

Homework #3

1. Microsoft .NET provides a synchronization primitive called a `CountdownEvent`. Programs use `CountdownEvent` to synchronize on the completion of many threads (similar to `CountDownLatch` in Java). A `CountdownEvent` is initialized with a count, and a `CountdownEvent` can be in two states, nonsignalled and signalled. Threads use a `CountdownEvent` in the nonsignalled state to `Wait` (block) until the internal count reaches zero. When the internal count of a `CountdownEvent` reaches zero, the `CountdownEvent` transitions to the signalled state and wakes up (unblocks) all waiting threads. Once a `CountdownEvent` has transitioned from nonsignalled to signalled, the `CountdownEvent` remains in the signalled state. In the nonsignalled state, at any time a thread may call the `Decrement` operation to decrease the count and `Increment` to increase the count. In the signalled state, `Wait`, `Decrement`, and `Increment` have no effect and return immediately.

- (a) Use pseudo-code to implement a thread-safe `CountdownEvent` using locks and condition variables by implementing the following methods:

```
class CountdownEvent {
    ...private variables...
    CountdownEvent (int count) { ... }
    void Increment () { ... }
    void Decrement () { ... }
    void Wait () { ... }
}
```

Notes:

- The `CountdownEvent` constructor takes an integer count as input and initializes the `CountdownEvent` counter with count. Positive values of count cause the `CountdownEvent` to be constructed in the nonsignalled state. Other values of count will construct it in the signalled state.
- `Increment` increments the internal counter.

- Decrement decrements the internal counter. If the counter reaches zero, the CountdownEvent transitions to the signalled state and unblocks any waiting threads.
- Wait blocks the calling thread if the CountdownEvent is in the nonsignalled state, and otherwise returns.
- Each of these methods is relatively short.

Answer:

```
class CountdownEvent {
    int counter;
    bool signalled;
    Lock lock;
    Condition cond;

    CountdownEvent(int count) {
        counter = count;
        if (counter > 0) {
            signalled = false;
        } else {
            signalled = true;
        }
        lock = new Lock();
        cond = new Condition();
    }

    void Increment() {
        lock.Acquire();
        if (signalled == false) {
            counter++;
        } // otherwise do nothing if already signalled
        lock.Release();
    }

    void Decrement() {
        lock.Acquire();
        if (signalled == false) {
            counter--;
            if (counter == 0) {
```

```

        signalled = true;
        cond.Broadcast();
    }
} // otherwise do nothing if already signalled
lock.Release();
}

void Wait () {
    lock.Acquire();
    if (signalled == false) {
        cond.Wait(&lock);
    } // otherwise do nothing if already signalled
    lock.Release();
}
}

```

- (b) Semaphores also increment and decrement. How do the semantics of a CountdownEvent differ from a Semaphore?

Answer: Their semantics differ in a number of ways. Semaphores implement atomic counters, and blocking depends upon the internal state of the counter. Threads always explicitly block on CountdownEvents by calling Wait; threads may block on Semaphores when calling Acquire/P/Decrement, but not always. A CountdownEvent is a “one-shot” primitive: once a CountdownEvent is signalled, its methods are essentially no-ops. Semaphores can go back and forth between blocking and passing, entirely depending on the counter state. Semaphores block when the counter is nonpositive; CountdownEvents block only when positive. Incrementing a Semaphore unblocks one waiting thread; CountdownEvents wake all waiting threads.

2. A common pattern in parallel scientific programs is to have a set of threads do a computation in a sequence of phases. In each phase i , all threads must finish phase i before any thread starts computing phase $i + 1$. One way to accomplish this is with barrier synchronization. At the end of each phase, each thread executes `Barrier::Done(n)`, where n is the number of threads in the computation. A call to `Barrier::Done` blocks until all of the n threads have called `Barrier::Done`. Then, all threads proceed. You may assume that the process allocates a new Barrier for each iteration,

and that all threads of the program will call Done with the same value.

- (a) Implement a Barrier using a CountdownEvent in the previous exercise.

Answer:

```
class Barrier {
    CountdownEvent ce;

    Barrier (int n) {
        ce = new CountdownEvent (n);
    }

    void Done () {
        ce.Decrement ();
        ce.Wait ();
    }
}
```

- (b) Write a monitor that implements Barrier using Mesa semantics.

Answer:

```
monitor Barrier {
    int called = 0;
    Condition barrier;

    void Done (int needed) {
        called++;
        if (called == needed) {
            called = 0;
            barrier.Broadcast();
        } else {
            barrier.Wait();
        }
    }
}
```

- (c) Implement Barrier using an explicit lock and condition variable.

Answer:

```

class Barrier {
    int called = 0;
    Lock lock;
    Condition barrier;

    void Done (int needed) {
        lock.Acquire();
        called++;
        if (called == needed) {
            called = 0;
            barrier.Broadcast(&lock;);
        } else {
            barrier.Wait(&lock;);
        }
        lock.Release();
    }
}

```

3. Consider a problem in which there is a producer p and two consumers $c1$ and $c2$. The producer produces pairs of values $\langle a, b \rangle$. The producer does not have to wait in Put for a consumer, and the monitor will have to accumulate the values in auxiliary data structures to ensure nothing gets lost (you can assume the use of lists or arrays). Assume that Put can accumulate at most k pairs of values. Consumer $c1$ consumes the a values of these pairs and $c2$ consumes the b values of these pairs. A consumer consumes only one value per call.

Hint: This problem is very similar to the producer/consumer problem—it just so happens that objects are produced in pairs, and each part of a pair is consumed individually.

Write a Mesa-style monitor for this problem. It should have three entry methods: `void Put(int a, b)` that p would use to produce values, `int GetA(void)` that $c1$ would use to consume a values, and `int GetB(void)` that $c2$ would use to consume b values. For synchronization, you should only use condition variables.

An example sequence of calls could be:

```

Put(10,20)
GetA() -> returns 10
Put(300,400)
GetA() -> returns 300
GetB() -> returns 20
GetA() blocks the caller

```

Answer:

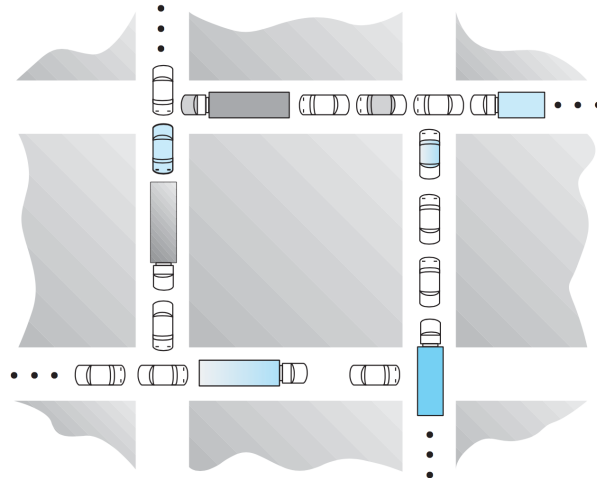
```

monitor ProCon{
    int k = k; //at most k pairs
    int ctA; //keep track until k
    int ctB; //keep track until k
    ConditionVar notEmptyA ; //count of empty buffers (all empty at start)
    ConditionVar notEmpty B; //count of empty buffers (all empty at start)
    ConditionVar notFull ; //count of full buffers (all full at start)
    List * alist = new List(k); //buffer for a's produced
    List * blist = new List(k); //buffer for b's produced
    void Put(int a, int b){
        while(ctA >= k || ctB >= k ){ wait(notFull); } //can't put unless there's space
        ctA++;
        ctB++;
        alist->Append(a); //new resource a
        blist->Append(b); //new resource b
        signal(notFull);
        signal(notEmptyA);
        signal(notEmptyB);
    }
    int GetA(void){
        while(ctA <= 0){ wait(notEmptyA); } //can't take unless not empty
        ctA--;
        return alist->Remove() //remove a from buffer
    }
    int GetB(void){
        while(true){ wait(notEmptyB); } //can't take unless full
        ctB--;
        return blist->Remove() //remove a from buffer
    }
}

```

}

4. [Silberschatz] Consider the traffic deadlock depicted in the following figure.



- a) Show that the four necessary conditions for deadlock indeed hold in this example.

Answer: The four necessary conditions for a deadlock are (1) mutual exclusion; (2) hold-and-wait; (3) no preemption; and (4) circular wait. The mutual exclusion condition holds since only one car can occupy a space in the roadway. Hold-and-wait occurs where a car holds onto its place in the roadway while it waits to advance in the roadway. A car cannot be removed (i.e. preempted) from its position in the roadway. Lastly, there is indeed a circular wait as each car is waiting for a subsequent car to advance. The circular wait condition is also easily observed from the graphic.

- b) State a simple rule that will avoid deadlocks in this system

Answer: A simple rule that would avoid this traffic deadlock is that a car may not advance into an intersection if it is clear it will not be able to immediately clear the intersection.

5. [Silberschatz] A single-lane bridge connects the two Vermont villages of North Tunbridge and South Tunbridge. Farmers in the two villages use this bridge to deliver their produce to the neighboring town. The bridge can become deadlocked if a northbound and a southbound farmer get on

the bridge at the same time. (Vermont farmers are stubborn and are unable to back up.) Using semaphores and/or mutex locks, design an algorithm in pseudocode that prevents deadlock.

- (a) Using exactly one semaphore, design an algorithm that prevents deadlock. Initially, do not be concerned about starvation (the situation in which northbound farmers prevent southbound farmers from using the bridge, or vice versa).

Answer:

```
semaphore ok_to_cross = 1;
void enter bridge() {
    ok_to_cross.wait();
}
void exit bridge() {
    ok_to_cross.signal();
}
```

- (b) Modify your solution so that it is starvation-free.

Answer:

```
monitor bridge {
    int num_waiting_north = 0;
    int num_waiting_south = 0;
    int on_bridge = 0;
    condition ok_to_cross;
    int prev = 0;
    void enter_bridge_north() {
        num_waiting_north++;
        while (on_bridge ||
            (prev == 0 && num_waiting_south > 0))
            ok_to_cross.wait();
        num_waiting_north--;
        prev = 0;
    }
    void exit_bridge_north() {
        on_bridge = 0;
        ok_to_cross.broadcast();
    }
}
```



```

void enter_bridge_south() {
    num_waiting_south++;
    while (on_bridge ||
           (prev == 1 && num_waiting_north > 0))
        ok_to_cross.wait();
    num_waiting_south--;
    prev = 1;
}

void exit_bridge_south() {
    on_bridge = 0;
    ok_to_cross.broadcast();
}
}

```

6. [Silberschatz] Consider the variation of the Dining Philosophers problem (See Section 31.6 of the OSTEP textbook for a description of the problem), where all unused forks are placed in the center of the table and any philosopher can eat with any two forks. Assume that requests for forks are made one at a time. Describe a simple rule for determining whether a particular request can be satisfied without causing deadlock given the current allocation of forks to philosophers.

Answer: The following rule prevents deadlock: when a philosopher makes a request for the first chopstick, do not grant the request if there is no other philosopher with two chopsticks and if there is only one chopstick remaining.

7. Annabelle, Bertrand, Chloe and Dag are working on their term papers in CS 318, which is a 10,000 word essay on My All-Time Favorite Race Conditions. To help them work on their papers, they have one dictionary, two copies of Roget's Thesaurus, and two coffee cups.

Annabelle needs to use the dictionary and a thesaurus to write her paper;

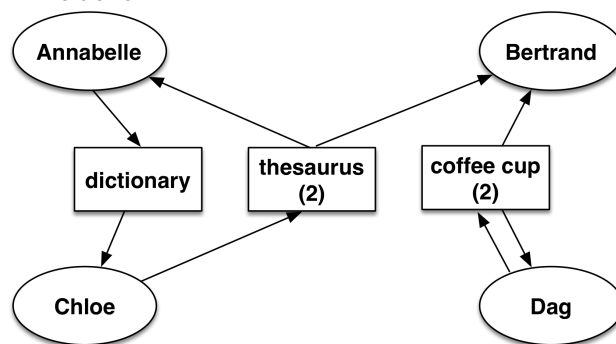
- Bertrand needs a thesaurus and a coffee cup to write his paper;
- Chloe needs a dictionary and a thesaurus to write her paper;
- Dag needs two coffee cups to write his paper (he likes to have a cup of regular and a cup of decaf at the same time to keep himself in balance).

Consider the following state:

- Annabelle has a thesaurus and need the dictionary.
- Bertrand has a thesaurus and a coffee cup.
- Chloe has the dictionary and needs a thesaurus.
- Dag has a coffee cup and needs another coffee cup.

- (a) Is the system deadlocked in this state? Explain using a resource allocation graph.

Answer: The resource allocation graph, shown below, can be fully reduced. Bertrand is not blocked. Erasing the edges incident on Bertrand unblocks Chloe and Dag. Erasing their edges unblocks Annabelle.



- (b) Is this state reachable if the four people allocated and released their resources using the Banker's algorithm? Explain.

Answer: Yes. The resource allocation graph is also the maximum claims graph. Since it can be fully reduced, the state is attainable using the Banker's algorithm.