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```
1. The answers are below:
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```
(a) > seq(1, 28, by = 3)
[1] 1 4 7 10 13 16 19 22 25 28
```

- (b) > paste(rep(letters[-1:-23], 3:1), rep(letters[1:3], 2), sep = "")
 [1] "xa" "xb" "xc" "ya" "yb" "zc"
- (c) > rep(1:3 < 2, 2)
 [1] TRUE FALSE FALSE TRUE FALSE FALSE</pre>
- (d) > cumsum(10^(seq(0, 8, by = 2)))
 [1] 1 101 10101 1010101 101010101
- (e) > 1:4 + rep(0:3, rep(4, 4))
 [1] 1 2 3 4 2 3 4 5 3 4 5 6 4 5 6 7

2. The answers are below:

> str(eurocities.df)

'data.frame': 209 obs. of 3 variables:
\$ Athens : chr "Athens" "Athens" "Athens" "Athens" ...

\$ Barcelona: chr "Brussels" "Calais" "Cherbourg" "Cologne" ...

\$ X3313 : int 2963 3175 3339 2762 3276 2610 4485 2977 3030 4532 ...

> head(eurocities.df)

Athens Barcelona X3313

1 Athens Brussels 2963

2 Athens Calais 3175

3 Athens Cherbourg 3339

4 Athens Cologne 2762

5 Athens Copenhagen 3276

6 Athens Geneva 2610

>

> distance.mean = mean(eurocities.df\$X3313)

> distance.mean

[1] 1496.498

(b) > maxd = max(eurocities.df\$X3313)

> con = (eurocities.df\$X3313 == maxd)

> maxdnum = rownames(eurocities.df)[con]

> eurocities.df[maxdnum, 1:2]

Athens Barcelona

10 Athens Lisbon

> maxdnum = which.max(eurocities.df\$X3313)

> maxpair = c(eurocities.df\$Athens[maxdnum], eurocities.df\$Barcelona[maxdnum])

```
> maxpair
   [1] "Athens" "Lisbon"
(c) > length(which((eurocities.df$Athens == "Paris"
            | eurocities.df$Barcelona == "Paris")
           & eurocities.df$X3313 <= 300))
   [1] 2
(d) > num = which(eurocities.df$Athens == "Copenhagen"
                 | eurocities.df$Barcelona == "Copenhagen")
   >
   > copenhargen.df = data.frame(eurocities.df[num,])
   > d_sort = sort(copenhargen.df$X3313)
   > d_min3 = d_sort[1:3]
   > d min3
   [1] 269 460 650
   > cities3 = character(3)
   > for (i in 1:3) {
       min_No = which(copenhargen.df$X3313 == d_min3[i])
      cities3[i] = copenhargen.df$Barcelona[min_No]
       if (cities3[i] == "Copenhagen")
         cities3[i] = copenhargen.df$Athens[min_No]
   + }
   > cities3
   [1] "Hook of Holland" "Hamburg"
                                            "Stockholm"
(e) > num_start = which((eurocities.df$Athens == "Rome"
                        | eurocities.df$Athens == "Stockholm")
                       & (eurocities.df$Barcelona != "Rome"
                           & eurocities.df$Barcelona != "Stockholm"))
   > num_end = which((eurocities.df$Barcelona == "Rome"
                      | eurocities.df$Barcelona == "Stockholm")
                     & (eurocities.df$Athens != "Rome"
                         & eurocities.df$Athens != "Stockholm"))
   > start.df = data.frame(eurocities.df[num_start,])
   > end.df = data.frame(eurocities.df[num_end,])
   > ## col is the column that contain the other same cities to the 2 cities
   > findcity.min = function(df, col, cityvec) {
       rows = rownames(df)
      rownum = nrow(df)
       colnum = ncol(df)
       distances = numeric(rownum \%/\% 2)
       cityvec.sort = sort(cityvec)
       for (i in seq(2, rownum, by = 2)) {
         # find the row number of two distances from 1 same city
         twodt.No = rows[df[, col] == cityvec.sort[i]]
         # add the two distance from the same sity
```

```
+
          }
          mindt = min(distances)
          distance_num = 1:length(distances)
          min_num = distance_num[distances == mindt]
          min_city = cityvec.sort[min_num * 2]
          list(city = min_city, min = mindt)
      + }
      > lst1 = findcity.min(start.df, 2, start.df$Barcelona)
      > lst1
      $city
      [1] "Vienna"
      $min
      [1] 3314
      > lst2 = findcity.min(end.df, 1, end.df$Athens)
      > 1st2
      $city
      [1] "Copenhagen" "Hamburg"
                                     "Munich"
      $min
      [1] 2700
      > if (lst1$min < lst2$min) lst1$city else lst2$city</pre>
      [1] "Copenhagen" "Hamburg"
                                  "Munich"
3. The answers are below:
   (a) > hemite1 = function(xseq, n) {
          for (x in xseq) {
            res = 0
      +
            for (m in 0:floor(n / 2)) {
              res = res + (-1)^m / (factorial(m) * factorial(n - 2 * m))
      * x^(n - 2 * m) / 2^m
            print(factorial(n) * res)
          }
      + }
      > hemite1(seq(-2, 2, by = .2), 5)
      [1] 18
       [1] 12.42432
```

distances[i %/% 2] = df[twodt.No[1], colnum] + df[twodt.No[2], colnum]

```
[1] 6.47424
   [1] 1.06176
   [1] -3.20832
   [1] -6
   [1] -7.20768
   [1] -6.91776
   [1] -5.37024
   [1] -2.92032
   [1] 0
   [1] 2.92032
   [1] 5.37024
   [1] 6.91776
   [1] 7.20768
   [1] 6
   [1] 3.20832
   [1] -1.06176
   [1] -6.47424
   [1] -12.42432
   [1] -18
(b) > hemite2 = function(xseq, n) {
       for (x in xseq) {
         upval = floor(n / 2)
   +
         mrange = 0:upval
         res = factorial(n) * sum((-1)^mrange
                                   / (factorial(mrange) * factorial(n - 2 * mrange))
                                   * x^(n - 2 * mrange) / 2^mrange)
         print(res)
   +
       }
   + }
   > hemite2(seq(-2, 2, by = .2), 5)
   [1] 18
   [1] 12.42432
   [1] 6.47424
   [1] 1.06176
   [1] -3.20832
   [1] -6
   [1] -7.20768
   [1] -6.91776
   [1] -5.37024
   [1] -2.92032
   [1] 0
   [1] 2.92032
   [1] 5.37024
   [1] 6.91776
   [1] 7.20768
```

```
[1] 6
      [1] 3.20832
      [1] -1.06176
      [1] -6.47424
      [1] -12.42432
      [1] -18
   (c) > hemite3.1 = function(x, m, n) {
          (-1)^m / (factorial(m) * factorial(n - 2 * m)) * x^(n - 2 * m) / 2^m
      + }
      >
      > hemite3.2 = function(x, n) {
          factorial(n) * sum(x)
      + }
      > hemite.seq = function(x, n) {
          m = 0:floor(n / 2)
          hemite3.3 = function(x, m) hemite3.1(x, m, n)
          hemite3.4 = function(x) hemite3.2(x, n)
         o = outer(x, m, hemite3.3)
          apply(o, 1, hemite3.4)
      + }
      > x = seq(-2, 2, by = .2)
      > hemite.seq(x, 5)
       [1] 18.00000 12.42432
                                 6.47424 1.06176 -3.20832 -6.00000 -7.20768
        -6.91776 -5.37024 -2.92032
             0.00000
                       2.92032
                                 5.37024 6.91776 7.20768 6.00000
                                                                          3.20832
      -1.06176 -6.47424 -12.42432
      [21] -18.00000
4. The answers are below:
  > hemite.coef = function(n) {
      if (n > 0) {
        x = seq(length = n + 1, from = 1)
        # contruct the value matrix
        A = outer(x, 0:n, "^")
        H = hemite.seq(x, n) # use functions in question 3
        # using round when x are not intergers
        round(solve(A, H))
      }
      else 1
  + }
  > hemite = function(n) {
```

```
coef.matrix = matrix(0, nrow = n + 1, ncol = n + 1,
  +
                           dimnames = list(paste("H", 0:n, sep = ""),
                                            paste("x^", 0:n, sep = "")))
  +
      for (i in 0:n) {
        coef.matrix[i + 1,] = c(hemite.coef(i), rep(0, n - i))
      }
      coef.matrix
  + }
  >
  > hemite(0)
     x^0
  HO 1
  > hemite(1)
     x^0 x^1
  НО
       1 0
  H1
       0
           1
  > hemite(3)
     x^0 x^1 x^2 x^3
      1 0
               0
  НО
  H1
       0
           1
               0
           0
  H2 -1
      0 -3
  НЗ
               0
  > hemite(10)
                       x^3
                             x^4 x^5 x^6 x^7 x^8 x^9 x^10
       x^0 x^1 x^2
  НО
         1
              0
                   0
                         0
                               0
                                    0
                                        0
                                            0
                                                0
                                                    0
         0
                   0
                                                         0
  H1
              1
                          0
                                0
                                    0
                                        0
                                            0
  H2
        -1
              0
                         0
                                0
                                   0
                                       0
                                                         0
                   1
                                            0
  НЗ
         0
             -3
                   0
                         1
                                0
                                    0
                                            0
         3
             0
  H4
                  -6
                         0
                                1
                                    0
                                       0 0
  Н5
         0
             15
                   0
                       -10
                                0
                                    1
                                      0 0
                                                         0
  Н6
       -15
              0
                  45
                          0
                             -15
                                    0
                                       1
                                            0
                                                0
                                                         0
         0 -105
                                0 -21
  H7
                   0
                       105
                                      0
                                            1
                                                0
                                                    0
                                                         0
       105
              0 - 420
                          0
                              210
                                    0 -28
                                            0
                                                    0
                                                         0
  Н8
                                                1
         0 945
                   0 -1260
                                0 378
                                        0 -36
                                                0
                                                    1
                                                         0
  Н9
  H10 -945
              0 4725
                         0 -3150
                                    0 630
                                            0 - 45
5. The answers are below:
```

```
(a) > f = function(x) sin(x) + exp((-1) * x / 10)
   >
   > root = function(f, interval) {
       a = interval[1]
       b = interval[2]
       i = 1
   +
       while ((f(a) * f(b)) < 0
              && abs(f(a) - f(b)) > 1e-08
```

```
&& i < 1000) {
         c = (a + b) / 2
         tmp = f(c)
         if(sign(tmp) == sign(f(a)))
           a = c
         else
           b = c
         i = i + 1
       }
       if (i < 1000) {
         if ((f(a) * f(b)) < 0) a
           print("couldn't find root within this interval!")
           NA
         }
       }
       else {
         print("no root can be found!")
       }
   + }
   > root(f, c(0, 5))
   [1] 3.886584
(b) > allroot = function(f, interval) {
       a = interval[1]
       b = interval[2]
       points = seq(a, b, length.out = 1000)
       con = f(points) >= 0
       positives = sort(points[con])
       negatives = sort(points[!con])
       #print(positives)
       #print(negatives)
       if (positives[1] < negatives[1]) {</pre>
         low = positives[1]
         high = negatives[1]
         con = TRUE
       }
   +
       else {
         low = negatives[1]
         high = positives[1]
         con = FALSE
```

```
}
+
   roots = numeric(1000)
    i = 1
   j = 1
   up1 = length(positives)
   up2 = length(negatives)
   while(low < high) {</pre>
      if (con) {
        lows = positives[i:up1]
      }
      else {
        lows = negatives[i:up2]
+
      nums = which(lows < high)</pre>
+
      len = length(nums)
      low = lows[nums[len]]
      #print(c(low, high))
      # save each root
      roots[j] = root(f, c(low, high))
      j = j + 1
      low = high
      if (nums[len] == length(lows))
        high = lows[nums[len]]
      else
        high = lows[nums[len] + 1]
+
      if (con)
        i = which(negatives == low)
+
+
      else
        i = which(positives == low)
      con = !con
   }
   roots[1:(j - 1)]
+ }
> allroot(f, c(0, 50))
 [1] 3.886584 5.680796 9.809140 12.268792 15.913058
 18.694733 22.101059 25.050983 28.333185 31.372511
[11] 34.588989 37.676002 40.857516 43.969983 47.132865
```