

Relational Design Theory

Functional Dependencies

Relational design by decomposition

- "Mega" relations + properties of the data
- System decomposes based on properties
- Final set of relations satisfies normal form
 - No anomalies, no lost information
- Functional dependencies ⇒ Boyce-Codd Normal Form
- Multivalued dependences ⇒ Fourth Normal Form

Functional dependencies are generally useful concept

- Data storage compression
- Reasoning about queries optimization

Functional Dependencies

Example: College application info.

```
Student(SSN, sName, address,
HScode, HSname, HScity, GPA, priority)
Apply(SSN, cName, state, date, major)
```

Student(SSN, sName, address, HScode, HSname, HScity, GPA, priority)

Suppose priority is determined by GPA

Two tuples with same GPA have same priority

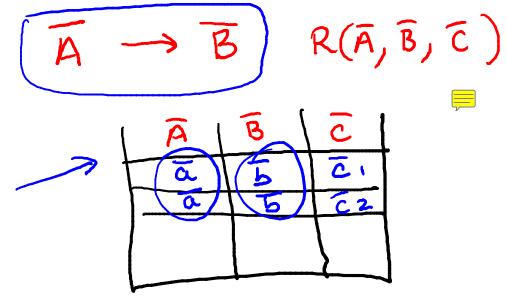
Student(SSN, sName, address, HScode, HSname, HScity, GPA, priority)

Two tuples with same GPA have same priority



Functional Dependency

- Based on knowledge of real world
- All instances of relation must adhere

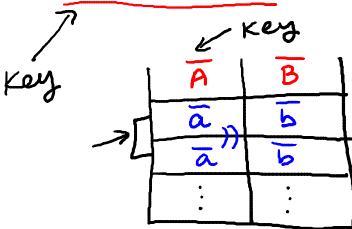


Student(SSN, sName, address, HScode, HSname, HScity, GPA, priority)

Apply(SSN, cName, state, date, major)

Functional Dependencies and Keys

- Relation with no duplicates
- R(A,B)
- Suppose $\bar{A} \rightarrow all$ attributes



Trivial Functional Dependency

Nontrivial FD

$$\overline{A} \rightarrow \overline{B} \quad \overline{B} \not = \overline{A}$$

Completely nontrivial FD

A	B	
4	1	
no	~~	
•		
•	:	

> Hscode

Rules for Functional Dependencies

Splitting rule

$$\rightarrow \overline{A} \rightarrow B_1, B_2, ..., B_m \leftarrow$$

 $\Rightarrow \overline{A} \rightarrow B_1, \overline{A} \rightarrow B_2 ...$

Can we also split left-hand-side?

$$A_1, A_2, \dots, A_n \rightarrow \overline{B}$$
 HSname
? $A_1 \rightarrow \overline{B}$ $A_2 \rightarrow \overline{B}$ X^7



No HSnawer HScity > HSvode

Rules for Functional Dependencies

Combining rule

$$\begin{array}{ccc}
\widehat{A} & \rightarrow B_1 \\
\widehat{A} & \rightarrow B_2 \\
\vdots \\
\widehat{A} & \rightarrow B_n
\end{array}$$

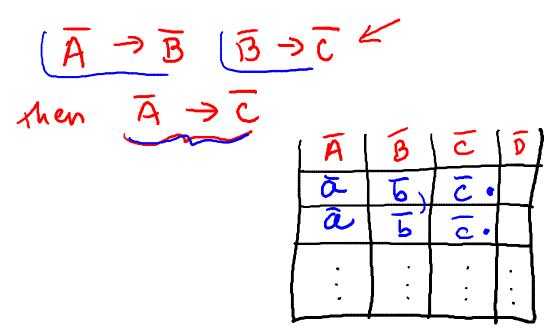
$$\begin{array}{c}
\widehat{A} & \rightarrow B_1, \dots, B_n
\end{array}$$

Rules for Functional Dependencies

Trivial-dependency rules

Rules for Functional Dependencies

Transitive rule



Closure of Attributes

Given relation, FDs, set of attributes Ā

Find all B such that
$$\bar{A} \to B$$
 $\bar{A} + \{A_1, ..., A_n\}^*$

And $C \to C$

Start with $\{A_1, ..., A_n, C_1D_1\} \in \mathcal{B}$

repeat until no change:

If $\bar{A} \to \bar{B}$ and \bar{A} in set all \bar{B} to set



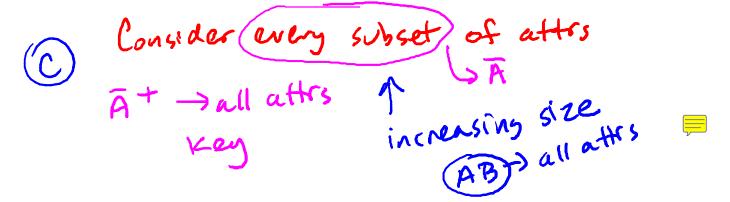
Closure Example

Student(SSN, sName, address, HScode, HSname, HScity, GPA, priority)

```
\checkmarkSSN \rightarrow SName, address, GPA
\bigcircGPA \rightarrow priority
 HScode → HSname, HScity
           ESSN, Hscode 3+ > octations.
            ESSN, HSLode, sName, address,
GPA, priority, HSname, HScity 3
```

Closure and Keys

How can we find all keys given a set of FDs?



Specifying FDs for a relation



- S₁ and S₂ sets of FDs
- S₂ "follows from" S₁ if every relation instance satisfying S₁ also satisfies S₂

```
52: 2 55N -> priority3
How to test? SSN > GPA GPA > priority }
  Does \overline{A} \to \overline{B} follow from S? 5^{\circ}
 (1) A+ based on & check if B in set.
 (2) Armstrong's Axioms
```

Functional Dependencies

Specifying FDs for a relation

Want: Minimal set of completely nontrivial FDs such that all FDs that hold on the relation follow from the dependencies in this set

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 - Functional dependencies ⇒ Boyce-Codd Normal Form
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