## 1. Let population growth model is represented by $\frac{dN}{dt} = rN(1 - \frac{N}{K})$ , where N represents the population size, r(>0) is the growth rate and K(>0) is the carrying capacity.

- a. Find all the fixed points of this model.
- b. Which of these fixed points are stable? Why? (Explain it from the perturbation technique. Consider  $\dot{x} = f(x)$ , a fixed point as x\*. Calculate the general condition of stability.)
- c. Analytically solve the differential equation and check whether long term evolution of the solution converges to the stable fixed point(s).
- d. The population will remain unchanged irrespective of r and K if it starts form a non-zero population (away from K). Is it correct? Explain. [2 + 3 + 4 + 1 = 10]

- Develop the pseudo code that uses the iterative QR method to determine a matrix's eigenvalues.

  Describe the mechanism. What causes the course Describe the mechanism. What causes the eigenvalues to stay constant throughout this iterative
- process?

  b. Explain the process (using pseudo code) to determine a connected undirected graph's leading eigenvector. When does this process become slower? Why?

  [(2.5 + 1) + (2.5 + 2) = 8]