

第一章前

1. A 位移和路程 B 位移的大小和路程.

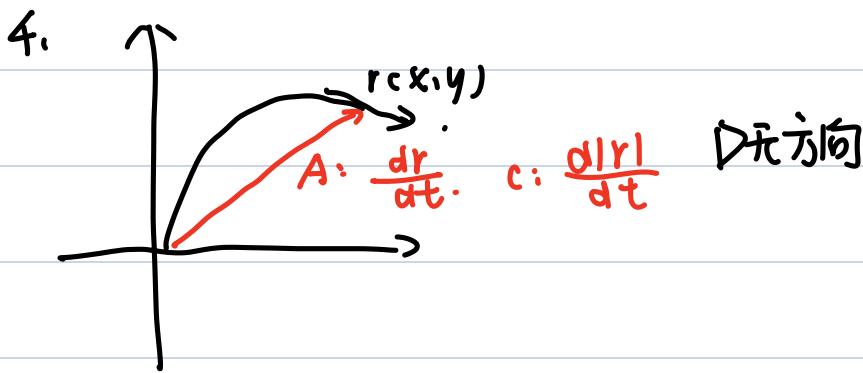
2. A: $\Delta V = 2V$.

$$3. \int_{x_0}^x dx = \int_0^3 v dt$$

$$x - 10 = \int_0^3 4t + 2 dt$$

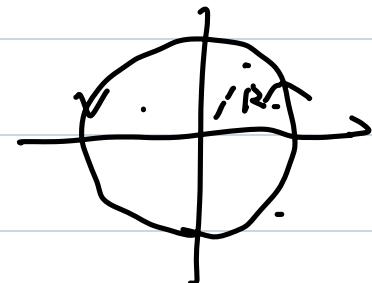
$$x = \cdot 2t^2 + 2t \Big|_0^3 + 10$$

$$x = 18 + 6 + 10 = 34 \text{ m.}$$



$$5. r = R \cos \omega t i + R \sin \omega t j.$$

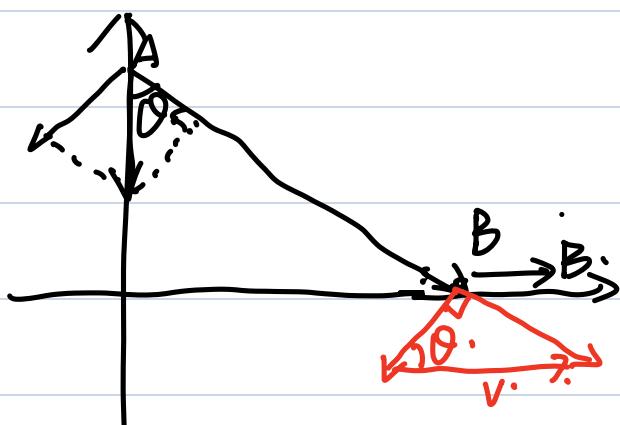
$$\vec{r}' = \vec{v} = -R \omega \sin \omega t \vec{i} + R \omega \cos \omega t \vec{j}.$$



$$\text{平均速度} = \frac{\vec{r}}{t} = \frac{2\pi R}{\pi w} \cdot \frac{2\pi w}{\pi} \vec{r}.$$

$$\text{速率} = \frac{|\vec{r}|}{t} = \frac{2\pi R}{2\pi w} = R w. (\text{速率只有大小}).$$

6



$$v \cdot \vec{i} = v \sin \theta.$$

$$v_A \cdot \cos \theta = v \sin \theta$$

$$v_A = v \cdot \tan \theta.$$

$$11. \quad r = (3t - 4t^2) \vec{i} + (-6t^2 + t^3) \vec{j}.$$

$$v = (3 - 8t) \vec{i} + (-12t + 3t^2) \vec{j}.$$

① 3代入 $x_1 = -2\vec{i} + (-2\vec{j})$

② 3代入 路程 / [时间] $x_2 = -9\vec{i} - 9\vec{j}$

③ 3代入 $v = -2\vec{i} - 9\vec{j}$.

$$12. \quad r = 3t \vec{i} + (19 - 2t^2) \vec{j}.$$

$$v = 3\vec{i} + (-4t) \vec{j}.$$

将 1S 5S 代入 v

$$r_1 = 3\vec{i} + 17\vec{j}$$

$$r_2 = 6\vec{i} + 11\vec{j}$$

$$\Delta r = 3\vec{i} - 6\vec{j}$$

$$|\Delta r| = \sqrt{9+36} = 3\sqrt{5}. \quad v = 3\sqrt{5} \text{ m/s.}$$

将 2S 代入:

$$v = 3\vec{i} + -8\vec{j}$$

$$|v| = \sqrt{9+64} = \sqrt{73} \text{ m/s.}$$

$$13. \quad a = 1 + 12x^2.$$

$$v = \frac{dx}{dt}$$

$$V = \frac{dx}{dt} \cdot \frac{dv}{dx}$$

$$V = \alpha \frac{dv}{dx}.$$

$$V \cdot dv = \alpha dx$$

$$\int_0^V V \cdot dv = \int_0^1 \alpha \cdot dx$$

$$\frac{1}{2}V^2 = \int_0^1 (1 + 12x^2) dx$$

$$\frac{1}{2}V^2 = x + 4x^3 \Big|_0^1$$

$$V = \sqrt{10} \text{ m/s}.$$

$$14. \quad r = \left(t - \frac{t^2}{2} \right) \vec{i} + \left(5 - 3t + \frac{t^3}{3} \right) \vec{j}.$$

$$V = (1-t) \vec{i} + (-3+t^2) \vec{j}$$

$$a = (-1) \vec{i} + (2t) \vec{j}.$$

$$a = -\vec{i} + 4t \vec{j}.$$

第二章前

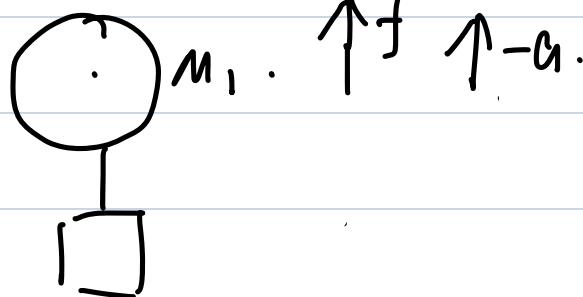
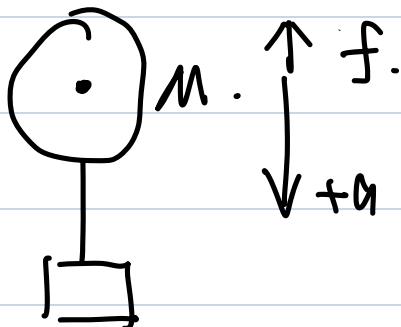
2.A.

3.A,B 同理,

C 杆速度一直增大 支持力一直增大

D 改变.

4.



$$\begin{cases} Mg - f = Ma \\ m'g - f = -m'a \end{cases}$$

$$f = Mg - Ma$$

$$-f = -m'(a+g)$$

$$f = m'(a+g)$$

$$\frac{Mg - Ma}{a+g} = m'$$

$$\Delta m = M - m' \\ = M - \frac{M(a+g)}{a+g}$$

$$\Delta m \cdot = \frac{2Ma}{a+g}$$

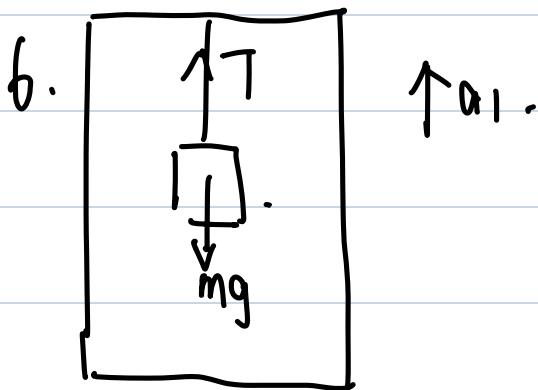
5 $F_A = Ma = Mg - N_1$

$$-Ma = Mg - N_3$$

$$N_1 = Mg - Ma \quad N_2 = Mg$$

$$N_3 = Mg + Ma$$

$$N_3 > N_2 > N_1 .$$

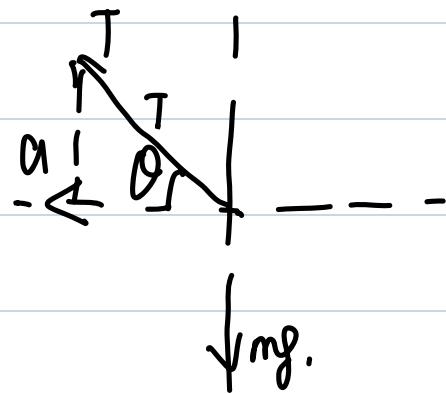


$$\begin{cases} \frac{1}{2}T - mg = ma_1 \\ T - mg = m_1 a'_2 \end{cases} \quad T = 2ma_1 + 2mg. \quad a'_2 = 2a_1 + g.$$

7. $MFN = f = mg$

$$FN = w^2 \cdot M \cdot R = \frac{mg}{R}$$

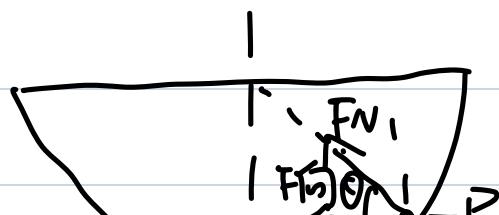
$$w = \sqrt{g/R}$$



$$\begin{cases} T \sin \theta = mg \\ T \cos \theta = ma \end{cases} \quad T = \frac{mg}{\sin \theta} \quad \frac{mg \cos \theta}{\sin \theta} = ma \quad a = g \cot \theta$$

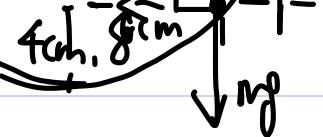
$\theta = u$

14



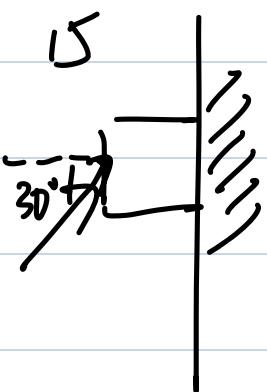
$$R = 10 \text{ cm} \quad \cos \theta = \frac{4}{5} \quad \sin \theta = \frac{3}{5}$$

$$\int FN \sin \theta = mg$$



$$F_{\text{fr}} = W \cdot M \cdot R = F \cdot L \cos \theta$$

$$\begin{aligned} W^2 \cdot M \cdot 0.08 &= \frac{mg \cos \theta}{\sin \theta} \\ W &= \sqrt{10 \times \frac{4}{3} \times \frac{1}{0.08}} \\ &= \sqrt{\frac{1000 \times 4}{3 \times 8 / 2}} \\ &= \sqrt{\frac{500}{3}} \\ &= \dots \end{aligned}$$

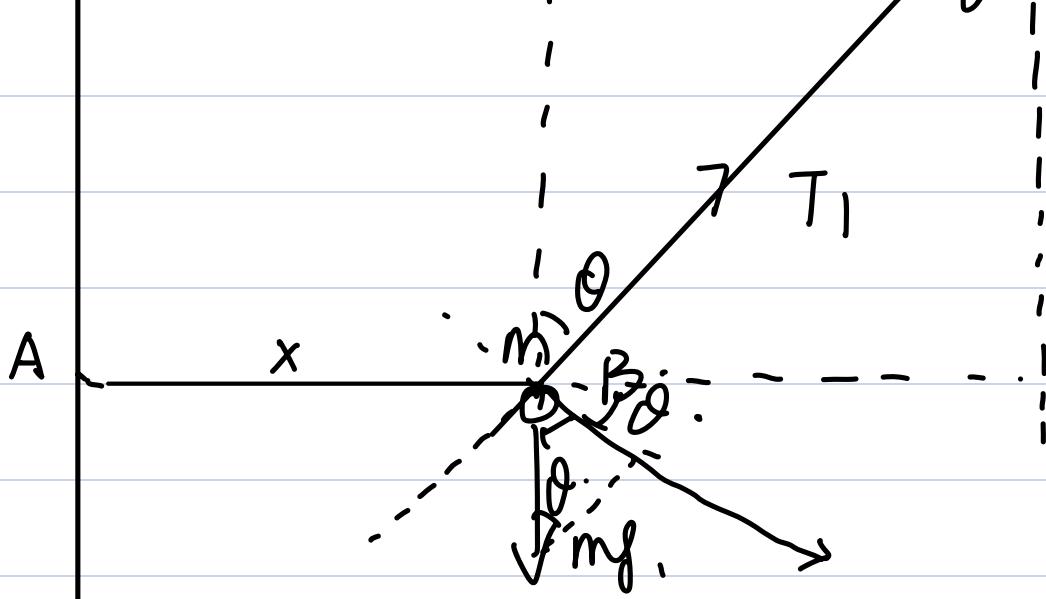


$$\begin{aligned} F \cdot \sin 30^\circ &= M F \cos 30^\circ \\ \frac{\sqrt{3}}{2} &= M \end{aligned}$$

16.

$$\begin{aligned} F &= k \Delta l \\ 2k \Delta l \cos 60^\circ &= mg \\ \Delta l &= \frac{mg}{F} \\ L_{\text{eff}} &= L + \frac{2mg}{F} \end{aligned}$$





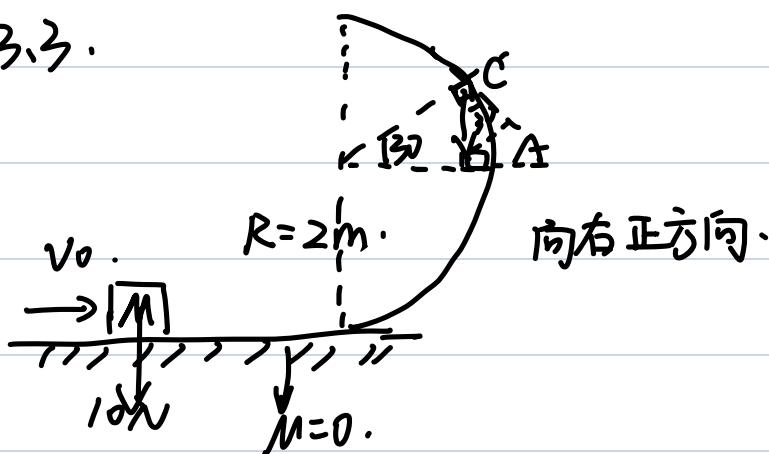
$$T_1 \cos \theta = mg \quad T_1 = \frac{mg}{\cos \theta}$$

$$T_2 = mg \cos \theta$$

$$T_1 : T_2 = \frac{mg}{\cos \theta} : mg \cos \theta = \frac{1}{\cos^2 \theta}$$

第三章前.

例 3.3.



$$mgR = \frac{1}{2}mv^2$$

$v_1 = \sqrt{2gR}$ v_2 是通过子弹 v_3 的高度.

$$\left\{ \begin{array}{l} -MV_1 + MV_0 = (M+m) \cdot V_2 \\ \frac{1}{2}(M+m) \cdot V_3^2 - \frac{1}{2}(M+m) \cdot V_2^2 = -(M+m) \cdot g h. \end{array} \right.$$

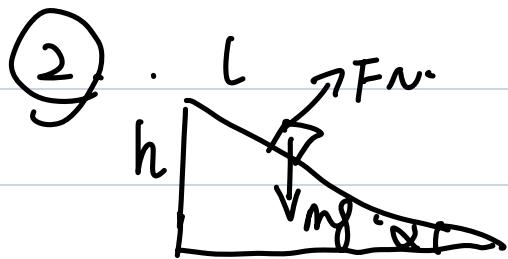
$$h = R + R \sin 2\alpha = \frac{3}{2}R$$

$$F[\vec{\omega}] = (M+m)gG \sin 2\alpha = (M+m) \cdot \frac{V_3^2}{R}$$

$$V_2 = \sqrt{\frac{7gR}{2}}$$

$$V_0 = \frac{M}{m} \sqrt{2gR} + \frac{M+m}{m} \sqrt{\frac{7gR}{2}} = 299,15 \text{ m/s.}$$

1. D.



$$\frac{1}{2}mv^2 = mgh.$$

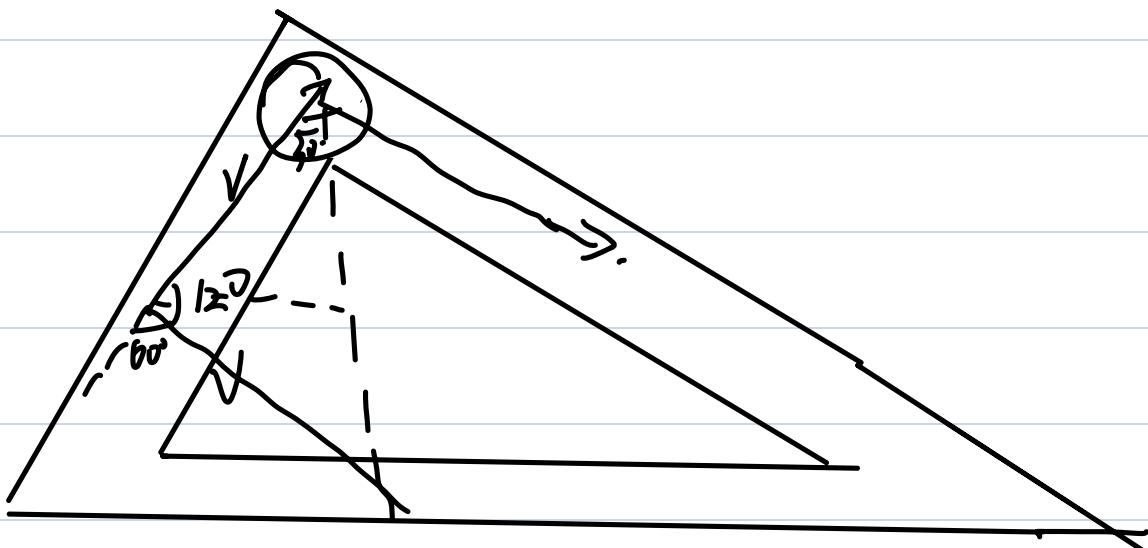
$$v = \sqrt{2gL \sin \alpha}$$

$$\frac{h}{L} = \sin \alpha$$

$$h = L \sin \alpha$$

$$I = M \cdot v = m \sqrt{2gL \sin \alpha}$$

3.



$$V' = V \cos 30^\circ \cdot 2 = \sqrt{3}V$$

4 A

b. ① 保守力做正功，势能减少。

②. ✓

③ · 摩擦力

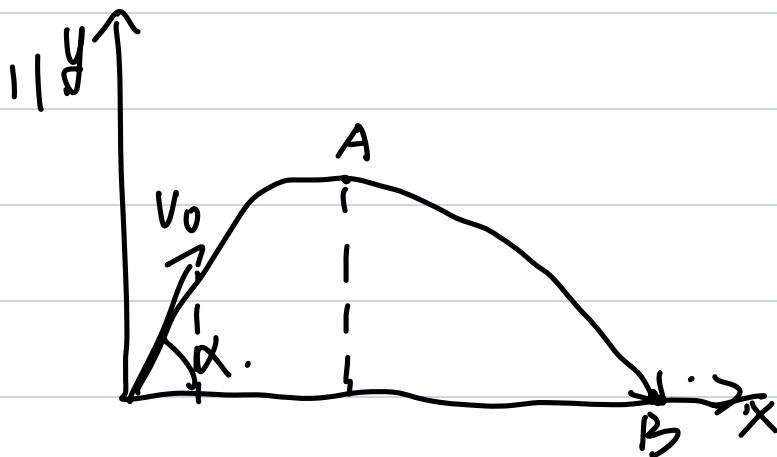
$$7. \vec{r} = A \cos \omega t \hat{i} + B \sin \omega t \hat{j} \quad t=0 \text{ or } \frac{\pi}{2\omega}$$

$$\frac{d\vec{r}}{dt} = \vec{v} = -A \omega \sin \omega t \hat{i} + B \omega \cos \omega t \hat{j}$$

$$V_{\text{末}} = B t \omega$$

$$V_{\text{末}} = -A \omega$$

$$\begin{aligned} W &= \frac{1}{2} m v_{\text{末}}^2 - \frac{1}{2} m v_0^2 \\ &= \frac{1}{2} m \omega^2 (A^2 - B^2). \end{aligned}$$



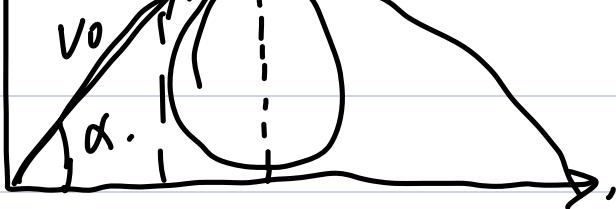
$$t = \frac{2 v_0 \sin \alpha}{g}$$

$$\begin{aligned} I &= F \cdot t \\ &= \frac{2 v_0 \sin \alpha}{g} m g \\ &= 2 m v_0 \sin \alpha. \end{aligned}$$

12.

$$V_x = v_0 \cos \alpha$$

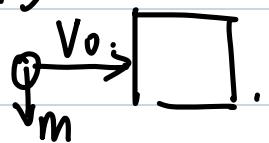
$$\frac{V^2}{R_m} = m g$$



$$\textcircled{1} \quad \frac{V^2}{g} = R \cdot = \frac{V_0^2 \cos^2 \alpha}{g}$$

③. - $mV_0 \sin \alpha$.

13. $M \cdot$



$$mV_0 = (M+m) \cdot V'$$

$$\frac{mV_0}{M+m} = V'$$

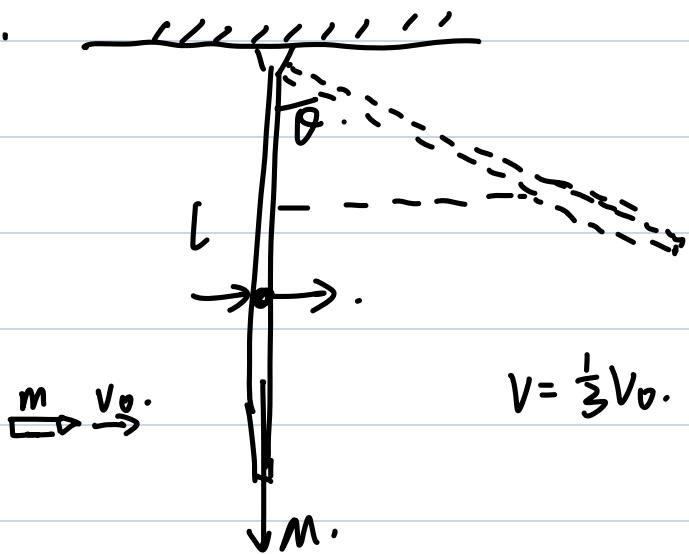
$$I = MV' = \frac{MV_0}{M+m}$$

14.

$$\begin{aligned} F \cdot t &= m \Delta V \\ F &= 375 \times 1 \times 50 \\ &= 18750 \text{ N} \end{aligned}$$

第四章前半

4.3.



$$\begin{aligned} L &= Jw = mv \\ &= mr^2 w \end{aligned}$$

$$V = \frac{1}{2} V_0$$

$$J = \frac{m r^2}{3}$$

$$mV_0 \frac{L}{2} = Jw + mV_0 \cdot \frac{L}{2} \cdot \frac{1}{3}$$

$$mV_0 \frac{L}{2} = \frac{ML^2}{3} w + \frac{L}{6} mV_0$$

$$\frac{1}{3} mV_0 = \frac{ML^2 w}{3}$$

$$\frac{mV_0}{ML^2} = w$$

$$\frac{1}{2} J w^2 = Mg \frac{L}{2} (1 - \cos \theta)$$

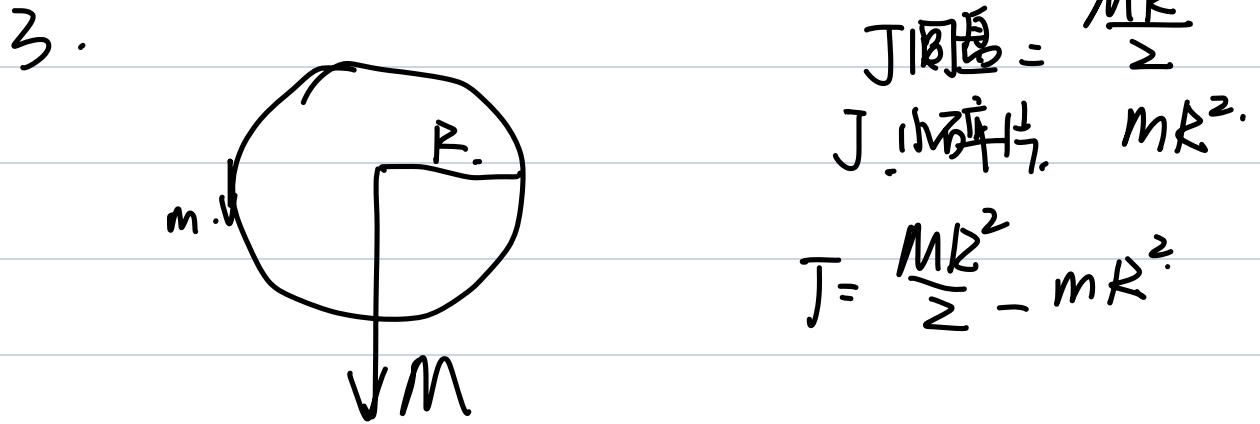
$$\cos \theta = 1 - \frac{m^2 V_0^2}{3M^2 g L}$$

$$1. P = F \cdot v \quad F = \frac{P}{v}$$

$$m \ddot{v} \cdot \frac{F}{m} = \frac{P}{m v t}$$

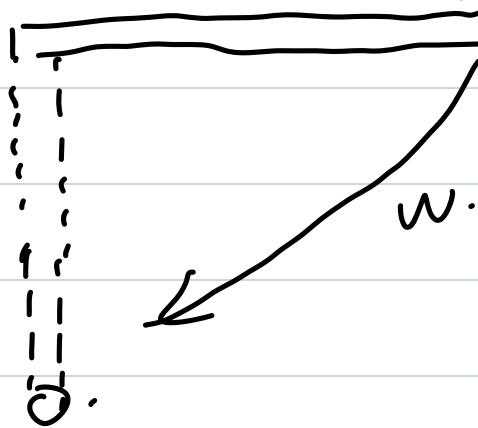
$$2. M = J \alpha.$$

$$= 3 \times 4 - 3 \times 5 = -3 \text{ kNm} \cdot$$



A.

4.



$$\vec{M} = |\vec{r}| \times |\vec{mg}| = (\vec{r}) \cdot \vec{mg} \cdot \sin\theta \\ = \frac{1}{2} mg \theta \sin\theta.$$

$$\alpha = \frac{\vec{M}}{I J T}, \quad \downarrow.$$

$$11. \quad \beta = 4at^3 - 3bt^2.$$

$$\int_{w_0}^u dw = \int_0^t 4at^3 - 3bt^2 dt$$

$$u - w_0 = \theta t^4 - b t^3.$$

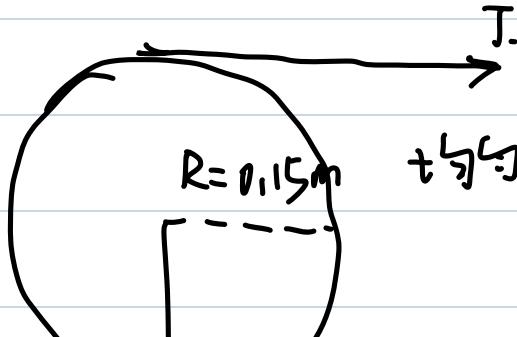
$$w = w_0 + at^4 - bt^3.$$

$$\int_0^\theta d\theta = \int_0^t w_0 + at^4 - bt^3 dt$$

$$\theta = w_0 t + \frac{a}{5} t^5 - \frac{b}{4} t^4$$

J 固定 = $\frac{mR^2}{2}$.

12.



t匀速地加速.

$$\alpha = 40\pi \text{ rad/s}.$$

$$\theta = \frac{1}{2}\alpha t^2 = \frac{1}{2} \times 40 \times \frac{1}{4} = 5\pi.$$

$$r = \frac{\theta}{2\pi} = 2.5 \text{ m}.$$

$$mg = 50 \text{ N}$$

$$F \times R = J \times \alpha$$

$$F \cdot R = \frac{MR^2}{J} \times \alpha$$

$$F = \frac{MR}{J} \alpha$$

$$= \frac{5}{2} \times \frac{3}{20} \times 40 = 15 \text{ N}$$

$$W = \frac{1}{2} J w^2 - 0$$

$$= \frac{1}{2} \times \frac{MR^2}{J} \cdot w^2 =$$

$$= \frac{1}{2} \times \frac{5}{2} \times \frac{9}{400} \cdot 40 \pi^2$$

$$= \frac{45}{4} \pi^2 \cdot J$$

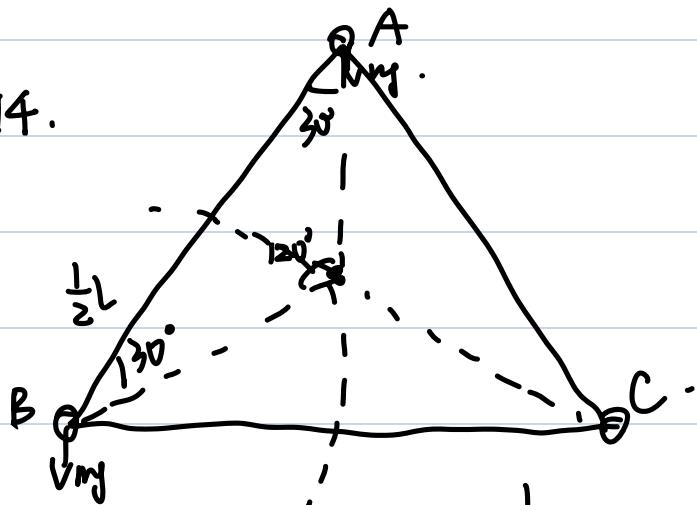
13.



$$\textcircled{1} \quad M = mg \times R = \frac{1}{2} mg \times L$$

$$\textcircled{2} \quad M = \frac{1}{3} mg \times \frac{1}{6} L = \frac{mgL}{18}$$

14.



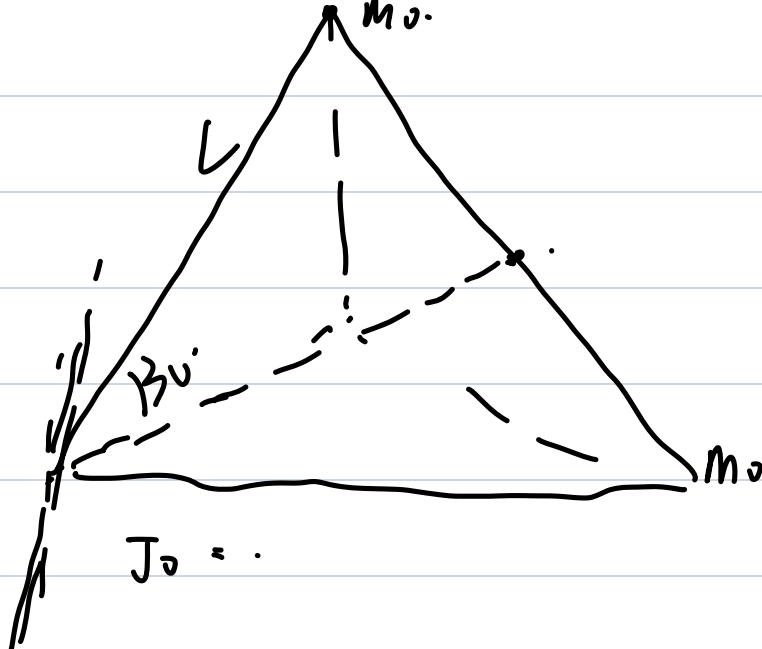
$$J = MR^2$$

$$\textcircled{1} \quad J_0 = 3 \times m \times \left(\frac{\frac{L}{2}}{\cos 30^\circ} \right)^2$$

$$= 3 \times m \times \left(\frac{L}{2} \times \frac{2}{\sqrt{3}} \right)^2$$

$$= 3m \times \frac{L^2}{3} = mL^2$$

(2)

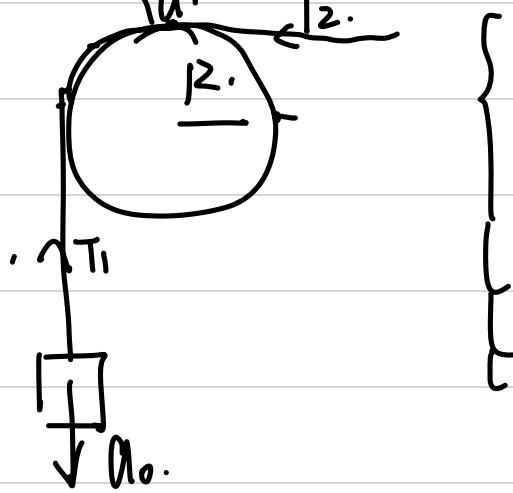


$$J_0 = 2 \times m \times l^2 = 2m l^2$$

~~त्रिभुजी तरिका~~

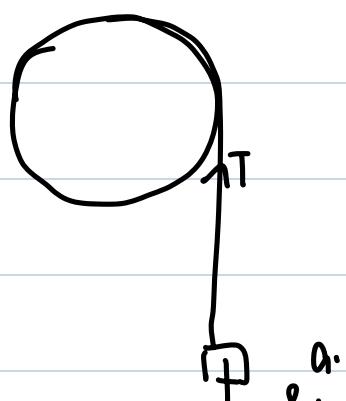
$$\frac{V^2}{R} \quad V^2 = 2gh.$$

15.



$$\left. \begin{array}{l} mg - T = ma_0. \\ TR = J\alpha. \end{array} \right\}$$

1b



$$\left. \begin{array}{l} (mg - T) = ma. \quad T = m(g - a) \\ J\alpha = T \times R. \\ \alpha = \frac{a}{R}. \end{array} \right\}$$

$$J = \frac{TR^2}{a} = \frac{m(g-a)R^2}{a}$$

↓ mg

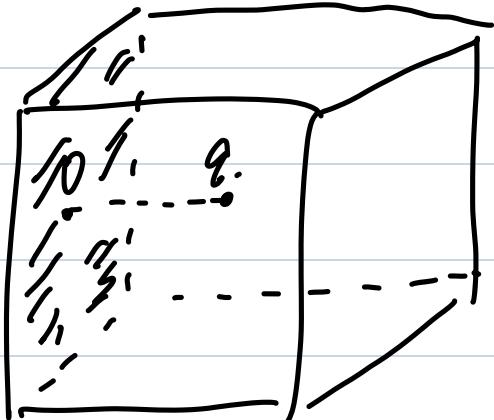
第五章前

1. A 质电

B. 方向

D: x.

2.

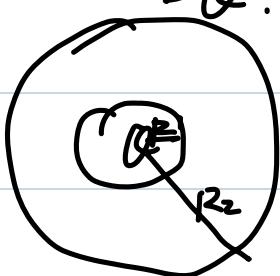


补充. $\rho = \frac{q}{\epsilon_0}$
 $\rho' = \frac{q}{6\epsilon_0}$

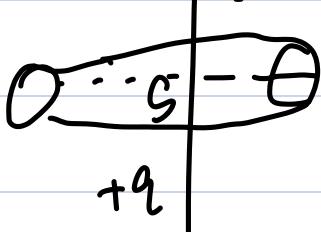
3. $\oint_s E \cdot dS \neq 0$ B.

$E_1 : 4\pi r^2 E_1 = \frac{Q}{\epsilon_0} \quad E_1 = \frac{Q}{\epsilon_0 4\pi r^2}$

4.



5 A



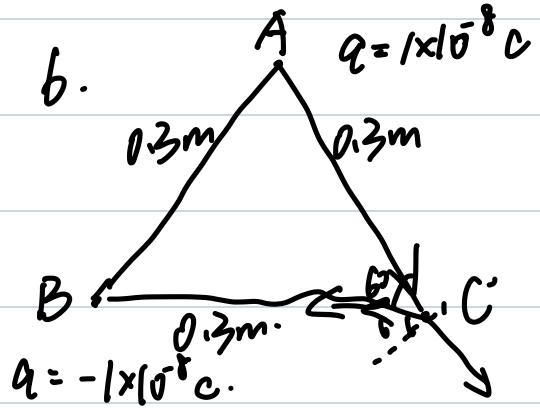
B.

设 $\sigma = \frac{Q}{S}$.

$2E \cdot Q = \frac{\sigma S}{\epsilon_0}$

$E = \frac{Q}{2\epsilon_0 S} = \frac{Q}{2S\epsilon_0}$.

$F = Eq = \frac{Q^2}{2S\epsilon_0}$



$$\textcircled{1} \quad E = \frac{kq}{r^2} = \frac{q}{4\pi\epsilon_0 r^2}$$

$$k = 9 \times 10^9$$

$$E_{xz} = E \times \cos 60^\circ \times 2 \\ = E = \frac{1 \times 10^{-8} \times 9 \times 10^9}{0.09} \\ = \frac{90}{9 \times 10^{-2}} = 1000 \text{ V/m.}$$

$$V = \frac{q}{kR}$$

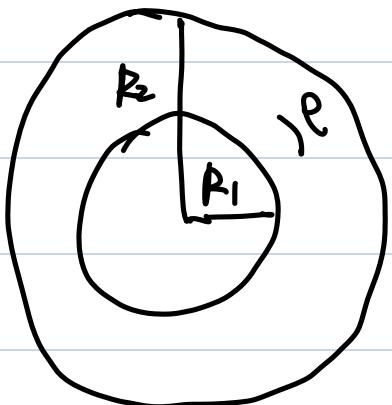
EP 5/10n

$$\textcircled{2} \quad V = \frac{kq}{R} - \frac{kq}{R} = 0 \text{ V}$$

$$11. \quad \phi = E \epsilon_0 \cdot \sin \theta$$

$$12. \quad \oint E \cdot dS = \frac{q_2}{\epsilon_0}$$

13



$$q, q_2 \cdot$$

$$\angle = 0^\circ$$

$$\textcircled{2} \quad V = \frac{4}{3}\pi r^3 - \frac{4}{3}\pi R_1^3$$

$$4\pi r^2 \cdot E_1 = \frac{4}{3}\pi(r^3 - R_1^3)P$$

$$E_1 = \frac{4\pi r(r^3 - R_1^3)}{3\epsilon_0 r^2}$$

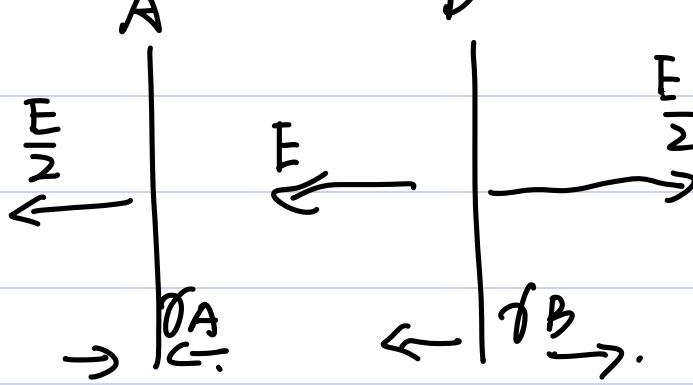
$$= \frac{3q_2 + 4\pi r^2}{3\epsilon_0 r^2} \frac{P}{R(r^3 - R_1^3)}$$

$$\textcircled{3} \quad V = \frac{4}{3}\pi(R_2^3 - R_1^3)$$

$$4\pi r^2 \cdot E_2 = \frac{4\pi(R_2^3 - R_1^3)P}{3\epsilon_0}$$

$$E_2 = \frac{(R_2^3 - R_1^3)P}{3r^2\epsilon_0}$$

14



$A E_1 \quad B E_2 \quad A$ 向右 B 向左

$$2E \cdot g = \frac{\sigma}{\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0}$$

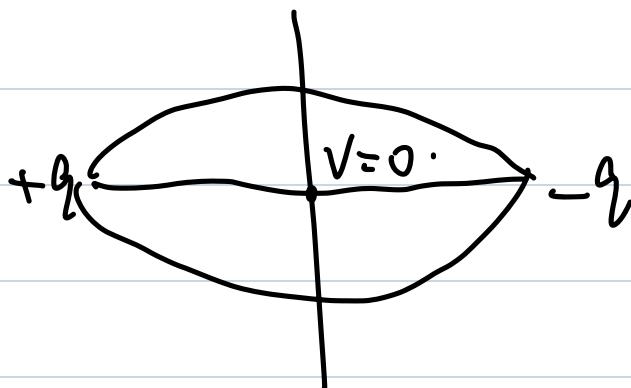
A左侧 右正向

$$\begin{cases} -\frac{E}{2} = \frac{\sigma_A}{2\epsilon_0} - \frac{\sigma_B}{2\epsilon_0} \\ -E = -\frac{\sigma_A}{2\epsilon_0} - \frac{\sigma_B}{2\epsilon_0} \end{cases}$$

$$-\frac{3E}{2} = -\frac{\sigma_B}{\epsilon_0} \quad \sigma_B = \frac{3E\epsilon_0}{2}$$

$$\sigma_A = -\frac{E\epsilon_0}{2}$$

15



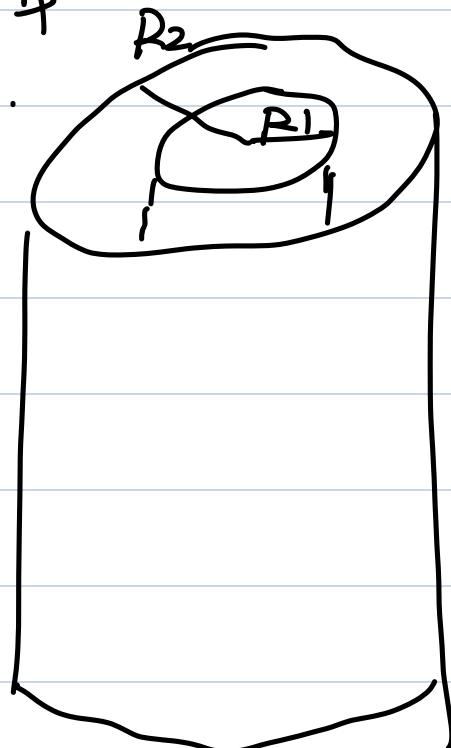
16



$$\begin{aligned} dq &= \lambda dl = \lambda R d\theta \cdot \\ \int_0^E dE &= 4 \int_0^{\frac{\pi}{2}} \frac{\lambda R \cos\theta}{4\pi q_0 R^2} d\theta \\ &= \frac{\lambda q_0 \sin \frac{\pi}{2}}{\pi q_0 R} \end{aligned}$$

$$V=0^\circ$$

第六章
6.2.



$$R_1 = 2.0 \text{ cm}$$

$$R_2 = 2.3 \text{ cm}$$

设单位线密度 λ .

$$E \cdot 2\pi r l = \frac{\lambda l}{\epsilon_0}$$

$$E = \frac{\lambda m}{2\pi \epsilon_0 r l}$$

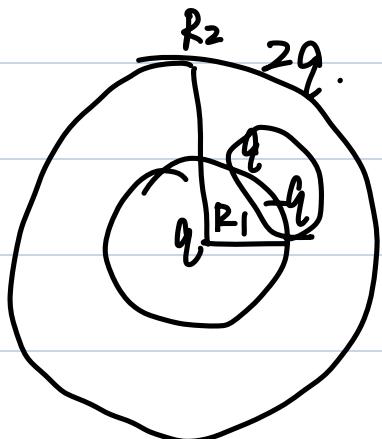
$$E = \frac{\lambda m}{2\pi \epsilon_0 R_1} \leq E_b$$

$$\lambda_{max} \leq 2\pi \epsilon_0 R_1 E_b$$

$$Um = \int_{R_1}^{R_2} E dr = \int_{R_1}^{R_2} \frac{\lambda}{2\pi \epsilon_0 r} dr = \frac{\lambda m}{2\pi \epsilon_0} \left| \ln \frac{R_2}{R_1} \right| = R_1 E_b \cdot \left| \ln \frac{R_2}{R_1} \right|$$

$$\approx 42 \text{ kV}$$

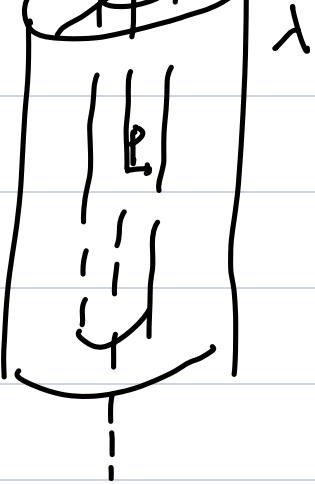
4.



$$V = \frac{Q}{4\pi \epsilon_0 R} \\ = \frac{2q}{4\pi \epsilon_0 R_2} \\ = \frac{q}{2\pi \epsilon_0 R_2}$$

5 b

$$E \cdot 2\pi r l = \frac{\lambda l}{\epsilon_0}$$



$$E = \frac{\lambda}{2\pi r \epsilon_0}$$

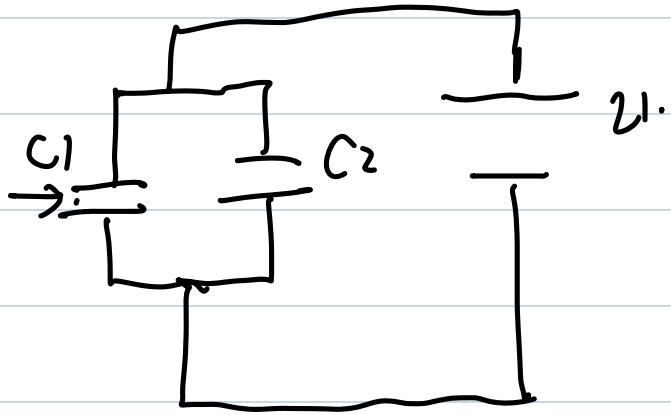
$$\int_a^b du = \int_a^b E dr.$$

$$u = \frac{\lambda}{2\pi \epsilon_0} \ln \frac{b}{a}.$$

b. $C = \frac{\epsilon_0}{4\pi \epsilon_0 d}$

C.

8.



21.

$$C_{\text{总}} = C_1 + C_2.$$

$$C = \frac{\epsilon_0}{4\pi \epsilon_0 d}.$$

$$C_2 = \frac{Q}{U} \text{ 不变.}$$

$$C_1 = \frac{Q_1}{U}.$$

9. $V = \frac{Q}{kR^2}.$

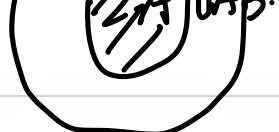
球形电容器仅与自身半径有关

$$C = \frac{Q}{U} = 4\pi \epsilon_0 R.$$

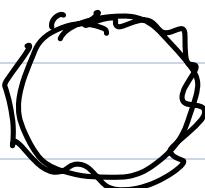
B

9 B.

$$C = \frac{Q}{U} = \frac{Q}{UA/2}.$$

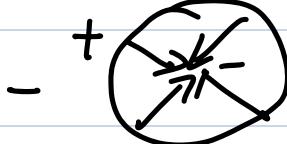


10

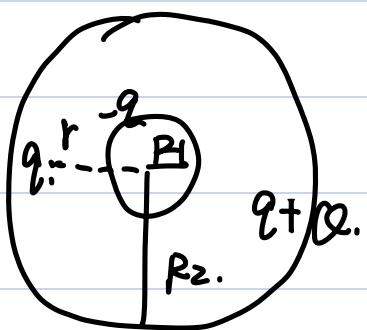


$$V_1=0 \quad V_2<0.$$

11. 不变, ; 变化

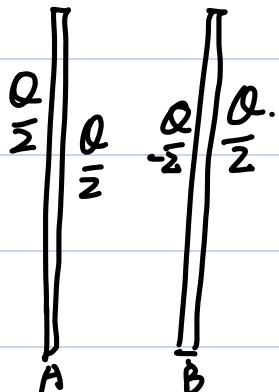


12



$$V = \frac{Q}{R} = \left(\frac{q}{r} - \frac{q}{R_1} + \frac{q+Q}{R_2} \right)$$

13



$$\sigma_{A\text{左}} = \frac{Q}{2d}$$

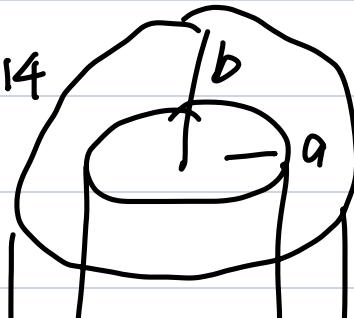
$$\sigma_{A\text{右}} = \frac{Q}{2d}$$

$$\sigma_{B\text{左}} = -\frac{Q}{2d}$$

$$\sigma_{B\text{右}} = \frac{Q}{2d}$$

电荷感应。

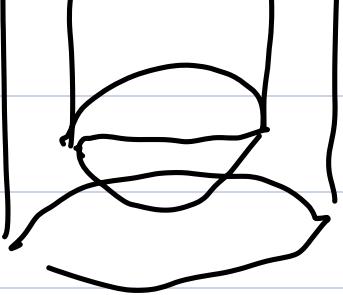
14



$$E \cdot 2\pi r b = \frac{\lambda b}{2\pi r}$$

$$E = \frac{\lambda}{2\pi r \epsilon_0}$$

$$\int_0^b du = \int_a^b E dr$$

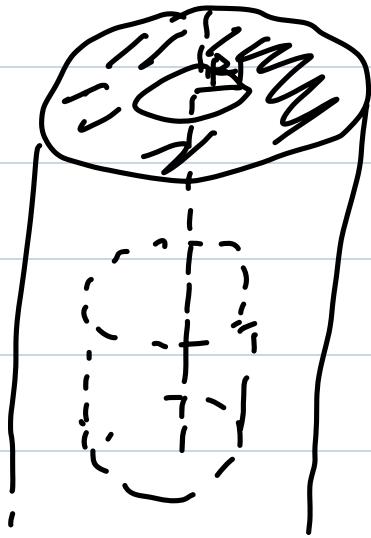


$$V = \frac{\lambda}{2\pi\epsilon_0} \ln \frac{b}{a}$$

$$\frac{V 2\pi\epsilon_0}{\ln b - \ln a} = \lambda$$

$$E = \frac{2\pi\epsilon_0 V}{(\ln b - \ln a) \cdot 2\pi r \epsilon_0} = \frac{V}{r c (\ln b - \ln a)}$$

15



$$E \cdot 2\pi r \Delta \phi = \frac{\lambda \cdot \Delta \phi}{\epsilon_0}$$

$$E = \frac{\lambda}{2\pi r \epsilon_0}$$

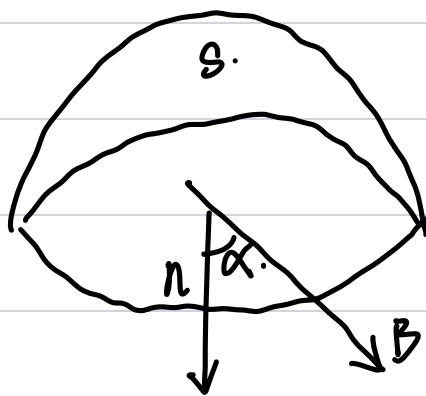
$$E_{\text{ext}} = \frac{E}{2r} = \frac{\lambda}{2\pi r \epsilon_0 \epsilon_r}$$

16. 不变.

第八章前

1.

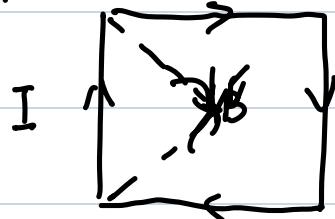
D



$$\varphi = -\pi r^2 B \cos \alpha .$$

$$= 1.47 \times 10^{-6}$$

2.



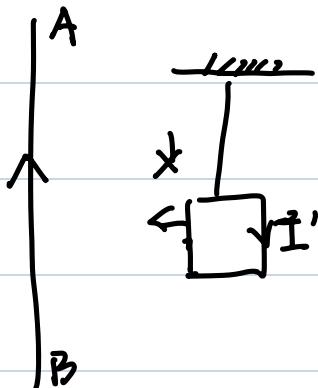
$$\frac{1}{4} \pi R B_1 = \frac{\mu_0 I}{4 \pi R} (\cos \theta_1 - \cos \theta_2) = \frac{\sqrt{2} \mu_0 I}{4 \pi L}$$

$$B_{1,2} = 4 \times \frac{\sqrt{2} \mu_0 I}{2 \pi L} = \frac{2\sqrt{2} \mu_0 I}{\pi L}$$

$$B_2 = 0$$

3

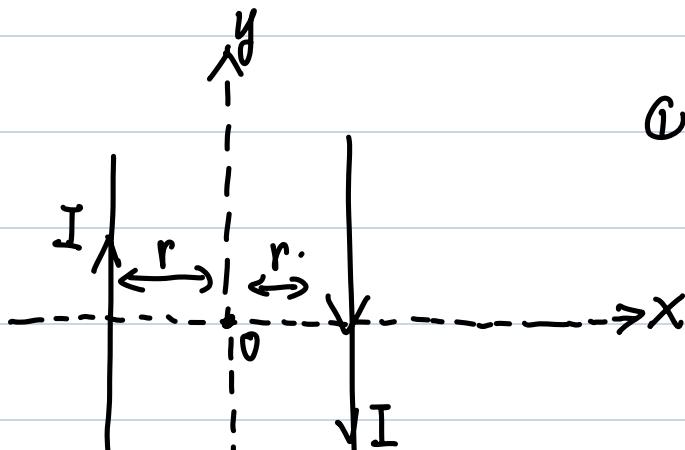
A

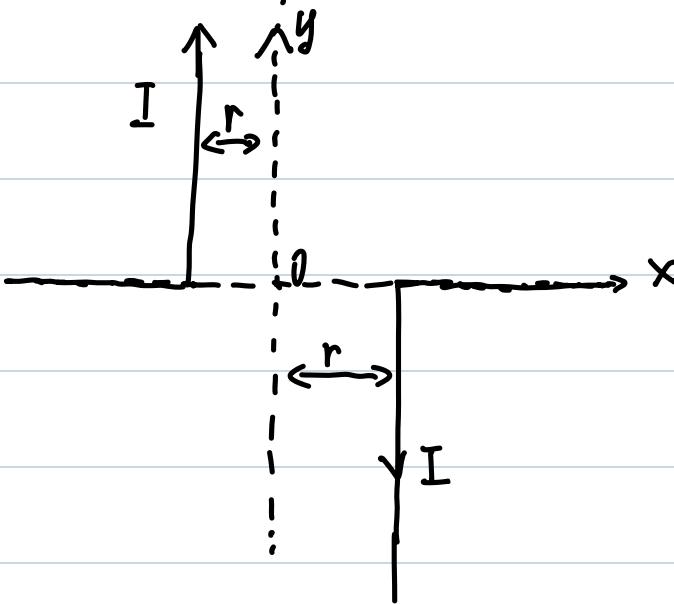


4

$$\textcircled{1} B \text{ at point } A = \frac{\mu_0 I}{2 \pi r}$$

$$B_0 = \frac{\mu_0 I}{\pi r}$$

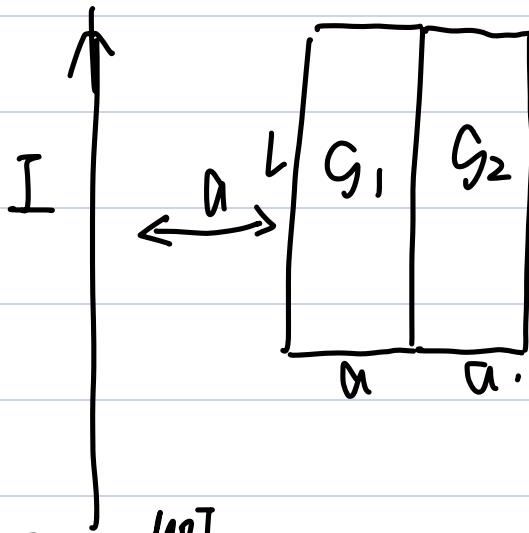




$$B_{\text{半环路}} = \frac{\mu_0 I}{4\pi r}$$

$$B' = \frac{\mu_0 I}{2\pi r} = \frac{B_0}{2}$$

14



$$B_0 = \frac{\mu_0 I}{2\pi r}$$

$$\varphi_1 = \int_0^{20} \frac{\mu_0 I}{2\pi r} L dr = \frac{\mu_0 I L}{2\pi a}$$

$$\varphi_2 = \int_{20}^{30} \frac{\mu_0 I}{2\pi r} L dr = \frac{\mu_0 I L}{2\pi a}$$

$$\varphi_1 : \varphi_2 = \frac{\ln 2a - \ln a}{\ln 3a - \ln 2a} = \ln 2 : \ln \frac{3}{2}$$

17 a: $\mu_0 I$.

b: $\mu_0 I$

c: $> \mu_0 I$.

$$22. B = \frac{\mu_0 I}{2\pi r}$$

$$\rho = BS = \int_{d_1}^{d_1+d_2} Bl \ dr.$$

$$= \int_{d_1}^{d_1+d_2} \frac{\mu_0 I V}{2\pi} r dr$$

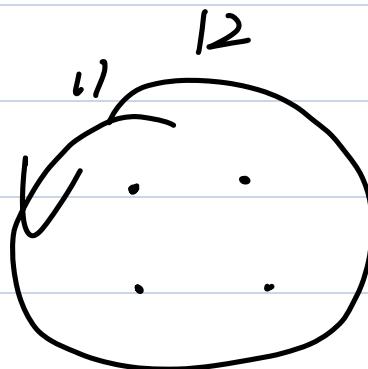
$$= \frac{\mu_0 I L}{2\pi} \ln \frac{d_1+d_2}{d_1}$$

第九章 前

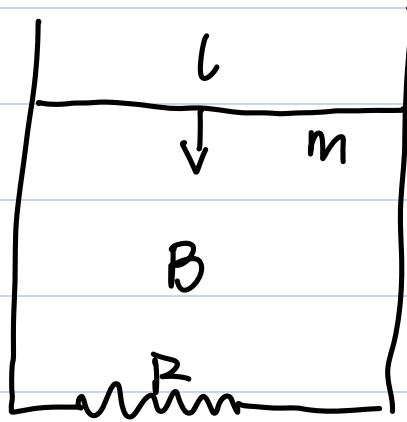
1.

$$E = -\frac{n BS}{dt} = 12 \times 0.05 = 0.6$$

$$I = \frac{D.b}{4} = 0.15 A$$



2.



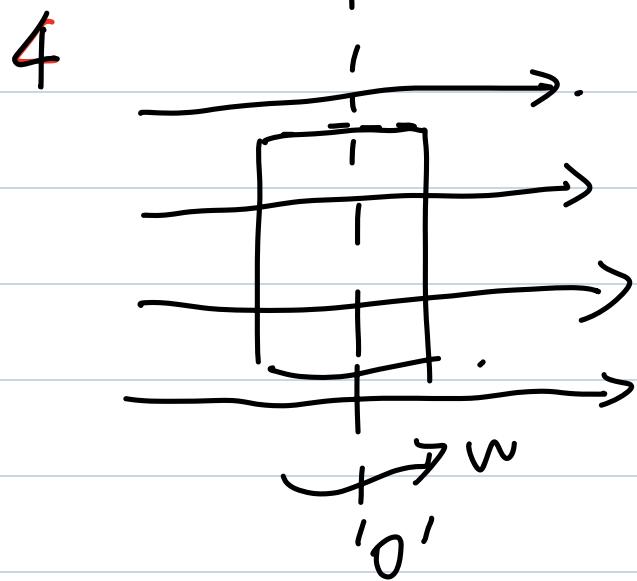
$$E = BlV$$

$$F = \frac{BlV}{R} = mf.$$

$$V = \frac{mqr}{B^2 l^2}$$



以速度 v 进入代表恒定有外力放工恒速.



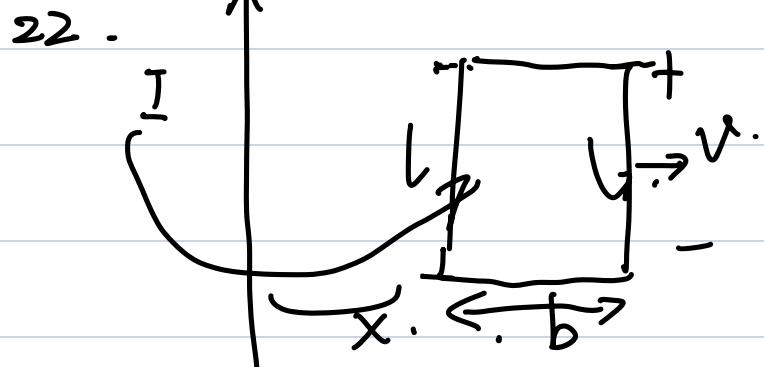
$$A: v$$

$$B: \frac{sw}{R/r}$$

$$C: x$$

$$D: x$$

$$I = \frac{nBSw}{R}.$$



$$B = \frac{M_0 I}{2\pi r}, \quad B_1 = \frac{M_0 I}{2\pi x}, \quad B_2 = \frac{M_0 I}{2\pi r(x+b)}$$

$$\begin{aligned}\phi &= \int_x^{x+b} B l \, dr \\ &= \int_x^{x+b} \frac{M_0 I l}{2\pi r} \, dr = \frac{M_0 I l}{2\pi} \ln \frac{x+b}{x}.\end{aligned}$$

$$\psi = MI$$

$$\frac{M_0 I l}{2\pi} \ln \frac{x+b}{x} = \frac{M_0 I l}{2\pi}$$

$$\frac{x+b}{x} = e$$

$$x+b = xe$$

$$xe - e = -b$$

$$x = \frac{b}{e-1}.$$

$$\begin{aligned}E &= (B_2 - B_1) \cdot l \\ &= \frac{M_0^2 l b (e-1)^2}{2\pi e b}.\end{aligned}$$

第十四章

$$\Delta = n_2 r_2 - n_1 r_1, \text{ 光程差}$$

$$\Delta \psi = 2\pi \frac{\Delta}{\lambda}$$

$$\Delta = \pm \begin{cases} k\lambda & \text{加强} \\ (2k+1)\frac{\lambda}{2} & \text{减弱} \end{cases}$$

杨氏双缝

双峰

$$ds \sin \theta = \pm \begin{cases} k\lambda & \text{明} \\ (2k+1) \cdot \frac{\lambda}{2} & \text{暗} \end{cases}$$

$$\sin \theta \approx \tan \theta = \frac{x}{d'}$$

屏到双缝

$$x = \pm \begin{cases} k \cdot \frac{d'}{a} & \text{明} \\ (k + \frac{1}{2}) \cdot \frac{d'}{a} & \text{暗} \end{cases}$$

薄膜干涉

$$d = 2nd + \frac{\lambda}{2} (\text{或 } \pi) = \begin{cases} k\lambda & \text{明} \\ (2k+1) \cdot \frac{\lambda}{2} & \text{暗} \end{cases}$$

劈尖干涉

$$dk+1 - dk = \frac{\lambda}{2n} = \frac{\lambda}{2}$$

$$\theta \approx \frac{\lambda n}{2b} = \frac{D}{L}$$

牛顿环

$$R_k = \sqrt{(k - \frac{1}{2}) R \lambda n} \quad \theta \parallel$$

$$\sqrt{KR\lambda n}$$

睛.

$$R = \frac{D_{k+m} - D_k}{4m \lambda}$$

单缝衍射.

以单缝，透镜焦距f，衍射角θ.

$$b \sin \theta = \begin{cases} 0 & \text{中央明纹} \\ 2k, \frac{\lambda}{2} = k\lambda & \text{暗纹} \\ (2k+1) \cdot \frac{\lambda}{2} & \text{明纹} \end{cases}$$

(2) 产生明暗衍射的条件是 $\lambda = b$ 或 $\lambda > b$.

(3). 相邻暗条纹之间距离为明纹宽度

中央 $l_0 = \frac{2f\lambda}{b}$

其余 $l = \frac{f\lambda}{b}$

图示(衍射)

$$Q_0 = 1.22 \frac{\lambda}{D} \rightarrow \text{入射半径}$$

$$Q_0 = \frac{q}{l}$$

光栅衍射

光栅透光缝宽为b 不透光为b'

光栅密数L+b 衍射角θ

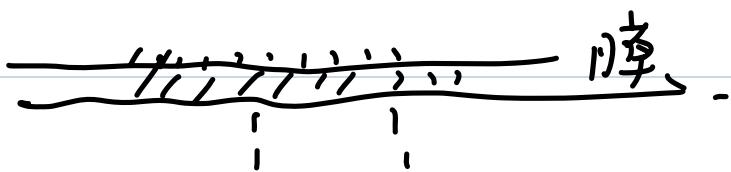
$$(b+b') \sin \theta = \pm k \lambda \text{ 主极大.}$$

说明

$$\textcircled{1} \quad k_{\max} < \frac{b+b'}{\lambda}.$$

$$\textcircled{2} \quad \frac{b+b'}{b} = \frac{k}{k'} \quad k' = 1, 2, 3 \dots$$

例 14.2.



$$\begin{cases} 2n d + \frac{\lambda_1}{2} = k \lambda_1 \\ 2n d + \frac{\lambda_2}{2} = (2k+1) \lambda_2. \end{cases}$$

$$k = \frac{\lambda_1}{2(\lambda_1 - \lambda_2)} = 3.$$

$$\text{且 } d = 5.92 \times 10^{-7} \text{ m} = 5.92 \text{ nm.}$$

$$1. \quad D = 3T_1 = 2T_1 \frac{\lambda}{\Delta} \\ \Delta = \frac{3}{2} \lambda.$$

$$N \chi = \Delta \\ \chi = \frac{3\lambda}{2n}$$

$$2. \quad \Delta t = r_2 + (n_2 - 1)t_2 - [r_1 + (n_1 - 1)t_1].$$

$$3. x = k \cdot \frac{D}{d} \cdot \lambda \xrightarrow{\text{单缝衍射}} \text{双缝距.}$$

$$n = \frac{c}{v} = \frac{\lambda f}{\lambda' f} = \frac{\lambda}{\lambda'} \quad \lambda' = \frac{\lambda}{n}.$$

$$x = k \cdot \frac{D}{d} \cdot \frac{\lambda}{n} =$$

$$\Delta x = \frac{D \lambda}{d n} = \frac{d' \lambda}{d n}.$$

$$4. \Delta x = (n-1) \cdot d = 5 \lambda$$

$$d = 6 \times 10^{-4} \text{ cm.}$$

$$13. \text{ 衍射强度 } I_0 = \frac{2f\lambda}{D} \uparrow \quad I_0 \downarrow.$$

$$D \sin \theta = (2k+1) \cdot \frac{\lambda}{2} \quad \text{干涉.}$$

$$14. I = \frac{2f\lambda}{D}$$

$$= \frac{\frac{3}{4}2f}{\frac{3}{2}}$$

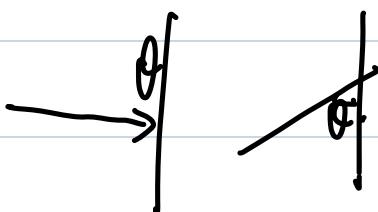
$$= \frac{3}{4} \times \frac{2}{3} = \frac{1}{2}$$

$$\lambda = \frac{D f}{2}$$

$$= \frac{1}{2} f$$

$$=$$

$$15. (b+b') \sin \theta = \frac{1}{2} \lambda \quad B \text{ 变大}$$



$$16. (b+b') \sin \theta = k \lambda.$$

$$b+b' = \frac{1}{E_{0.7}} = 2 \times 10^{-6} \text{ m.}$$

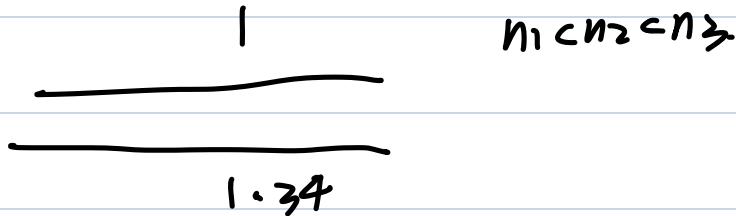
牛顿环

$$Q = \arcsin \frac{ka}{b+d} \quad |k=1|$$

$$= \arcsin \frac{5893 \times 10^{-9}}{2 \times 10^{-6}}$$

$$\approx 17.1^\circ.$$

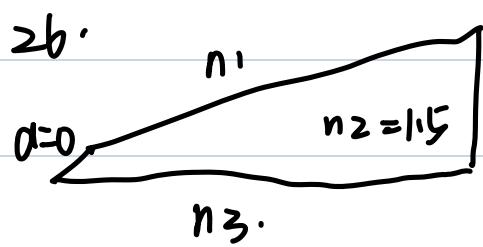
25. $n = 1.25$



$$2nd = \lambda$$

$$d = \frac{\lambda}{2n} = \frac{500 \times 10^{-9}}{2 \times 1.25} = 2 \times 10^{-7} m$$

$$S = \frac{V}{d} = \frac{1}{2 \times 10^{-7}} = 5 \times 10^6 m^{-2}$$

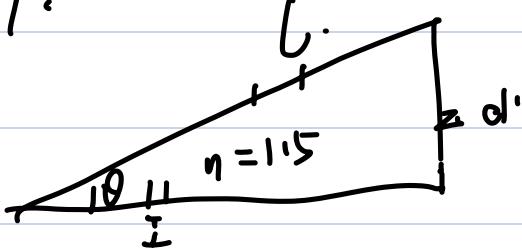


$$n_1 > n_2 < n_3. \quad \text{折射}$$

$$2nd + \frac{\Delta}{2} = k\lambda \quad (k=2)$$

$$d = \frac{3\lambda}{2 \times 3} = \frac{\lambda}{2} = 250 nm$$

27.



$$I = \frac{\Delta e}{\sin Q}$$

$$2nd + \frac{\Delta}{2} < (2k+1) \cdot \frac{\lambda}{2}$$

$$\text{折射} \quad \Delta d = d_2 - d_1 = \frac{\lambda}{2n}$$

$$\sin \theta = \frac{\Delta d}{L} = \frac{\lambda}{2nL} = \frac{600 \times 10^{-9}}{2 \times 1.5 \times 10^{-2}}$$

$$= 1.33 \times 10^{-4}$$

$$\theta \approx \sin \theta = 1.33 \times 10^{-4} \text{ rad.}$$

30. 半明後度. $I_0 = 2f \frac{\lambda}{D}$.

$$I_0 = 10^{-3} \text{ m.}$$

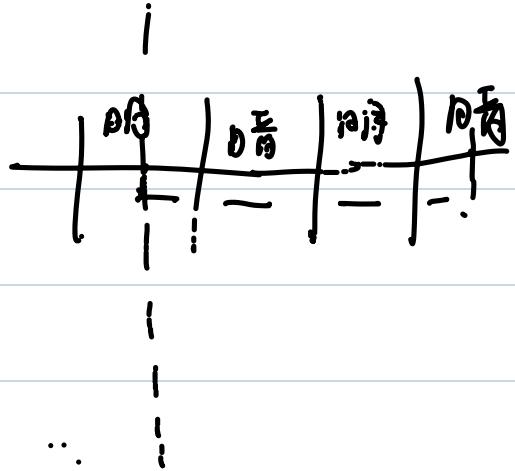
設用

$$a \sin \varphi = [2k+1] \cdot \frac{\lambda}{2}$$

$$\sin \varphi = \frac{3\lambda}{2a}$$

$$x_f = f' \sin \varphi = \frac{3\lambda}{2a} \cdot f' = 7.5 \times 10^{-4} \text{ m.}$$

$$\Delta x = 2 \cdot \frac{2\lambda}{a} \cdot f' = 2 \times 10^{-3} \text{ m.}$$



单缝衍射

31. $b \sin \theta = k \lambda$.

$$b = \frac{\lambda}{\sin \theta} = \frac{632.8 \times 10^{-9}}{\sin 5^\circ} \doteq 7.26 \times 10^{-6} \text{ m.}$$

圆孔衍射

32. $\theta = 1.22 \frac{\lambda}{D} = 2.24 \times 10^{-4} \text{ rad.}$

$$\theta = \frac{d}{l} = l = \frac{d}{\theta} = \frac{2 \times 10^3}{2.24 \times 10^{-4}} = 819 \text{ m.}$$



4). $(b+b') \sin \varphi = k \lambda$

$$\int d \sin b_0 = 3\lambda$$

$$d \sin 3\beta = 2\lambda_2.$$

$$\lambda_2 = \frac{5}{2} \lambda_1 = 510.35 \text{ nm}.$$

$$d \sin \varphi = 3\lambda.$$

$$d = 2041.4 \text{ nm}.$$

设 λ_1 与 λ_2 .

$$\begin{cases} d \sin \theta_1 = 2\lambda_1 \\ d \sin \theta_2 = 2\lambda_2 \end{cases}$$

$$\theta_1 = 23.07^\circ$$

$$\theta_2 = 48.13^\circ$$

$$\Delta\theta = \theta_2 - \theta_1 \approx 25^\circ$$

十七章前

1b. 2.

④ $W_0 = 4.2 \text{ eV}$

$$h\nu - W_0 = \frac{1}{2} m V_m^2$$

$$E_{km} = h\frac{c}{\lambda} - W$$

$$= 6.63 \times 10^{-34} \times \frac{3 \times 10^8}{2.5 \times 10^{-9}} - 4.2 \times 1.6 \times 10^{-19}$$

$$= 1.24 \times 10^{-19} \text{ J}$$

$$\hat{\textcircled{2}}. eU_0 = E_{km} = \frac{1}{2} m V^2$$

$$U_0 = \frac{1.24 \times 10^{-19}}{1.6 \times 10^{-19}} = 0.775 \text{ V}$$

$$\textcircled{3}. \left\{ \begin{array}{l} h\nu_0 = W \\ \nu_0 = \frac{c}{\lambda_0} \end{array} \right.$$

$$\nu_0 = \frac{c}{\lambda_0}$$

$$\lambda_0 = \frac{hc}{W} = 29 \text{ nm}$$

3. A

5D. 频率越大粒子性越强

$$b. P = \frac{h}{\lambda}$$

$$P = \frac{h}{\lambda} - \frac{h}{n\lambda} = \frac{h}{f\lambda}$$

$$E_k = P c = \frac{hc}{f\lambda}$$

$$Q = P c = \frac{hc}{\lambda}$$

D.

$$14. \quad h\nu = w_0$$

$$h\nu = w_0$$

$$eU_0 = h\frac{c}{\lambda} - w_0$$

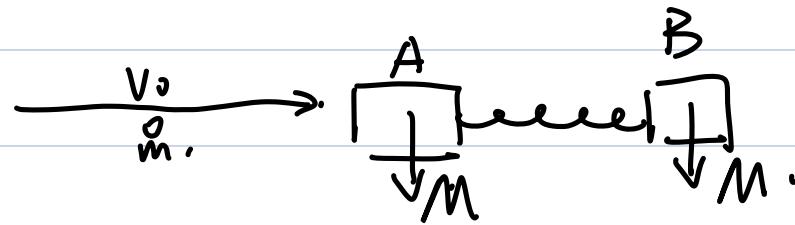
$$U_0 = \frac{hc}{\lambda e} - \frac{w_0}{e}$$

$$= 1.24 \cdot$$

大题.

动量与能量.

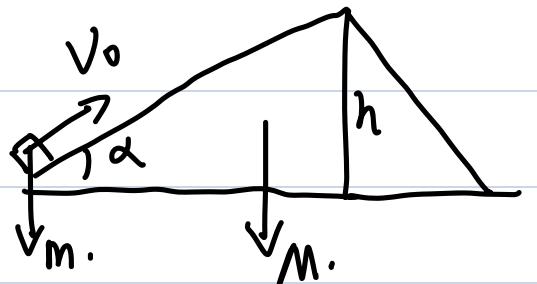
5.



$$\left\{ \begin{array}{l} m v_0 = (2M+m) \cdot V_{\text{共}} \\ \frac{1}{2} m v_0^2 = \frac{1}{2} (2M+m) \cdot V_{\text{共}}^2 + \frac{1}{2} k \Delta x^2 \end{array} \right.$$

$$\Delta x = \sqrt{\frac{M m^2 V_0^2}{(M+m)(2M+m) \cdot k}}$$

6.

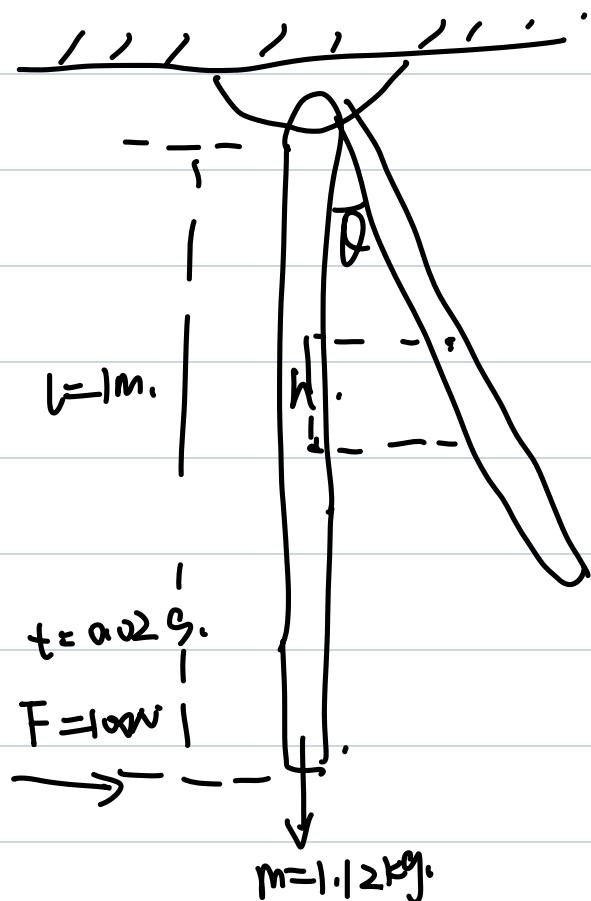


$$\left\{ \begin{array}{l} m v_0 \cos \alpha = (M+m) \cdot V_{\text{共}} \\ \frac{1}{2} m v_0^2 = mgh + \frac{1}{2} (M+m) \cdot V_{\text{共}}^2 \end{array} \right.$$

$$V_{\text{共}} = \sqrt{\frac{2(M+m)gh}{M+m \sin^2 \alpha}}$$

剛体力学

3.



$$J = \frac{ml^2}{3}$$

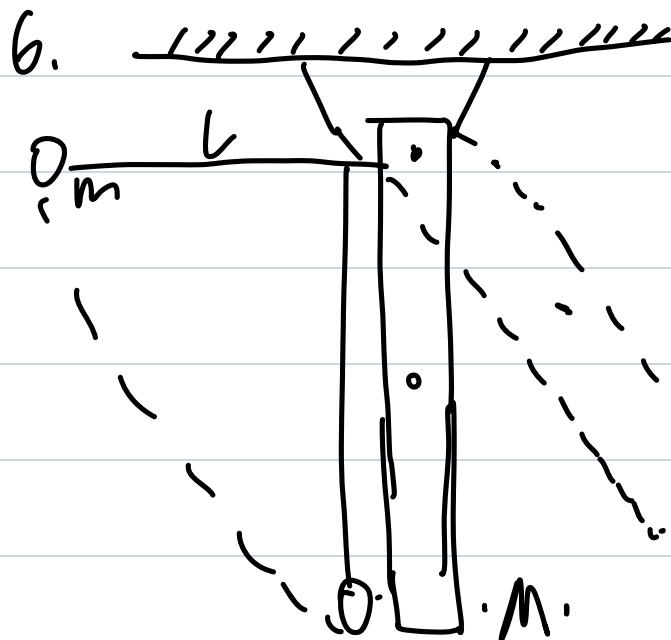
$$\textcircled{1} \quad l = P \times R$$

$$= F \Delta t \times R$$

$$= 100\text{N} \cdot 0.02\text{s} \times 1 = 2 \text{ kg} \cdot \text{s} \cdot \text{m} = J_{W_0}$$

$$\textcircled{2} \quad \frac{1}{2} J_{W_0}^2 = \frac{1}{2} mg(l - \cos\theta)$$

$$\theta = 88^\circ 38'$$



$$P \times R$$

$$J = \frac{1}{3} M l^2$$

$$\textcircled{1} \quad mgl = \frac{1}{2} mv^2$$

$$v = \sqrt{2gl}$$

$$\textcircled{2} \quad l = MV \times l = J_W$$

$$M \cdot \cancel{V} \cdot l^2 = \textcircled{1} \quad \frac{1}{3} M l^2 \cdot \cancel{V}$$

$$L \cdot \frac{1}{2}mv^2 = \frac{1}{2}JW^2$$

$$3m = M$$

$$\left\{ \begin{array}{l} V = \sqrt{2gL} \\ V = w \cdot l \\ w = \frac{\sqrt{2gL}}{l} \\ M = 3m \end{array} \right.$$

$$\textcircled{3} \quad \frac{1}{2}JW^2 = \frac{1}{2}Mg(l - \cos\theta)$$

$$\cancel{\frac{1}{2} \times \frac{1}{2} M \cancel{W^2} \frac{2gl}{l}} = \frac{1}{2} 3m g (l - \cos\theta)$$

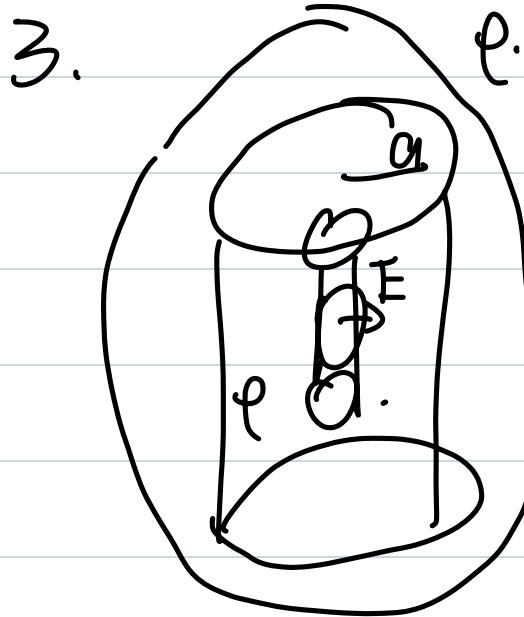
$$2mgl = 3mgl(1 - \cos\theta)$$

$$\frac{2}{3} = 1 - \cos\theta$$

$$\cos\theta = \frac{1}{3}$$

$$\theta = \arccos \frac{1}{3}$$

静电场



内: 取し $r \leq a$.

$$E \cdot 2\pi r l = \frac{q}{\epsilon_0} = \frac{\pi r^2 l \rho}{\epsilon_0}$$

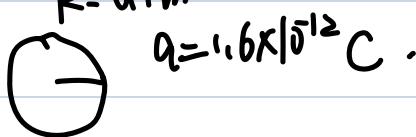
$$2\pi E \times l = \frac{\pi r^2 l \rho}{\epsilon_0}$$

$$E = \frac{r \rho}{2\epsilon_0}$$

$$\text{外} \quad E \cdot 2\pi r l = \frac{\pi a^2 l \rho}{\epsilon_0}$$

$$E = \frac{a^2 \rho}{2\epsilon_0 l}$$

b.



取外部.



$$E \cdot 4\pi R^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{4\pi R^2 \epsilon_0}$$

$$\int_0^R dp = \int_R^\infty E dR = -\frac{q}{4\pi \epsilon_0} \int_R^\infty \frac{1}{R^2} dR$$

$$p = \frac{-q}{4\pi \epsilon_0} \frac{1}{R}$$

$$p_{表1} = \frac{q}{4\pi \epsilon_0 R}$$

$$= 36 V$$

$$\therefore p_{表2} = 2p_{表1} = \frac{2q}{4\pi \epsilon_0 R}$$

$$= 57 V$$

电磁感应.

$$\text{1) } B = \mu_0 n I. \quad \text{螺线环} B \text{ 大小计算}$$

$$\varphi = BS = \mu_0 n I \cdot A$$

$$M_{12} = M_{21} \text{ 同.}$$

$$\varphi = M I.$$

$$M = \frac{\Phi}{I} = \mu_0 n A.$$

$$q = -\frac{d\varphi}{dt} = -M \frac{dI}{dt}.$$

$$= -MI_0 \cos \omega t.$$

$$= -\mu_0 n A I_0 \cos \omega t.$$

波动方程(1)  n=1.32

2.

$$\begin{cases} \Delta x_1 = 2n\lambda t = (2k_1+1) \cdot \frac{\lambda_1}{2} \\ \Delta x_2 = 2n\lambda t = (2k_2+1) \cdot \frac{\lambda_2}{2} \end{cases}$$

$$k_2 = k_1 - 1$$

$$t = 643nm$$

量子物理.

$$E = h\nu = W_0$$

$$3. \quad W = 2 \text{ eV}$$

$$h\nu = W_0$$

$$h\frac{c}{\lambda} = W_0$$

$$\frac{hc}{W_0} = \lambda$$

$$\lambda = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{2 \times 1.6 \times 10^{-19}}$$

$$= 6.22 \times 10^{-9} \text{ m.}$$

$$eU = h\nu - W_0$$

$$eU = h\frac{c}{\lambda} - W_0$$

$$eU + W_0 = h\frac{c}{\lambda}$$

$$\lambda = \frac{hc}{eU + W_0}$$

$$\lambda = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{5 \times 1.6 \times 10^{-19}} = 2.48 \times 10^{-9} \text{ m.}$$

5. 康普顿散射 $\Delta\lambda = \lambda - \lambda_0 = \frac{h}{m_e c} (1 - \cos\theta) = \frac{2h}{m_e c} \cdot \sin^2 \frac{\theta}{2}$

$\lambda_C = 2.43 \times 10^{-12} \text{ m.}$

电子静质量 $9.1 \times 10^{-31} \text{ kg}$

$$\Delta\lambda = \lambda - \lambda_0 = \lambda_C (1 - \cos\theta) = \lambda_C = 0.00243 \text{ nm.}$$

$$\therefore \Delta\lambda, \lambda_C.$$

$$\lambda = \Delta\lambda + \lambda_0 = 0.0524 \text{ nm}$$

$$\Delta\lambda = \lambda - \lambda_0 = \lambda_C (1 - \cos\theta) = 2\lambda_C = 0.00486 \text{ nm}$$

$$\lambda = \Delta\lambda + \lambda_0 = 0.05486 \text{ nm}$$