



ARISTOTLE
UNIVERSITY OF
THESSALONIKI

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Feasibility study of Muon Tomography application in a non-invasive representation of tumulus

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On behalf of the AUTH muon tomography team
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17th of June, 2021

Overview

- Study of the effectiveness of muon tomography in a geological structure of smaller scale and of archaeological interest
- A MicroMegas telescope will be placed near Appolonia's tumulus (EKATY programme)
- Simulation of the tumulus geometry
Scanning of its internal structure by measuring the flux deficit which determines the integrated 2D density in the direction of observation (Transmission muography)



Combination of several 2D projections (by moving the muon detector or by surrounding the object with several instruments) → 3D information

Presentation Outline

- **Muon Tomography**
- Simulation
 - Tumulus simulation
 - Test for different materials
 - Object inside the tumulus
 - Geant4-MatLab Generator
 - Telescope and real tumulus
- Back-projection method
 - Telescope below the tumulus
 - Telescope at the side of the tumulus
- Conclusions and future work

Muon Tomography

- A technique that uses cosmic muons to generate three-dimensional images of volumes

- Useful Information

Energy loss (Muon Radiography)
Multiple Coulomb Scattering
(Muon Scattering Tomography)



Large area detectors of Decision Sciences® enable scanning of commercial trucks

- Fields applied

Geology
Archaeology (Large hidden chamber in the Great Pyramid of Giza)
Security (tracking of dangerous cargo)



"Discovery of a big void in Khufu's Pyramid by observation of cosmic-ray muons", Kunihiro Morishima et al.

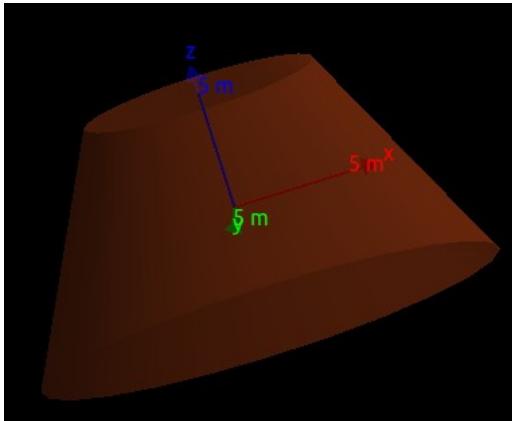
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Simulation

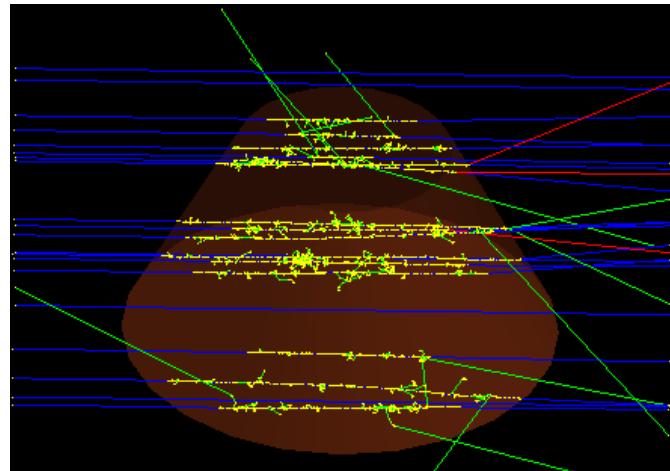
Tumulus simulation

- Geant4
- Uniform initial position at yz plane
- Initial momentum at $+x$
- Monoenergetic muons of 4GeV
- Material dirt ($\rho=1.2\text{g/cm}^3$)
Composition [*The Engineer ToolBox*]
Al(9%), Ca(3%), Fe (5%)/ Mg
(0.6%), K(2%), Si (29%), Na (2.4%)



Dimensions

- Top radius: 4m
 - Bottom radius: 8m
 - Height: 8m
- smaller dimensions for first tests



Ilia Kalaitzidou AUTH

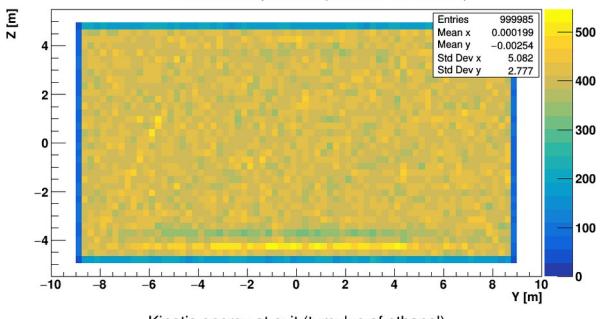
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Simulation

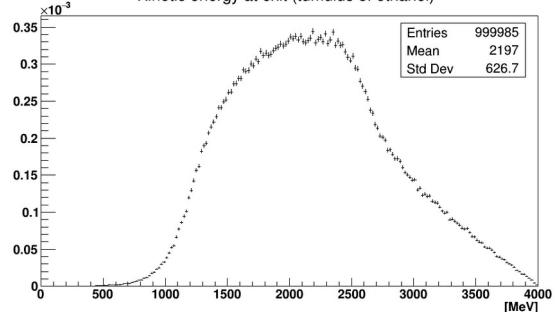
Test for different materials

◆ Ethanol ($\rho=0.78\text{g/cm}^3$)

Final muon position (tumulus of ethanol)

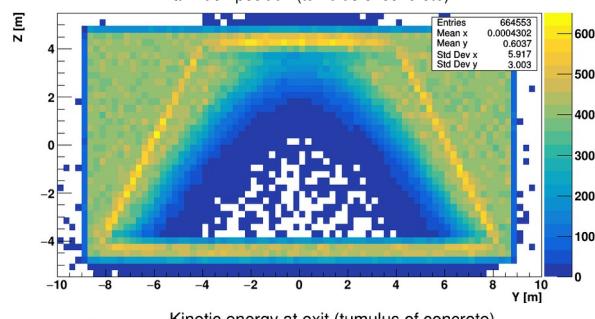


Kinetic energy at exit (tumulus of ethanol)

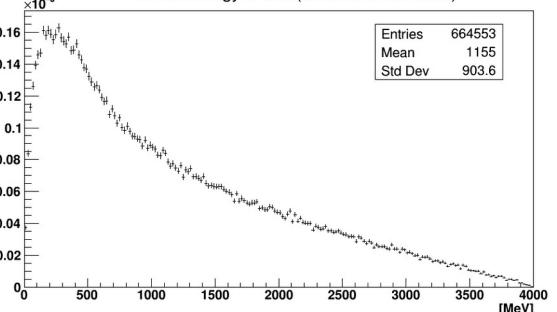


◆ Concrete ($\rho=2.3\text{g/cm}^3$)

Final muon position (tumulus of concrete)

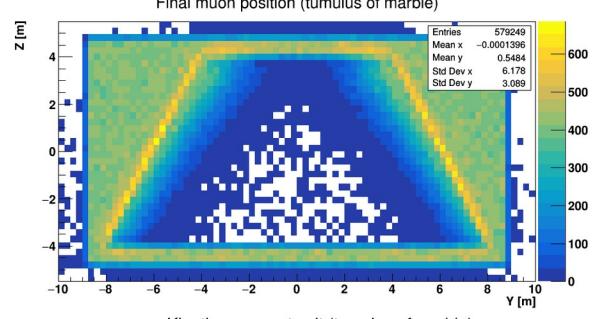


Kinetic energy at exit (tumulus of concrete)

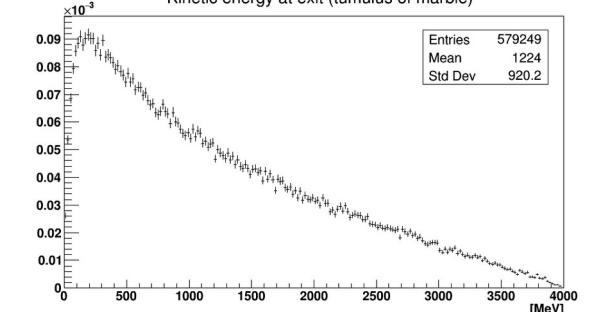


◆ Marble ($\rho=2.8\text{g/cm}^3$)

Final muon position (tumulus of marble)



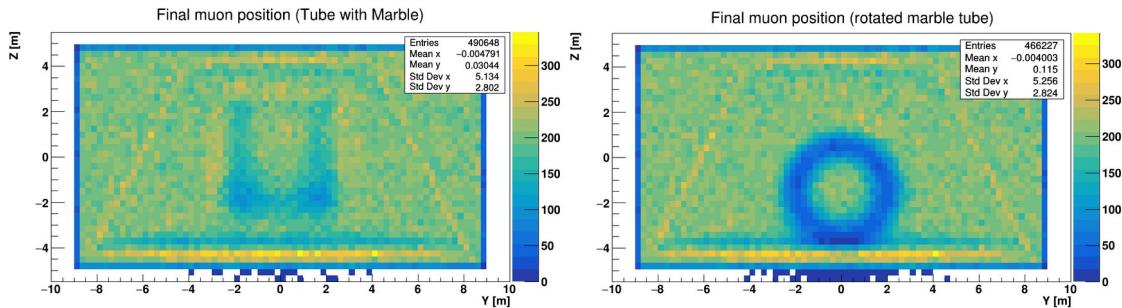
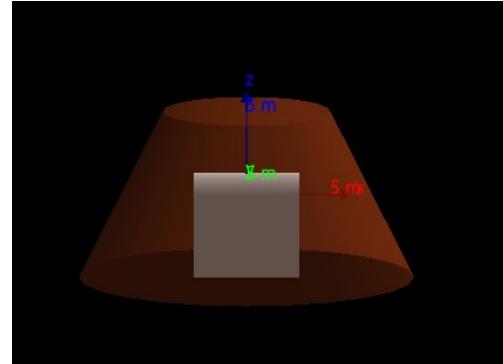
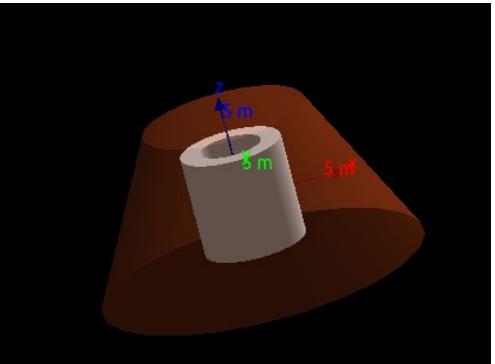
Kinetic energy at exit (tumulus of marble)



Simulation

Object inside the tumulus

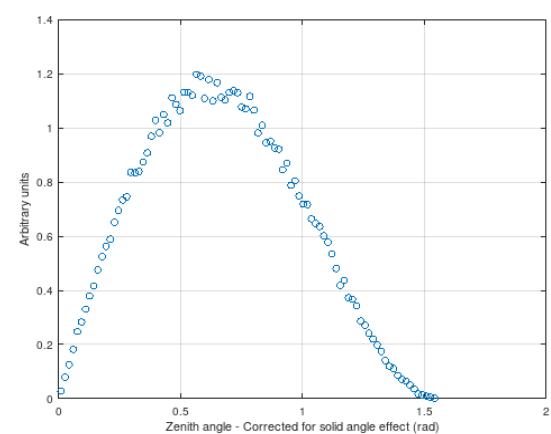
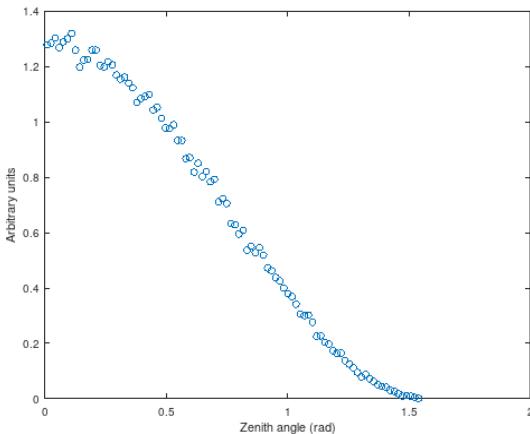
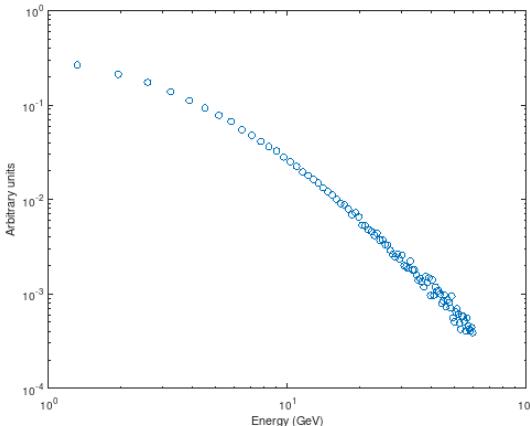
- Dimensions
 - Inner radius: 1.5m
 - Outer radius: 2.5m
 - Height: 5m
- Material → Marble
- i. Orientation parallel to z axis
- ii. 90° rotation around y axis and repositioning to touch the ground



Simulation Geant4-MatLab Generator

- Simulate cosmic muon distributions
- Generate user-defined histograms for use with the Geant4 General Particle Source
- Phenomenological model & statistical algorithms
- Implementation by postdoctoral researcher Georgios Tsiledakis

Chatzidakis, Stylianos. (2015). A Geant4-MATLAB Muon Generator for Monte-Carlo Simulations



MATLAB distributions

- Energy range 1-60 GeV
- Zenith angle range 0–90°

Simulation

Telescope and real tumulus

Real tumulus dimensions

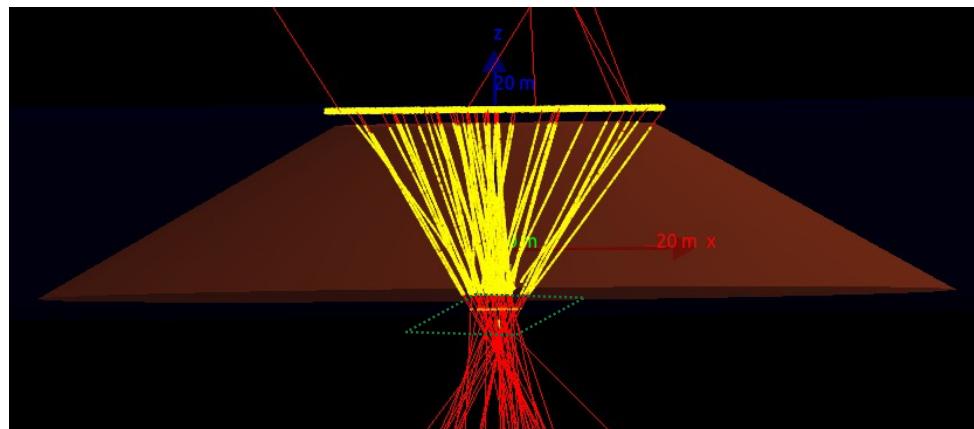
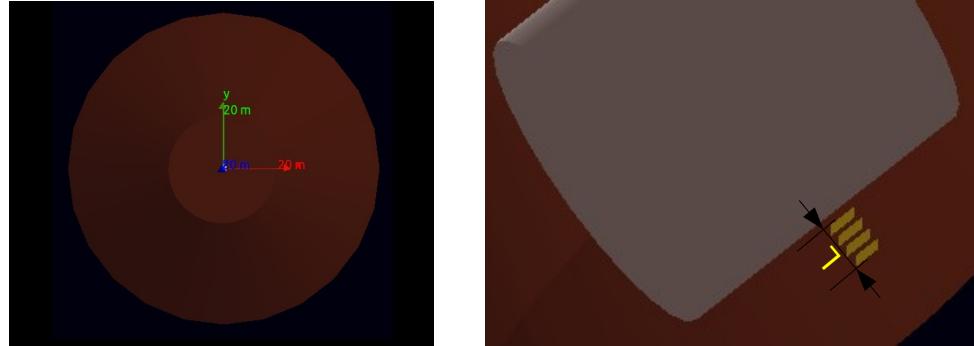
- Base diameter 92m
- Top diameter 32m
- Height 17m

Muon telescope

- 4 detection planes 45x45cm, spaced by 20cm ($L=60\text{cm}$)
- Very thin planes of vacuum
- Top detection plane 3m below tumulus base

Cut in the tracks

- Projection of the initial muon track
- Accepted area $\pm 3\text{m}$ from the detector centre
- Artificially kill the tracks that will not end to the accepted area

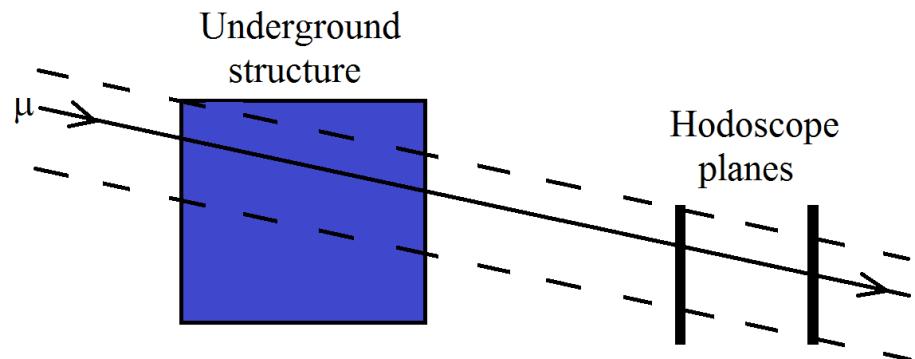


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 - **Telescope below the tumulus**
 - **Telescope at the side of the tumulus**
- Conclusions and future work

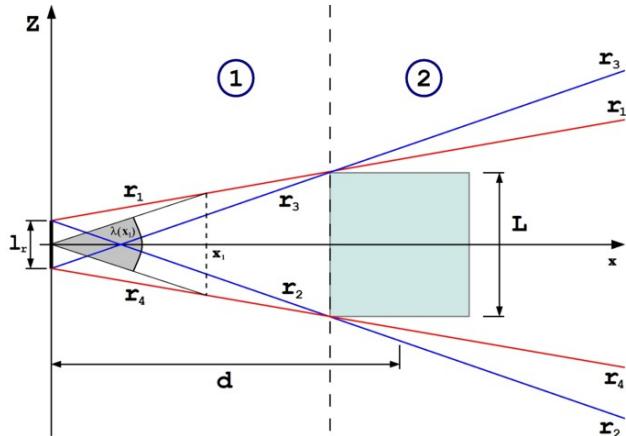
Back-Projection method

- Specify the size and the location of the hidden object
- Favorable for the imaging of hidden objects surrounded by a large amount of different density material
- Not point-like muon telescope compared to the object under investigation
- Comparable distance between detector-object to the detector size
- Both the direction of the muon tracks and their impact point on the detector are useful



"A projective reconstruction method of underground or hidden structures using atmospheric muon absorption data", L. Bonechi et al

Back-Projection method



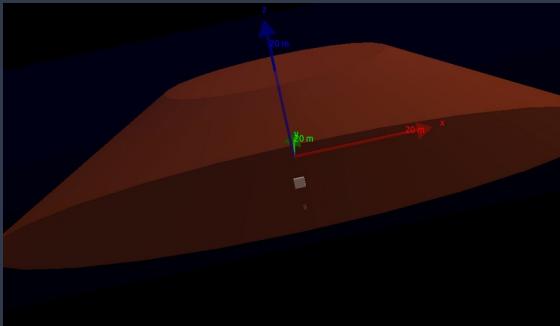
"A projective reconstruction method of underground or hidden structures using atmospheric muon absorption data", L. Bonechi et al

- Back-project muon tracks in vertical planes to the telescope axis
- Pitch (bin size) of back-planes: $p(x) = \delta_\theta x + p_0$
- Two-dimensional histograms ($y/p, z/p$)
- Subtract tumulus-with-monument histogram from uniform-tumulus histogram
- Width-to-pitch → rms of each projection
- Minimum of width-to-pitch ratio → object location
- FWHM at minimum → object dimensions

Back-projection method

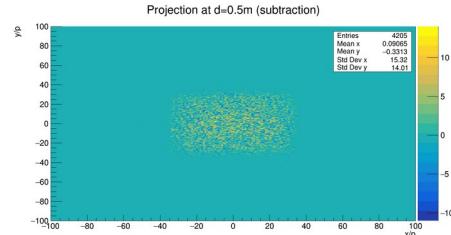
Telescope below the tumulus

- Iron and marble compact cylinder
- Diameter 1.5m, Height 1.5m
- Its side touches the ground
- Energy range 4-100GeV, Zenith angle 0-50°
- 34x34m generation plane, 1m above tumulus
- 1 billion initial muons
- Initial pitch 5mm → $\delta_\theta = 8.3\text{mrad}$ [$\text{atan}(p/L)$]

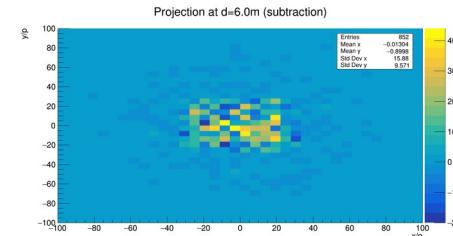
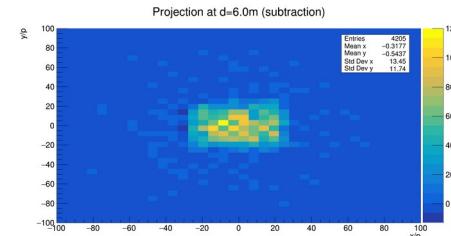
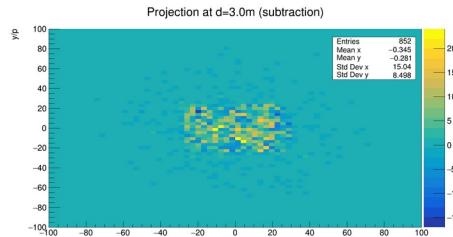
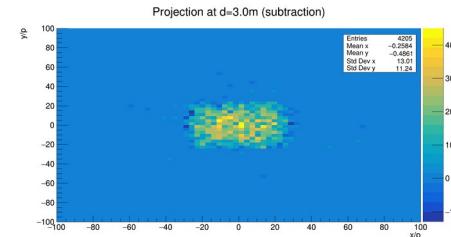
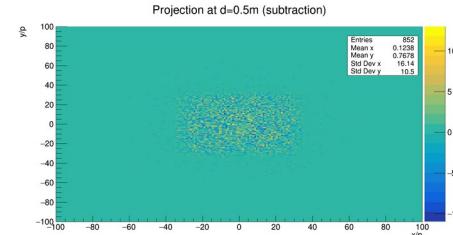


Jun 17, 2021

◆ Iron



◆ Marble

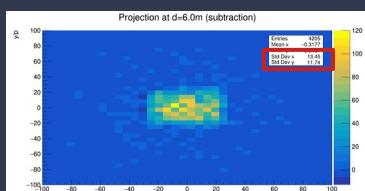
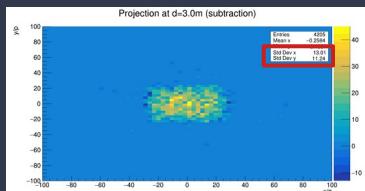
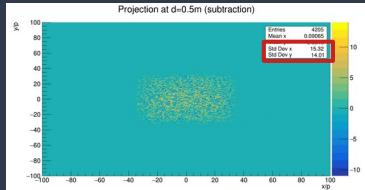


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Back-projection method

Telescope below the tumulus

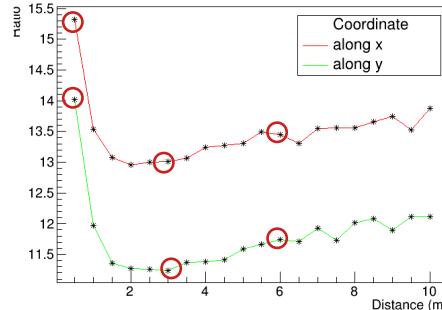


Iron



Width-to-pitch = Rms

Width-to-pitch Ratio

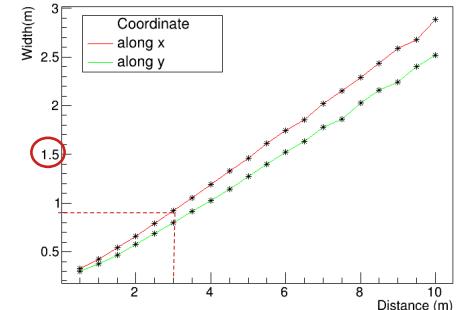


Marble

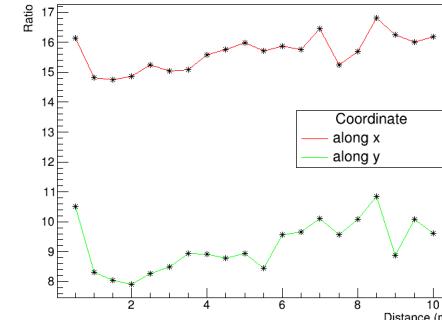


Width = FWHM*pitch

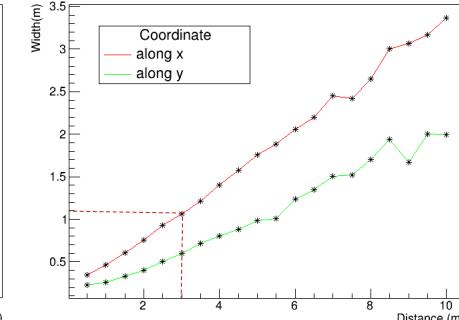
Monument's Width



Width-to-pitch Ratio



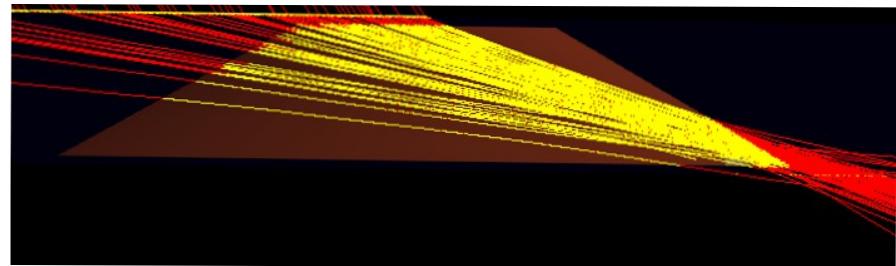
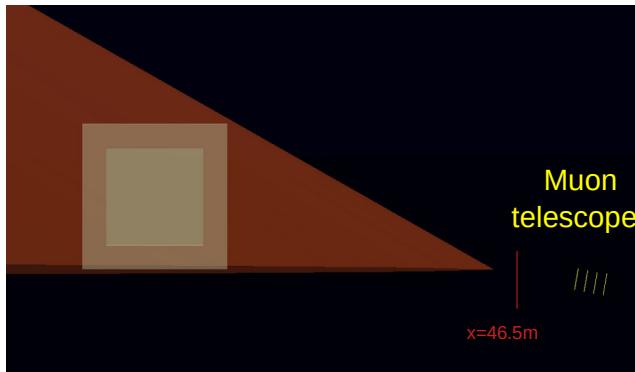
Monument's Width



Back-Projection method

Telescope at the side of the tumulus

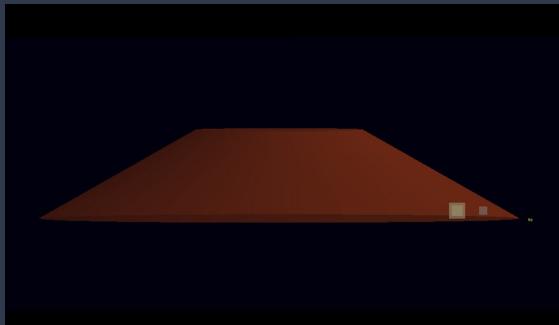
- Telescope centre at (48,0,-8.75)m below the ground level ($z=-8.5\text{m}$)
- 80° rotation around y
- Telescope “sees” the tumulus base
- Initial muon distributions
 - i. Energy: 15-30GeV
 - ii. Zenith: 70-88°
 - iii. Azimuth: 78-102°
- 300x40m generation plane at (-150,0,9.55)m
- Additional arrangement
 - i. Tracks calculated at $x=46.5\text{m}$ (the back-projection starts from the same plane)



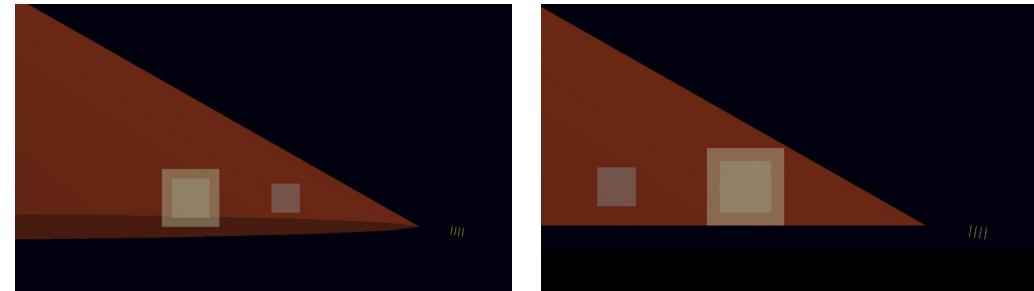
Back-projection method

Telescope at the side of the tumulus

- Two boxes at $x=34\text{m}$ & $x=39\text{m}$
- Large box \rightarrow Hollow box of 3m side and 0.5m width
Small box \rightarrow Compact box of 1.5m side
- Initial pitch $p=3\text{mm} \rightarrow \delta_\theta=5\text{mrad}$
- Materials: Marble & Iron (alternately)
- Monument width $\rightarrow 4\sigma$ (instead of FWHM)

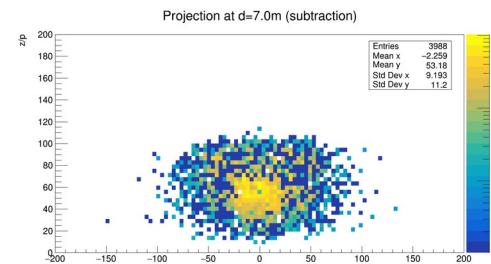
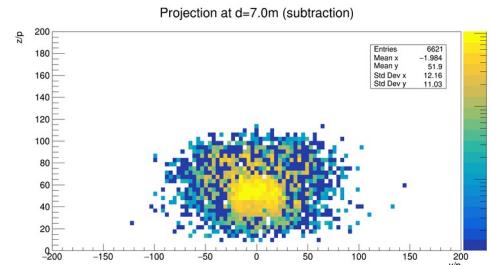


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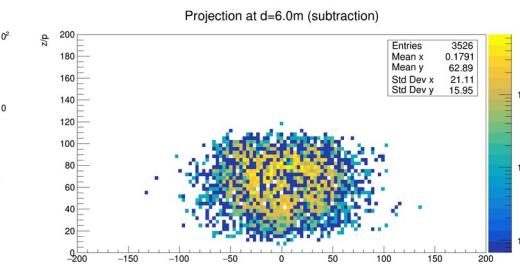
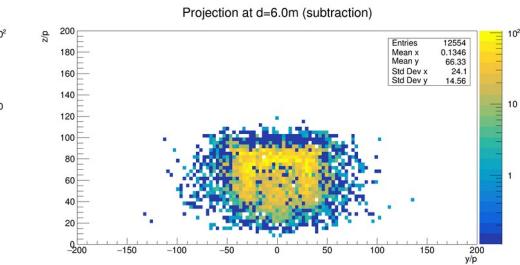


Large iron
box

Large marble
box



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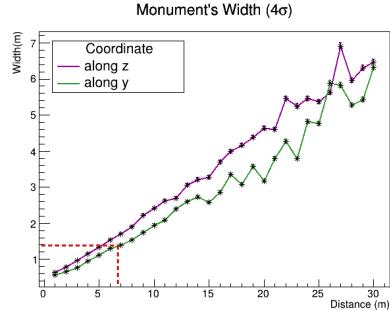
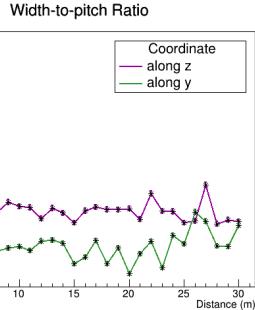
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Back-Projection method

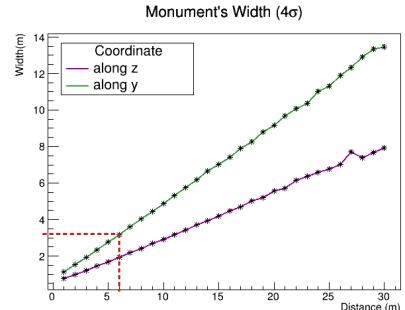
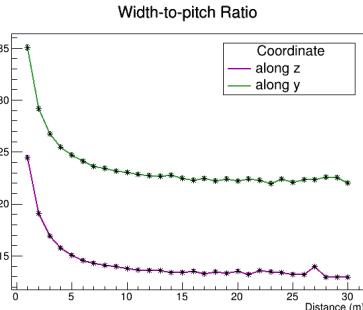
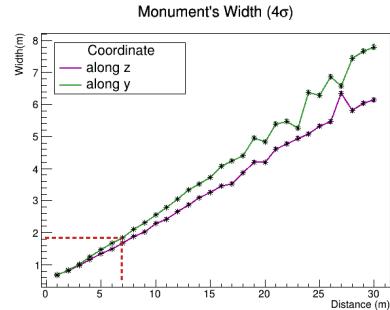
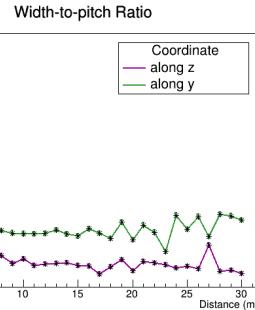
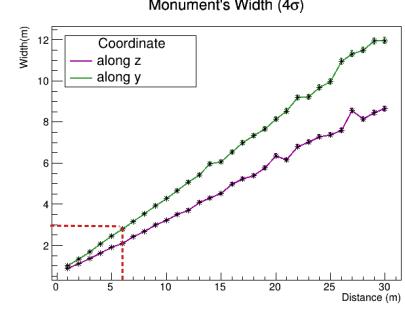
Telescope at the side of the tumulus

◆ Small box closer

◆ Large marble box
◆ Large iron box



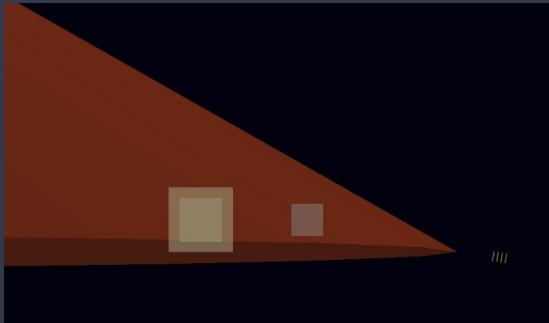
◆ Large box closer



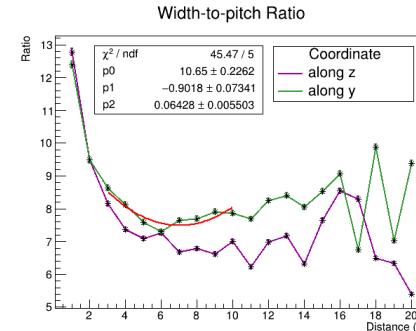
Back-projection method

Telescope at the side of the tumulus

- Large box at $x=34\text{m}$, small box at $x=39\text{m}$
- $p=5\text{mm} \rightarrow \delta_\theta=8.33\text{mrad}$
- Fit width-to-pitch ratio with a second order polynomial function in the region of the minimum
- Fit width distribution with a linear function in the same range

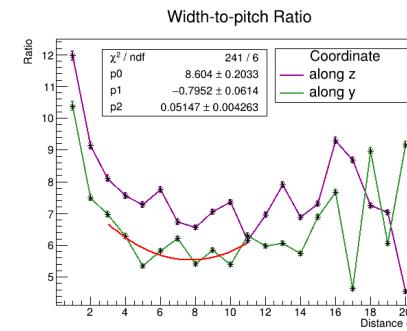


◆ Large marble box

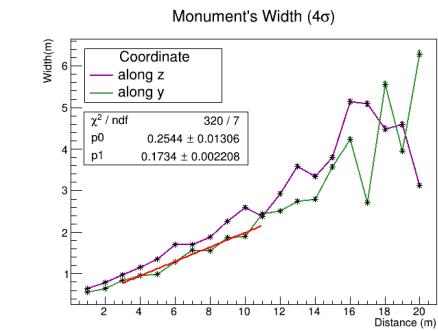
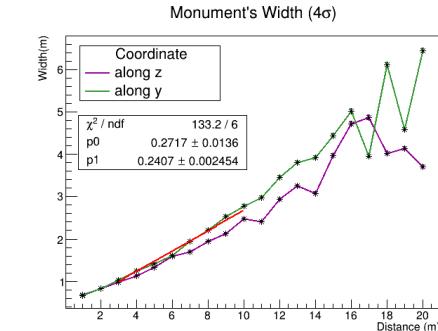


- Minimum of fitted function: d=7.015m (real distance d=6.75m)
- Width at $d=7.015\text{m}$: 1.9602m (real box width 1.5m)

◆ Large iron box



- Minimum of fitted function: d=7.72488m (real distance d=6.75m)
- Width at $d=7.72488\text{m}$: 1.59423m (real box width 1.5m)



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Conclusions and future work

- Muon tomography could be applied in the scanning of tumuli
- By back-projecting the muon tracks the hidden structure becomes observable under certain conditions
- The structure is properly localized when its distance from the telescope and its size are comparable to the telescope dimensions (Structure 3-4 times the telescope size & a few meters away)
- Considering setting up a second detection apparatus in the experiment would provide more information



Thank you for your time!!

References

- GEANT4 collaboration. URL <https://geant4.web.cern.ch/>
- CRY package. URL <https://nuclear.llnl.gov/simulation/>
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- S. Chatzidakis, S. Chrysikopoulou, and L.H. Tsoukalas. Developing a cosmic ray muon sampling capability for muon tomography and monitoring applications. Nuclear Instruments and Methods in Physics Research A, 804:33–42, 2015.
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Back-up slides

Muon angular distribution

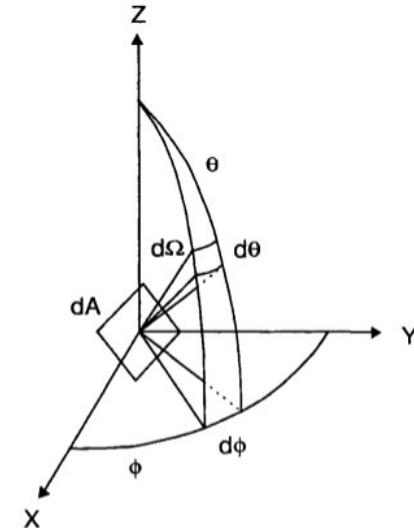
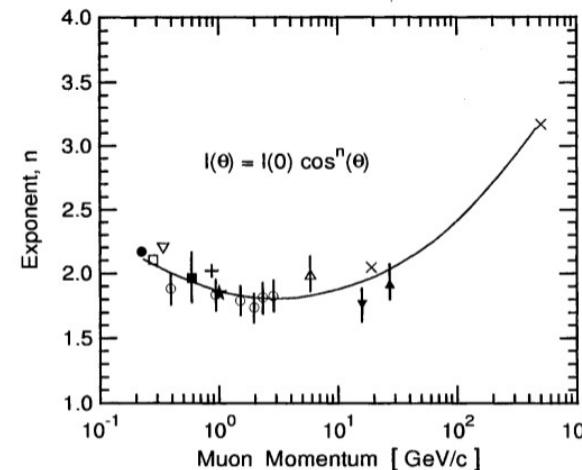
- Directional Intensity $I_i(\theta, \phi)$ of particles of a given kind i: The number of particles dN_i , incident upon an element of area dA , per unit time dt , within an element of solid angle $d\Omega$

$I_v = I(0^\circ)$ vertical intensity

- Flux J_i : Number of particles of a given kind i, traversing in a downward sense a horizontal element of an area dA , per unit time dt

$$I_i(\theta, \phi) = \frac{dN_i}{dA dt d\Omega} \quad [\text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}]$$

$$J_i = \int_{\Omega} I(\theta, \phi) \cos(\theta) d\Omega \quad [\text{cm}^{-2}\text{s}^{-1}]$$



$$I(\theta) = I(0^\circ) \cos^n(\theta)$$

MatLab code

Inverse transformation

Inverse transformation

The inverse transformation involves inversion of the Cumulative Distribution Function (CDF) to obtain random samples $X=F^{-1}(U)$, where U is the uniform probability density function.

- 1) Invert CDF F_x to obtain the expression $F_{x^{-1}}(U)$
- 2) Generate random numbers uniformly distributed $U(0,1)$
- 3) Obtain random variable X from $X=F_{x^{-1}}(U)$

The inverse transform takes a uniformly generated random number and transforms it to a random observation x distributed as F_x

The muon angular distribution follows a squared cosine distribution, where A is the normalization constant

$$f_\Theta(\theta) = A \cos^2(\theta)$$

Correcting for the solid angle effect, where C is the normalization constant

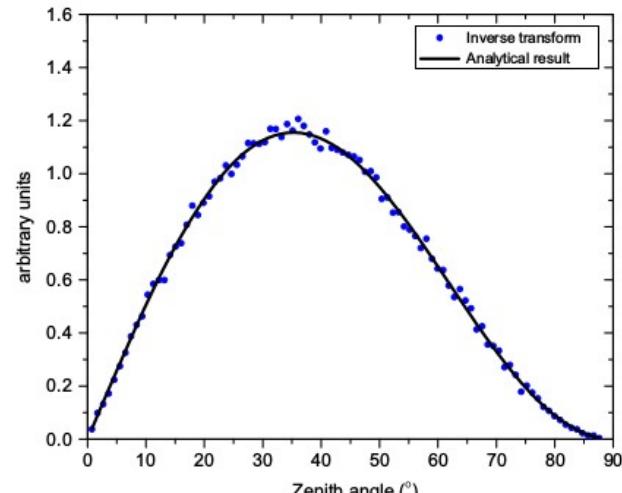
$$f_\Theta(\theta) = 2C\pi \sin(\theta) \cos^2(\theta)$$

Calculating the CDF $F_\Theta(\theta) = \int_0^\theta 2C\pi \sin(\theta) \cos^2(\theta) d\theta = 1 - \cos^3(\theta)$

The inverse transformation

$$\theta = \arccos \left(\sqrt[3]{1 - F_\Theta(U)} \right)$$

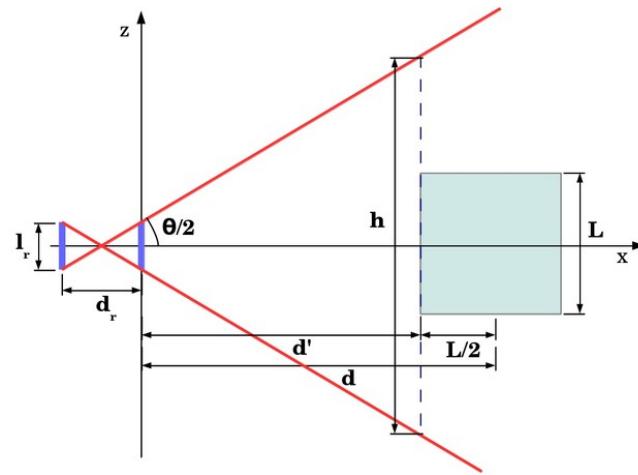
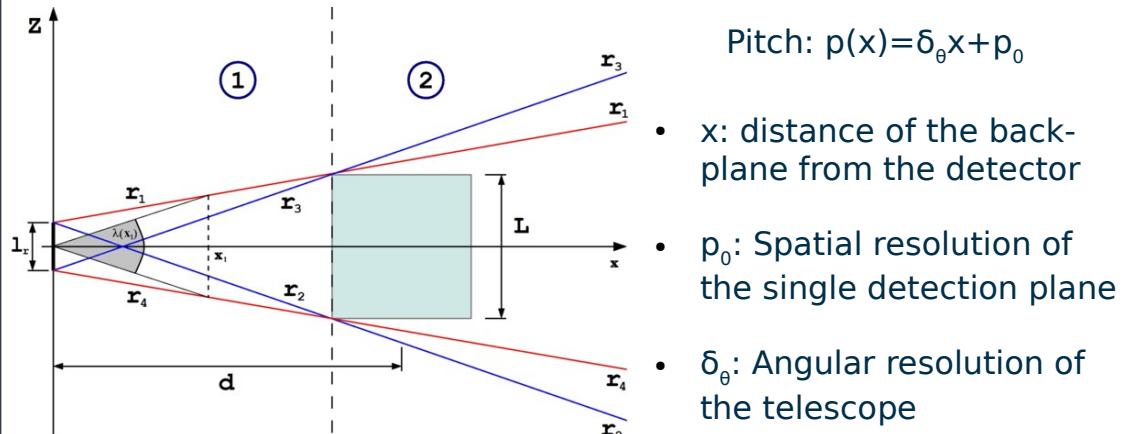
100000 zenith angles were randomly selected using the inverse transformation



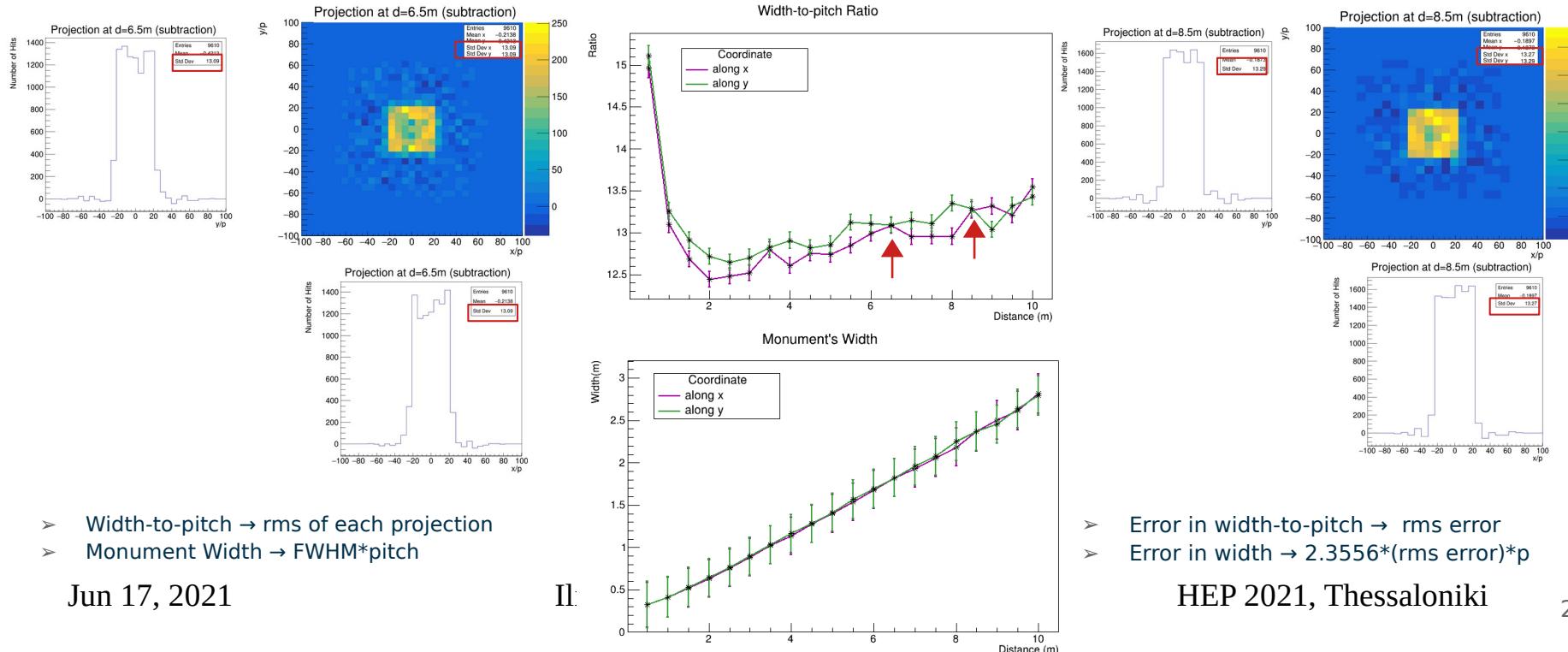
Chatzidakis, Stylianos. (2015). A Geant4-MATLAB Muon Generator for Monte-Carlo Simulations
HEP 2021, Thessaloniki

Back-projection method

- Signal tracks lying within the four lines r_1, r_2, r_3 and r_4
- Space to the right of the detector ($x > 0$) → two zones: zone "1" limited by red lines, zone "2" limited by blue lines
- Width-to-pitch of the signal at distance d approximated as the angular aperture $\lambda(d)$
- The structure of side L has to be contained within the aperture of the hodoscope accepted angle h



Width and Errors



- Width-to-pitch → rms of each projection
- Monument Width → FWHM*pitch

Jun 17, 2021

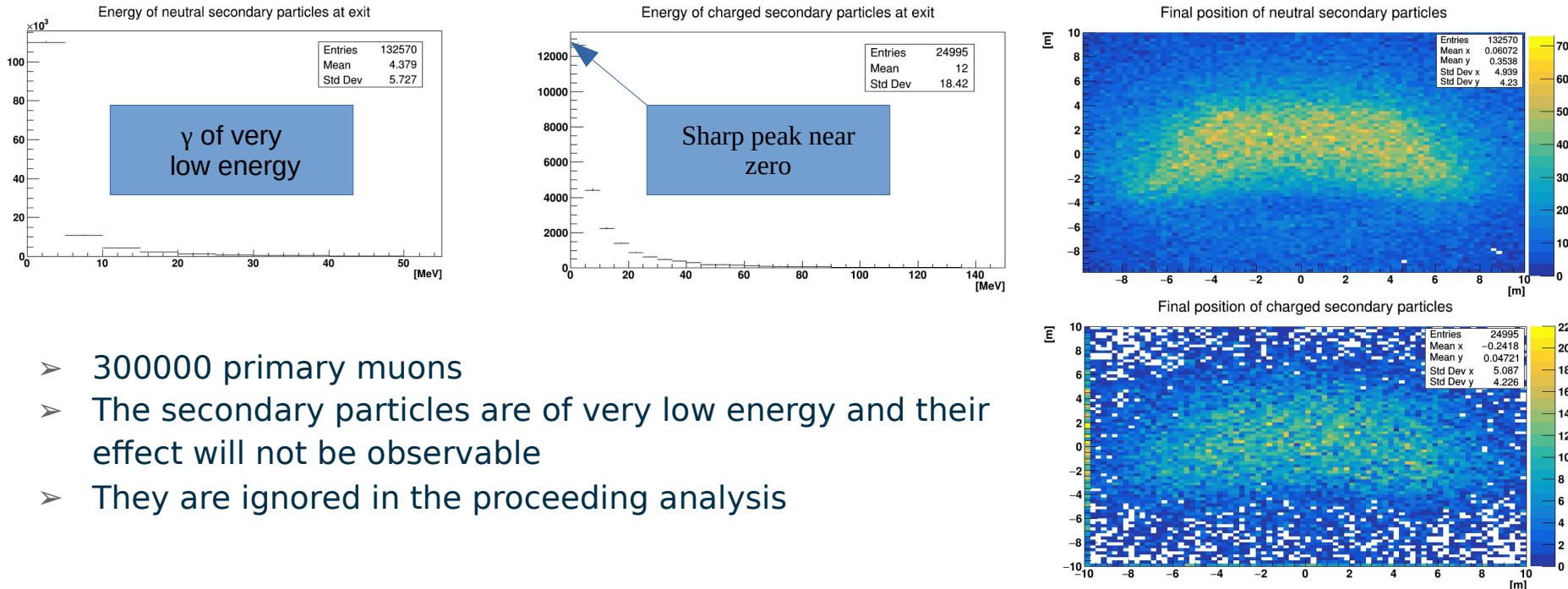
II

- Error in width-to-pitch → rms error
- Error in width → $2.3556 * (\text{rms error}) * p$

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Tumulus simulation

Secondary particles

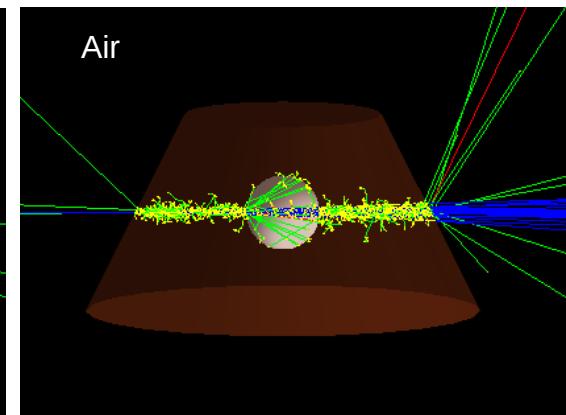
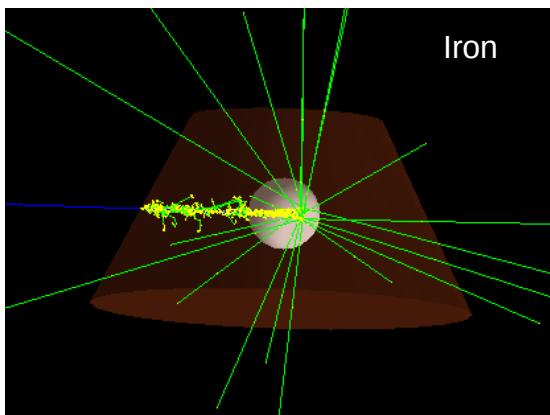
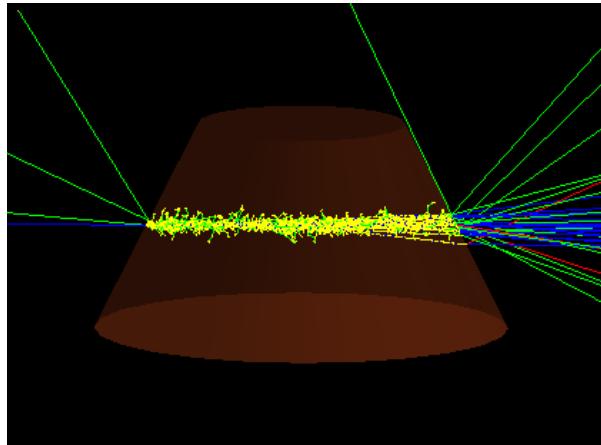


- 300000 primary muons
- The secondary particles are of very low energy and their effect will not be observable
- They are ignored in the proceeding analysis

Tumulus simulation

Object inside the tumulus

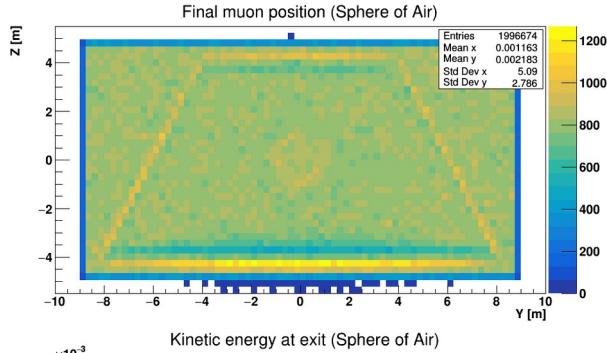
- Sphere of 1.5m radius in the centre
- Visualization of 20 muons generated at a constant position
- Muons are completely stopped by 3m of iron
- Less ionizations inside the void sphere



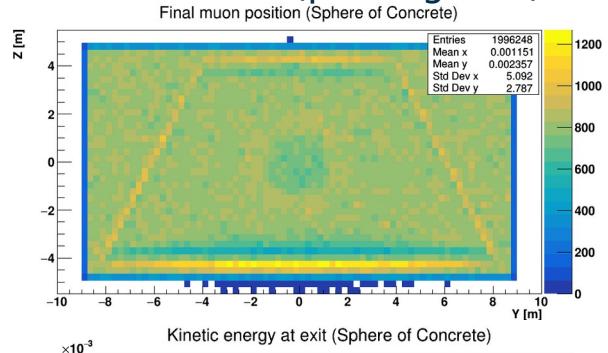
Tumulus simulation

Object inside the tumulus

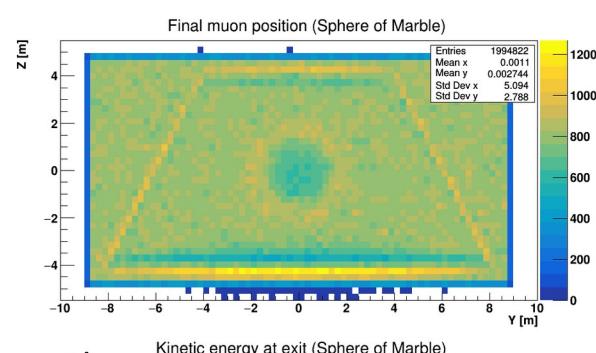
◆ Air ($\rho=0.0012\text{g/cm}^3$)



◆ Concrete ($\rho=2.3\text{g/cm}^3$)



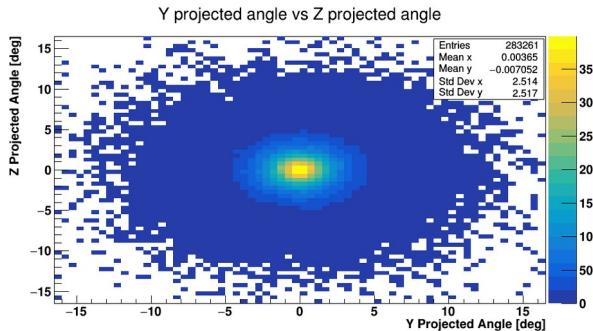
◆ Marble ($\rho=2.8\text{g/cm}^3$)



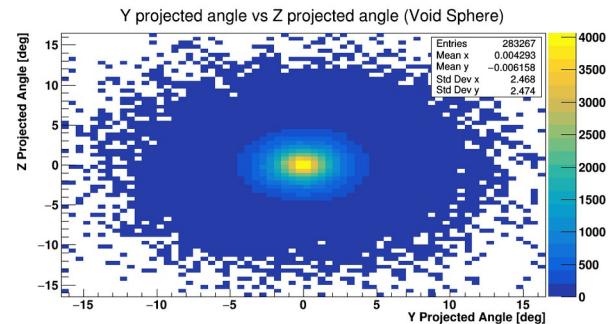
Tumulus simulation

Sphere inside the tumulus

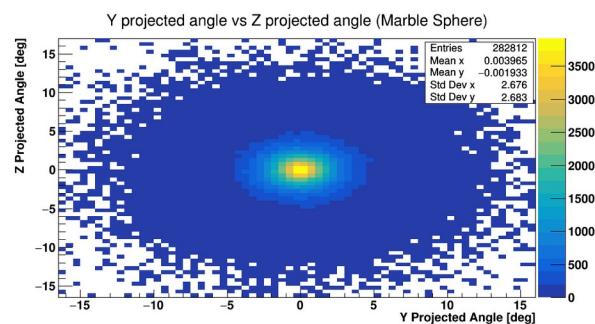
◆ Without sphere



◆ Sphere with air



◆ Sphere of marble

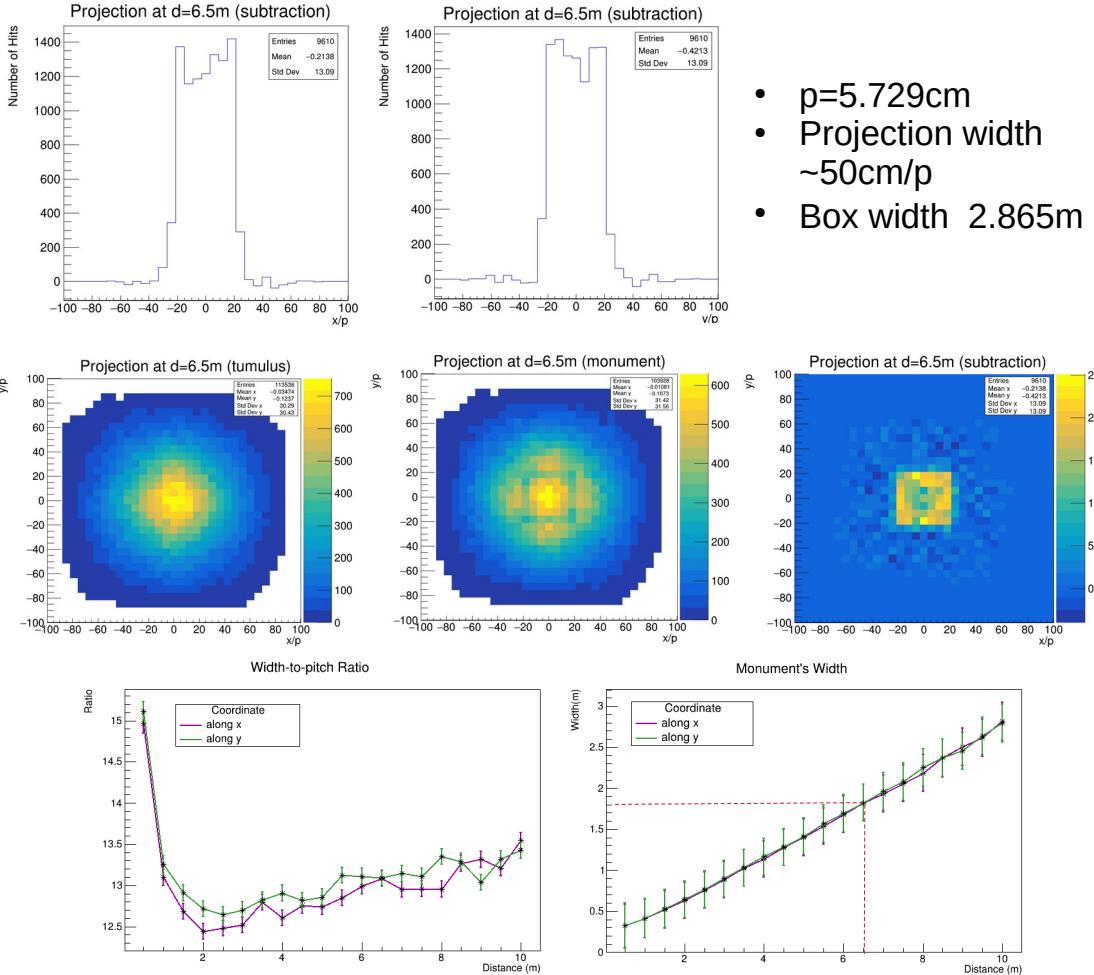
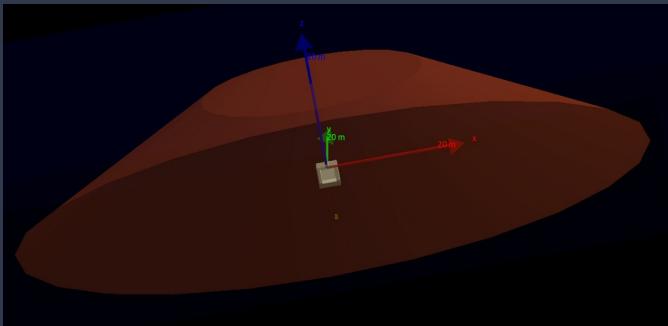


- Y projected angle vs Z projected angle with respect to the x axis at exit
- Only muons that traversed the tumulus
- Multiple Scattering is more important for materials of larger density
(the different density material is relatively small → No apparent differentiation → Clearer image with more statistics)

Back-projection method

Telescope below the tumulus

- Iron hollow box
- Outer side 3m, Inner side 2m
- Box base 6.5m from top detection plane



Jun 17, 2021

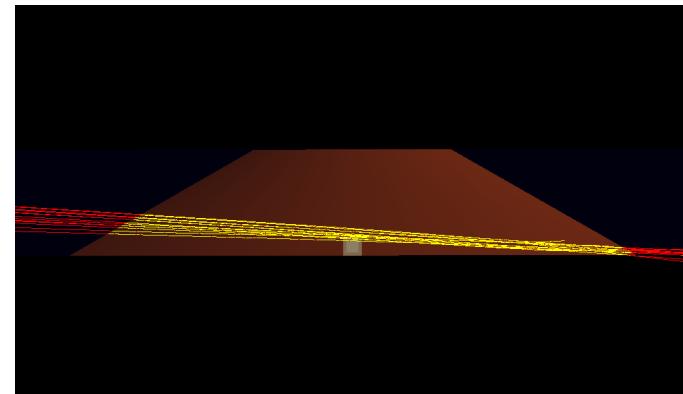
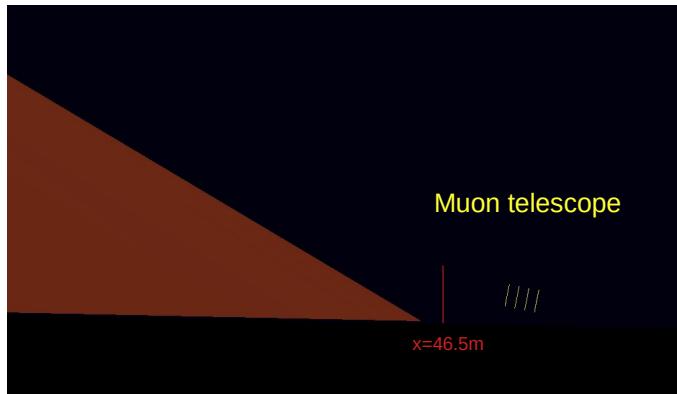
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Back-Projection method

Telescope at the side of the tumulus

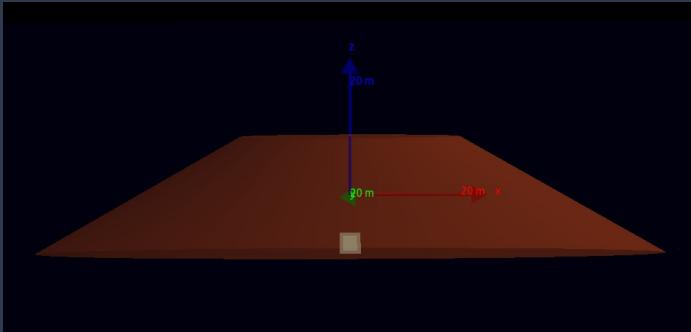
- Telescope centre at (48,0,-8)m
- 80° rotation around y
- Telescope “sees” the tumulus base
- Initial muon distributions
 - i. Energy: 15-50GeV
 - ii. Zenith: 80-90°
 - iii. Azimuth: 85-95°
- 400x20m generation plane at (-400,0,9)m
- Additional arrangements
 - i. Tracks calculated at $x=46.5\text{m}$ (the back-projection starts from the same plane)
 - ii. Reject tracks with $\theta_z < 80^\circ$ & $\theta_z > 90^\circ$
 - iii. Initial pitch 1mm → $\delta_\theta = 1.67\text{mrad}$



Back-projection method

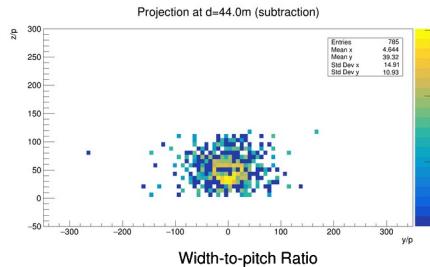
Telescope at the side of the tumulus

- “Thin” box: 3m outer side, 2m inner side
- “Thick” box: 3m outer side, 0.5m inner side
- Its base touches the ground
- Marble
- Box at $x=0$
- 4 billion initial muons

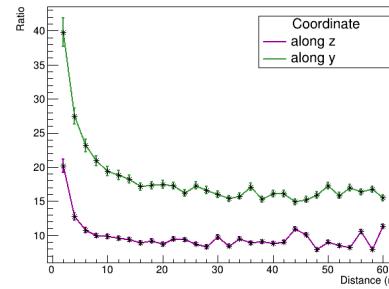


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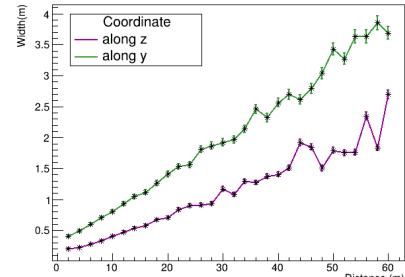
◆ “Thin” box



Width-to-pitch Ratio

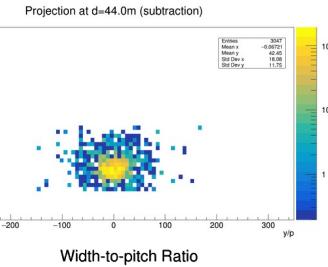


Monument's Width

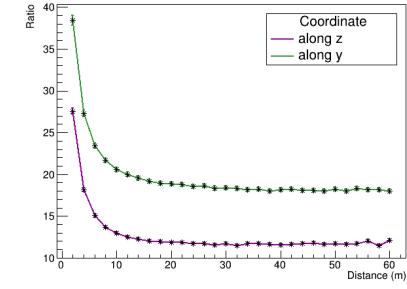


Ilia Kalaitzidou AUTh

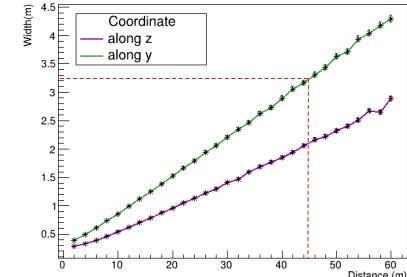
◆ “Thick” box



Width-to-pitch Ratio



Monument's Width

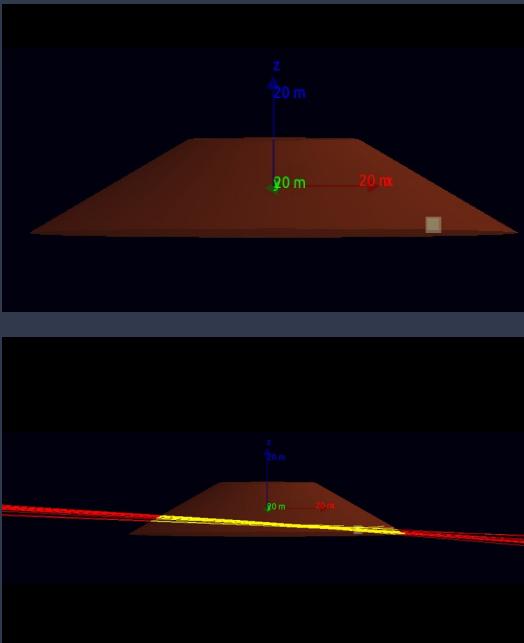


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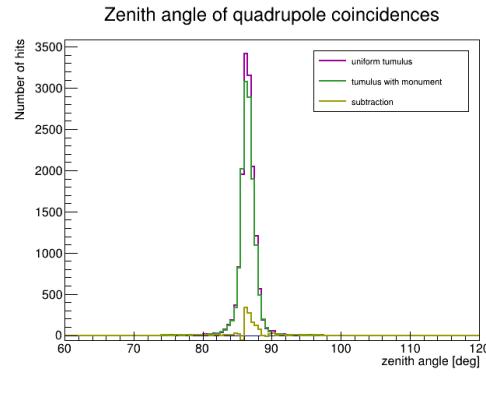
Back-projection method

Telescope at the side of the tumulus

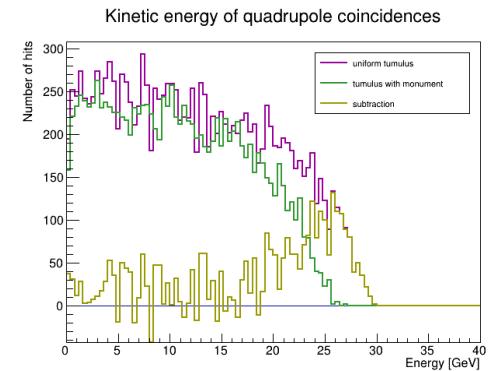
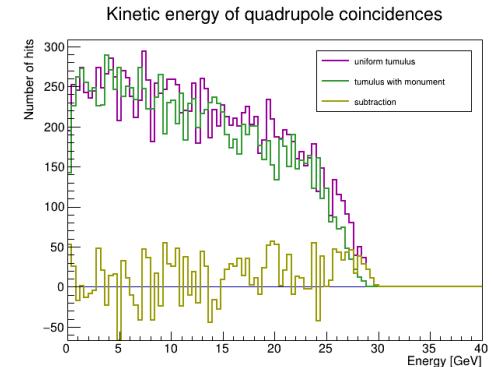
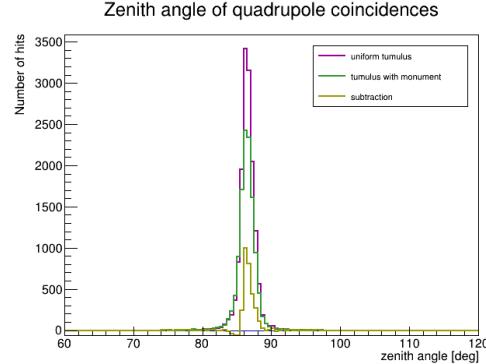
- Box at $x=30\text{m}$



◆ “Thin” box



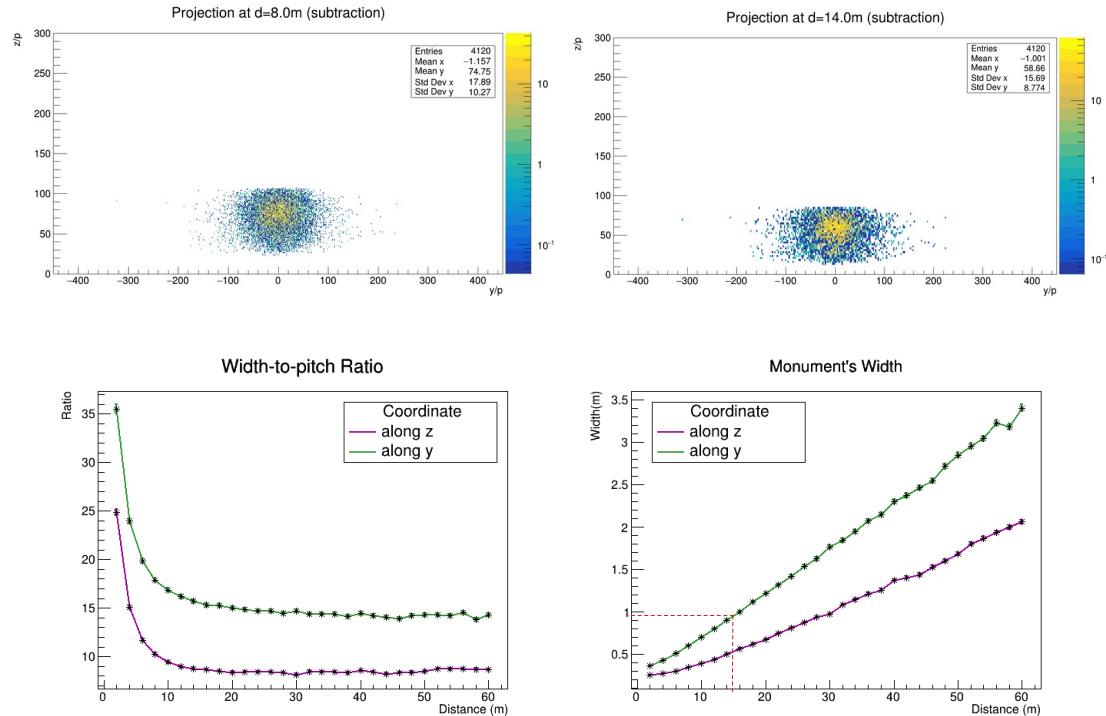
◆ “Thick” box



Back-projection method

Telescope at the side of the tumulus

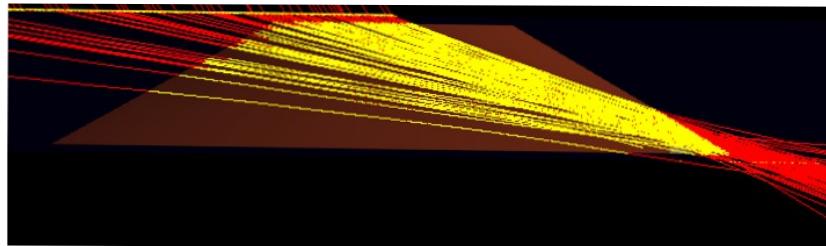
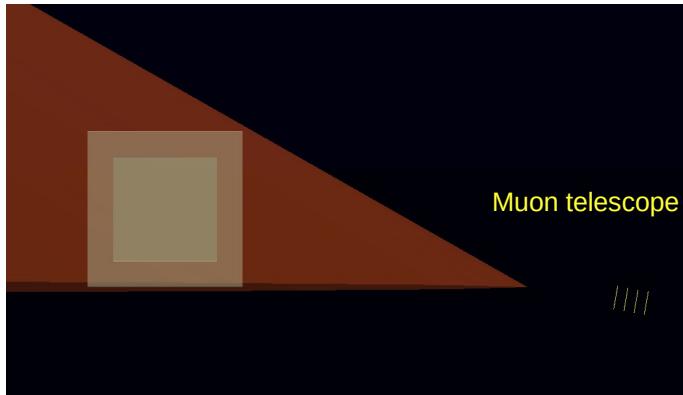
- Box at $x=30\text{m}$
- Energy range $20\text{-}30\text{GeV}$
- Zenith angle range $85\text{-}90^\circ$
- “Thick” marble box
- 2 billion initial muons



Back-Projection method

Telescope at the side of the tumulus

- Telescope centre at (48,0,-8.75)m below the ground level ($z=-8.5\text{m}$)
- Box at $x=39\text{m}$

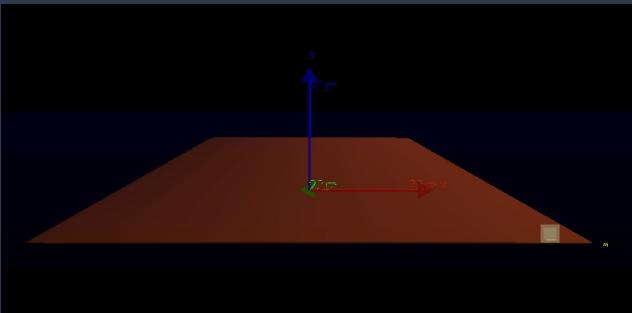


- Initial muon distributions
 - i. Energy: 15-30GeV
 - ii. Zenith: $70\text{-}88^\circ$
 - iii. Azimuth: $78\text{-}102^\circ$
- 300x40m generation plane at (-150,0,9.55)m

Back-projection method

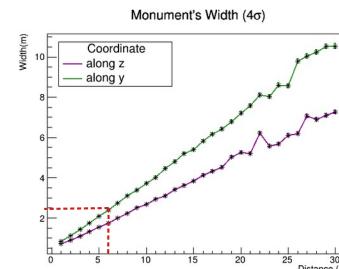
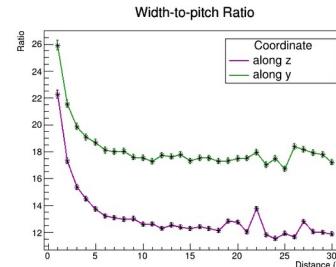
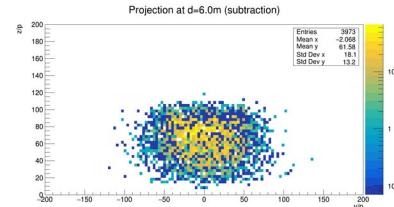
Telescope at the side of the tumulus

- Box at $x=39\text{m}$
- “Thick” marble box
- Two pitch values:
 $p=3\text{mm} \rightarrow \delta_\theta=5\text{mrad}$
 $p=5\text{mm} \rightarrow \delta_\theta=8.33\text{mrad}$
- Monument width $\rightarrow 4\sigma$ (instead of FWHM)

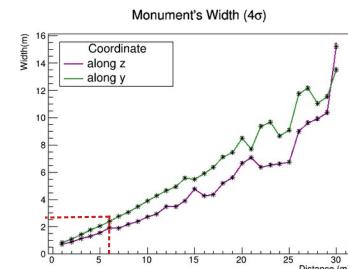
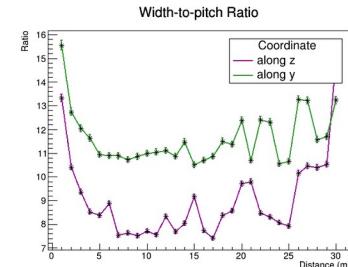
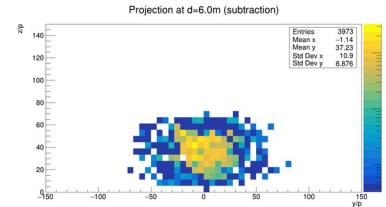


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◆ 3mm pitch



◆ 5mm pitch



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