

查询优化 Query Optimization

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▶ 课程概要



- Part 0: Overview
 - Ch1: Introduction
- Part 1 Relational Languages
 - Ch2: Relational model
 - Ch3: Introduction to SQL
 - Ch4: Intermediate SQL
 - Ch5: Advanced SQL

Part 2 Database Design

- Ch6: Database design via E-R model
- Ch7: Relational database design

Part 3 Application Design & Development

- Ch8: Complex data types
- Ch9: Application development

Part 4 Big Data Analytics

- Ch10: Big data
- Ch11: Data analytics

Part 5 Storage Management & Indexing

- Ch12: Physical storage systems
- Ch13: Data storage structures
- Ch14: Indexing

Part 6 Query Processing & Optimization

- Ch15: Query processing
- Ch16: Query optimization

Part 7 Transaction Management

- Ch17: Transactions
- Ch18: Concurrency control
- Ch19: Recovery system

Part 8 Parallel & Distributed Database

- Ch20: Database system architecture
- Ch21-23: Parallel & distributed storage, query processing & transaction processing

Advanced topics

DB Platform: **OceanBase**, MongoDB, Neo4J

- ...

▶目录



- 概述
- · 关系表达式的转换
- · 表达式执行代价估计
- · 执行计划选择
- ・ 物化视图*
- · 查询优化中的高级话题*

> 查询优化概述

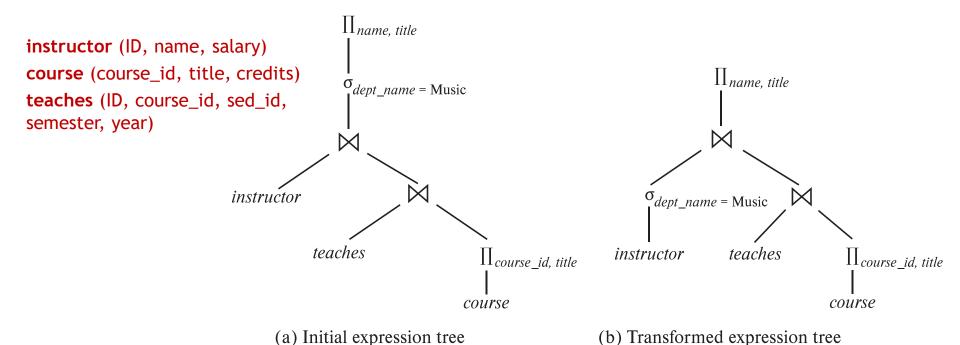


- Alternative ways to execute (执行) a given query
 - equivalent expressions
 - different algorithms for each operation
- The cost difference between a good way and a bad way of executing a query can be enormous
- Estimate the cost of operations
 - depend on the statistical information about relations which the database should maintain
 - need to estimate the statistics for intermediate results to compute the cost of complex expressions

▶ 查询优化概述 (续)



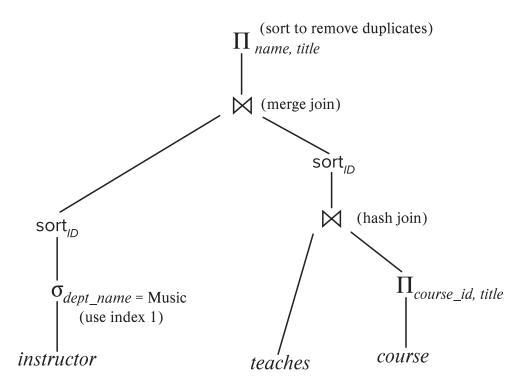
• 查询: 找出Music系所有教师的名字以及每位教师所教授课程的名称



▶ 查询优化概述 (续)



• 执行计划需明确每个运算使用的算法以及运算之间的执行如何协调



▶ 查询优化概述 (续)



- · Cost-based Optimization,基于代价的优化
 - 步骤1: 产生逻辑上与给定表达式等价的表达式
 - 使用等价规则
 - 步骤2: 对所产生的表达式以不同方式标注,产生不同的查询执行计划
 - 步骤3: 估计每个执行计划的代价,选择估计代价最小的执行计划

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关系表达式转换



Equivalence of two relational algebra expressions

- Generate the same set of tuples on every legal database instance
- Note: the order of tuples is irrelevant

Equivalence rule (等价规则)

- The expressions of two forms are equivalent
- Can replace expression of first form by the second, or vice versa

▶ 等价规则



• 规则1: 合取选择运算可分解为单个选择运算的序列

$$\sigma_{\theta_1 \wedge \theta_2}(E) = \sigma_{\theta_1}(\sigma_{\theta_2}(E))$$

规则2:选择运算满足交换律 (commutative)

$$\sigma_{\theta_1}(\sigma_{\theta_2}(E)) = \sigma_{\theta_2}(\sigma_{\theta_1}(E))$$

• 规则3: 多个连续投影中只有最后一个运算是必需的, 其余可忽略

$$\Pi_{t_1}(\Pi_{t_2}(...(\Pi_{tn}(E))...)) = \Pi_{t_1}(E)$$

• **规则4**:选择操作可以与笛卡尔积以及 θ 连接相结合

$$\sigma_{\theta}(E_1 \times E_2) = E_1 \bowtie_{\theta} E_2$$

$$\sigma_{\theta 1}(E_1 \bowtie_{\theta 2} E_2) = E_1 \bowtie_{\theta 1 \land \theta 2} E_2$$

▶ 等价规则(续)



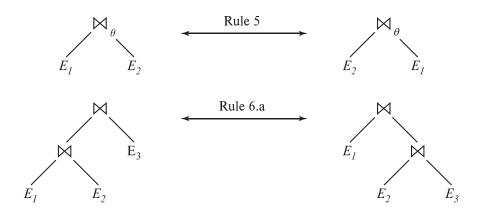
· 规则5:θ连接满足交换律

$$- E_1 \bowtie_{\theta} E_2 = E_2 \bowtie_{\theta} E_1$$

规则6a: 自然连接满足结合律

$$- (E_1 \bowtie E_2) \bowtie E_3 = E_1 \bowtie (E_2 \bowtie E_3)$$

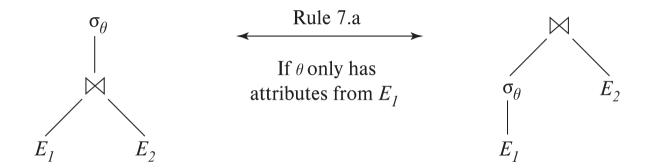
- 规则6b: θ连接满足下列形式的结合律:
 - $(E_1 \bowtie_{\theta_1} E_2) \bowtie_{\theta_2 \land \theta_3} E_3 = E_1 \bowtie_{\theta_1 \land \theta_3} (E_2 \bowtie_{\theta_2} E_3)$, 要求其中 θ_2 只涉及 θ_2 和 θ_3 的属性



> 等价规则(续)



- 规则7: 选择操作在下面两个条件下对θ连接满足分配律
 - a. 当选择条件 θ_0 中的所有属性只涉及参与连接的表达式之一(如 E_1)时: $\sigma_{\theta_0}(E_1 \bowtie_{\theta} E_2) = (\sigma_{\theta_0}(E_1)) \bowtie_{\theta} E_2$
 - b. 当选择条件 θ_1 只涉及 E_1 的属性,选择条件 θ_2 只涉及 E_2 的属性时: $\sigma_{\theta_1 \wedge \theta_2}(E_1 \bowtie_{\theta} E_2) = (\sigma_{\theta_1}(E_1)) \bowtie_{\theta} (\sigma_{\theta_2}(E_2))$



▶ 等价规则(续)



- **规则8**: 令 L_1 、 L_2 分别代表 E_1 、 E_2 的**属性子集**,投影操作在下列条件下对 θ 连接满足分配率
 - a. 如果连接条件 θ 只涉及 L_1 ∪ L_2 中的属性:

$$\prod_{L_1 \cup L_2} (E_1 \bowtie_{\theta} E_2) = (\prod_{L_1} (E_1)) \bowtie_{\theta} (\prod_{L_2} (E_2))$$

- b. 针对连接 E_1 ⋈_θ E_2
 - $\Diamond L_3 = E_1 \sqcup U$ 电极性 $\partial L_2 = U$ 电极性 $\partial L_3 = U$ $\partial L_3 = U$
 - $\Diamond L_4 \not= E_2$ 出现在连接条件 θ 中但不在 $L_1 \cup L_2$ 中的属性

$$\prod_{L_{1} \cup L_{2}} (E_{1} \bowtie_{\theta} E_{2}) = \prod_{L_{1} \cup L_{2}} ((\prod_{L_{1} \cup L_{3}} (E_{1})) \bowtie_{\theta} (\prod_{L_{2} \cup L_{4}} (E_{2})))$$

▶ 等价规则(续)



- 规则9:集合的并和交满足交换律
 - $E_1 \cup E_2 = E_2 \cup E_1$
 - $\quad E_1 \cap E_2 = E_2 \cap E_1$

(set difference is not commutative)

- 规则10:集合的并和交满足结合律
 - $(E_1 \cup E_2) \cup U_3 = E_1 \cup (E_2 \cup E_3)$
 - $(E_1 \cap E_2) \cap U_3 = E_1 \cap (E_2 \cap E_3)$
- 规则11:选择操作对并、交、差满足分配率
 - $\quad \sigma_{\theta}(E_1 E_2) = \sigma_{\theta}(E_1) \sigma_{\theta}(E_2)$
 - similarly for ∪ and ∩ in place of −
 - $\quad \sigma_{\theta}(E_1 E_2) = \sigma_{\theta}(E_1) E_2$
 - similarly for ∩ in place of -, but not for ∪?
- 规则12:投影对并的分配律
 - $\Pi_L(E_1 \cup E_2) = (\Pi_L(E_1)) \cup (\Pi_L(E_2))$

▶ 例1: Selections First



 Find the names of all instructors in Music department, along with the titles of the courses that they teach

```
\Pi_{name, title}(\sigma_{dept \ name= \ 'Music'}(instructor \bowtie (teaches \bowtie \Pi_{course \ id, title} (course))))
```

Transformation using rule 7a

```
\Pi_{name, title}((\sigma_{dept \ name= \ 'Music'}(instructor)) \bowtie (teaches \bowtie \Pi_{course \ id. \ title} (course)))
```

例2: Multiple Transformations



 Find the names of all instructors in Music department who have taught a course in 2021, along with the titles of the courses that they taught

```
\Pi_{\textit{name, title}}(\sigma_{\textit{dept\_name= "Music"} \land \textit{year= 2021}}(\textit{instructor} \bowtie (\textit{teaches} \bowtie \Pi_{\textit{course id, title}}(\textit{course}))))
```

Rule 6a:

```
\Pi_{name, \ title}(\sigma_{dept\_name= \text{``Music''} \land year= 2021}((instructor \bowtie teaches) \bowtie \Pi_{course\_id, \ title}(course)))
```

Rule 7a:

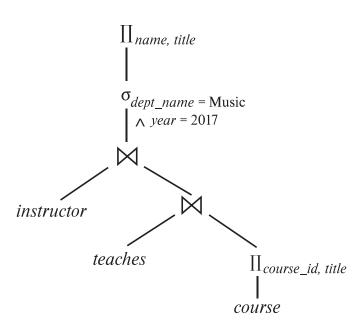
```
\Pi_{name, \ title}((\sigma_{dept\_name= \ "Music" \land year = 2021}(instructor \bowtie teaches)) \bowtie \Pi_{course\_id, \ title}(course))
```

Rule1 & 7a:

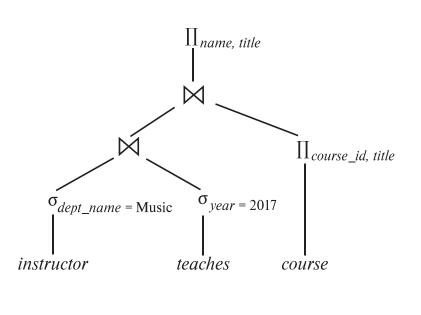
```
\Pi_{name, \ title}((\sigma_{dept\_name= \text{``Music''}}(instructor) \bowtie \sigma_{year=2021} \ (teaches)) \bowtie \Pi_{course\_id, \ title}(course))
```

例2: Multiple Transformations





(a) Initial expression tree



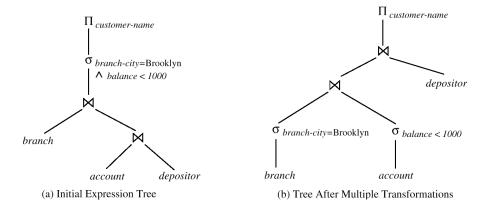
(b) Tree after multiple transformations

▶ 练习



- Query: Find the names of all the customers who have an account with balance less than \$1000 at the Brooklyn branch
 - $\Pi_{CN}(\sigma_{BC="Brooklyn" \land balance < 1000}(branch \bowtie (account \bowtie depositor)))$
 - CN: customer name, BC: branch city
- Task: Give one equivalent expression with better execution performance
- One solution:

 $\Pi_{CN}((\sigma_{BC="Brooklyn"}(branch) \bowtie \sigma_{balance < 1000}(account)) \bowtie depositor)$



连接顺序



• For three relations r_1 , r_2 , and r_3 ,

$$(r_1 \bowtie r_2) \bowtie r_3 = r_1 \bowtie (r_2 \bowtie r_3)$$

• If $r_2 \bowtie r_3$ is quite large and $r_1 \bowtie r_2$ is small, we choose $(r_1 \bowtie r_2) \bowtie r_3$

so that we can compute and store a smaller temporary relation

▶ 连接顺序(续)



Consider the expression

 $\Pi_{name, \ title}(\sigma_{dept_name=\ 'Music''} \ (instructor) \bowtie teaches) \bowtie \Pi_{course_id, \ title} \ (course))))$

Solution A

- compute teaches $\bowtie \Pi_{course_id, title}$ (course) first, and join the result with $\sigma_{dept_name=\ 'Music''}$ (instructor)
- the result of the first join is likely to be a large relation

Solution B

- − compute $\sigma_{dept_name=\ 'Music''}$ (instructor) \bowtie teaches first
- only a small fraction of instructors are likely to be from the Music department

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关系的统计信息



• 关系(表)的统计信息

- n_r : the number of tuples in relation r
- b_r : the number of blocks of r
- s_r : the size of a tuple of r
- f_r : the number of tuples that fit into one block
- V(A, r): the number of distinct values that appear in r for attribute A, i.e., the size of $\Pi_A(r)$
- If the tuples of r are stored together physically in a file, then: $b_r = \left| \frac{n_r}{f_r} \right|$

索引的基本信息



- F_i : the average fan-out(扇出) of internal nodes of index i
 - for tree-structured indices such as B+-tree
- HT_i: the number of levels in index i
 - i.e., the height of i
 - for a balanced tree index (e.g., B+-tree) on attribute A of relation r, $HT_i = \left\lceil log_{F_i}(V(A,r)) \right\rceil$
 - for a hash index, HT_i is 1
- LB_i: the number of lowest-level index blocks in i
 - i.e., the number of blocks at the leaf level of the index

▶ 查询代价的估计



Recall that

- Disk access is the predominant cost, and is also relatively easy to be estimated
- The number of block transfers from disk is used as a measure of the actual cost of execution
- It is assumed that all block transfers have the same cost

简单选择操作结果大小估计



- $\sigma_{A=a}(r)$
 - 假设取值**均匀分布**,则可估计选择结果有 $n_r/V(A,r)$ 个元组
- $\sigma_{A \leq V}(r)$
 - Let c denote the estimated number of tuples satisfying the condition. If $\min(A,r)$ and $\max(A,r)$ are available in database catalog and we assume that values are uniformly distributed (值均匀分布)
 - C = 0, if $v < \min(A, r)$
 - $C = n_r \cdot \frac{v \min(A, r)}{\max(A, r) \min(A, r)}$
 - $C = n_r$, if $v \ge \max(A, r)$
 - In absence of statistical information, c is assumed to be $n_r/2$

> 复杂选择操作结果大小估计



- Selectivity (中选率) of the condition $heta_i$
 - The probability that a tuple in the relation r satisfies θ_i
 - If s_i is the number of tuples satisfying θ_i , the selectivity of θ_i is given by s_i/n_r
- 合取: $\sigma_{\theta 1 \wedge \theta 2 \wedge \cdots \wedge \theta n}(r)$
 - Estimated number of tuples:

$$n_r * \frac{s_1 * s_2 * \dots * s_n}{n_r^n}$$

- 析取: $\sigma_{\theta 1 \vee \theta 2 \vee \cdots \vee \theta n}(r)$
 - Estimated number of tuples:

$$n_r * \left(1 - (1 - \frac{s_1}{n_r}) * (1 - \frac{s_2}{n_r}) * ... * (1 - \frac{s_n}{n_r})\right)$$

- 取反: $\sigma_{\neg \theta}(r)$
 - Estimated number of tuples: $n_r size(\sigma_{\theta}(r))$

连接操作结果大小估计



Cartesian product

- $r \times s$ contains $n_r * n_s$ tuples

Natural join

- If $R \cap S = \emptyset$, then $r \bowtie s$ is the same as $r \times s$
- If $R \cap S$ is a key for R, then a tuple of s will join with **at most** one tuple from r, and size $(r \bowtie s) \leq n_s$
- If $R \cap S$ is a foreign key in S referencing R, the number of tuples in $r \bowtie S$ is exactly the same as the number of tuples in S, i.e., N
 - E.g., for depositor \bowtie customer, customer-name in depositor is a foreign key of customer, and the result has exactly $n_{depositor}$ tuples

· 连接操作结果大小估计(续)



- Catalog information for join examples:
 - $n_{customer} = 10,000, f_{customer} = 25, b_{customer} = 10,000/25 = 400$
 - $n_{depositor} = 5,000$, $f_{depositor} = 50$, $b_{depositor} = 5,000/50 = 100$
 - V(customer-name, depositor) = 2,500, which implies that, on average, each customer has two accounts
- E.g., *depositor* ⋈ *customer*
 - $n_{depositor} = 5000$

> 连接操作结果大小估计(续)



- If $R \cap S = \{A\}$ is not a key for R or S
 - If we assume that every tuple t in R produces tuples in $R \bowtie S$, the number of tuples in $R \bowtie S$ is estimated to be:

$$n_r * \frac{n_s}{V(A,s)}$$

— If the reverse is true, the estimate obtained will be:

$$n_S * \frac{n_r}{V(A,r)}$$

The lower of these two estimates is probably the more accurate one

· 连接操作结果大小估计(续)



- Estimate the size of depositor ⋈ customer without using the information about foreign keys:
 - V(customer-name, depositor) = 2500, and
 V(customer-name, customer) = 10000
 - The two estimates are
 5000 * 10000/2500 = 20,000 and
 5000 * 10000/10000 = 5000
- Choose the lower estimate, which is the same as the earlier estimation using foreign keys

▶ 其他操作结果集大小估计



投影

- Estimated size of $\Pi_A(r) = V(A, r)$

· 聚集

- Estimated size of ${}_{A}g_{F}(r) = V(A, r)$

・集合操作

- For unions/intersections of selections on the same relation: rewrite and use size estimate for selections
 - E.g., $\sigma_{\theta 1}(r) \cup \sigma_{\theta 2}(r)$ can be rewritten as $\sigma_{\theta 1 \vee \theta 2}(r)$
- For operations on different relations:
 - estimated size of $r \cup s =$ size of r +size of s
 - estimated size of $r \cap s = \min\{\text{size of } r, \text{ size of } s\}$
 - estimated size of r s =size of r
 - All the three estimates may be quite inaccurate, but provide upper bounds for the sizes

▶ 其他操作结果集大小估计(续)



Outer join

- Estimated size of $r \implies s = \text{size of } r \bowtie s + \text{size of } r$
 - Case of right outer join is symmetric
- Estimated size of $r \supset \subseteq s$ = size of $r \bowtie s$ + size of r + size of s

Estimation of Distinct Values



- Selections: $\sigma_{\theta}(r)$
 - If θ forces A to take a specified value:
 - If A = 3, $V(A, \sigma_{\theta}(r)) = 1$
 - If θ forces A to take one of a specified set of values
 - $V(A, \sigma_{\theta}(r))$ = the number of specified values
 - e.g., $(A = 1 \lor A = 3 \lor A = 4)$
 - If the selection condition θ is of the form A op v
 - Estimated $V(A, \sigma_{\theta}(r)) = V(A, r) * s$, where s is the selectivity of the selection
 - In all the other cases: use approximate estimate of $\min(V(A,r), n_{\sigma_{\theta}(r)})$
 - More accurate estimate can be obtained using probability theory

Estimation of Distinct Values (Cont.)



- Joins: $r \bowtie s$
 - If all attributes in A are from r
 - Estimated size of $V(A, r \bowtie s) = \min(V(A, r), n_{r\bowtie s})$
 - If A contains attributes A_1 from r and A_2 from s, then
 - $V(A, r \bowtie s) = \min(V(A_1, r) * V(A_2 A_1, s), V(A_1 A_2, r) * V(A_2, s), n_{r \bowtie s})$
 - More accurate estimate can be obtained using probability theory

Projection

- Estimation of distinct values are straightforward for projections
- They are the same in $\Pi_A(r)$ as in r

Aggregation

- For $\min(A)$ and $\max(A)$, the number of distinct values can be estimated as $\min(V(A,r),V(G,r))$ where G denotes grouping attributes
- For other aggregates, assume that all values are distinct, and use V(G,r)

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枚举等价表达式



Equivalent expression generation

- Query optimizers use equivalence rules to systematically generate expressions equivalent to the given expression
- Generate all equivalent expressions by repeatedly executing the following step until no more expressions can be found
 - Given an expression E, if any sub-expression E_s of E matches one side of an equivalence rule, the optimizer generates a new expression where E_s is transformed to match the other side of the rule

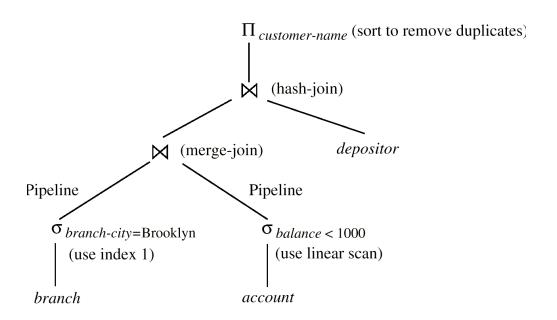
Issues

- The above approach is very expensive in space and time
 - Space requirements can be reduced by sharing common sub-expressions for equivalent expressions
 - Time requirements can be reduced by not generating all expressions

> 执行计划



 An execution plan defines exactly what algorithm is used for each operation, and how the execution of the operations is coordinated



执行计划的选择



Two general approaches

- Search all the plans and choose the best plan in a cost-based fashion
- Uses heuristics to choose a plan

Interaction of evaluation operations

- Choosing the cheapest algorithm for each operation independently may not yield the best overall algorithm
 - merge-join may be costlier than hash-join, but may provide a sorted output which reduces the cost for an outer level aggregation
 - nested-loop join may provide opportunity for pipelining

▶ 基于代价的优化



- To find the best join-order for $r_1 \bowtie r_2 \bowtie \cdots \bowtie r_n$
 - There are (2(n-1))!/(n-1)! different join orders for above expression (cf. Exercise 16.12)
 - E.g., with n = 3, the number is 12

$$r_1 \bowtie (r_2 \bowtie r_3), r_1 \bowtie (r_3 \bowtie r_2), (r_2 \bowtie r_3) \bowtie r_1, (r_3 \bowtie r_2) \bowtie r_1$$

 $r_2 \bowtie (r_1 \bowtie r_3), r_2 \bowtie (r_3 \bowtie r_1), (r_1 \bowtie r_3) \bowtie r_2, (r_3 \bowtie r_1) \bowtie r_2$
 $r_3 \bowtie (r_1 \bowtie r_2), r_3 \bowtie (r_2 \bowtie r_1), (r_1 \bowtie r_2) \bowtie r_3, (r_2 \bowtie r_1) \bowtie r_3$

- With n = 7, the number is 665,280
- With n = 10, the number is greater than 17.6 billion

No need to generate all the join orders

– Using dynamic programming. The least-cost join order for any subset of $\{r_1, r_2, ..., r_n\}$ is computed only once and stored for future use

动态规划优化



To find the best join tree for a set S of n relations

- Consider all possible plans of the form: $S_1 \bowtie (S S_1)$ where S_1 is any non-empty subset of S
- When the plan for any subset is computed, store it and reuse it when it is required again, instead of re-computing it
- Recursively compute costs for joining subsets of S to find the cost of each plan. Choose the cheapest.

> 连接顺序优化算法

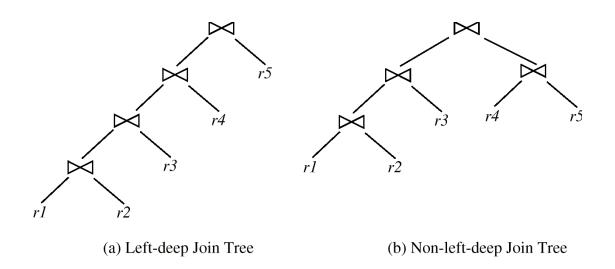


```
procedure findbestplan(S)
                                          Dynamic-programming algorithm
   if (bestplan[S].cost \neq \infty)
     return bestplan[S]
   if (S contains only 1 relation)
     set bestplan[S].plan and bestplan[S].cost based on best way of accessing S
   else for each non-empty subset S1 of S such that S1 \neq S
     P1= findbestplan(S1)
     P2= findbestplan(S - S1)
     A = best algorithm for joining results of P1 and P2
     cost = P1.cost + P2.cost + cost of A
     if cost < bestplan[S].cost
           bestplan[S].cost = cost
           bestplan[S].plan = "execute P1.plan;
            execute P2.plan;
            join results of P1 and P2 using A"
   return bestplan[S]
```

> 左深连接树



 In left-deep join trees, the right-hand-side input for each join is a relation, not the result of an intermediate join



Cost of Optimization



Complexity of dynamic programming

- The time complexity is $O(3^n)$. With n = 10, this number is 59000 instead of 17.6 billion
- Space complexity is $O(2^n)$

Complexity for finding the best left-deep join tree

- Consider n alternatives with one relation as right-hand side input and the other relations as left-hand side input.
- Using (recursively computed and stored) least-cost join order for each alternative on left-handside, choose the cheapest of the n alternatives.
- If only left-deep trees are considered, time complexity of finding best join order is $O(n2^n)$
- Space complexity remains at $O(2^n)$
- Cost-based optimization is expensive, but worthwhile for queries on large datasets (typical queries have small n, generally < 10)

▶ 启发式优化 (Heuristic Optimization)



- Cost-based optimization is expensive, even with dynamic programming
- DBMS may use heuristics to reduce the number of choices that must be made in a cost-based fashion
- Heuristic optimization transforms the query-tree by using a set of rules that typically (but not in all cases) improve execution performance:
 - Perform selection early (reduce the number of tuples)
 - Perform projection early (reduce the number of attributes)
 - Perform most restrictive selection and join operations before other similar operations
 - Some systems use only heuristics, others combine heuristics with partial cost-based optimization

> 启发式优化的主要步骤



- Deconstruct conjunctive selections into a sequence of single selection operations (Equiv. rule 1.)
- Move selection operations down the query tree for the earliest possible execution (Equiv. rules 2, 7a, 7b, 11)
- Execute first those selection and join operations that will produce the smallest relations (Equiv. rule 6)
- Replace Cartesian product operations that are followed by a selection condition by join operations (Equiv. rule 4a)
- Deconstruct and move as far down the tree as possible the lists of projection attributes, creating new projections where needed (Equiv. rules 3, 8a, 8b, 12)
- Identify those subtrees whose operations can be pipelined, and execute them using pipelining

▶ 作业



- 16.5 (第7版)
 - Canvas上提交,单个PDF文件
 - Deadline: xxx
 - Consider the relations $r_1(A, B, C)$, $r_2(C, D, E)$, and $r_3(E, F)$, with primary keys A, C, and E, respectively. Assume that r_1 has 1000 tuples, r_2 has 1500 tuples, and r_3 has 750 tuples. Estimate the size of $r_1 \bowtie r_2 \bowtie r_3$, and give an efficient strategy for computing the join.