

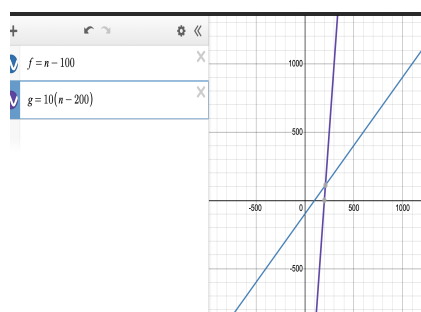
# cs5800 homework1

yin.zheng

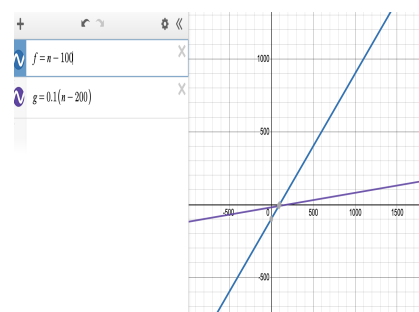
January 2022

1 In each of the following situations, indicate whether  $f = O(g)$ , or  $f = \omega(g)$ , or both (in which case  $f = \theta(g)$ ).

- (a) There is  $C$  and  $C'$  make  $C * g(n) \leq f(n) \leq C' * g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$



(a) Big O

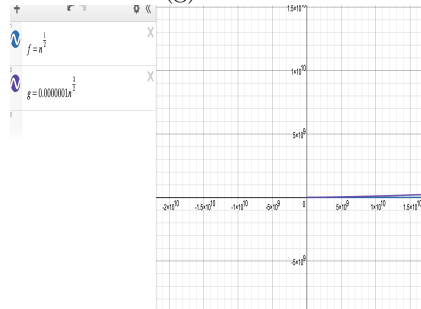


(b) Big Omega

Figure 1: Image for a)

- (d) There is  $C$  and  $C'$  make  $C * g(n) \leq f(n) \leq C' * g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$

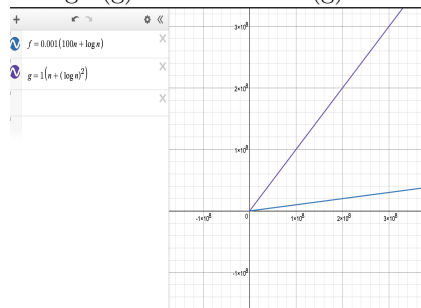
- (b) No matter how small  $C$  is  $C \cdot g(n)$  can always be bigger than  $f(n)$  when  $n \geq n_0$ , so there's  $f = O(g)$



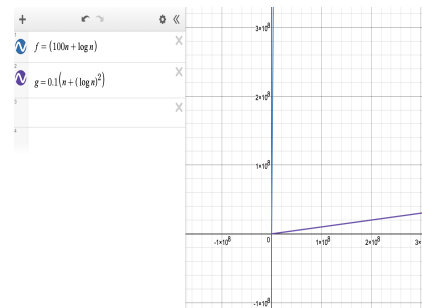
(a) Big O

Figure 2: Image for b)

- (c) There is  $C$  and  $C'$  make  $C \cdot g(n) \leq f(n) \leq C' \cdot g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$

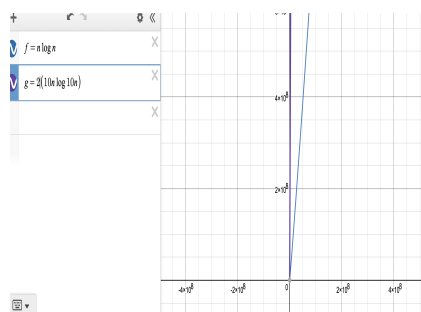


(a) Big O

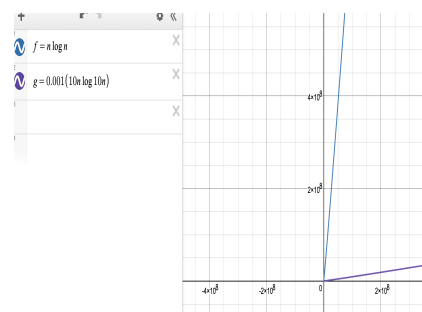


(b) Big Omega

Figure 3: Image for c)



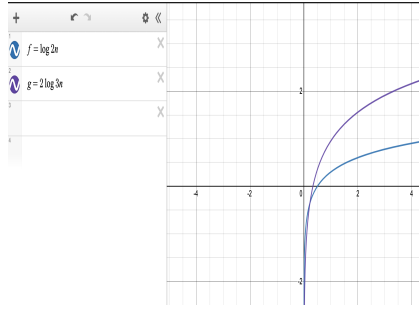
(a) Big O



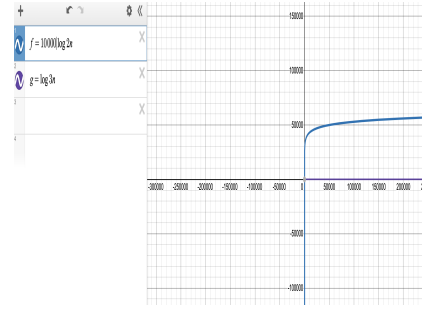
(b) Big Omega

Figure 4: Image for d)

- (e) There is  $C$  and  $C'$  make  $C * g(n) \leq f(n) \leq C' * g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$



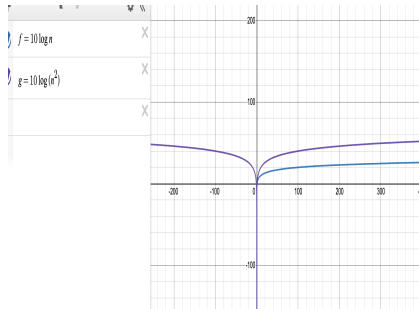
(a) Big O



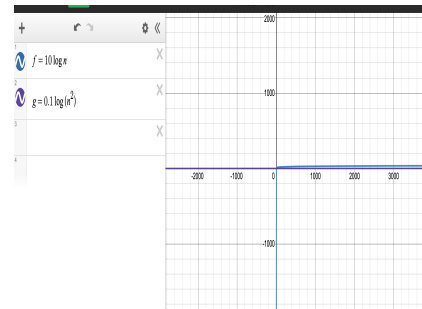
(b) Big Omega

Figure 5: Image for e)

- (f) There is  $C$  and  $C'$  make  $C * g(n) \leq f(n) \leq C' * g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$



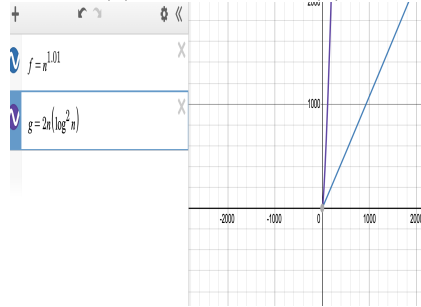
(a) Big O



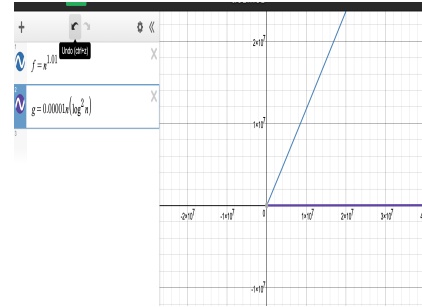
(b) Big Omega

Figure 6: Image for f)

- (g) There is  $C$  and  $C'$  make  $C * g(n) \leq f(n) \leq C' * g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$



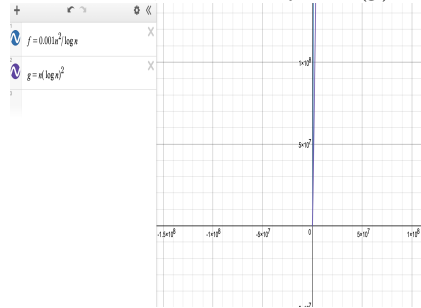
(a) Big O



(b) Big Omega

Figure 7: Image for g)

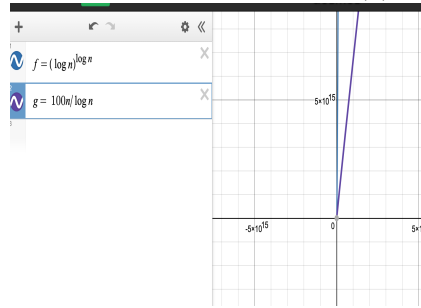
- (h) No matter how big  $C$  is,  $C * g(n)$  can always smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big omega

Figure 8: Image for h)

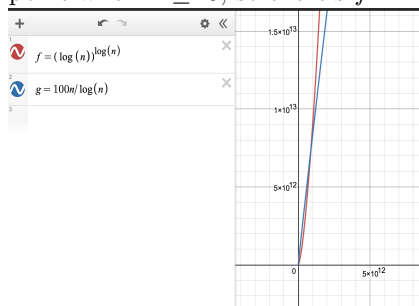
- (i) No matter how big  $C$  is,  $C * g(n)$  can always smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big Omega

Figure 9: Image for i)

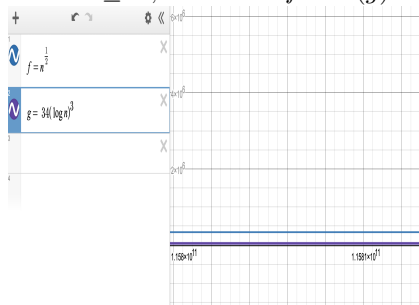
- (j) this is j No matter how big C is,  $C \cdot g(n)$  can always smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big Omega

Figure 10: Image for i)

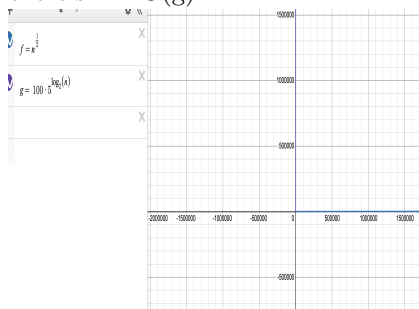
- (k) No matter how big C is,  $C \cdot g(n)$  can always smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big Omega

Figure 11: Image for k)

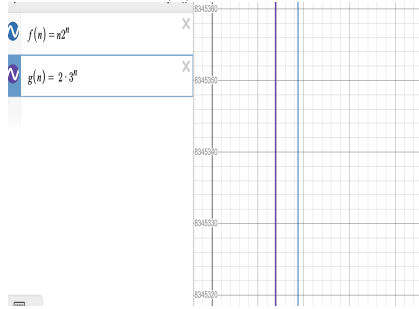
- (l) No matter how small C is  $C \cdot g(n)$  can always bigger than  $f(n)$  when  $n \geq n_0$ , so there's  $f = O(g)$



(a) Big O

Figure 12: Image for l)

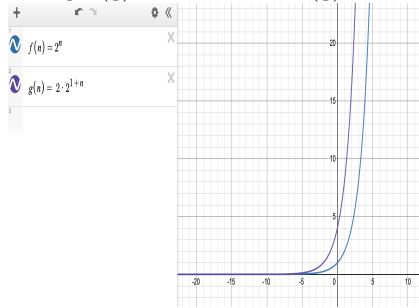
- (m) No matter how small  $C$  is  $C \cdot g(n)$  can always be bigger than  $f(n)$  when  $n \geq n_0$ , so there's  $f = O(g)$



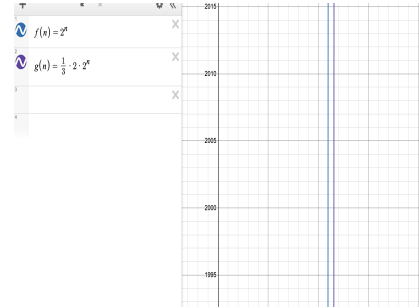
(a) Big O

Figure 13: Image for m)

- (n) There is  $C$  and  $C'$  make  $C \cdot g(n) \leq f(n) \leq C' \cdot g(n)$ , so there's  $f = O(g)$ ,  $f = \Omega(g)$  and  $f = \Theta(g)$



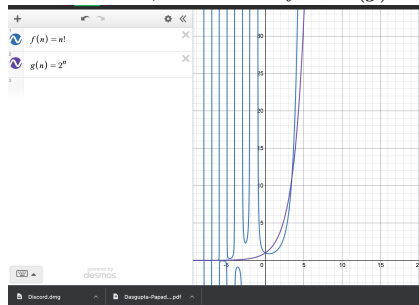
(a) Big O



(b) Big Omega

Figure 14: image for n

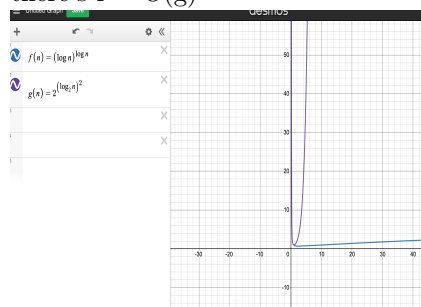
- (o) No matter how big  $C$  is,  $C \cdot g(n)$  can always be smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big Omega

Figure 15: Image for i)

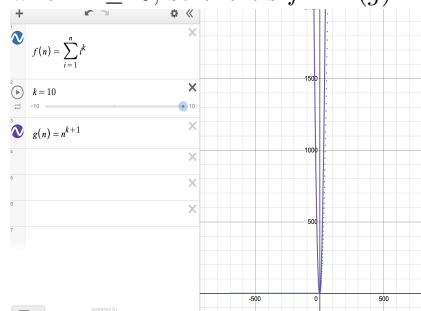
- (p) No matter how small  $C$  is  $C \cdot g(n)$  can always be bigger than  $f(n)$  when  $n \geq n_0$ , so there's  $f = O(g)$



(a) Big O

Figure 16: Image for i)

- (q) No matter how big  $C$  is,  $C \cdot g(n)$  can always be smaller than  $f(n)$  at some point when  $n \geq n_0$ , so there's  $f = \Omega(g)$



(a) Big Omega

Figure 17: Image for i)