

# Package ‘MaximinInfer’

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**Type** Package

**Title** Inference for Maximin Effect in high-dimensional settings

**Version** 0.1.0

**Author** Zhenyu Wang; Zijian Guo

**Maintainer** Zhenyu Wang <wangzy0701@gmail.com>

**Description** The package implements the sampling and aggregation method for the covariate shift maximin effect, which was proposed in arXiv:2011.07568. It constructs the confidence interval for any linear combination of the high-dimensional maximin effect.

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.1.1

**Suggests** knitr,  
rmarkdown

**VignetteBuilder** knitr

**Imports** MASS,  
stats,  
CVXR,  
glmnet,  
intervals,  
SIHR

**Depends** R (>= 2.10)

## R topics documented:

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decide_delta	<i>decide delta data-dependently</i>
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### Description

decide\_delta will tell if the estimator is stable or not without ridge penalty at first. If instable, it picks a ridge penalty data-dependently.

### Usage

```
decide_delta(object, step_delta = 0.1, MAX_iter = 100, verbose = FALSE)
```

### Arguments

object	Object of class inheriting from "Maximin"
step_delta	The step size of searching delta (Default = 0.1)
MAX_iter	Maximum of iterations for searching (Default = 100)
verbose	Print information about delta and reward (Default = 'FALSE')

### Value

delta	The data-dependent ridge penalty
reward.ratio	The ratio of penalized reward over non-penalized reward

### Examples

```
## heterogenous data and covariates shift
X1 = sample_data$X1
X2 = sample_data$X2
Y1 = sample_data$Y1
Y2 = sample_data$Y2
X.target = sample_data$X.target

## loading
loading = rep(0, 100) # dimension p=100
loading[98:100] = 1

## call
mm <- Maximin(list(X1, X2), list(Y1, Y2), loading, X.target, covariate.shift = TRUE)
out <- decide_delta(mm)
out$delta
out$reward.ratio
```

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infer	<i>Inference method for class "Maximin"</i>
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## Description

Point estimator and Confidence interval based on Maximin object

## Usage

```
infer(
  object,
  delta = 0,
  gen.size = 500,
  threshold = 0,
  alpha = 0.05,
  alpha.thres = 0.01
)
```

## Arguments

object	Object of class inheriting from "Maximin"
delta	The ridge penalty (Default = 0)
gen.size	The generating sample size (Default = 500)
threshold	Should generated samples be filtered or not? if 0, use normal threshold to filter; if 1, use chi-square threshold to filter; if 2, do not filter (Default = 0)
alpha	confidence value to construct confidence interval (Default = 0.05)
alpha.thres	confidence value to select generated samples (Default = 0.01)

## Value

weight	The weight vector for groups, of length $L$
point	The point estimator of the linear combination
mm.effect	The aggregated maximin effect (coefficients), of length $p$ or $p + 1$
CI	Confidence interval for the linear combination

## Examples

```
## heterogenous data and covariates shift
X1 = sample_data$X1
X2 = sample_data$X2
Y1 = sample_data$Y1
Y2 = sample_data$Y2
X.target = sample_data$X.target

## loading
loading = rep(0, 100) # dimension p=100
loading[98:100] = 1

## call
mm <- Maximin(list(X1, X2), list(Y1, Y2), loading, X.target, covariate.shift = TRUE)
mmInfer <- infer(mm)
```

Maximin

*Class Maximin***Description**

‘Maximin’ returns the class "Maximin", which provides materials for later inference method.

**Usage**

```
Maximin(
  Xlist,
  Ylist,
  loading,
  X.target = NULL,
  cov.target = NULL,
  covariate.shift = TRUE,
  lam.value = c("CV", "CV.min"),
  intercept = TRUE,
  intercept.loading = FALSE
)
```

**Arguments**

Xlist	list of design matrix for source data, of length $L$
Ylist	list of outcome vector for source data, of length $L$
loading	Loading, of length $p$
X.target	Design matrix for target data, of dimension $n.target \times p$ (default = ‘NULL’)
cov.target	Covariance matrix for target data, of dimension $p \times p$ (default = ‘NULL’)
covariate.shift	Covariate shifts or not between source and target data (default = ‘TRUE’)
lam.value	The method to be used to obtain Lasso estimator of high-dimensional regression vector for each group
intercept	Should intercept be fitted for the initial estimator (default = ‘TRUE’)
intercept.loading	Should intercept be included for the loading (default = ‘FALSE’)

**Details**

The algorithm implemented scenarios with or without covariate shift. If ‘cov.target’ is specified, the ‘X.target’ will be ignored; if not, while ‘X.target’ is specified, ‘cov.target’ will be estimated by ‘X.target’. If both are not specified, the algorithm will automatically set ‘covariate.shift’ as ‘FALSE’.

**Value**

‘Maximin’ returns an object of class "Maximin". The function ‘infer’ is used to do further inference. An object of class "Maximin" is a list containing the following components.

Gamma.prop	The proposed debiased regression covariance matrix
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Coef.est	matrix, of dimension $p(+1) \times L$ where each column corresponds to the Lasso estimator of the high-dimensional regression vector for a given group
Point.vec	vector, of length $L$ with the $l$ -th entry as the debiased estimator of the linear combination of the $l$ -th high-dimensional regression vector
L	The number of groups
gen.mu	The mean vector for sampling the regression covariance matrix
gen.Cov	The variance matrix for sampling the regression covariance matrix

MaximinInfer

*The Wrapper function for Maximin inference*

## Description

MaximinInfer is a wrapper for class Maximin and the method infer.

## Usage

```
MaximinInfer(
  Xlist,
  Ylist,
  loading,
  X.target = NULL,
  cov.target = NULL,
  covariate.shift = TRUE,
  lam.value = c("CV", "CV.min"),
  intercept = TRUE,
  intercept.loading = FALSE,
  delta = 0,
  gen.size = 500,
  threshold = 0,
  alpha = 0.05,
  alpha.thres = 0.01
)
```

## Arguments

Xlist	list of design matrix for source data, of length $L$
Ylist	list of outcome vector for source data, of length $L$
loading	Loading, of length $p$
X.target	Design matrix for target data, of dimension $n.target \times p$ (default = 'NULL')
cov.target	Covariance matrix for target data, of dimension $p \times p$ (default = 'NULL')
covariate.shift	Covariate shifts or not between source and target data (default = 'TRUE')
lam.value	The method to be used to obtain Lasso estimator of high-dimensional regression vector for each group
intercept	Should intercept be fitted for the initial estimator (default = 'TRUE')
intercept.loading	Should intercept be included for the loading (default = 'FALSE')

delta	The ridge penalty (Default = 0)
gen.size	The generating sample size (Default = 500)
threshold	Should generated samples be filtered or not? If 0, use normal threshold to filter; if 1, use chi-square threshold to filter; if 2, do not filter. (Default = 0)
alpha	confidence value to construct confidence interval (Default = 0.05)
alpha.thres	confidence value to select generated samples (Default = 0.01)

### Details

The algorithm implemented scenarios with or without covariate shift. If 'cov.target' is specified, the 'X.target' will be ignored; if not, while 'X.target' is specified, 'cov.target' will be estimated by 'X.target'. If both are not specified, the algorithm will automatically set 'covariate.shift' as 'FALSE'.

### Value

weight	The weight vector for groups, of length $L$
point	The point estimator of the linear combination
mm.effect	The aggregated maximin effect (coefficients), of length $p$ or $p + 1$
CI	Confidence interval for the linear combination

### Examples

```
## heterogenous data and covariates shift
X1 = sample_data$X1
X2 = sample_data$X2
Y1 = sample_data$Y1
Y2 = sample_data$Y2
X.target = sample_data$X.target

## loading
loading = rep(0, 100) # dimension p=100
loading[98:100] = 1

## call
mmInfer <- MaximinInfer(list(X1, X2), list(Y1, Y2), loading, X.target, covariate.shift = TRUE)
```

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measure_instability	<i>measurement of instability</i>
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### Description

compute the instability measurement given a specific ridge penalty

**Usage**

```
measure_instability(
  object,
  delta = 0,
  gen.size = 500,
  threshold = 0,
  alpha.thres = 0.01
)
```

**Arguments**

object	Object of class inheriting from "Maximin"
delta	The ridge penalty (Default = 0)
gen.size	The generating sample size (Default = 500)
threshold	Should generated samples be filtered or not? if 0, use normal threshold to filter; if 1, use chi-square threshold to filter; if 2, do not filter. (Default = 0)
alpha.thres	confidence value to select generated samples (Default = 0.01)

**Value**

measure	The measurement of instability
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**Examples**

```
## heterogenous data and covariates shift
X1 = sample_data$X1
X2 = sample_data$X2
Y1 = sample_data$Y1
Y2 = sample_data$Y2
X.target = sample_data$X.target

## loading
loading = rep(0, 100) # dimension p=100
loading[98:100] = 1

## call
mm <- Maximin(list(X1, X2), list(Y1, Y2), loading, X.target, covariate.shift = TRUE)
out <- measure_instability(mm)
out$measure
```

sample\_data

*Sample Data for Analysis***Description**

Datasets for the simple testing and running examples. The data is heterogenous with 2 groups, and covariates shift between target data and source data.

**Usage**

```
sample_data
```

**Format**

list with source data and target data, which are:

**X1** Design matrix for the 1st group source data

**X2** Design matrix for the 2nd group source data

**Y1** Outcome vector for the 1st group source data

**Y2** Outcome vector for the 2nd group source data

**X.target** Design matrix for the target data



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