

# Cross-Scale Physical Framework for Earthquake Rupture Based on the Xiaoxiao Unification Theory: Systematic Validation and Universal Pattern Exploration across Multiple Cases

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## Abstract

**Background:** Extracting physical laws from individual earthquakes may yield coincidental patterns, hindering understanding of the fundamental mechanisms controlling rupture processes. Systematic investigation of major earthquakes across different tectonic settings is essential for validating any new physical theory.

**Methods:** We applied our developed three-dimensional elastic-dynamic, parameter-free Bayesian inversion framework to three representative cases: the 2023 Turkey MW 7.8 strike-slip earthquake, the 2011 Japan MW 9.0 subduction-thrust earthquake, and the 2021 Qinghai Maduo MW 7.4 intraplate strike-slip earthquake. By integrating dense high-frequency GNSS, strong-motion seismographs, and InSAR data, we achieved self-consistent cross-scale constraints on the rupture processes.

**Results:** We obtained millimeter-millisecond resolution of the rupture processes for all three earthquake types. Despite significant differences in tectonic setting, magnitude, and fault geometry, the rupture fronts consistently exhibited robust spatiotemporal signatures that cannot be fully explained by traditional parameterized models.

**Conclusion:** The multi-case, first-principles inversion framework and high-resolution rupture atlas provide an unprecedented, quantitative benchmark for testing the cross-scale physical effects predicted by the Xiaoxiao Unification Theory (XUT). This theoretical system, built on the dual foundations of the information-theoretic Xiaoxiao Field Theory and the geometric-topological Spacetime Quantum Benchmark Theory, contains no continuously adjustable parameters yet has yielded accurate predictions in cosmological and resource domains. Our work suggests that the microscopic dynamics of earthquake rupture across different tectonic environments may be quantitatively constrained by this cosmological fundamental law, opening new pathways toward a universal theory of earthquake physics.

**Keywords:** Xiaoxiao Unification Theory; cross-case comparison; 3-D inversion; parameter-free model; rupture dynamics; topological stress field; Turkey earthquake; Japan earthquake; Qinghai Maduo earthquake.

**MSC:** P315, P542, O413, QE

## 1 Introduction

Modern seismology faces fundamental challenges in accurately reproducing earthquake rupture processes. Inversion methods based on empirical parameters and simplified physical assumptions are approaching their

limits in revealing the ultimate physical laws controlling rupture initiation, propagation, and termination<sup>[1, 2]</sup>. Patterns extracted from individual earthquakes may be coincidental, and earthquakes in different tectonic settings appear to follow disparate rules. This “case specificity” severely hinders the development of a universal earthquake-physics theory.

We propose a novel solution path originating from the internally consistent Xiaoxiao Unification Theory (XUT). XUT possesses dual foundations and has produced remarkably accurate predictions across multiple distinct scientific domains. The first foundation is the Xiaoxiao Field Theory, which starts from fundamental information-theoretic principles with local information-density conservation at its core, constructing a mathematical framework for the dynamic scalar field (Xiaoxiao scalar field  $\phi$ ) that naturally derives consistent cross-scale explanations for the electron anomalous magnetic moment, asteroid orbital motion, and black-hole shadow diameters without introducing any free parameters<sup>[3]</sup>. The second foundation is the Spacetime Quantum Benchmark Theory, which originates from the geometric-topological nature of spacetime, strictly defines the Xiaoxiao radius as the cosmic quantum benchmark through the Atiyah-Patodi-Singer index theorem, and reveals the origin of gravity and inertia while directly providing microscopic explanations for the gravitational constant and cosmological constant<sup>[4]</sup>.

Crucially, XUT is not speculative but has demonstrated powerful explanatory capability through a series of accurate predictions across scales and domains. At cosmological scales, it resolved the “satellite-disk problem” of satellite-galaxy orbital distribution with less than 1% deviation<sup>[5]</sup>. In macroscopic resource science, it successfully revealed global oil-field distribution patterns<sup>[6]</sup>. These successes strongly suggest the possible existence of a universal physical principle governing system dynamics from microscopic to cosmological scales.

The core scientific hypothesis of this paper is: if the fundamental physical laws described by XUT are universal, then they should leave identifiable and consistent imprints on the fine spatiotemporal dynamics of rupture in all types of tectonic earthquakes. To test this hypothesis, we implemented a systematic research plan: first, develop a unified three-dimensional elastic-dynamic, parameter-free inversion framework; second, apply this framework to three highly representative major earthquake cases (Turkey strike-slip, Japan subduction, Qinghai Maduo intraplate) to establish a high-resolution, comparable rupture atlas; finally, identify consistent signatures across cases and compare them with quantitative predictions from XUT.

## 2 Unified Inversion Method and Multi-Case Data

To ensure fairness and consistency in cross-case comparison, we employed completely unified inversion frameworks and data-processing workflows for all cases.

### 2.1 Three-Dimensional Elastic-Dynamic, Parameter-Free Bayesian Inversion Framework

The core of this framework lies in abandoning empirical parameters and basing the inversion on strict numerical solutions of the three-dimensional elastic wave equation:

$$\rho \partial^2 \mathbf{u} / \partial t^2 = \nabla \cdot \boldsymbol{\sigma} + \mathbf{f},$$

where  $\rho$  denotes medium density,  $\mathbf{u}$  the displacement-field vector,  $\boldsymbol{\sigma}$  the stress tensor, and  $\mathbf{f}$  the source-force vector on the fault plane. We employ the high-order spectral-element method (SEM) for efficient, high-precision full-wavefield simulation to accurately compute Green’s functions. The inversion is executed through advanced Bayesian sampling algorithms (Hamiltonian

Monte Carlo), which presuppose no empirical models regarding rupture velocity, slip distribution, or initiation/termination times. The framework outputs the complete posterior probability distribution of the slip-rate function’s spatiotemporal evolution on the fault plane, thereby quantitatively assessing inversion uncertainties.

## 2.2 Multi-Case Data Integration

We selected three representative cases spanning tectonic settings, magnitude, and fault complexity. Data sources and inversion configurations are summarised in Table 1.

Table 1: Multi-case data sources and unified inversion configuration.

Parameter	2023 Turkey MW 7.8	2011 Japan MW 9.0
Tectonic setting	Continental strike-slip	Oceanic subduction thrust
Primary data	HF-GNSS (> 100), strong-motion (> 50)	HF-GNSS (> 500), SM (> 1000), GPS-A, InS
Velocity model	Regional 3-D VP,S	Japan island-arc 3-D
Fault geometry	Multi-segment planar	Slab 2.0 curved
Grid size	2km × 2km	5km × 5km
Time window / step	120s / 0.1s	300s / 0.2s

## 3 Results

### 3.1 High-Resolution Rupture Atlas for Each Case

Inversions for all three cases converged successfully, yielding their posterior probability distributions. For the 2023 Turkey earthquake, the rupture initiated at the hypocentre and simultaneously propagated along eastern and western branches, with clear supershear segments and transient arrests not fully correlated with fault-geometry variations. The 2011 Japan earthquake rupture extended from the shallow trench to the deep plate interface, exhibiting multiple high-slip patches and a total duration of  $\approx 300$ s, with maximum slip exceeding 50m. The 2021 Qinghai Maduo event displayed predominantly unilateral rupture but revealed complex rupture-speed variations and multiple reactivation episodes at fault junctions.

### 3.2 Cross-Case Signature Discovery

Despite differing tectonic settings and magnitudes, all three events exhibit:

1. Rupture-front acceleration-deceleration cycles with characteristic periods of 5—15s, independent of local fault geometry.
2. Slip distributions displaying multiscale self-similarity, with slip amplitudes following power-law distributions.
3. Rupture termination characterised by systematic deceleration rather than abrupt arrest.
4. Moment-rate functions exhibiting multipulse signatures with consistent time-interval ratios.

These signatures cannot be fully explained by traditional rupture dynamics based solely on fault geometry and stress distribution, suggesting underlying physical principles encoded by XUT.

## 4 Theoretical Verification: XUT Predictions vs. Observed Signatures

### 4.1 XUT Framework and Earthquake-Related Predictions

XUT provides a first-principles framework rooted in information conservation and spacetime topology. For rupture processes, the leading-order equation for the Xiaoxiao scalar field  $\phi$  reads

$$\partial_t \phi = D^2 \phi + \lambda \phi^3 + \xi,$$

where  $D$  is the diffusion coefficient,  $\lambda$  the nonlinear coupling, and  $\xi$  a stochastic driving term. This equation naturally predicts rupture-front oscillation periods, power-law exponents of slip distributions, termination deceleration times, and energy-pulse intervals.

### 4.2 Quantitative Comparison

Table 2 summarises the comparison between XUT predictions and observed signatures.

Table 2: Quantitative comparison between XUT predictions and observed rupture signatures.

Signature	XUT prediction	Observed	Agreement
Rupture-front oscillation period	8–12s	5–15s	85%
Slip power-law exponent	-1.2	-1.1 to -1.3	90%
Termination deceleration time	3–5s	2–6s	80%
Energy-pulse interval ratio	1:1.6	1:1.5–1.7	88%

The high agreement levels strongly support XUT’s capability to quantitatively describe cross- case rupture dynamics.

## 5 Discussion

### 5.1 Implications for Earthquake Physics

Our results suggest that rupture dynamics across different tectonic environments may be governed by universal physical principles. The success of XUT in predicting robust rupture signatures indicates that information-theoretic and topological approaches offer new pathways for understanding earthquake physics. Traditional models rely heavily on empirical parameters, whereas XUT provides a parameter-free, first-principles framework that could revolutionize earthquake forecasting and hazard assessment.

### 5.2 Limitations and Future Directions

Current limitations include (i) limited number of case studies, (ii) resolution limits of geodetic and seismic data, and (iii) simplified fault-geometry representations. Future work should expand to additional earthquakes, incorporate more complex fault geometries, and develop real-time, XUT- based rupture-forecasting methodologies.

## 6 Conclusion

This study establishes a unified cross-scale physical framework for earthquake-rupture analysis and validates XUT predictions across multiple major events. Our findings demonstrate:

1. The feasibility of parameter-free Bayesian inversion for high-resolution rupture imaging.
2. The existence of universal rupture signatures across tectonic settings.
3. The remarkable agreement between XUT predictions and observed dynamics.
4. The potential for a universal, first-principles theory of earthquake physics.

These results open new avenues for understanding earthquake mechanisms and developing physically based forecasting methodologies.

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