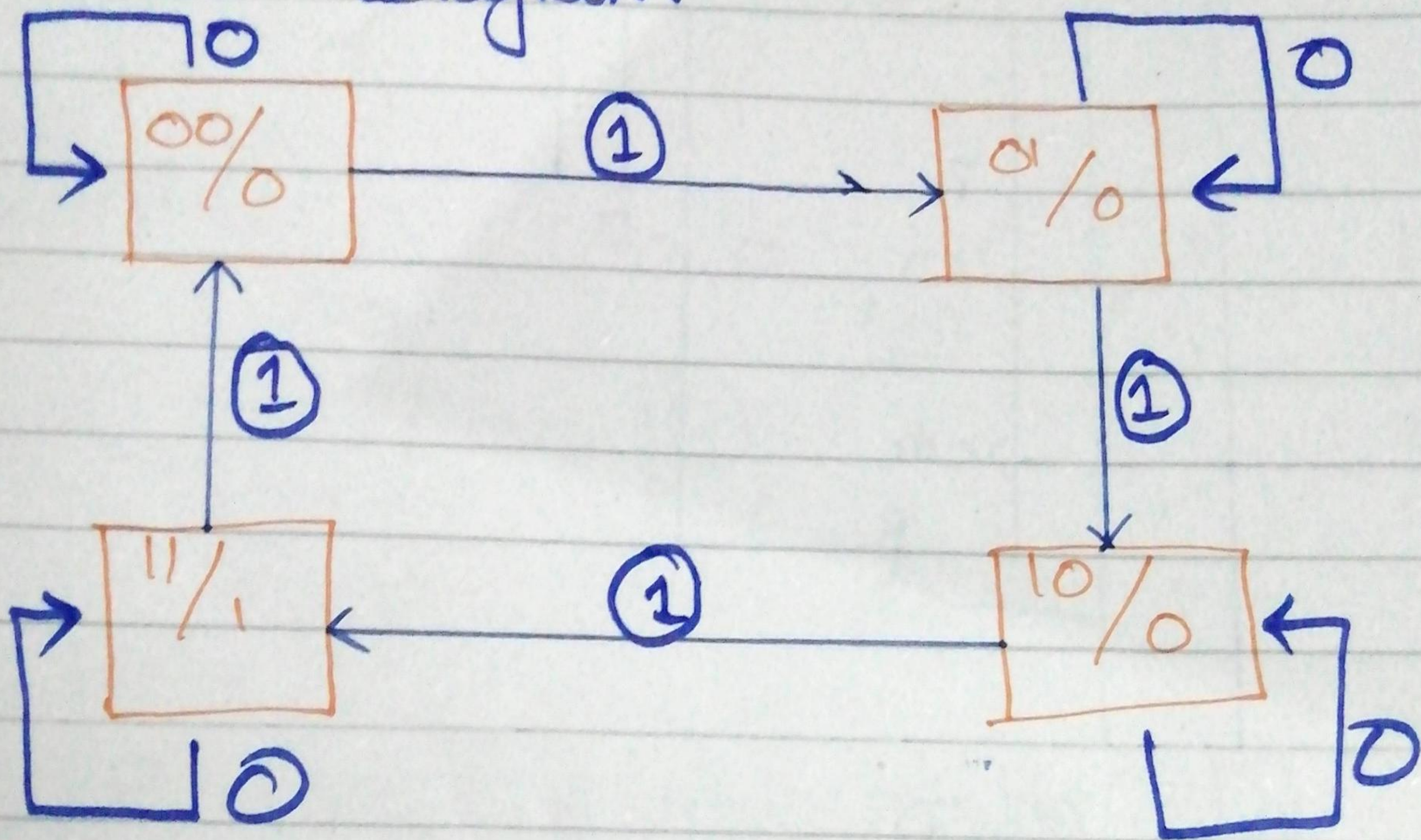
1st Form

Present State		Input x	Next State		Output y
A	B		A	B	
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	1	0
0	1	1	1	0	0
1	0	0	1	0	0
1	0	1	1	1	0
1	1	0	1 1	1	1
1	1	1	0	0	1

2nd Form

Present		Next State		Output	
A	B	x=0	x=1	x=0	x=1
0	0	AB 00	AB 01	X 0	X 0
0	1	01	10	0	0
1	0	10	11	0	0
1	1	11	00	1	1

State Diagram



Q4 19F-0228

Design a counter with T flip-flops that goes through the following binary repeated sequence:

0, 1, 3, 7, 6, 4

010, 101 don't care conditions

Draw Logic Diagram

Present State			Next state					
A	B	C	A(t+1)	B(t+1)	C(t+1)	T _A	T _B	T _C
0	0	0	0	0	1	0	0	1
0	0	1	0	1	1	0	1	0
0	1	0	X	X	X	X	X	X
0	1	1	1	1	1	1	0	0
1	0	0	0	0	0	1	0	0
1	0	1	X	X	X	X	X	X
1	1	0	1	0	0	0	1	0
1	1	1	1	1	0	0	0	1

k-maps

Equations

for

T_A

A \ BC	00	01	11	10
0	0	0	1	X
1	1	X	0	0

$$T_A = \bar{A}B + A\bar{B}$$

$$= A \oplus B$$

for

T_B

A \ BC	00	01	11	10
0	0	1	0	X
1	0	X	0	1

$$T_B = \bar{B}C + B\bar{C}$$

$$= B \oplus C$$

for

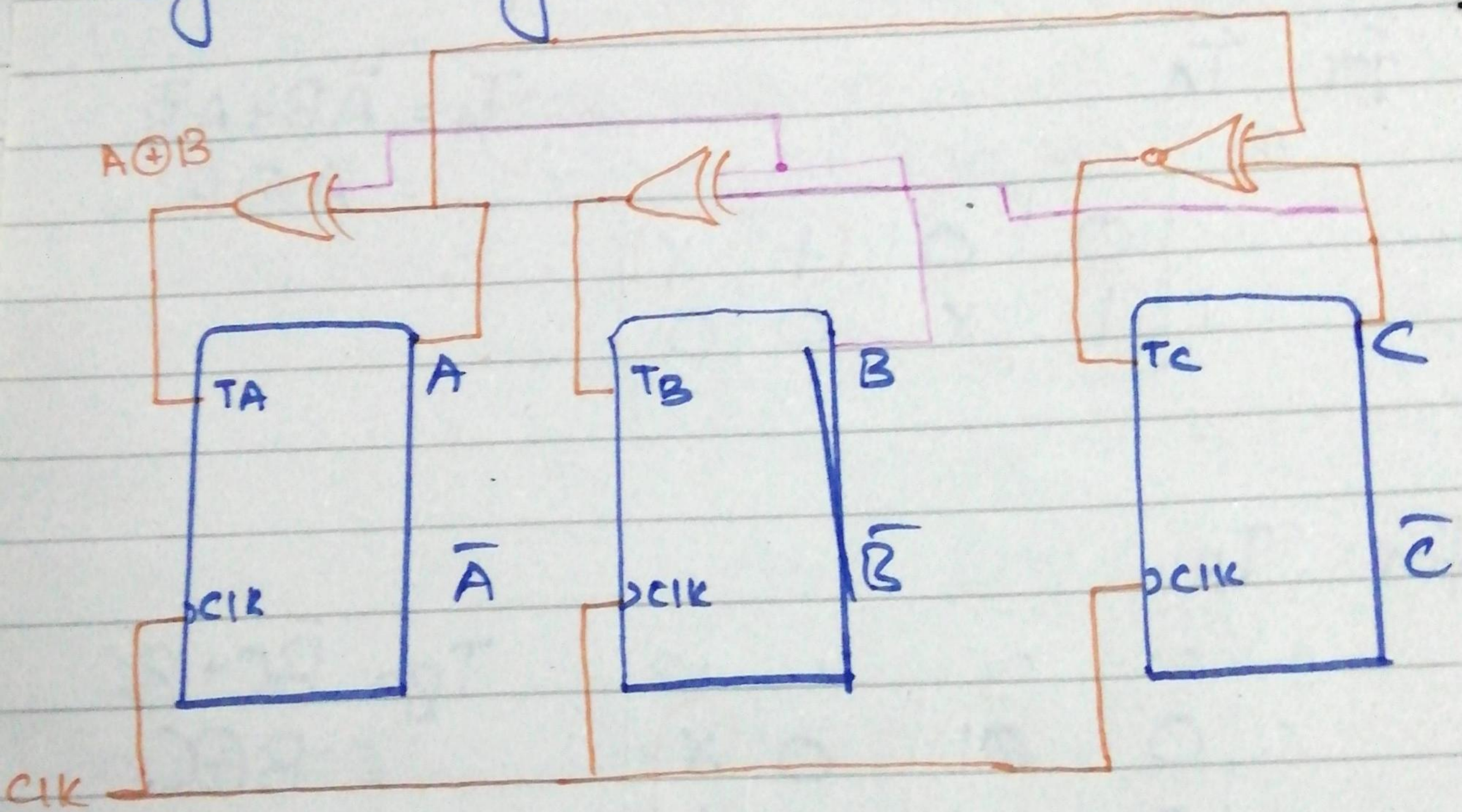
T_C

A \ BC	00	01	11	10
0	1	0	0	X
1	0	X	1	0

$$T_C = \bar{A}\bar{C} + AC$$

$$= A \cdot C$$

Logic Diagram



Q5:

State	Next State				Output (F)			
	$xy=00$	$xy=01$	$xy=10$	$xy=11$	$xy=00$	$xy=01$	$xy=10$	$xy=11$
a	b	d	c	b	0	1	1	0
b	a	c	f	d	1	0	1	1
c	b	d	c	b	0	1	1	0
d	b	d	a	b	0	1	1	0
e	b	c	a	b	0	1	1	0
f	c	d	g	f	0	1	1	0
g	a	b	d	g	1	1	0	1

a) Reduced Table:

State	Next State				Output			
a	b	a	a	b	0	1	1	0
b	a	a	f	a	1	0	1	1
e	b	a	a	b	0	1	1	0
f	a	a	g	f	0	1	1	0
g	a	b	a	g	1	1	0	1

State diagram:

