Why Transformers Need Adam: A Hessian Perspective

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Thanks Prof. Hong for the invitation!

Background

- **Adam** becomes the most popular algorithms in deep learning (DL). (>~~170,000 citations, by May 2024~~, >198k citations, by Oct 2024)

- **Default in** LLM (large language models)

```
optimizer = optim.Adam(net.parameters(), lr=args.lr, betas=(args.beta1, args.beta2), eps=1e-08,
                       weight_decay=args.weightdecay, amsgrad=False)
```

- **Empirical fact (sad?): Adam seems to be the only choice for ChatGPT**
  --Recent new algorithms (Sophia, Lion, etc.)
  cannot beat Adam on billion-parameter models.

Overview of this talk

Part I:

- Why LLM training requires Adam, not SGD?
- We explain it from Hessian spectrum perspective

Part II:

- **Adam-mini:** A "mini" version of Adam
- Saves memory by **45%-50%;** same loss curve as Adam
- Can achieve **49.6%** higher throughput on Llama2-7B pre-training (saves **30%** training time)

Contents

Let us start with SGD…

- Consider $\min_x f(x) := \sum_{i=1}^{n} f_i(x)$.

  n: number of samples (or mini-batches of samples)

  x: trainable parameters

- In the k-th iteration: Randomly sample τ_k from $\{1,2,\dots,n\}$

SGD (Stochastic gradient descent): $x_{k+1} = x_k - \eta_k \nabla f_{\tau_k}(x_k)$

SGD with momentum (SGDM):

$$m_k = (1-\beta_1)\nabla f_{\tau_k}(x_k) + \beta_1 m_{k-1}$$

$$x_{k+1} = x_k - \eta_k m_k$$

⇐ 1st order momentum

⇐ Iterate update

Adam

- $\min_x f(x) \coloneqq \sum_{i=1}^n f_i(x)$. In the k-th iteration: Randomly sample τ_k from $\{1,2,\dots,n\}$

- Adam (Kingma and Ba'15):
- $m_k = (1-\beta_1)\nabla f_{\tau_k}(x_k) + \beta_1 m_{k-1}$
- $v_k = (1-\beta_2)\nabla f_{\tau_k}(x_k) \circ \nabla f_{\tau_k}(x_k) + \beta_2 v_{k-1}$
- $x_{k+1} = x_k - \eta_k \frac{\sqrt{1-\beta_2^k}}{1-\beta_1^k} \frac{m_k}{\sqrt{v_k}}$

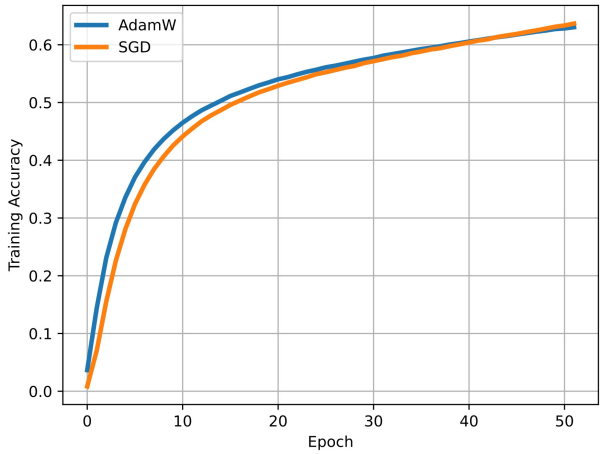
⇐ 1st order momentum

⇐ 2nd order momentum

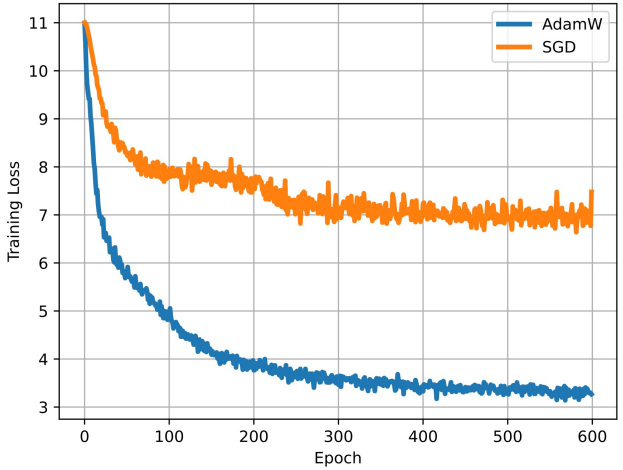
⇐ Iterate update

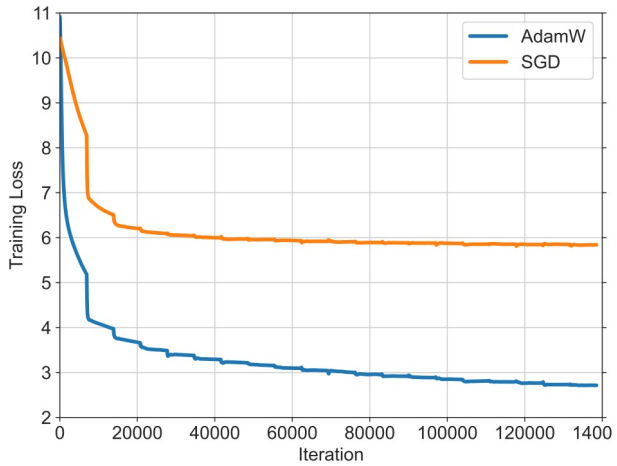
- β_1: Controls the 1st-order momentum m_k. Default setting: $\beta_1 = 0.9$
- β_2: Controls the 2nd-order momentum v_k. Default setting: $\beta_2 = 0.999$
- One important difference with SGD:
  - -- Adam use coordinate-wise lr $\frac{\eta}{v_i}$ ‘
  - -- SGD uses single lr η for all

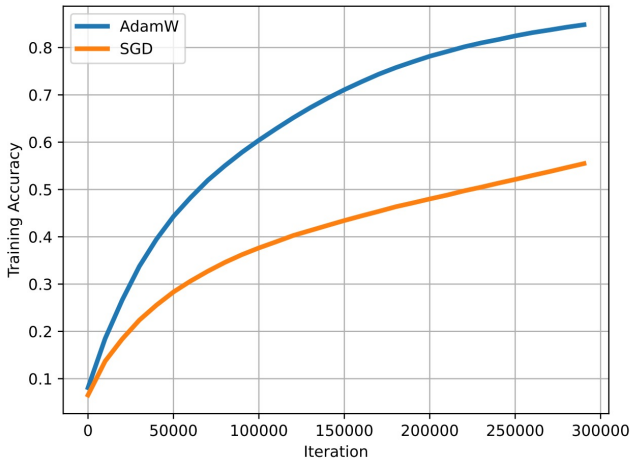
SGD works well on CNN, largely underperforms Adam on Transformers



VGG (CNN)







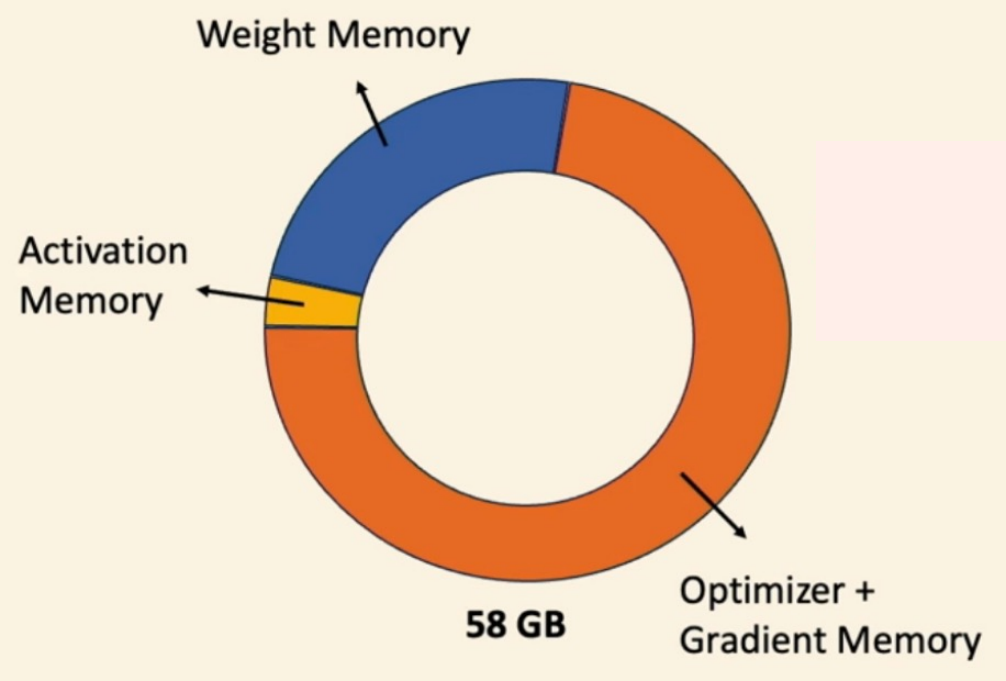
GPT2 BERT ViT

Transformers Need Adam, but why?

However, Adam is expensive to use…

- Adam needs memory for m and v
  -- In total: 2x model size

  -- becomes a major overhead for LLMs: e.g., for 7B models



[Figure from a recent talk by Meta]

- Palm-540B: Adam alone takes **50x** A100-80GB GPUs …

Literature on Why Adam better than SGD

- One perspective [J. Zhang et al. 19]
  NLP problems exhibit **heavy-tailed noise** in g → SGD fails

- However, [Chen, Kunstner, Schmidt'21] provides negative evidence:
  SGD is worse than Adam on Transformers, even in **full-batch case**
  (with no stochasticity)

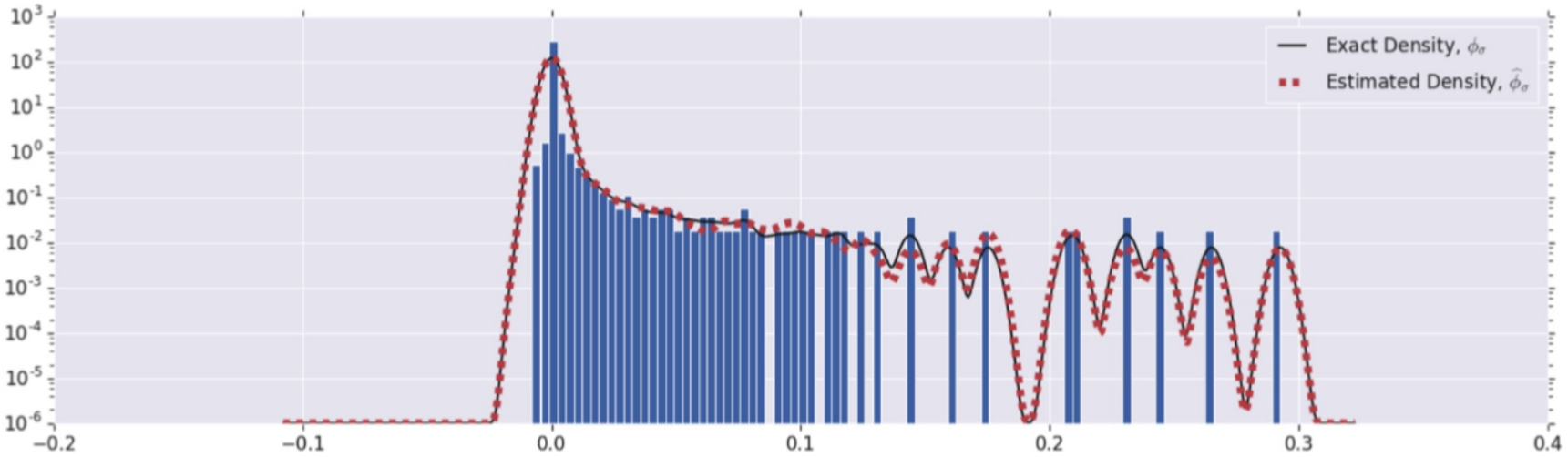
- So there shall be other reasons...

What problem structure might hamper SGD?

- **Hessian eigenvalues** largely decides behavior of gradient methods [Nocedal & Wright'99, Nesterov'13, Goh'17, Sun'2019]
- For instance: ill-conditioning slow down GD
- Can Hessian spectrum explain the gap of SGD and Adam?
- Unfortunately, no (not directly)…

Preliminary: Hessian spectrum

y-axis: frequency



x-axis: Eigenvalues.

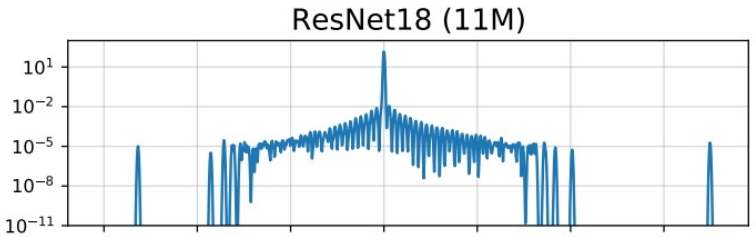
Figure from [Ghorbani et al. 19]

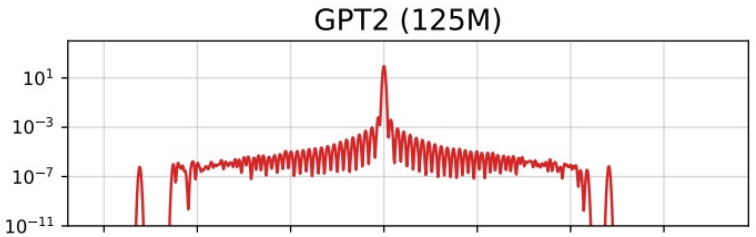
What is spectrum: histogram of eigenvalues

Remark: How to plot Hessian spectrum?
We use Stochastic Lanczos Quadrature (SQL)
[Bai, Fahey, and Golub 1996]
(will take >10 pages to explain, omitted today)

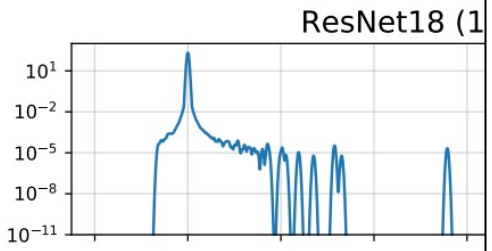
We will compute the Hessian spectrum for a wide range of neural networks

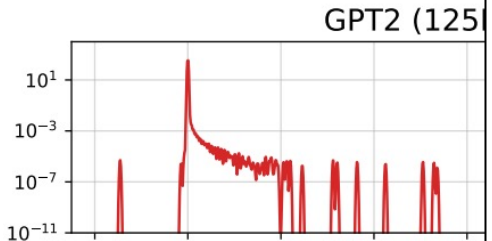
Hessian spectrum cannot explain the gap



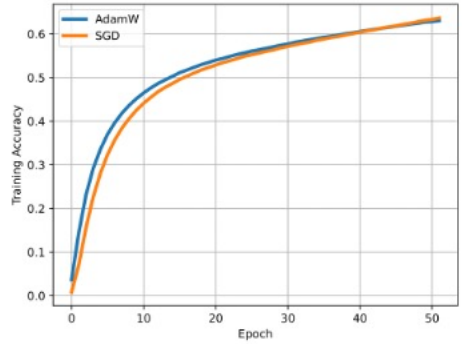


(a) Initialization

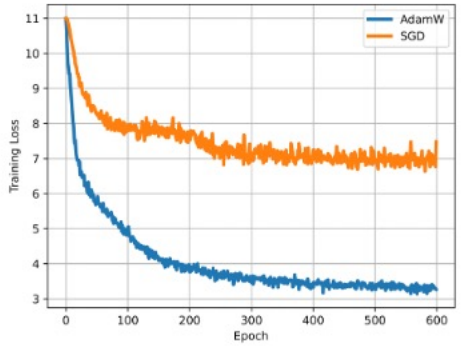




(c) 50% ste



SGD ≈ Adam on CNNs



SGD ≪ Adam on Transformers

CNN and Transformers: Spectrum looks quite similar!
(see more figures in the paper)

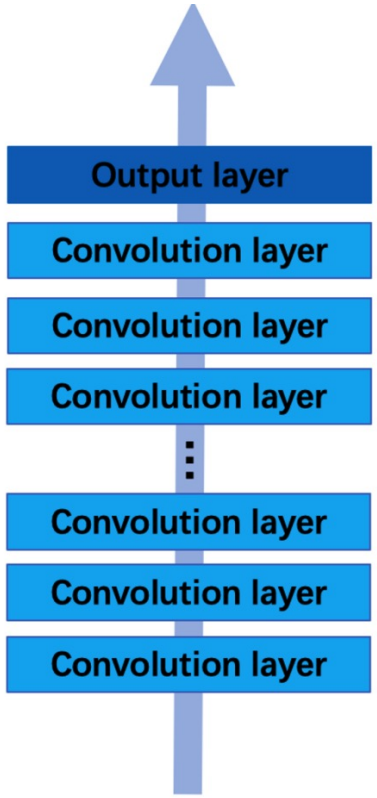
Something must be overlooked…

- Full hessian spectrum does not seem informative enough
- What else?
- We find one important features that are overlooked:

  The build-up rules of the architecture

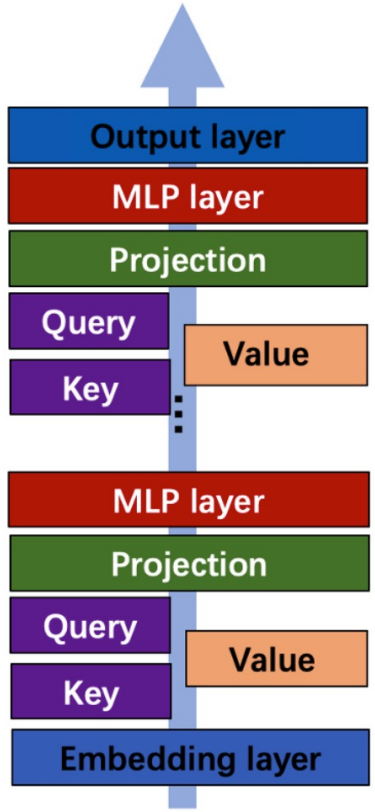
  -- Transformers are stacked up by different kinds of layers

Build-up rules of architectures



CNNs:

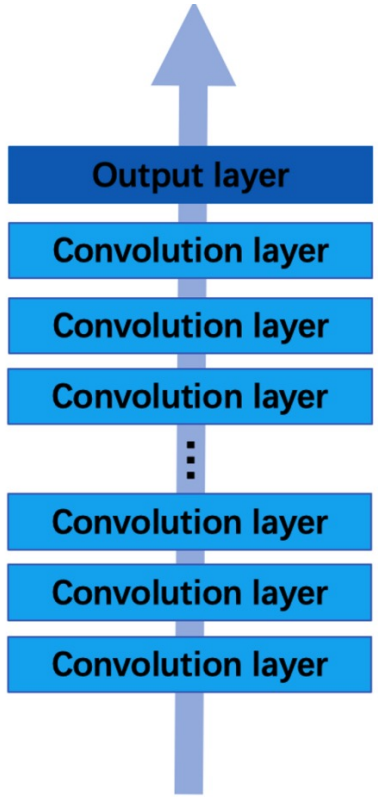
repetitive stack of similar layers



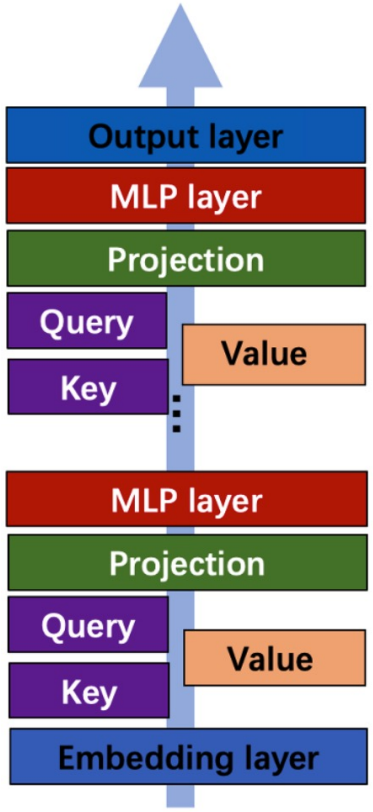
Transformers:

each block follow different design (e.g., Q, K, V, MLP)

Build-up rules of architectures



CNNs



Transformers

We hypothesize:

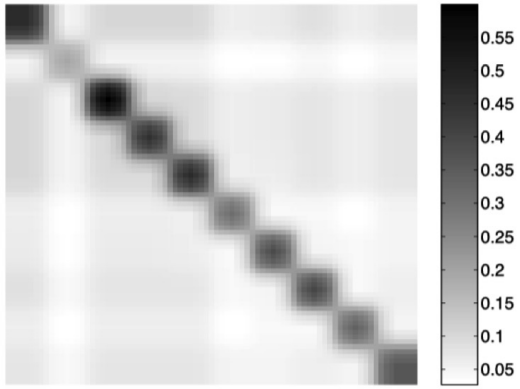
Different designs among parameter blocks

will affect

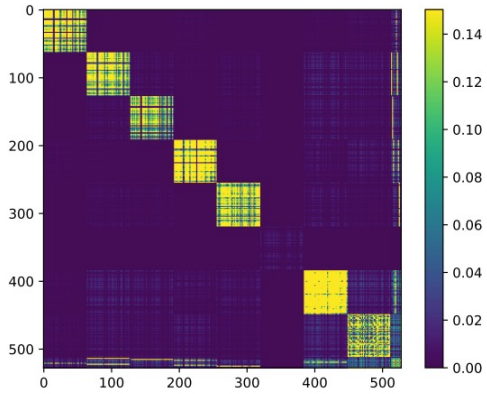
Hessian of these parameter blocks.

This inspires us to investigate the **blockwise Hessian spectra** (i.e., principle diag blocks in Hessian)

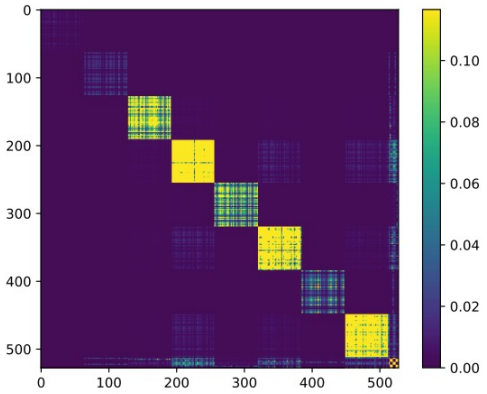
Another reason for studying blockwise Hessian **near Block Diagonal structure**



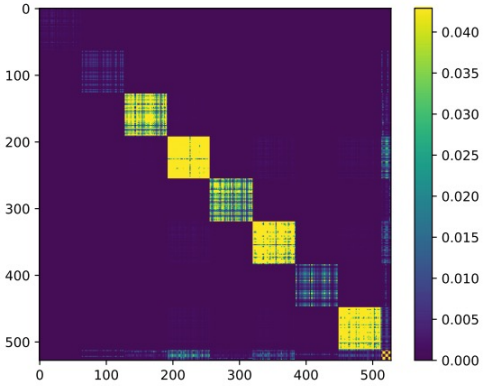
(a) Exact Hessian of a MLP (Collobert, 2004)



(b) Hessian of an MLP at 1% step



(c) Hessian of an MLP at 50% step



(d) Hessian of an MLP at 100% step

Proof (from Collobert 2004): for 1-hidden-layer network $f(\theta, x)$ + **Cross Entropy loss**, we have

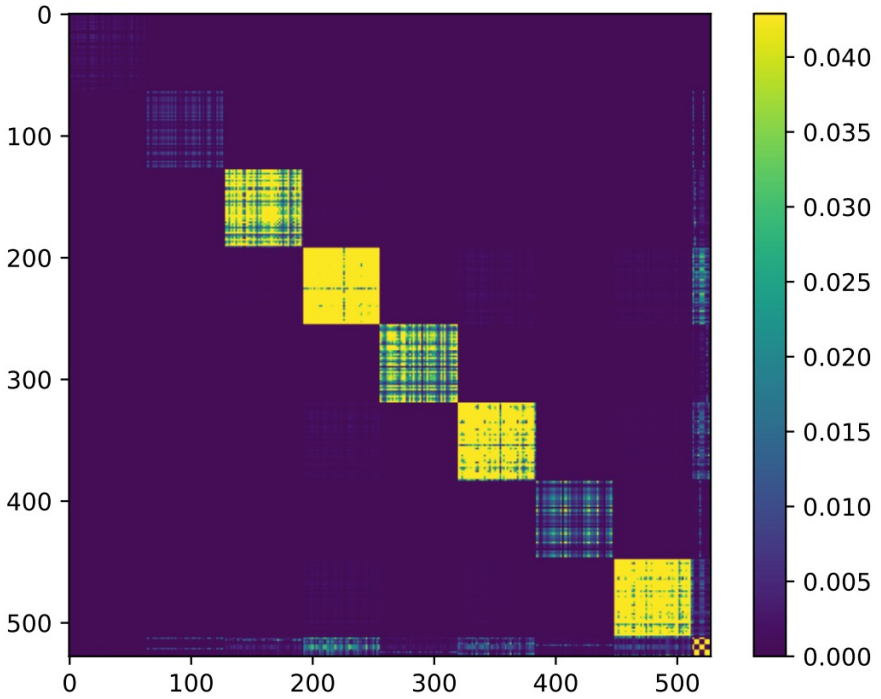
$$\frac{\partial^2 \ell(f(\theta,x),y)}{\partial w_i \partial w_j} = p_\theta(y|x)\left(1-p_\theta(y|x)\right) v_i v_j \phi'\left(w_i^\top x\right)\phi'\left(w_j^\top x\right) xx^\top \quad \text{for } i \neq j,$$

where $w_i \in R^{\,data\ dimension}$: the weight associated with the i-th output neuron

When we maximize $p_\theta(y|x)$, $p_\theta(y|x)\left(1-p_\theta(y|x)\right)$ will quickly shrink to zero

But this structure is largely overlooked for both Opt & DL community (sadly…)

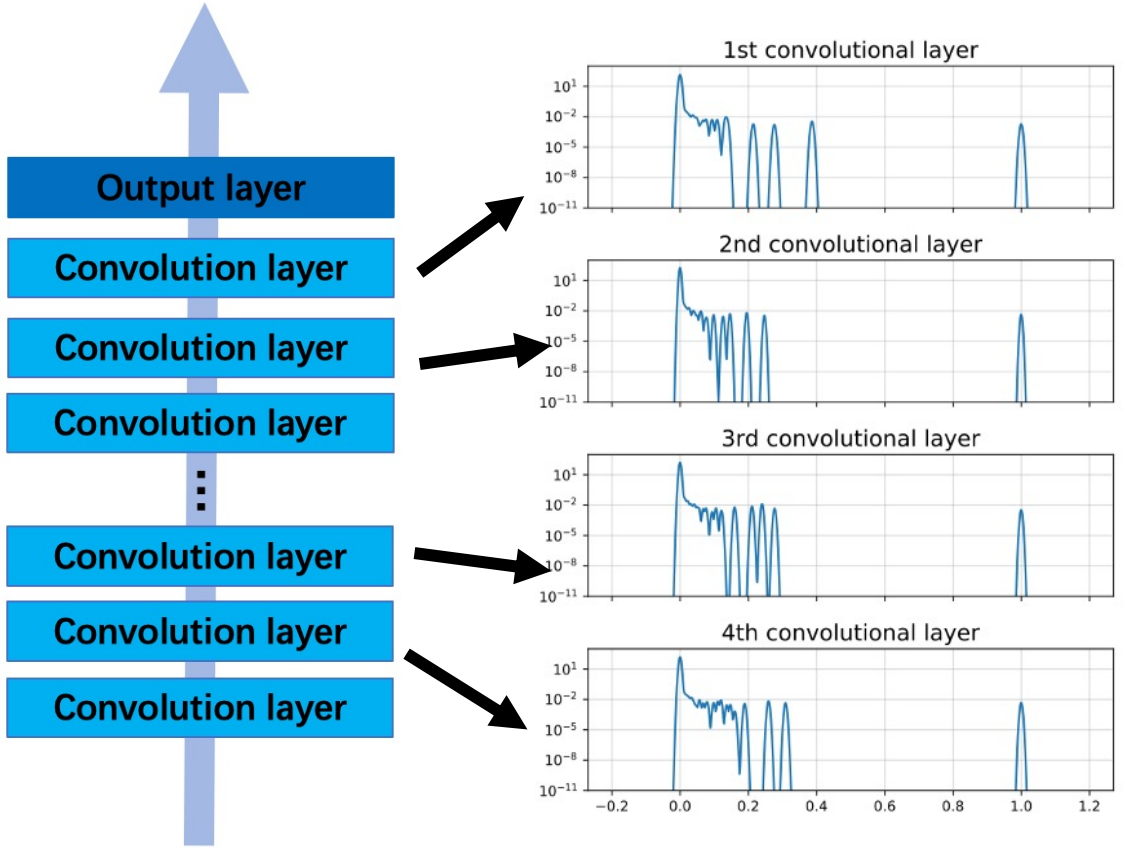
Blockwise Hessian spectrum might matters



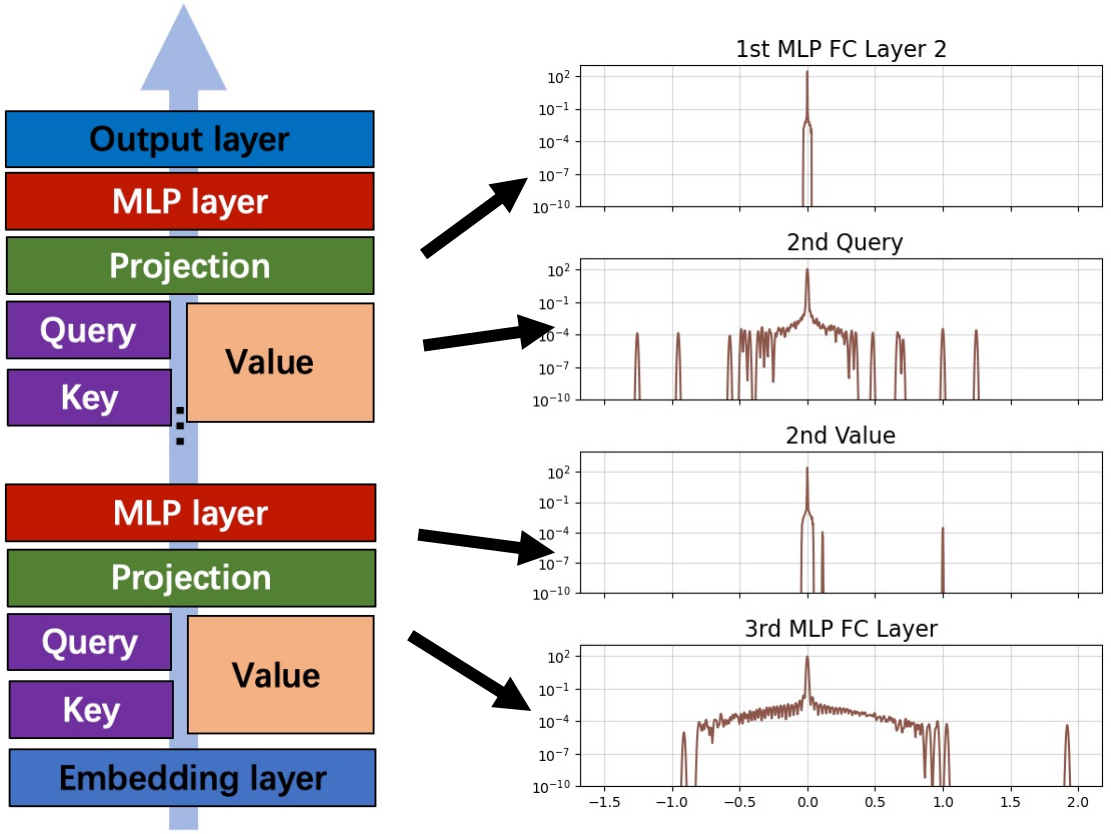
Conjecture: Eigenvalues in **each block (e.g., Q, K, V)** could be important

- What extra info over full spectrum?
- By linear algebra: **location** of eigenvalues

Blockwise Hessian spectrum



ResNet18



BERT

CNNs: blockwise spectrum are quite **similar**
We call it ``**homogeneity**”

Transformers: blockwise spectrum are largely **different**
We call it ``**heterogeneity**”

JS-distance among blocks

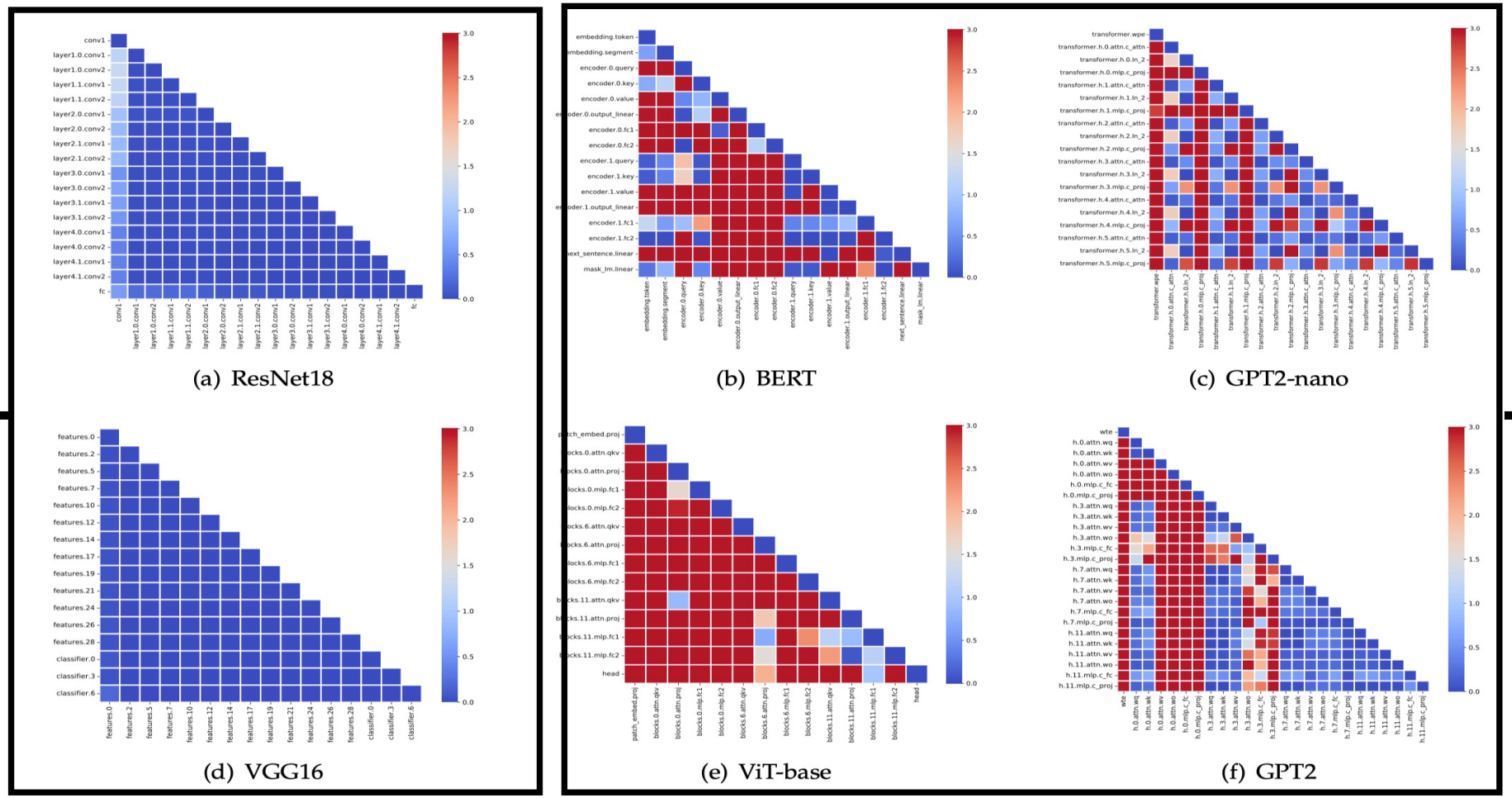
CNNs ←  → Transformers

Figure 4: The JS distance among blockwise Hessian spectra for different models at initialization.

Observation 1: Heterogeneity is widely observed in Transformers, but not on CNNs!

Our Explanation: Why Transformer Needs Adam

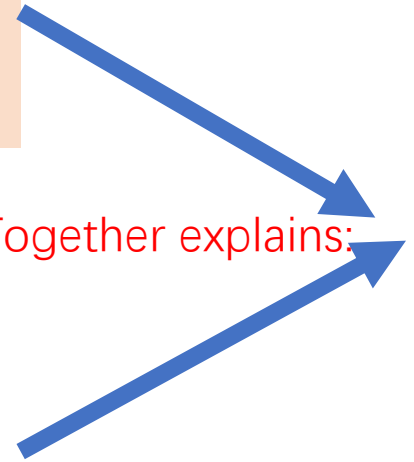
Observation 1:
Transformer's block Hessian are heterogeneous

Previous part

Observation 2:
If block Hessian are heterogeneous,
then SGD worse than Adam.

Next part:

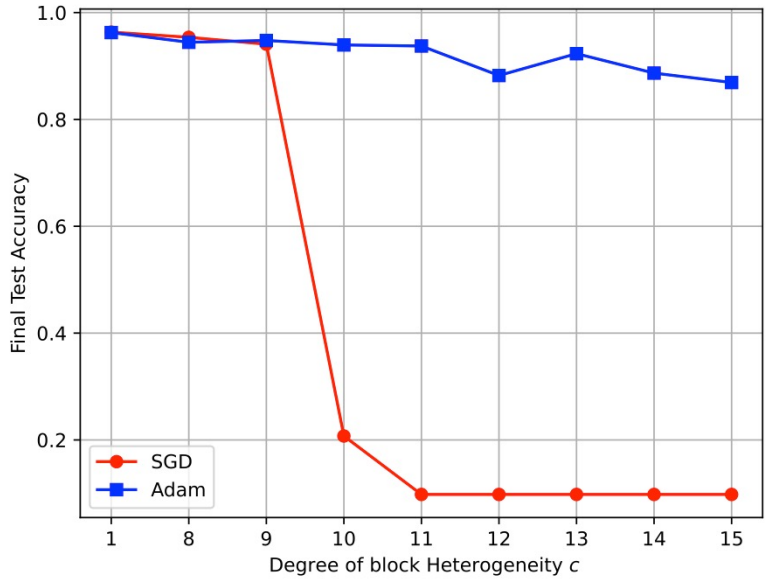
Claim 2: Hetereogeneity causes SGD worse than Adam.



Original claim:
Transformer:
SGD worse than Adam.

Hetereogeneity makes SGD worse: Example 2 (pure MLP)

- **Q:** Is Transformer the only architecture that is heterogeneous & SGD worse?
- **A:** No! We provide a few more heterogeneous examples that SGD is worse.



x-axis: degree of Heterogeneity
y-axis: final converged accuracy

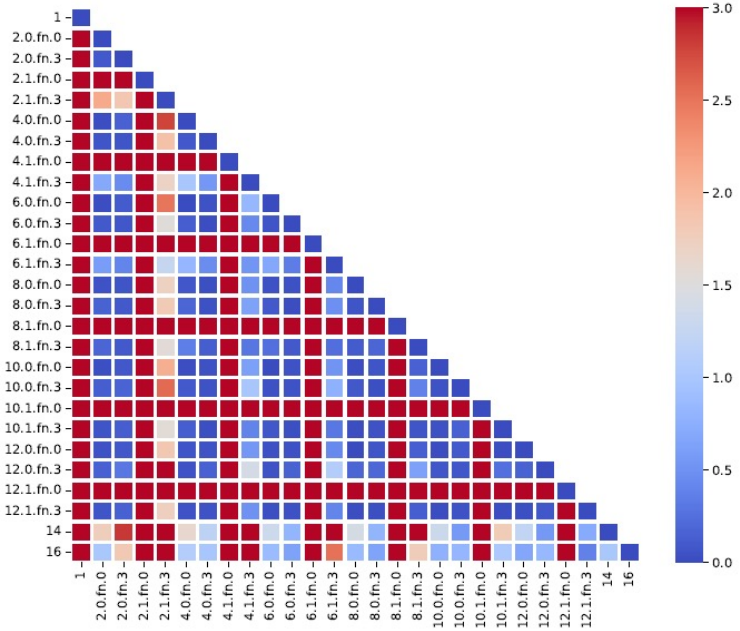
Example 2:
A man-made MLP on MNIST:
We exert heterogeneity by scaling each layer differently

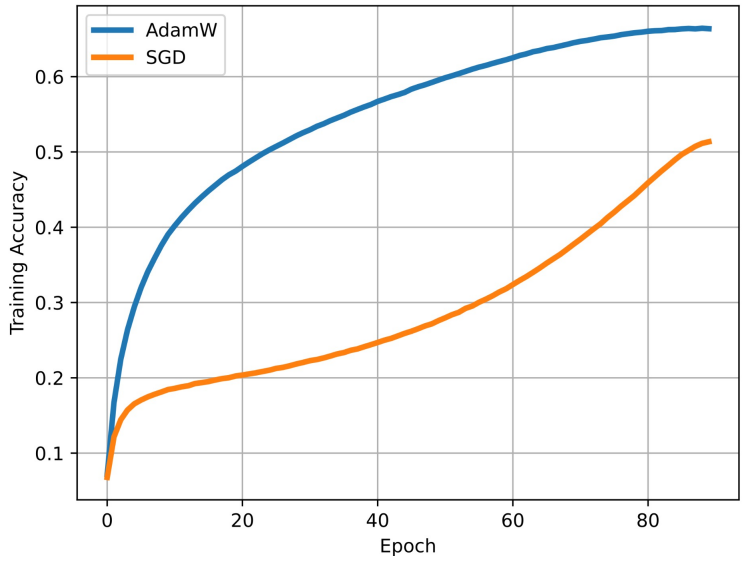
Observation:
SGD fails as heterogeneity grows
while Adam remains unaffected

Hetereogeneity makes SGD worse: Example 3 (MLP-mixer)

Example 3: MLP-mixer [1]

A pure MLP architecture that outperforms CNNs on ImageNet





Observation:

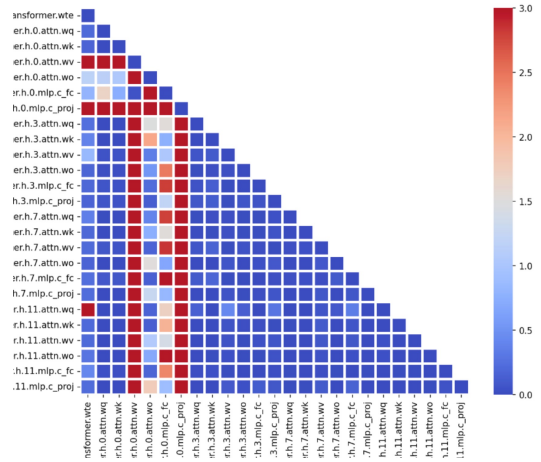
--MLP mixer is heterogeneous

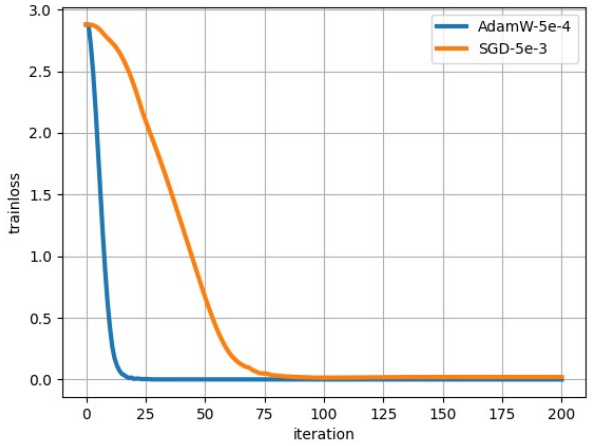
--SGD performs worse than Adam

[1] MLP-mixer: An All-MLP Architecture for Vision. Tolstikhin et al. , NeurIPS 2021

Heterogeneity is redued after training

- We find **pretrained Transformers** suffer less heterogeneity
- May explain why fine-tuning is easier
- SGD could work here: still slower, but can reach similar loss as Adam
- Similar phenomena also holds for ViT-base

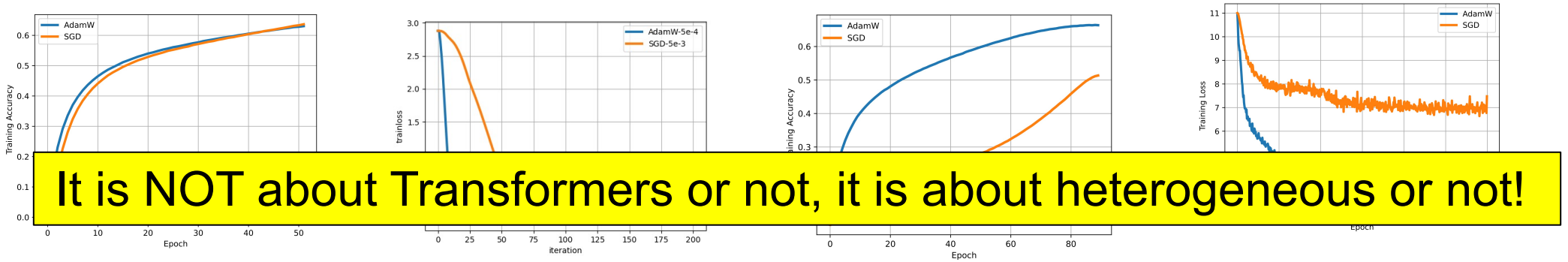




GPT2-125M (pretrained on 25B tokens): finetuning on a subset of Alpaca

Observation 3: Heterogeneity tends to reduce after (pre)-training

SGD performance v.s. Heterogeneity in Hessian



It is NOT about Transformers or not, it is about heterogeneous or not!

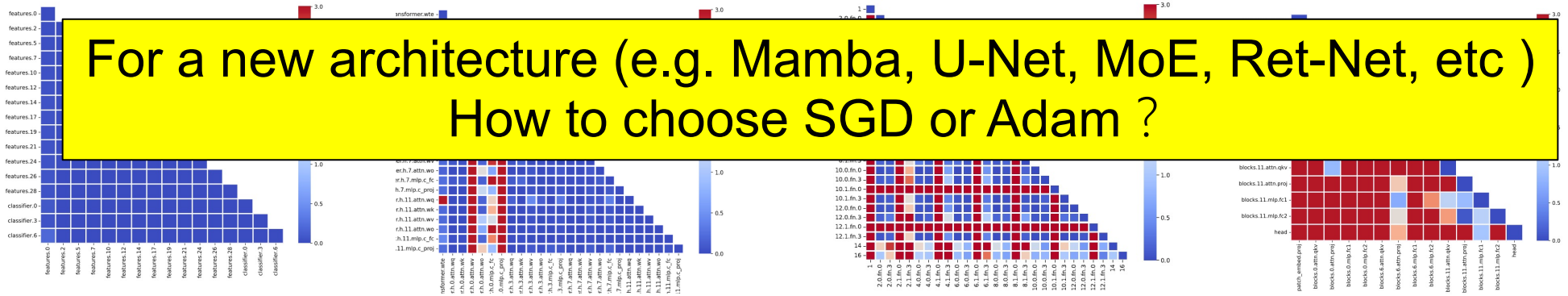
Easy for SGD

Difficult for SGD

Homogeneity in Hessian

Heterogeneity in Hessian

For a new architecture (e.g. Mamba, U-Net, MoE, Ret-Net, etc)
How to choose SGD or Adam ?



CNN | Transformer (pretrained) | MLP-mixer | Transformer

Empirical guidance: choose SGD or Adam?

- Introduce metric to **predict** the failure of SGD **before launching the training**

- **Our metric:** average JS distance of spectrum among blocks at step = 0, called JS^0
- This metric could be efficiently computed using Stochastic Lanczos Quadrature
  Our **PyTorch implementation**: https://github.com/zyushun/hessian-spectrum

Model	ResNet18	VGG16	GPT2 (pretrained)	MLP-mixer	BERT	GPT2	ViT-base
JS^0	0.10	0.09	18.84	34.90	53.38	83.23	286.41

For CNNs: 100x smaller than Transformers!

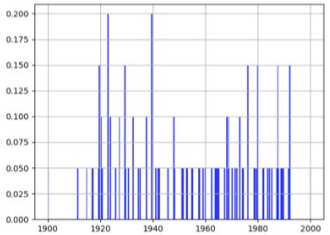
Initial theory

Hetereogeneity makes SGD worse: Quadratic Prob

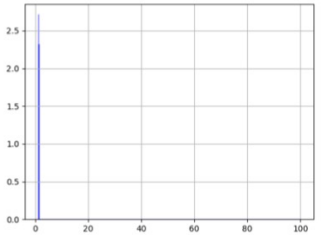
- Case study on quadratic models

$$\min_w \frac{1}{2} w^T H w, H = diag(H1, H2, H3, H4), H \text{ is PD}$$

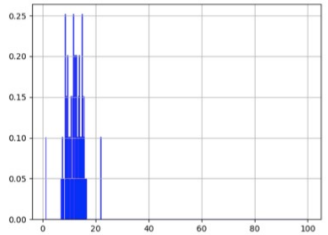
Case 1: H with Transformer-type spectra: sampled from GPT2



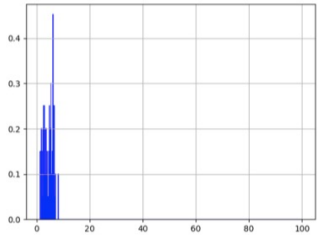
(a) Spectrum of H_1



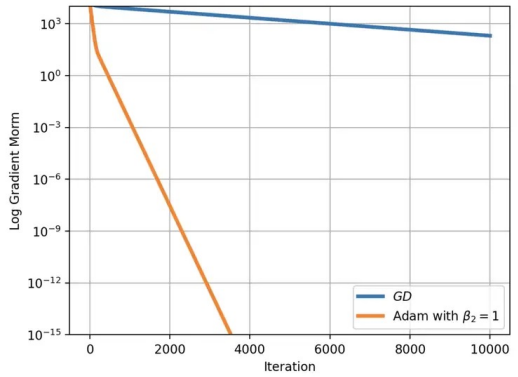
(b) Spectrum of H_2



(c) Spectrum of H_3



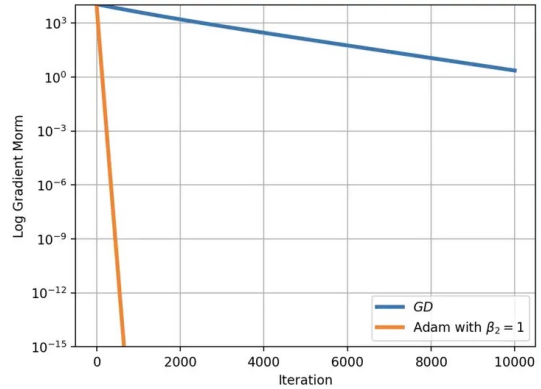
(d) Spectrum of H_4



GD is slower than Adam

Case 2: H with simplified **heterogeneous** spectra

Eigenvalues of H_l : { 1, 2, 3 } , { 99, 100, 101 } , { 1998, 1999, 2000 }



GD is slower than Adam

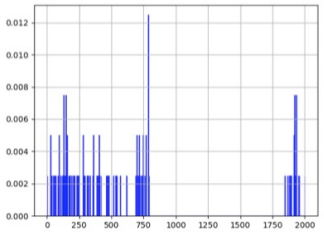
Remark:
Same condition number for case 1 & 2
but the performance is different, due to **homo & heterogeneity**

Homogeneity can make SGD work: (quadratic prob)

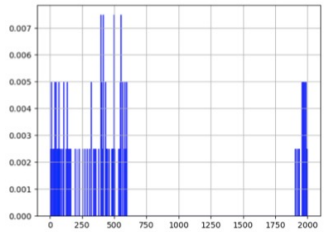
- Case study on quadratic models

$$\min_w \frac{1}{2} w^T H w, H = diag(H1, H2, H3), H \text{ is PD}, \quad H_l \in R^{3\times 3}, l = 1,2,3$$

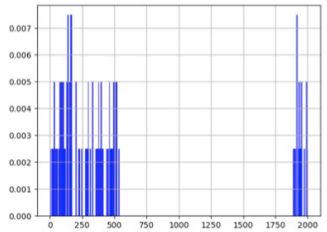
Case 3: H with CNN-type spectra: sampled from ResNet18



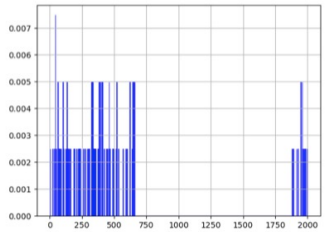
(a) Spectrum of H_1



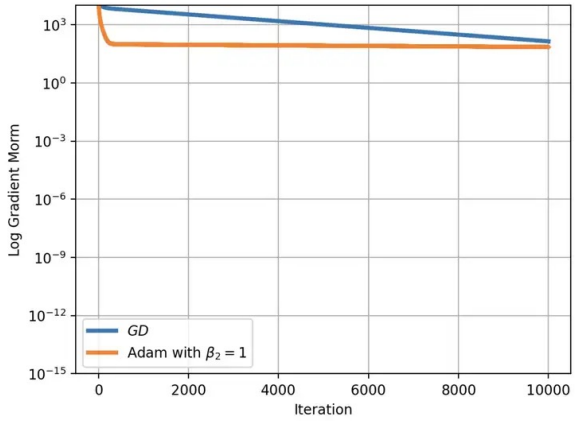
(b) Spectrum of H_2



(c) Spectrum of H_3



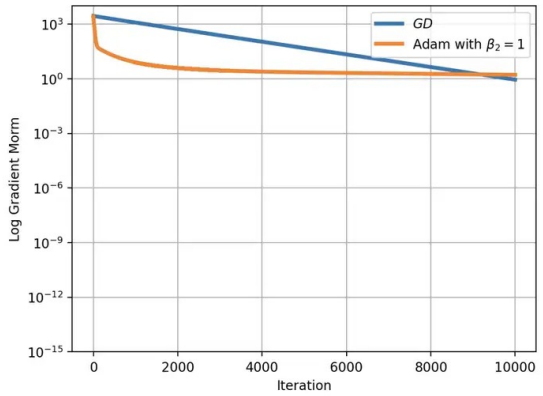
(d) Spectrum of H_4



GD is similar as Adam

Case 4: H with simplified **homogeneous** spectra

Eigenvalues of H_l : { 1, 99, 1998 } , { 2, 100, 1999 } , { 3, 101, 2000 }



GD is similar as Adam

Remark:
Same condition number for case 1 & 3
All eigenvalues are the same for case 2 & 4
but the performance is different, due to **homo & heterogeneity**

Theoretical results

A well-known result for GD: Consider $\min_w f(w) = \frac{1}{2} w^T H w$, where H is PD, then there exits a H and w^0 :

$$f\left(w_{GD}^{t+1}\right) - f^* \geq \left(1 - \frac{2}{\kappa}\right)\left(f(w_{GD}^t) - f^*\right)$$

where $\boldsymbol{\kappa}$ is the condition number of H

Theorem 1(Adam): Consider $\min_w f(w) = \frac{1}{2} w^T H w$, where H a block-diagonal PD matrix with L blocks, then:

$$f\left(w_{Adam}^{t+1}\right) - f^* \leq \max_{l \in [L]} \left(1 - \frac{1}{\kappa_{Adam,l}}\right)\left(f\left(w_{Adam}^{t+1}\right) - f^*\right)$$

where $\kappa_{Adam,l} = r\,\boldsymbol{\kappa_l}$, $\boldsymbol{\kappa_l}$ is the condition number of H_l; r is a constant related to initialization w^0

Comparing Two Results

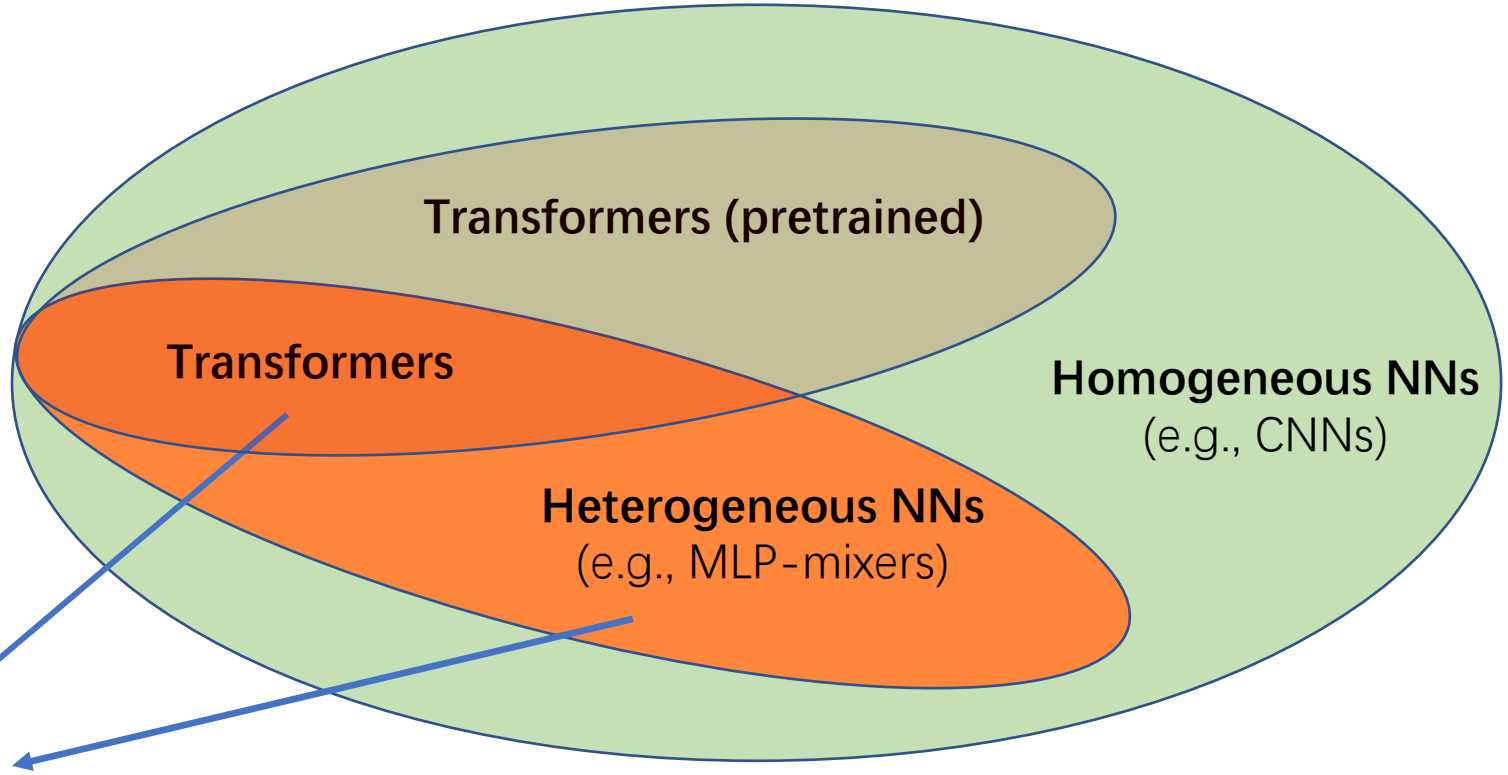
- **Compare GD vs Adam:**
  -Adam is faster than GD when $r \, \boldsymbol{max_l} \, \boldsymbol{\kappa_l} \leq \boldsymbol{\kappa}$,

Happens in the heterogeneous quadratic examples 1 & 2

Quantity of Adam ~20x smaller, and Adam is also 20x faster

- **This provides a partial theoretical explanation why Adam works better than SGD on Hetergeneous case**

Summarize in one figure



SGD < Adam here!

Why is SGD slow?
-- SGD assigns **one lr for all** parameter blocks
-- Cannot handle heterogeneity across blocks

Why Adam?
--Each block needs (at least) one customized lr
-- could be provided by v

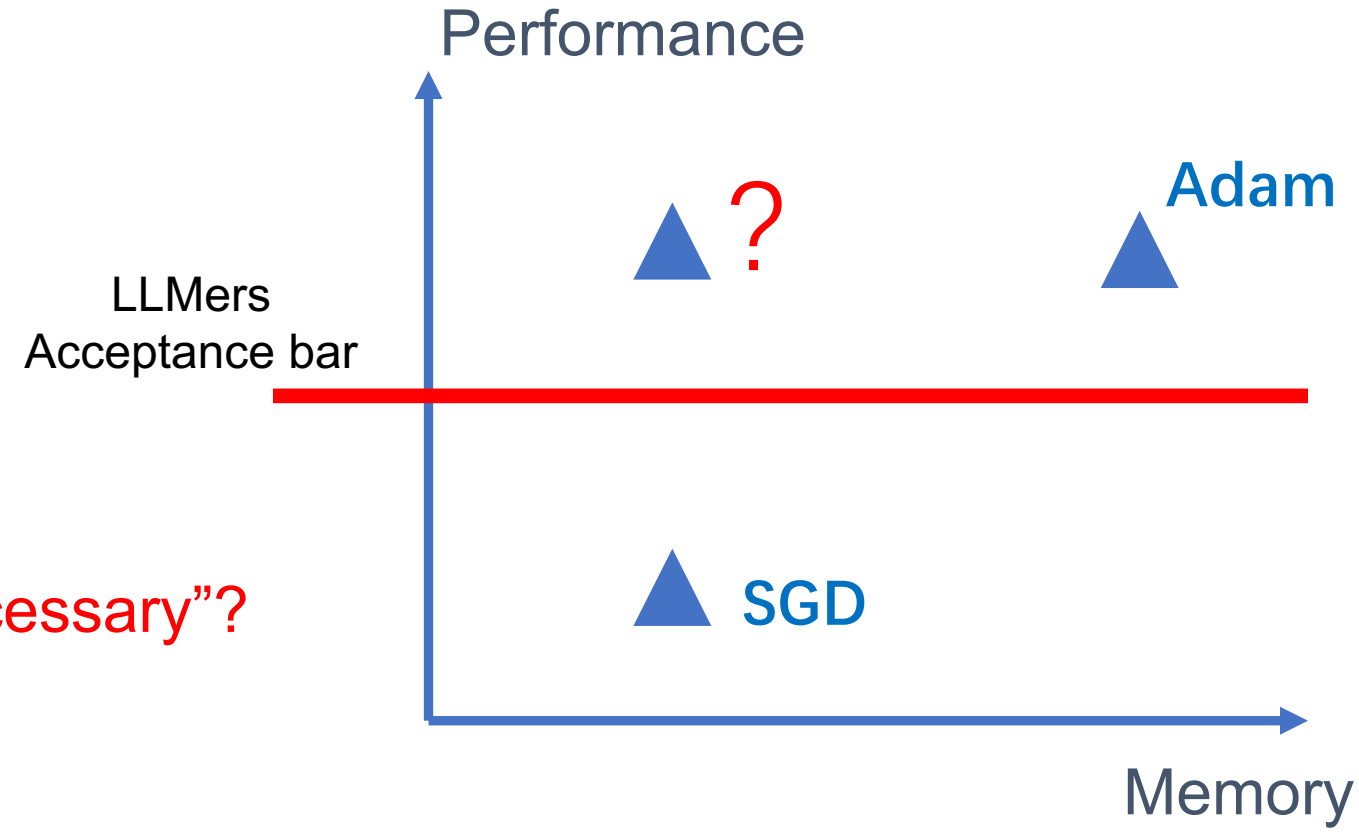
Contents

Is Adam really “necessary”?

But… this mainly shows:

SGD is not sufficient,
Adam is “sufficient”

Question: Is Adam really“necessary”?



How to slim down Adam?

Major difference of Adam with SGD: its diagonal preconditioner

$$w \leftarrow w - \eta \; D \circ m$$

-- SGD: $D_{SGD} = I$

-- Adam: $D_{Adam} = Diag(\frac{1}{\sqrt{v_1}}, \frac{1}{\sqrt{v_2}}, \dots, \frac{1}{\sqrt{v_2}})$

- Why D_{Adam} helps: D_{Adam} assigns different lrs for each parameters
- In optimization theory: converges faster when $\kappa(D_{Adam}H) \leq \kappa(H)$
- **Caveat**:
  D_{Adam} is not always effective!
  Related to an old topic in linear algebra

A bit of history: diagonal preconditioner

Q1: For what kind of Hessian H do we have $\kappa(D_{Adam}H) \leq \kappa(H)$?

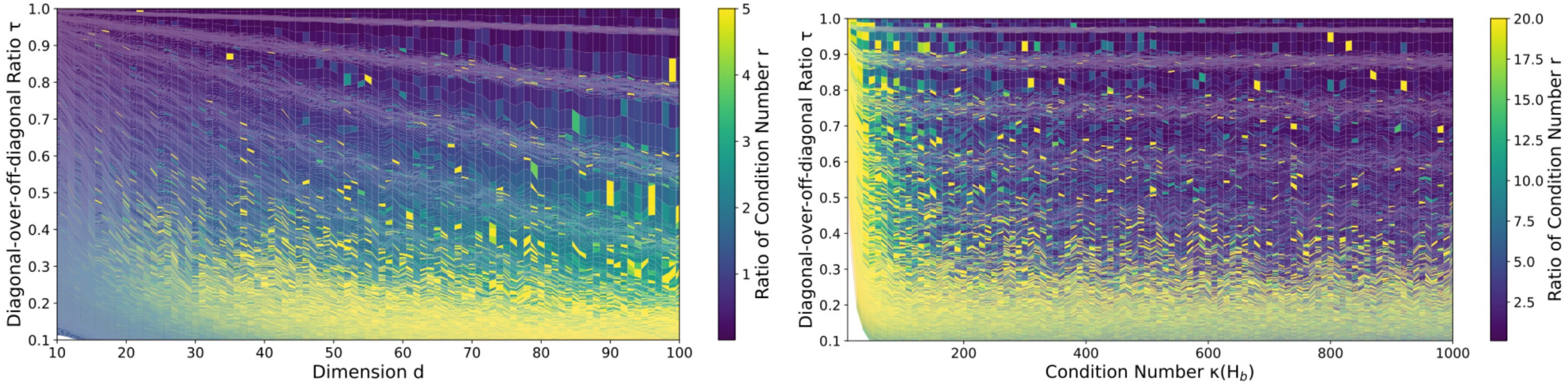
- This is a pure linear algebra problem, but NOT easy to answer…
- In **[1]:** A similar question for $D_{Jacobi} = Diag(\frac{1}{h_{11}}, \ldots \frac{1}{h_{nn}})$, not well answered so far

- We still lack theoretical understanding of D_{Adam}

Q1 (numerical-version): what Hessian structure does Neural Nets have?
Is D_{Adam} effective on this class of H?

[1] Worst-case Complexity of Cyclic Coordinate Descent, **Sun** and Ye, 2017, Mathematical Programming

Numerical results on random H and D_{Adam}



(a) r v.s. dimension d

(b) r v.s. dimension $\kappa(H_b)$

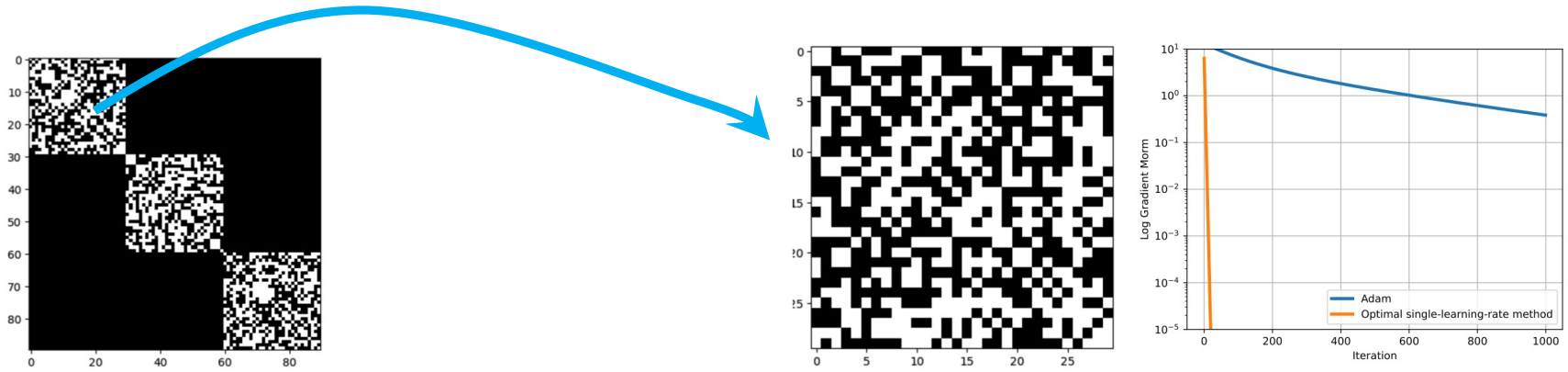
$$\tau = \frac{\sum_i |H_{b,i,i}|}{\sum_{i,j} |H_{b,i,j}|}, \quad r = \frac{\kappa(D_{\text{Adam}} H_b)}{\kappa(H_b)},$$

$\tau \to 1 : H \to$ pure diagonal

Observation: D_{Adam} is NOT effective when H is dense

How effective is D_{Adam} on dense block?

$\min_x \frac{1}{2} x^T H x$, where $H = Diag(H_1, H_2, H_3), H_i$ are random PD (dense) matrices



(a) Hessian matrix (c) Dense sub-block (d) Sub-problem loss

- **Another Case: Dense block.**
  We take the 1st sub-block H_1 in (a) and use it for a new problem (c)

-- Figure (c): **GD with (a different) optimal lr** outperforms **Adam**,
even though Adam uses more lr!
-- This means: D_{Adam} is NOT so effective on H_1!

Our Explanation: Why Transformer Needs Adam

Observation 1:
Adam is good for block-Hessian.

Previous Part 1

Observation 2:
Adam is bad for dense Hessian

Previous slide

Together reveals:

Implication:
Adam mainly handles "cross-block" challenge,
NOT "within-block" challenge.

Further Implication:
We may replace Adam's coordinate-wise lr by block-wise lr

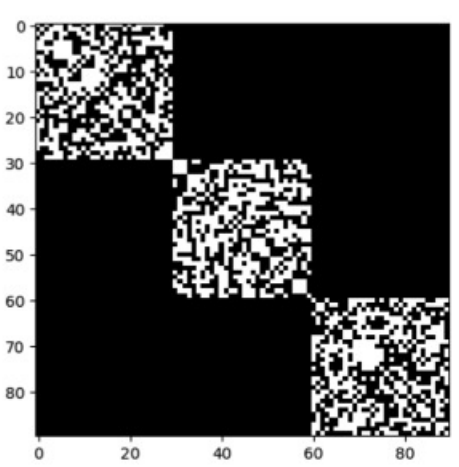
How effective is D_{Adam} on this block-diagonal Hessian?

- We explore it numerically on quadratic functions:

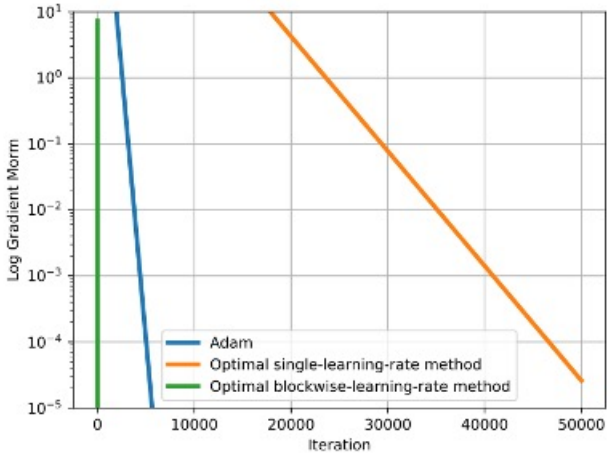
$$\min_x \frac{1}{2} x^T H x, \text{ where } H = Diag\,(H_1, H_2, H_3), H_i \text{ are random}$$

Algorithm (block-wise optimal lr method):
-- Collect optimal lr's for each block
-- Apply them to **"blockwise" version of GD,**

Observation: Figure (b): **blockwise GD** outperforms Adam with only 3 learning rates!



(a) Hessian matrix



(b) Total loss

Using Fewer Learning Rates?

- More lrs do not neccessarily bring extra gain
  (This reveals a drawback of design in $Adam$)
- For each block, a single **but good** lr can outperform $Adam$
- But how to find these good lrs without grid-search?

Adam-mini (Framework)

- **Adam-mini:**
  - **Step 1**: partition the gradient g into B sub-vectors according to the dense Hessian sub-block $g_b, b = [B]$
  - **Step 2:** for each g_b, calculate:

$$\boxed{v_b = (1-\beta_2) * \mathbf{mean}(g_b \circ g_b) + \beta_2 * v_b, \quad b = 1, \cdots B}$$

  - **Step 3:** then use $\frac{\eta}{\sqrt{v_b}}$ as the lr for the parameters associated with g_b

- **Step 1 is important, and will be discussed later.**

Adam-mini: an illustration

- Illustration: For a problem with 5 parameters, $w \leftarrow w - \eta\, u \circ m$

  Adam: u = $(\frac{1}{\sqrt{v_1}}, \frac{1}{\sqrt{v_2}}, \frac{1}{\sqrt{v_3}}, \frac{1}{\sqrt{v_4}}, \frac{1}{\sqrt{v_5}})$

  Adam-mini: if block partition is (1,2,3); (4,5), then

  u = $(\frac{1}{\sqrt{(v_1+v_2+v_3)/3}}, \frac{1}{\sqrt{(v_1+v_2+v_3)/3}}, \frac{1}{\sqrt{(v_1+v_2+v_3)/3}}, \frac{1}{\sqrt{(v_4+v_5)/2}}, \frac{1}{\sqrt{(v_4+v_5)/2}})$

- Benefits: reduce # learning rates: from # parameters to # blocks
- For LLMs, we will show that this would free ≥ 90% elements in v
- **Remark:** Cheap way to find "good lrs" , but might not be optimal
- **Remaining question:** How to partition parameters for a given problem, e.g., Transformers?

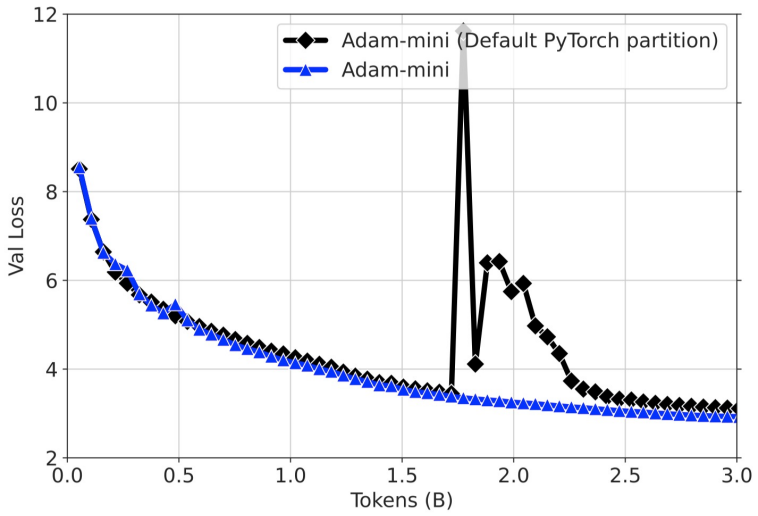
Parameter Partition: Failed Attempt

Failed Attempt:

- Default PyTorch partition strategy **(layer-by-layer)** is a naive candidate

- Unfortunately, this default strategy over-simplifies the problem

- Observe **training instability** on 1B models

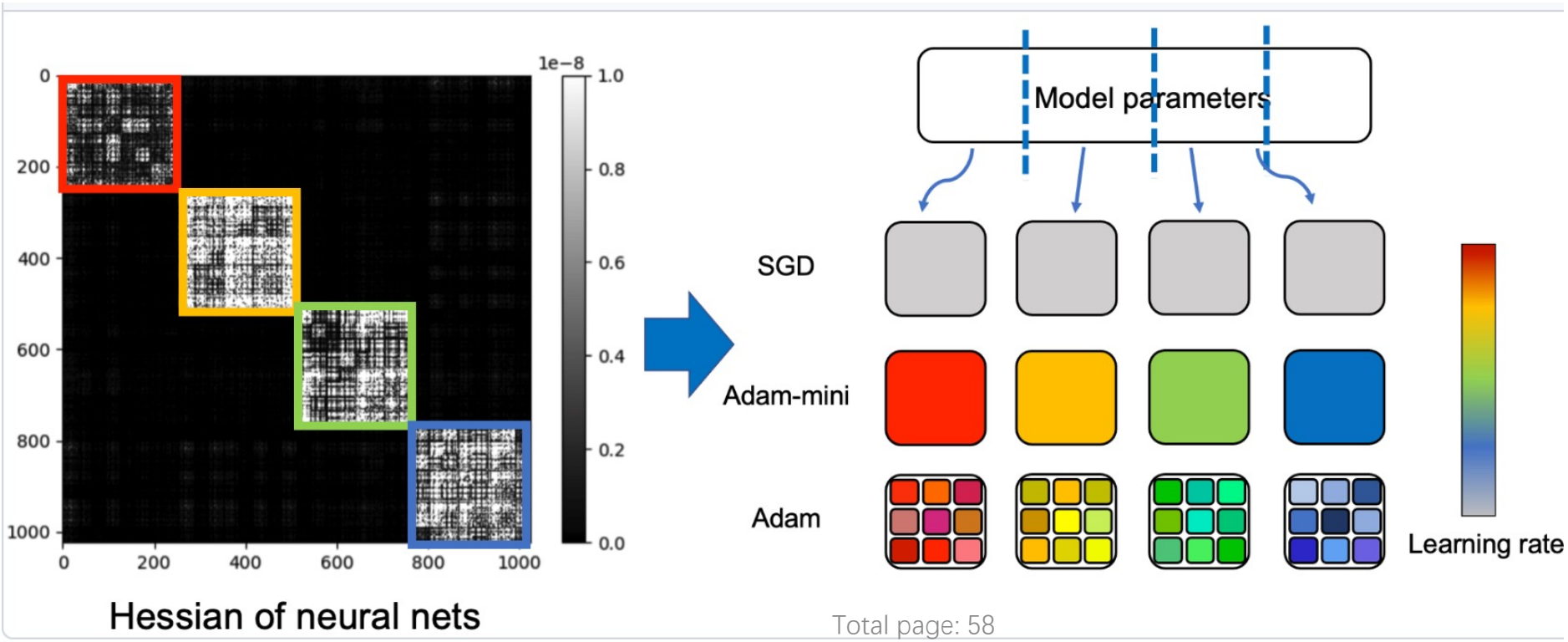


Why?

We suspect the default PyTorch partition did not fully capture the **Hessian structure**

Partition Principle

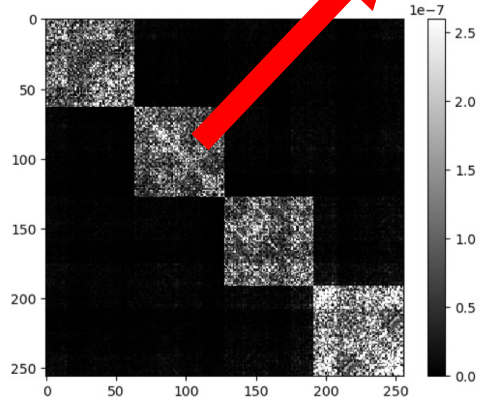
Partition Principle:
Partition parameters into blocks s.t. each block is associated with a dense sub-block in Hessian.



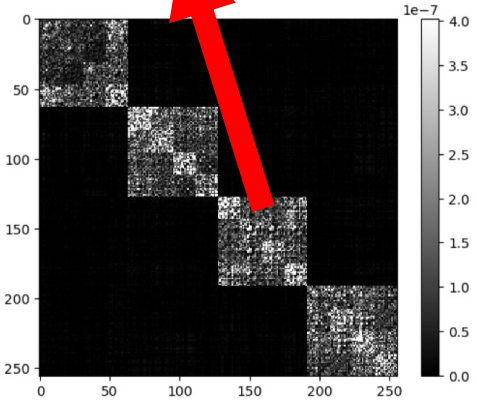
Applying Principle to Transformer **(non-equal sized blocks)**

#blocks = **#attention heads**

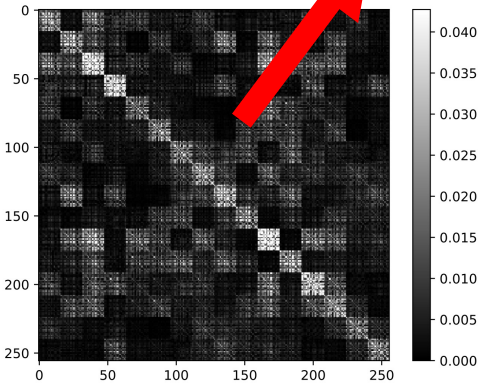
Less clear (treat as **#output neurons**)



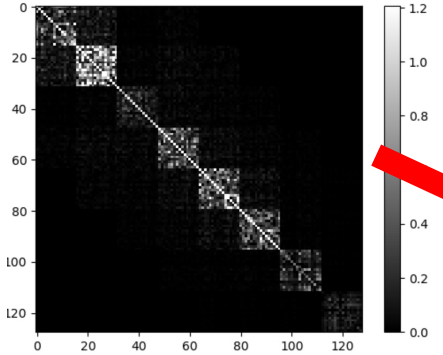
(a) `query` (4 heads)



(b) `key` (4 heads)

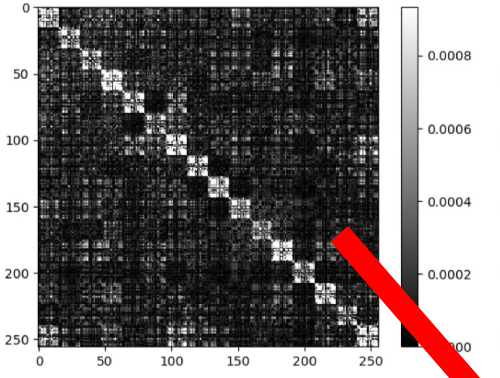


(c) `value` (4 heads)

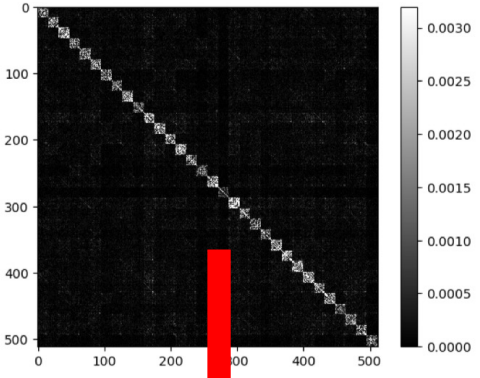


Embedding layer (8 tokens)

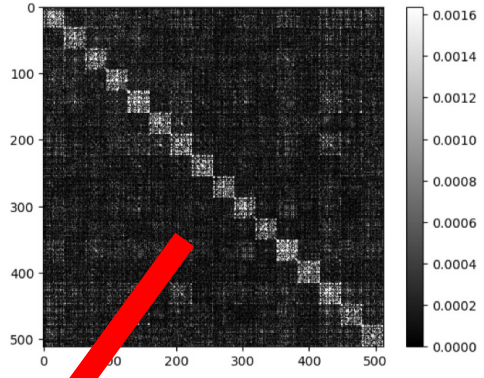
#blocks = **#tokens**



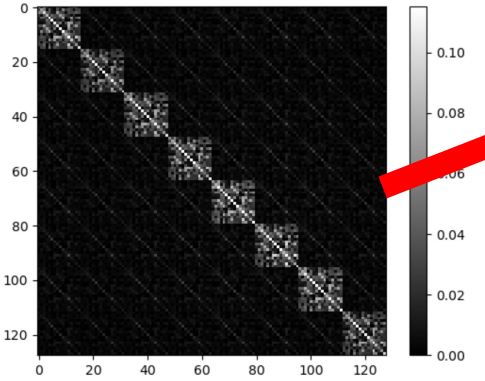
(d) `attn.proj` (16 neurons)



(e) `mlp.fc1` (32 neurons)



(f) `mlp.proj` (16 neurons)



Output layer (8 tokens)

#blocks = **#output neurons**

Transformer Partition Strategy

General Partition Principle:
Partition parameters into blocks s.t. each block is associated with a dense sub-block in Hessian.

Partition Rules for Transformers:

-- For Q & K: each head is a block.

-- For V, attn.proj, mlp.fc1, mlp.proj: each output neuron is a block.

-- For embed & output layer: each token is a block

Complete form of Adam-mini

Algorithm 1 Adam-mini in Pytorch style

Input weight-decay coefficient λ and current step t
Choose `param_blocks` from **Algorithm 2 or 3**
Choose `embd_blocks` from **Algorithm 4**
for `name, param` in `param_blocks` **do**
  g = `param.grad`
  `param` = `param` - $\eta_t * \lambda *$ `param`
  $m = (1-\beta_1) * g + \beta_1 * m$
  $\hat{m} = \frac{m}{1-\beta_1^t}$
  if `param` in `embd_blocks` **then**
    $v = (1-\beta_2) * g \circ g + \beta_2 * v$
  else
    $v = (1-\beta_2) * \mathbf{mean}(g \circ g) + \beta_2 * v$
  end if
  $\hat{v} = \frac{v}{1-\beta_2^t}$
  `param` = `param` - $\eta_t * \frac{\hat{m}}{\sqrt{\hat{v}}+\epsilon}$
end for

Algorithm 2 Partition for Transformers

```
param_blocks = {}
for name, param in parameters do
  if name is Query or Key then
    Partition param by heads as param[0..heads-1]
    for i = 0...heads-1 do
      param_blocks[name+i]=param[i]
    end for
  else
    param_blocks[name]=param
  end if
end for
return param_blocks
```

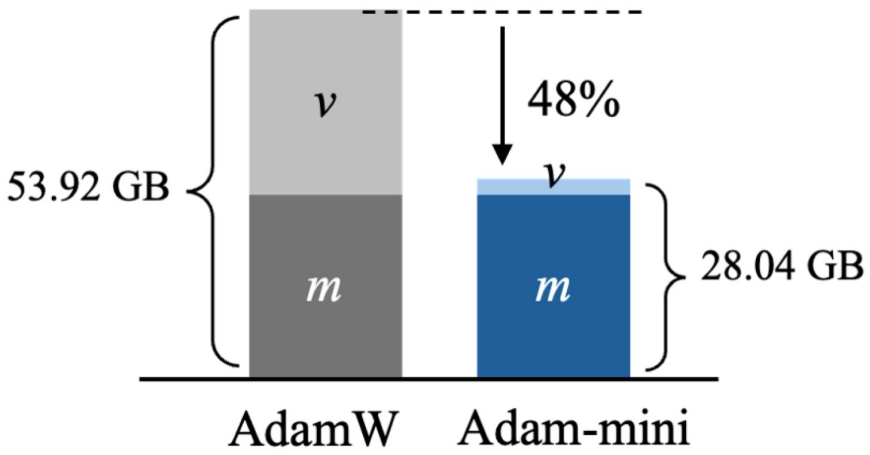
Algorithm 3 Partition for non-Transformers

```
param_blocks = {}
for name, param in parameters do
  param_blocks[name]=param
end for
return param_blocks
```

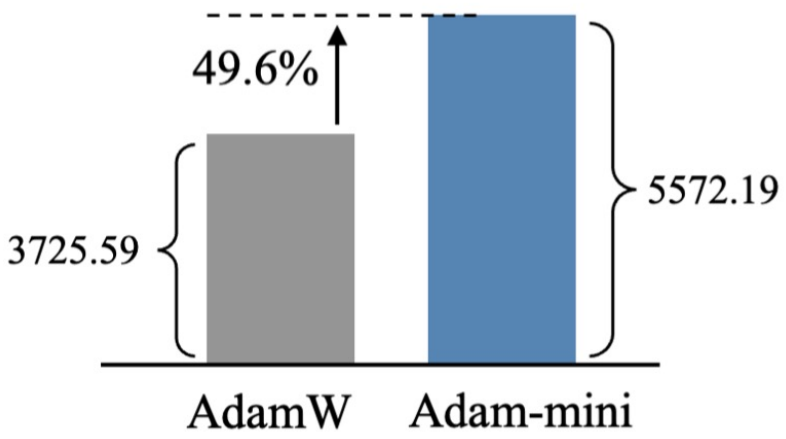
Algorithm 4 Get_embd_blocks

```
if Transformer then
  return [Embedding layer, Output layer]
else
  return []
end if
```

Memory cut down & Throughput enhancement



(a) Memory (↓)



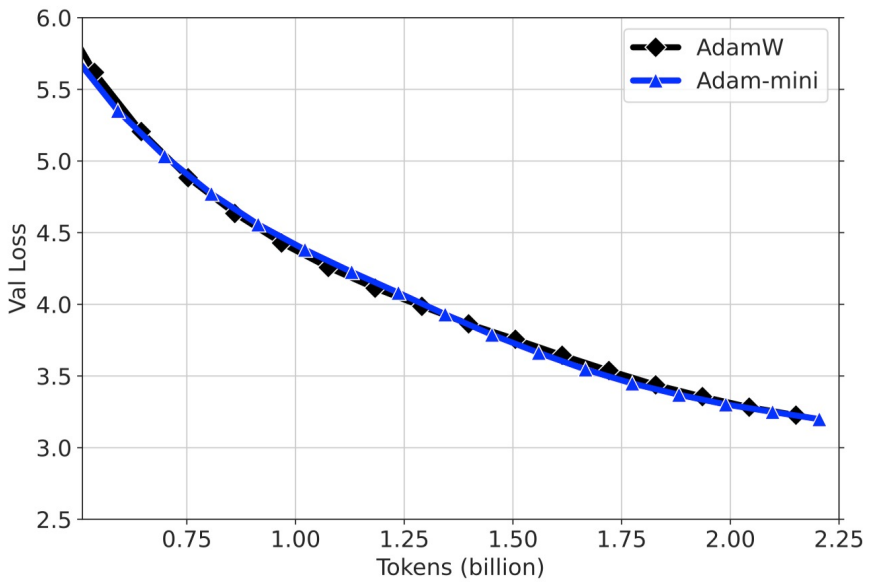
(b) Throughput (↑)

Saves about **50%** memory of Adam

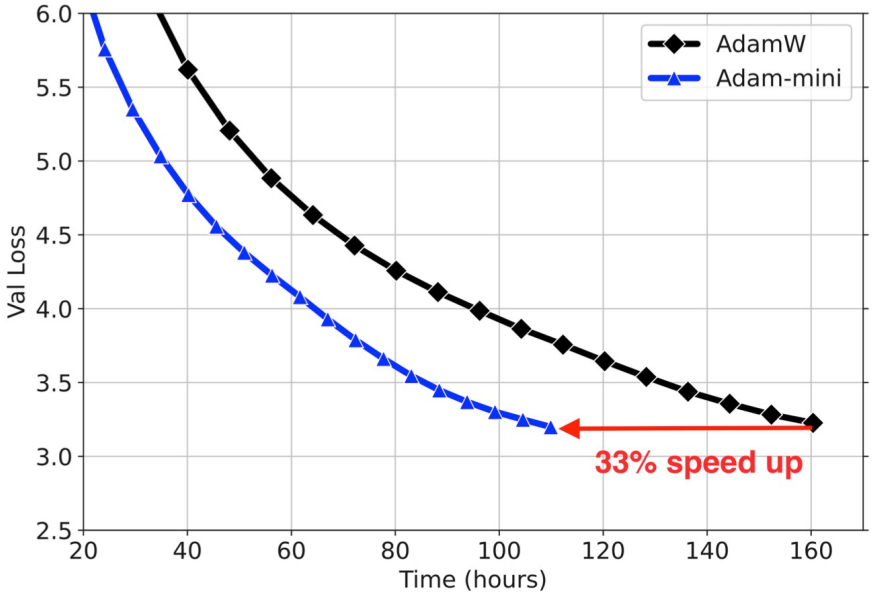
Can increase about **50%** throughput of Adam
(# processed data per second)

Why? Reduce communication + larger batch size per GPU

Llama2-7B: pre-training



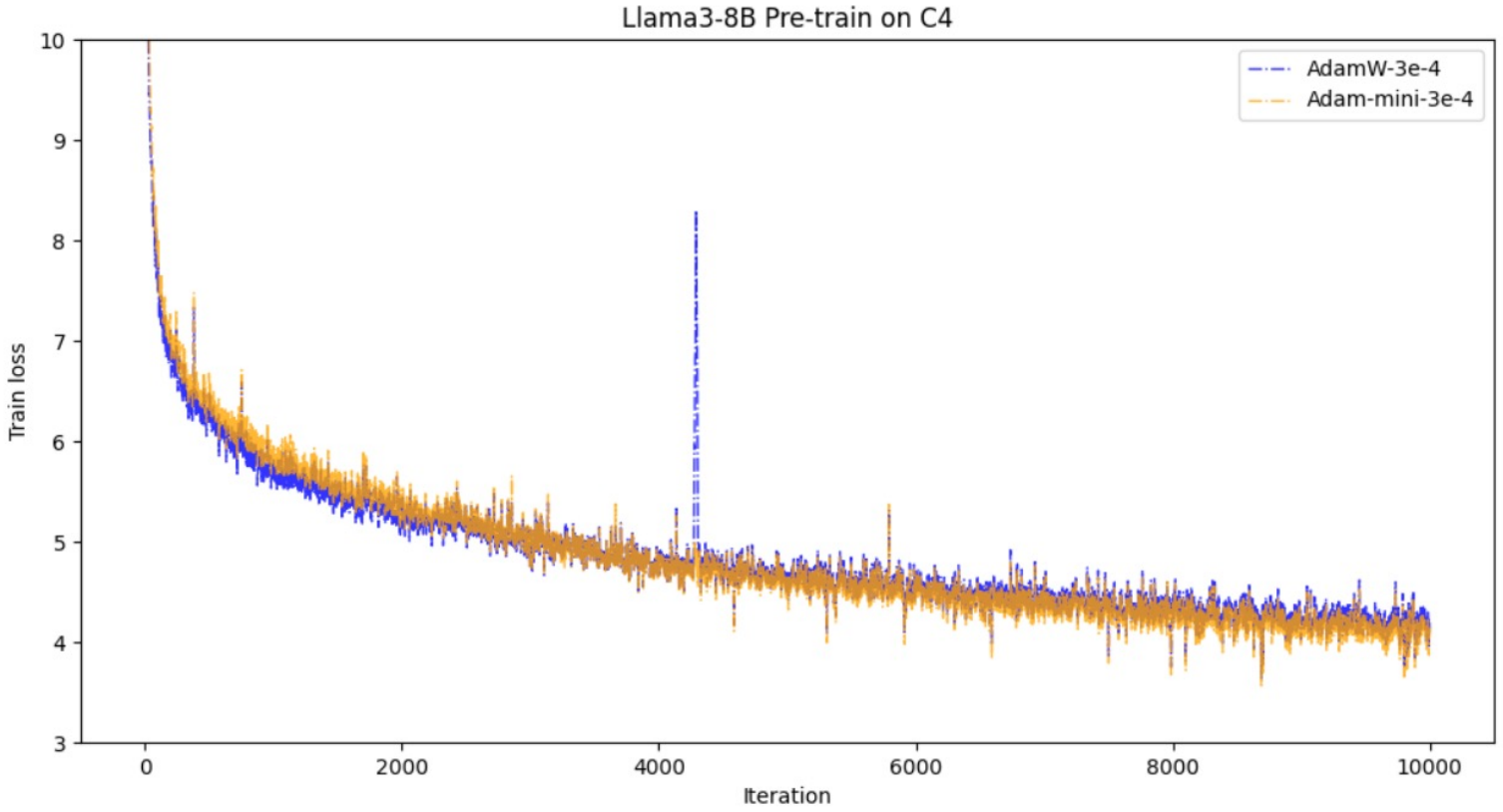
(b) Loss v.s. iteration



(c) Loss v.s. time

- Same loss curve as Adam
- **33% less time** to process the same # tokens (tested on 2x A800-80GB GPUs)

LLama3-8B Pretrain: **Independent verifier from PyTorch team**



lessw2020 commented 5 days ago • edited Author

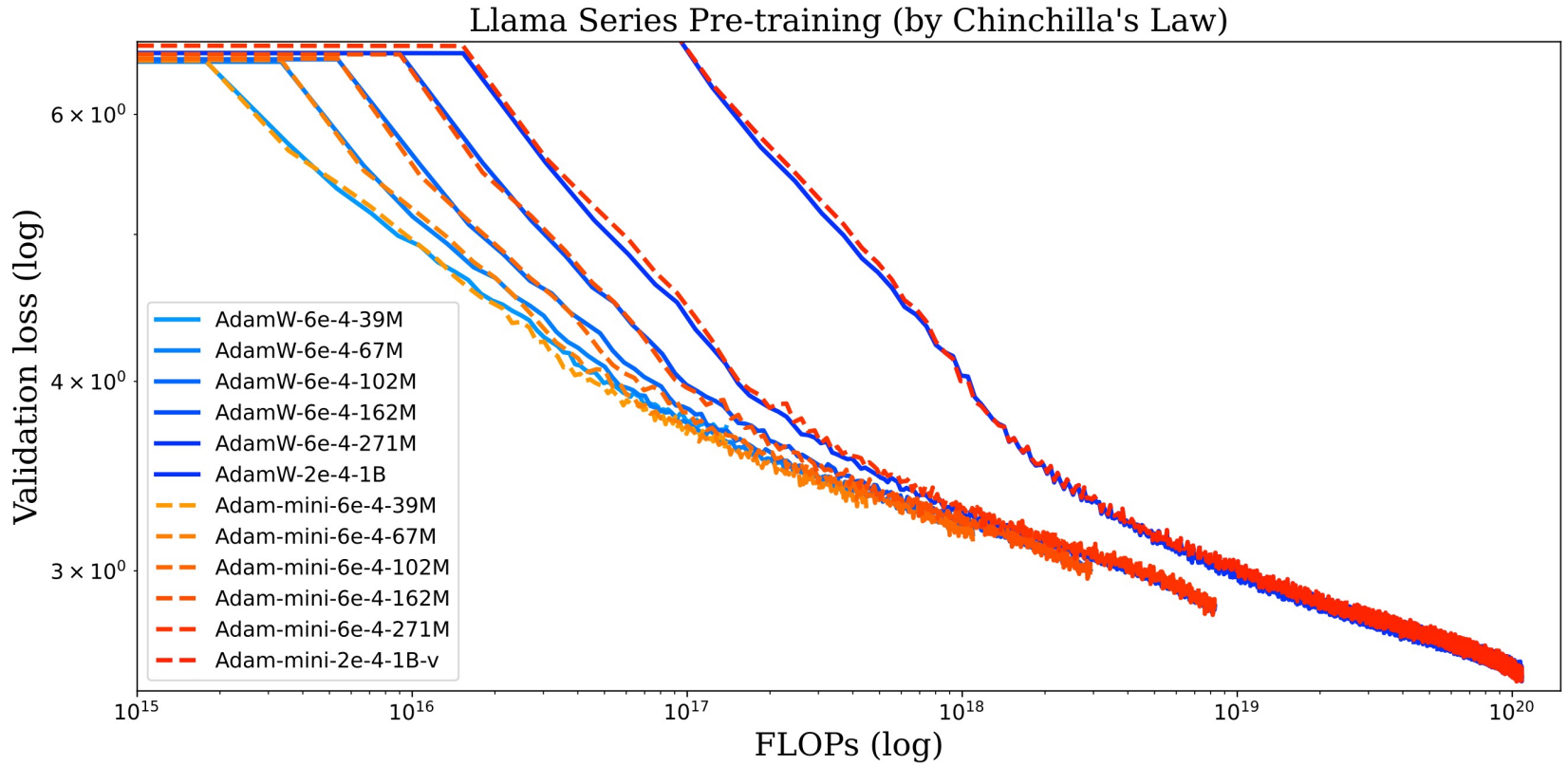
Hi **@zyushun** - congrats! With a slight bump in lr (3e-4 mini vs 1e-4 adamw) and mini shows very similar curves but with overall outperformance! This is imo a very big accomplishment as most optimizers can't do this (meet / exceed adamw) at 8B scale and esp not while reducing memory so significantly.

Highlight:

"This is imo a very big accomplishment as most optimizers can't do this (meet / exceed adamw) at 8B

… and especially not while reducing memory so significantly"

Scaling laws of Adam-mini: from 39M to 1B



Total cost for this figure:
About 300 GPU hours
on 4x A800-80GB GPUs

- We train Llama series (from 39M to 1B) for complete pre-training runs ("complete" under the definition of Chinchila's law: # data= 20 * # parameters)
- For all models, **Adam-mini** performs similarly to **AdamW**

This serves as an evidence that **Adam-mini** can work on larger models, e.g., 30B, 100B (if the scaling law holds)

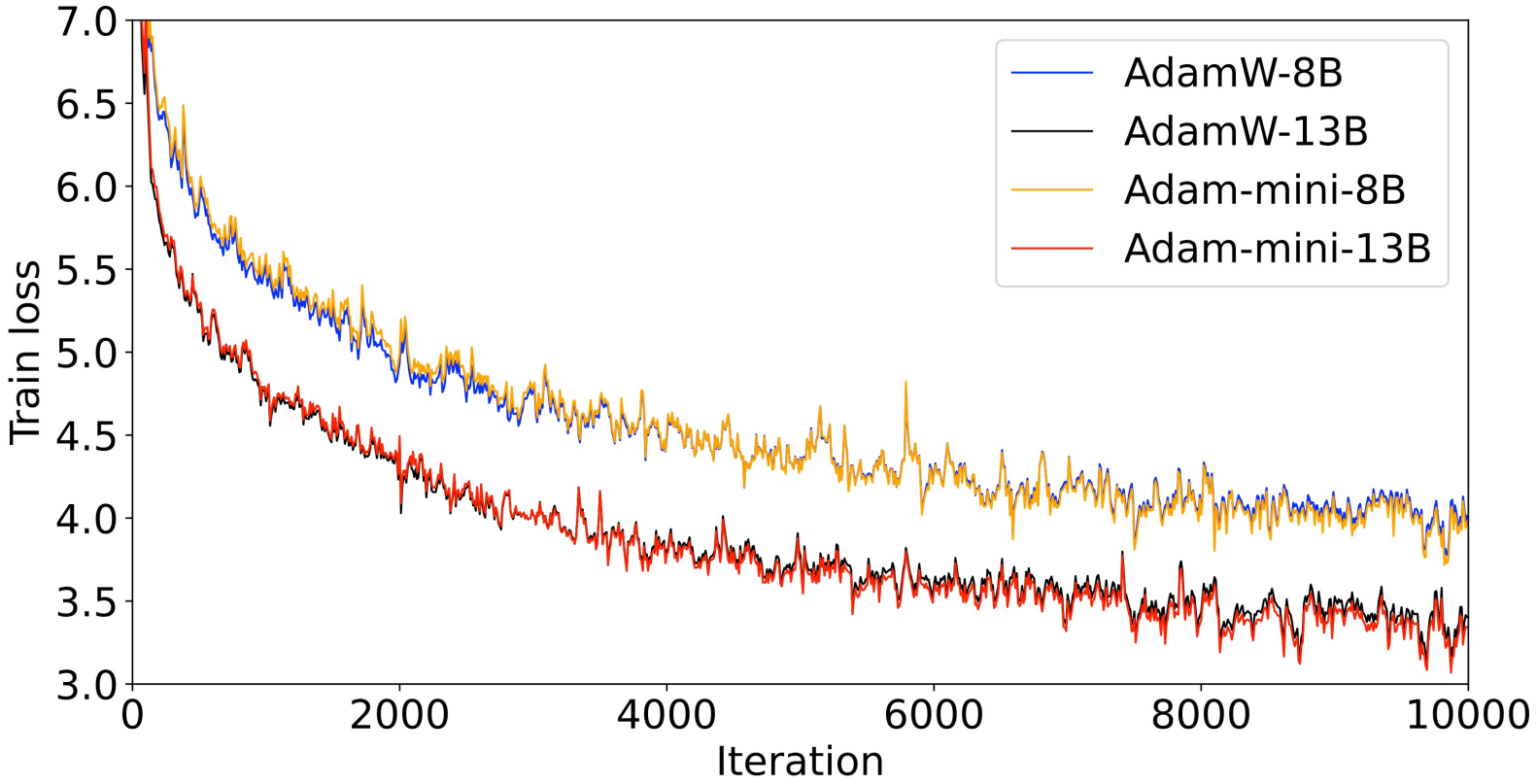
Scaling laws of Adam-mini: from 39M to 1B

Model size	39M	67M	102M	162M	271M	1B
Total tokens	1.02B	1.76B	2.67B	4.25B	7.10B	26.21B
AdamW	41.741	29.413	23.873	20.149	17.178	12.810
Adam-mini	**38.696**	**27.093**	**23.038**	**19.645**	**17.035**	**12.753**

- We train Llama series (from 39M to 1B) for complete pre-training runs ("complete" under the definition of Chinchila's law: # data= 20 * # parameters)
- For all models, **Adam-mini** performs slightly better than **AdamW**

This serves as an evidence that **Adam-mini** can work on larger models, e.g., 30B, 100B (if the scaling law holds)

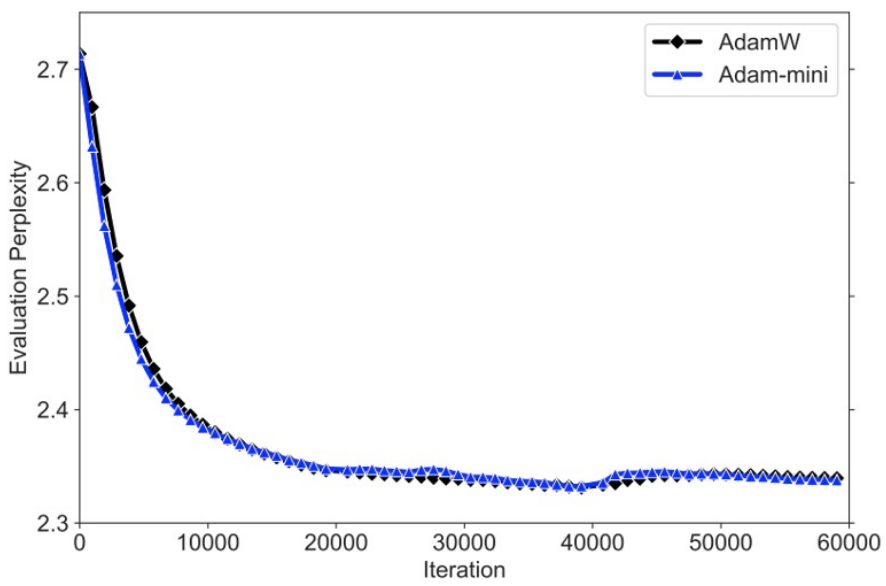
Llama 3-8B and Llama 2-13B



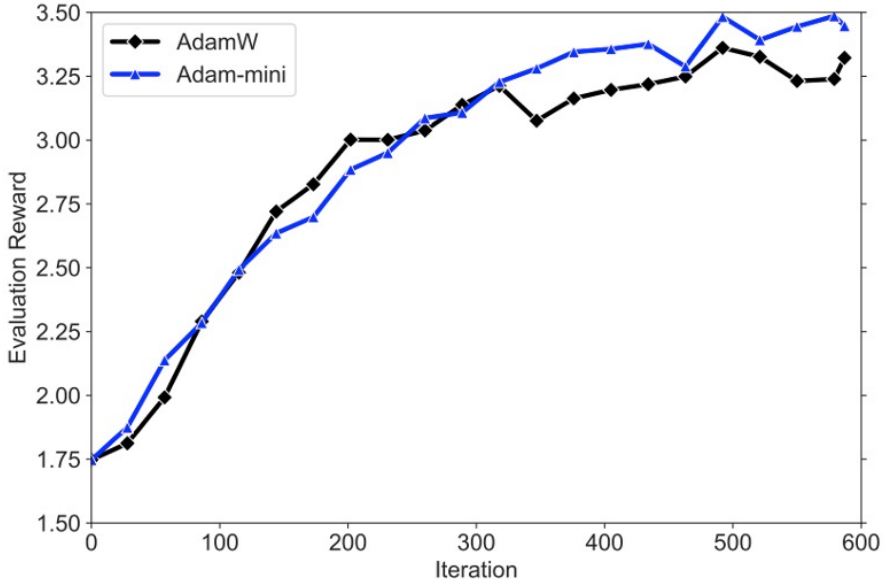
Adam-mini performs slightly better than **AdamW,** with **50%** less memory

Llama2-7B: SFT and RLHF

Finetuning tasks for Llama2-7B pre-trained model (released by Meta).



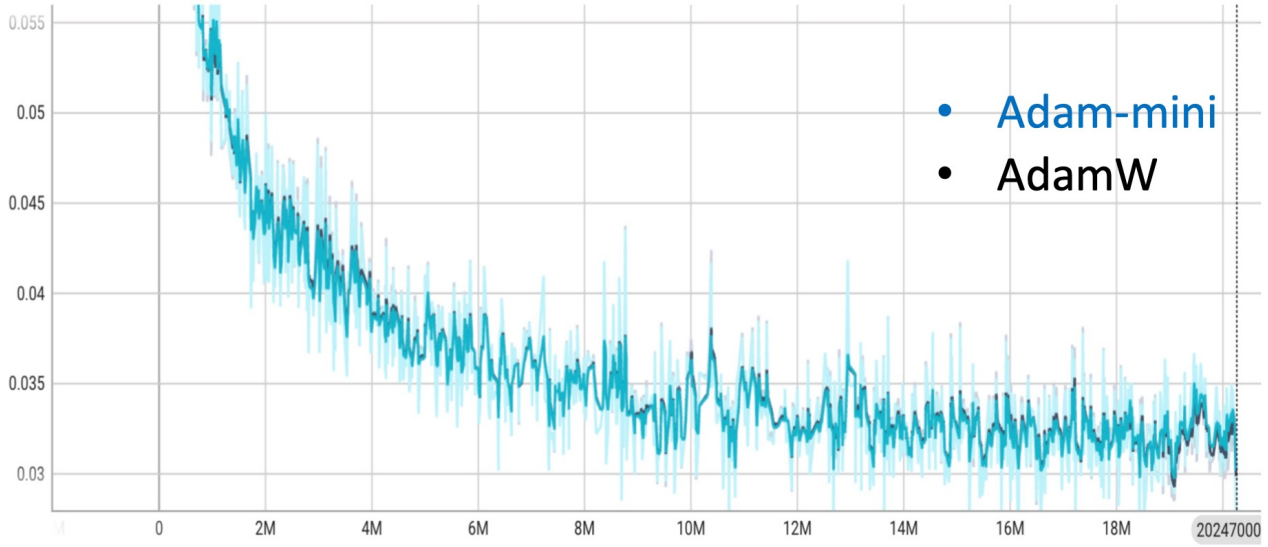
(b) SFT



(c) RLHF

Adam-mini performs slightly better than **AdamW**, with **50%** less memory

Diffusion models

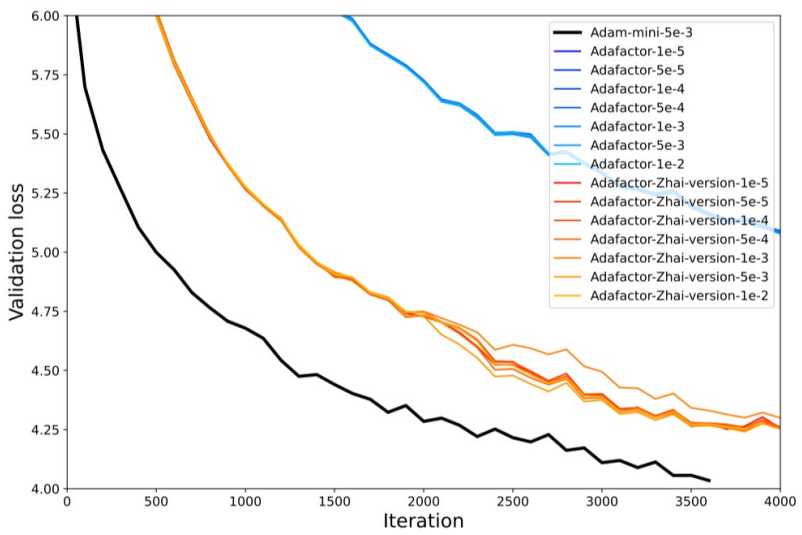


Diffusion model training:
Loss vs. iteration

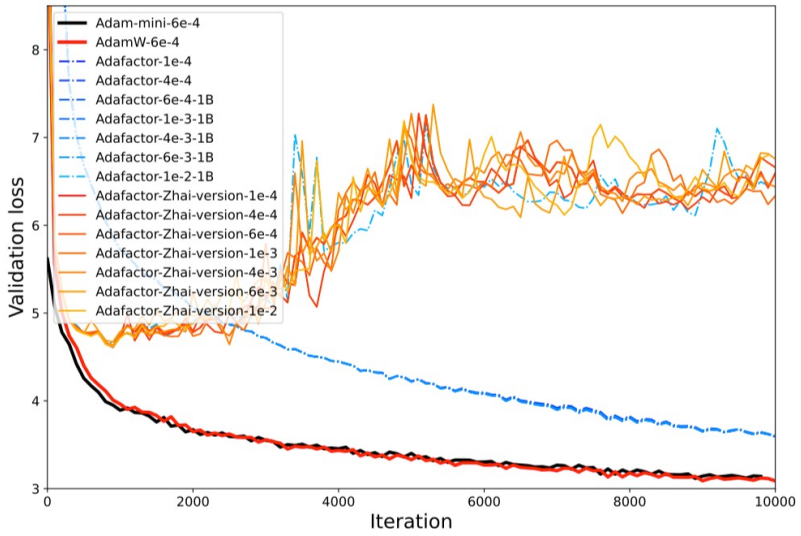
Independent verifier on twitter:
SDXL: Stable Diffusion XL **(sized 2.6B)**
One of the SOTA Diffusion model

Adam-mini performs slightly better than **AdamW**, with **50%** less memory

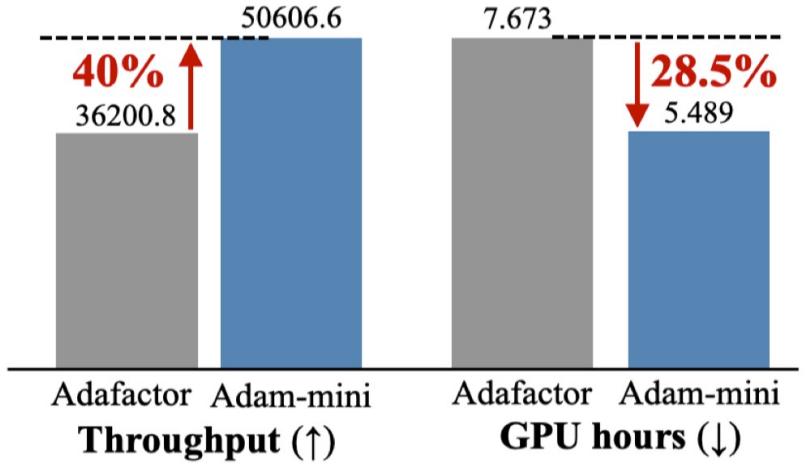
Comparison to Adafactor (variants)



(a) Llama 2-20M



(b) Llama 2-1B



(c) Throughput comparison

We did NOT find the good hyperparams for Adafactor to work
Further, Adafactor **has higher latency** (due to more matrix produts)

Summary

- We provide an explanation why Transformer needs Adam, not SGD

  Hetereogeneity of block-Hessian-spectra causes SGD to underperform Adam

- We propose a 50%-memory-saving variant of Adam: Adam-mini

  Two features: Principled block partition; block-mean of v

How to Use? Just 1-line code change

```
pip install adam-mini
```

```
from adam_mini import Adam_mini
```

```
optimizer = Adam_mini(
            named_parameters = model.named_parameters(),
            lr = lr,
            betas = (beta1,beta2),
            eps = eps,
            weight_decay = weight_decay,
            model_sharding = True,
            dim = model_config.dim,
            n_heads = model_config.n_heads,
            n_kv_heads = model_config.n_kv_heads,
            )
```

Same values as AdamW!

Your model config

We support: DDP, FSDP, Deepspeed, Torchtitan, HF trainer 🤗

Code: https://github.com/zyushun/Adam-mini

👆 Code for Adam-mini
Currently:
-- 300+ stars
-- 1500+ download via pip install
(in the last two weeks)

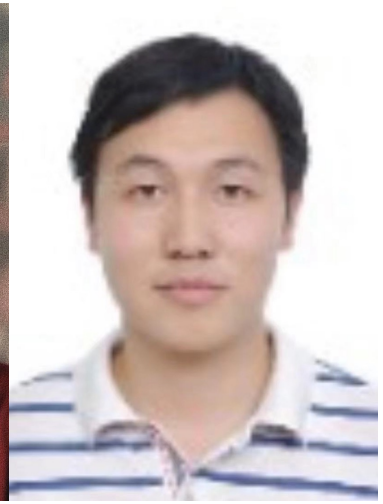
If you like Adam, Adam-mini is a no-brainer switch!

Mainly based on:

- **Zhang**, Chen, Ding, Li, Sun, & Luo, Why Transformers Need Adam: A Hessian Perspective, NeurIPS 24
- **Zhang***, Chen*, Li, Ding, Chen, Ye, Luo & Sun, Adam-mini: Use Fewer Learning Rate To Gain More, arxiv preprint.
- **Thanks to all the collaborators!**

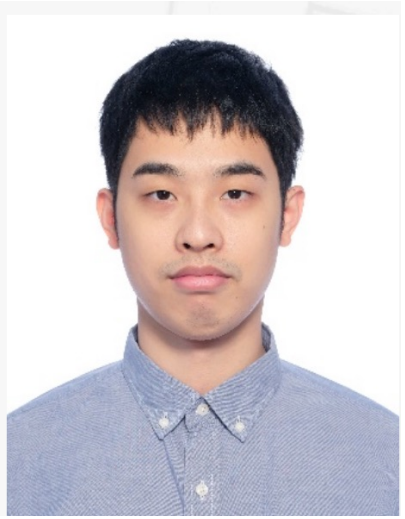
Yushun Zhang

Congliang Chen



Ziniu Li

Tian Ding



Ruoyu Sun

Zhi-Quan Luo