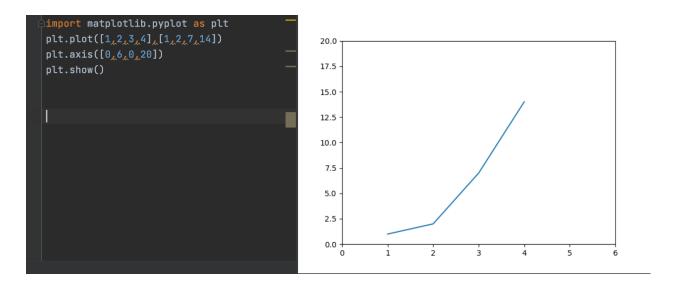
Assignment 0 - COMP 576

Zan (Tian) Zhang

1. Conda info

```
active environment : base
    active env location : /Users/zanzhang/opt/anaconda3
           shell level : 2
      user config file : /Users/zanzhang/.condarc
populated config files : /Users/zanzhang/.condarc
         conda version: 4.9.2
    conda-build version : 3.20.5
        python version: 3.8.5.final.0
      virtual packages : __osx=10.16=0
                         __unix=0=0
                           _archspec=1=x86_64
      base environment : /Users/zanzhang/opt/anaconda3 (writable)
          channel URLs: https://repo.anaconda.com/pkgs/main/osx-64
                         https://repo.anaconda.com/pkgs/main/noarch
                         https://repo.anaconda.com/pkgs/r/osx-64
                         https://repo.anaconda.com/pkgs/r/noarch
         package cache : /Users/zanzhang/opt/anaconda3/pkgs
                          /Users/zanzhang/.conda/pkgs
      envs directories : /Users/zanzhang/opt/anaconda3/envs
                          /Users/zanzhang/.conda/envs
              platform : osx-64
            user-agent : conda/4.9.2 requests/2.24.0 CPython/3.8.5 Darwin/21.5.0 OSX/10.16
               UID:GID: 501:20
            netrc file : /Users/zanzhang/.netrc
          offline mode : False
(base) Sweets-Mac-Pro:~ zanzhang$
```

- 2. See below
- 3. Task 3



4. Task 4



5. Github account: zzhang786



6. https://github.com/zzhang786/zz93_Assignment_0

History:

Untitled

September 14, 2022

```
[8]: import numpy as np
      import scipy.linalg
 [9]: a=np.arange(20).reshape(4,5)
 [9]: array([[ 0, 1, 2, 3, 4],
             [5, 6, 7, 8, 9],
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19]])
[10]: a.ndim
[10]: 2
[11]: a.size
[11]: 20
[12]: a.shape
[12]: (4, 5)
[14]: a.shape[2-1]
[14]: 5
[15]: a.shape[1-1]
[15]: 4
[16]: a.shape[0-1]
[16]: 5
[17]: a.shape[2-1]
[17]: 5
```

```
[18]: np.array([[1.,2.,3],[4.,5.,6.]])
[18]: array([[1., 2., 3.],
             [4., 5., 6.]])
[20]: np.block([[1, 2], [3, 4]])
[20]: array([[1, 2],
             [3, 4]])
[21]: a[-1]
[21]: array([15, 16, 17, 18, 19])
[22]: a[1, 4]
[22]: 9
[23]: a[1]
[23]: array([5, 6, 7, 8, 9])
[24]: a[0:5]
[24]: array([[ 0, 1, 2, 3, 4],
             [5, 6, 7, 8, 9],
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19]])
[27]: a=np.arange(49).reshape(7,7)
      a
[27]: array([[ 0, 1, 2, 3, 4, 5, 6],
             [7, 8, 9, 10, 11, 12, 13],
             [14, 15, 16, 17, 18, 19, 20],
             [21, 22, 23, 24, 25, 26, 27],
             [28, 29, 30, 31, 32, 33, 34],
             [35, 36, 37, 38, 39, 40, 41],
             [42, 43, 44, 45, 46, 47, 48]])
[28]: a[0:5]
[28]: array([[ 0, 1, 2, 3, 4, 5, 6],
             [7, 8, 9, 10, 11, 12, 13],
             [14, 15, 16, 17, 18, 19, 20],
             [21, 22, 23, 24, 25, 26, 27],
             [28, 29, 30, 31, 32, 33, 34]])
```

```
[29]: a[-5:]
[29]: array([[14, 15, 16, 17, 18, 19, 20],
             [21, 22, 23, 24, 25, 26, 27],
             [28, 29, 30, 31, 32, 33, 34],
             [35, 36, 37, 38, 39, 40, 41],
             [42, 43, 44, 45, 46, 47, 48]])
[30]: a[0:3,4:9]
[30]: array([[ 4, 5, 6],
             [11, 12, 13],
             [18, 19, 20]])
[47]: a=np.arange(25).reshape(5,5)
      a[0:5]#[Out]# array([[ 0, 1, 2, 3, 4],
[47]: array([[ 0, 1, 2, 3, 4],
             [5, 6, 7, 8, 9],
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19],
             [20, 21, 22, 23, 24]])
[33]: a[-5:]
[33]: array([[ 0, 1, 2, 3, 4],
             [5, 6, 7, 8, 9],
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19]])
[35]: a[0:3, 4:9]
[35]: array([[ 4],
             [ 9],
             [14]])
[48]: a[np.ix_([1, 3, 4], [0, 2])]
[48]: array([[5, 7],
             [15, 17],
             [20, 22]])
[49]: a[2:21:2,:]
[49]: array([[10, 11, 12, 13, 14],
             [20, 21, 22, 23, 24]])
```

```
[50]: a[::2,:]
[50]: array([[ 0, 1, 2, 3, 4],
            [10, 11, 12, 13, 14],
            [20, 21, 22, 23, 24]])
[51]: a[::-1,:]
[51]: array([[20, 21, 22, 23, 24],
            [15, 16, 17, 18, 19],
            [10, 11, 12, 13, 14],
            [5, 6, 7, 8, 9],
            [ 0, 1, 2,
                         3, 4]])
[52]: a[np.r_[:len(a),0]]
[52]: array([[ 0, 1, 2, 3, 4],
            [5, 6, 7, 8, 9],
            [10, 11, 12, 13, 14],
            [15, 16, 17, 18, 19],
            [20, 21, 22, 23, 24],
            [0, 1, 2, 3, 4]])
[53]: a.transpose()
[53]: array([[ 0, 5, 10, 15, 20],
            [ 1, 6, 11, 16, 21],
            [ 2, 7, 12, 17, 22],
            [3, 8, 13, 18, 23],
            [4,
                  9, 14, 19, 24]])
[54]: a.conj().transpose()
[54]: array([[ 0, 5, 10, 15, 20],
            [ 1, 6, 11, 16, 21],
            [2, 7, 12, 17, 22],
            [3, 8, 13, 18, 23],
            [4, 9, 14, 19, 24]])
[60]: b=np.arange(25).reshape(5,5)
     b
[60]: array([[ 0, 1, 2, 3, 4],
            [5, 6, 7, 8, 9],
            [10, 11, 12, 13, 14],
            [15, 16, 17, 18, 19],
            [20, 21, 22, 23, 24]])
```

```
[61]: a @ b
[61]: array([[ 150,
                     160,
                          170,
                                180,
                                      190],
                     435,
                           470, 505, 540],
             [ 400,
             [ 650,
                     710, 770, 830, 890],
                     985, 1070, 1155, 1240],
             [ 900,
             [1150, 1260, 1370, 1480, 1590]])
[62]: a * b
[62]: array([[ 0,
                          4,
                               9,
                                   16],
                     1,
             [ 25, 36, 49, 64, 81],
             [100, 121, 144, 169, 196],
             [225, 256, 289, 324, 361],
             [400, 441, 484, 529, 576]])
[63]: a/b
     /var/folders/c3/x6v88t2n49793nvyhs2wv48m0000gn/T/ipykernel_93034/1348051284.py:1
     : RuntimeWarning: invalid value encountered in true_divide
       a/b
[63]: array([[nan,
                    1., 1., 1.,
                                   1.],
             [ 1.,
                    1.,
                         1.,
                              1.,
             [ 1.,
                   1., 1., 1.,
                                   1.],
             [ 1., 1., 1., 1.,
                                   1.],
             [ 1., 1., 1., 1.,
                                   1.]])
[64]: a**3
[64]: array([[
                  0,
                         1,
                                8,
                                      27,
                                             64],
               125,
                              343,
                       216,
                                     512,
                                            729],
             [ 1000,
                      1331, 1728,
                                    2197,
                                           2744],
                      4096, 4913, 5832,
             [ 3375,
                                           6859],
                     9261, 10648, 12167, 13824]])
             [ 8000,
[65]: (a > 0.5)
[65]: array([[False,
                      True,
                                           True],
                             True,
                                    True,
             [ True,
                      True,
                             True,
                                    True,
                                           True],
                      True, True,
                                           True],
             [True,
                                    True,
             [True,
                      True, True,
                                    True,
                                           True],
             [True,
                     True, True,
                                    True,
                                           True]])
[66]: np.nonzero(a > 0.5)
```

```
[66]: (array([0, 0, 0, 0, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 4, 4, 4,
            4, 4]),
      array([1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2,
            3, 4]))
[68]: np.nonzero(a>0.5)
[68]: (array([0, 0, 0, 0, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 4, 4, 4,
            4, 4]),
      array([1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2,
            3, 4]))
[77]: v=np.arange(20).reshape(4,5)
     a[:,np.nonzero(v>0.5)[0]]
[77]: array([[ 0, 0, 0, 0, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3,
                                                                    3,
             3, 3, 3],
            [5, 5, 5, 5, 6, 6, 6, 6, 7, 7, 7, 7, 7, 8,
             8, 8, 8],
            [10, 10, 10, 10, 11, 11, 11, 11, 12, 12, 12, 12, 12, 13, 13,
            13, 13, 13],
           [15, 15, 15, 15, 16, 16, 16, 16, 16, 17, 17, 17, 17, 17, 18, 18,
            18, 18, 18],
            23, 23, 23]])
[85]: v.T>0.5
     a[:, v.T > 0.5]
[85]: array([[False, True, True,
                                True],
           [ True,
                   True, True,
                                True],
           [ True,
                   True, True,
                                True],
           [ True, True, True,
                                True],
           [ True, True, True,
                                True]])
[91]: v=np.array([[1],[2],[3],[4],[0.1]])
[91]: array([[1.],
           [2.],
            [3.],
            [4.],
            [0.1]
[94]: a[a < 0.5]=0
     a
```

```
[94]: array([[ 0, 1, 2, 3, 4],
            [5, 6, 7, 8, 9],
            [10, 11, 12, 13, 14],
            [15, 16, 17, 18, 19],
            [20, 21, 22, 23, 24]])
[95]: a * (a > 0.5)
      a
[95]: array([[ 0, 1, 2, 3, 4],
            [5, 6, 7, 8, 9],
            [10, 11, 12, 13, 14],
            [15, 16, 17, 18, 19],
            [20, 21, 22, 23, 24]])
[97]: a[:] = 3
      a
[97]: array([[3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3]])
[100]: y = a.copy()
      У
[100]: array([[3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3],
            [3, 3, 3, 3, 3]])
[103]: y = a[1, :].copy()
      У
[103]: array([3, 3, 3, 3, 3])
[104]: y = a.flatten()
      У
3, 3, 3])
[105]: np.arange(1., 11.)
[105]: array([ 1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
```

```
[106]:
       np.r_[:10.]
[106]: array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
[107]: np.arange(1.,11.)[:, np.newaxis]
[107]: array([[ 1.],
              [2.],
              [3.],
              [4.],
              [5.],
              [ 6.],
              [7.],
              [8.],
              [ 9.],
              [10.]])
[108]: np.zeros((3, 4))
[108]: array([[0., 0., 0., 0.],
              [0., 0., 0., 0.],
              [0., 0., 0., 0.]])
[109]: np.zeros((3, 4, 5))
[109]: array([[[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
              [[0., 0., 0., 0., 0.],
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]
               [0., 0., 0., 0., 0.]]
[110]: np.ones((3, 4))
[110]: array([[1., 1., 1., 1.],
              [1., 1., 1., 1.],
              [1., 1., 1., 1.]])
[111]: np.eye(3)
```

```
[111]: array([[1., 0., 0.],
              [0., 1., 0.],
              [0., 0., 1.]])
[112]: np.diag(a)
[112]: array([3, 3, 3, 3, 3])
[113]: np.diag(v, 0)
[113]: array([1.])
[126]: from numpy.random import default_rng
       rng = default_rng(42)
       rng.random((3, 4))
[126]: array([[0.77395605, 0.43887844, 0.85859792, 0.69736803],
              [0.09417735, 0.97562235, 0.7611397, 0.78606431],
              [0.12811363, 0.45038594, 0.37079802, 0.92676499]])
[127]: np.linspace(1,3,4)
                                                             ])
[127]: array([1.
                        , 1.66666667, 2.333333333, 3.
[129]: np.mgrid[0:9.,0:6.]
[129]: array([[[0., 0., 0., 0., 0., 0.],
               [1., 1., 1., 1., 1., 1.]
               [2., 2., 2., 2., 2., 2.],
               [3., 3., 3., 3., 3., 3.]
               [4., 4., 4., 4., 4., 4.]
               [5., 5., 5., 5., 5., 5.]
               [6., 6., 6., 6., 6., 6.]
               [7., 7., 7., 7., 7., 7.]
               [8., 8., 8., 8., 8., 8.]
              [[0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.]])
[132]: np.ogrid[0:9.,0:6.]
```

```
[132]: [array([[0.],
    [1.],
    [2.],
    [3.],
    [4.],
    [5.],
    [6.],
    [7.],
    [8.]]),
  array([[0., 1., 2., 3., 4., 5.]])]
[133]: np.meshgrid([1,2,4],[2,4,5])
[133]: [array([[1, 2, 4],
    [1, 2, 4],
    [1, 2, 4]]),
  array([[2, 2, 2],
    [4, 4, 4],
    [5, 5, 5]])]
[141]: np.ix_([1,2,4],[2,4,5])
[141]: (array([[1],
    [2],
    [4]]),
  array([[2, 4, 5]]))
[143]: np.tile(a, (3, 4))
[144]: np.concatenate((a,b),1)
```

```
[144]: array([[ 3, 3, 3, 3, 0, 1, 2, 3, 4],
             [ 3,
                   3, 3, 3,
                              3, 5, 6, 7, 8, 9],
                          3, 3, 10, 11, 12, 13, 14],
             [ 3,
                      3,
                   3,
             [3, 3, 3, 3, 15, 16, 17, 18, 19],
             [ 3,
                   3,
                      3,
                         3, 3, 20, 21, 22, 23, 24]])
[145]: np.concatenate((a,b))
[145]: array([[ 3, 3,
                          3,
                              3],
                      3,
             [ 3,
                  3,
                      3,
                          3,
                              3],
             [3, 3,
                      3,
                          3,
                              3],
             [3,
                  3,
                      3,
                          3,
                              3],
             [3, 3,
                          3,
                      3,
                              3],
             [0, 1, 2, 3,
                              4],
             [5, 6, 7, 8, 9],
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19],
             [20, 21, 22, 23, 24]])
[146]: a.max()
[146]: 3
[147]: a.max(0)
[147]: array([3, 3, 3, 3, 3])
[148]: a.max(1)
[148]: array([3, 3, 3, 3, 3])
[149]: np.maximum(a, b)
[149]: array([[ 3, 3, 3, 4],
             [5, 6, 7, 8,
             [10, 11, 12, 13, 14],
             [15, 16, 17, 18, 19],
             [20, 21, 22, 23, 24]])
[151]: np.sqrt(a @ b)
[151]: array([[12.24744871, 12.84523258, 13.41640786, 13.96424004, 14.49137675],
             [12.24744871, 12.84523258, 13.41640786, 13.96424004, 14.49137675],
             [12.24744871, 12.84523258, 13.41640786, 13.96424004, 14.49137675],
             [12.24744871, 12.84523258, 13.41640786, 13.96424004, 14.49137675],
             [12.24744871, 12.84523258, 13.41640786, 13.96424004, 14.49137675]])
```

```
[153]: np.logical_and(a,b)
                      True,
[153]: array([[False,
                                          True],
                            True,
                                   True,
             [True,
                      True,
                             True,
                                    True,
                                          True],
             [True,
                      True,
                             True,
                                    True,
                                          True],
             [True,
                      True,
                             True,
                                   True,
                                          True],
                      True,
                             True,
                                          True]])
             [True,
                                   True,
[154]: np.logical_or(a,b)
[154]: array([[ True,
                      True,
                             True,
                                          True],
                                   True,
             [True,
                      True,
                            True,
                                          True],
                                   True,
             [ True,
                      True,
                             True,
                                          True],
                                   True,
                                          True],
             [ True,
                      True, True,
                                   True,
             [True,
                      True, True,
                                   True,
                                          True]])
[155]: a & b
[155]: array([[0, 1, 2, 3, 0],
             [1, 2, 3, 0, 1],
             [2, 3, 0, 1, 2],
             [3, 0, 1, 2, 3],
             [0, 1, 2, 3, 0])
[156]: a | b
[156]: array([[ 3, 3, 3, 3, 7],
             [7, 7, 7, 11, 11],
             [11, 11, 15, 15, 15],
             [15, 19, 19, 19, 19],
             [23, 23, 23, 23, 27]])
[167]: c = np.array([[1., 2.], [3., 4.]])
      np.linalg.inv(c)
[167]: array([[-2., 1.],
             [1.5, -0.5]
[168]: np.linalg.pinv(a)
[168]: array([[0.01333333, 0.01333333, 0.01333333, 0.01333333],
             [0.01333333, 0.01333333, 0.01333333, 0.01333333],
             [0.01333333, 0.01333333, 0.01333333, 0.01333333],
             [0.01333333, 0.01333333, 0.01333333, 0.01333333],
             [0.01333333, 0.01333333, 0.01333333, 0.01333333]])
```

```
[170]: np.linalg.matrix_rank(a)
[170]: 1
[272]: np.linalg.lstsq(a, b, rcond=None)
[272]: (array([[-0.02470314, -0.99426878, 0.24219306, -1.14861772, -0.45412453],
               [-1.57705109, -0.14924059, 0.45581515, -0.19976327, -0.1638319],
               [-1.46953047, -1.97687497, -0.39631202, -2.63141169, -1.54497317],
               [-0.27431161, -1.07540872, 0.03782807, -2.75632378, -1.24713453],
               [ 3.20349588, 3.7034493 , 0.33499671, 5.27929192, 3.32657953]]),
       array([], dtype=float64),
       array([2.65088822, 0.8711694, 0.63173817, 0.3178289, 0.11755287]))
[273]: np.linalg.solve(a.T, b.T)
[273]: array([[ 0.00000000e+00, -2.76036162e-17, 0.00000000e+00,
               1.00000000e+00, -2.18879201e-17],
              [0.00000000e+00, 2.30117314e-17, 1.00000000e+00,
               2.64098866e-17, 4.91314893e-17],
              [ 0.00000000e+00, 3.82746311e-17, -7.57194853e-18,
               5.73068798e-17, 1.00000000e+00],
              [ 1.00000000e+00, -2.26739682e-17, 4.06700635e-17,
              -6.28095737e-18, -4.91652864e-17],
              [-1.68592397e-17, 1.00000000e+00, -8.26305469e-17,
              -8.63574988e-17, 4.33516032e-17]])
[179]: U, S, Vh = np.linalg.svd(a);
      V = Vh.T
      V
[179]: array([[-0.4472136, 0.89442719, 0.
                                                   , 0.
                                                                , 0.
                                                                             ],
                                                   , -0.5
             [-0.4472136 , -0.2236068 , -0.5
                                                                 , -0.5
                                                                             ],
              [-0.4472136, -0.2236068, -0.16666667, -0.16666667, 0.83333333],
             [-0.4472136, -0.2236068, -0.16666667, 0.83333333, -0.16666667],
             [-0.4472136 , -0.2236068 , 0.83333333, -0.16666667, -0.16666667]])
[188]: A = np.array([[1,-2j],[2j,5]])
      L = np.linalg.cholesky(A)
      L
[188]: array([[1.+0.j, 0.+0.j],
             [0.+2.j, 1.+0.j])
```

```
[191]: D,V = np.linalg.eig(a)
[191]: array([1.50000000e+01+0.00000000e+00j, 1.10535203e-32+1.49491076e-24j,
              1.10535203e-32-1.49491076e-24j, 0.00000000e+00+0.00000000e+00j,
              9.27495619e-65+0.00000000e+00j])
[192]: V
[192]: array([[-4.47213595e-01+0.00000000e+00j, 3.05673275e-17+5.18266518e-09j,
                3.05673275e-17-5.18266518e-09j, -4.87104483e-49+0.00000000e+00j,
               -9.50718352e-50+0.00000000e+00j],
              [-4.47213595e-01+0.00000000e+00j, 8.66025404e-01+0.00000000e+00j,
                8.66025404e-01-0.00000000e+00j, -3.09522653e-32+0.00000000e+00j,
                2.79765981e-16+0.00000000e+00j],
              [-4.47213595e-01+0.00000000e+00j, -2.88675135e-01-1.72755506e-09j,
               -2.88675135e-01+1.72755506e-09j, -2.98122760e-16+0.00000000e+00j,
                8.16496581e-01+0.00000000e+00j],
              [-4.47213595e-01+0.00000000e+00j, -2.88675135e-01-1.72755506e-09j,
               -2.88675135e-01+1.72755506e-09j, -7.07106781e-01+0.00000000e+00j,
               -4.08248290e-01+0.00000000e+00j],
              [-4.47213595e-01+0.00000000e+00j, -2.88675135e-01-1.72755506e-09j,
               -2.88675135e-01+1.72755506e-09j, 7.07106781e-01+0.00000000e+00j,
               -4.08248290e-01+0.00000000e+00j]])
[220]: w, v = np.linalg.eig((a, b))
[220]: array([[ 1.50000000e+01+0.00000000e+00j, 1.10535203e-32+1.49491076e-24j,
                1.10535203e-32-1.49491076e-24j,
                                                 0.0000000e+00+0.0000000e+00j,
                9.27495619e-65+0.00000000e+00j],
              [ 6.39116499e+01+0.00000000e+00j, -3.91164992e+00+0.00000000e+00j,
                3.19626490e-15+0.00000000e+00j, -1.64396509e-15+0.00000000e+00j,
                8.90756696e-17+0.00000000e+00j]])
[221]: v
[221]: array([[[-4.47213595e-01+0.00000000e+00j,
                 3.05673275e-17+5.18266518e-09j,
                 3.05673275e-17-5.18266518e-09j,
                -4.87104483e-49+0.00000000e+00j,
                -9.50718352e-50+0.00000000e+00j],
               [-4.47213595e-01+0.00000000e+00j,
                 8.66025404e-01+0.00000000e+00j,
                 8.66025404e-01-0.00000000e+00j,
                -3.09522653e-32+0.00000000e+00j,
                 2.79765981e-16+0.00000000e+00j],
```

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-2.88675135e-01-1.72755506e-09j,
                -2.88675135e-01+1.72755506e-09j,
                -2.98122760e-16+0.00000000e+00j,
                 8.16496581e-01+0.00000000e+00j],
               [-4.47213595e-01+0.00000000e+00j,
                -2.88675135e-01-1.72755506e-09j,
                -2.88675135e-01+1.72755506e-09j,
                -7.07106781e-01+0.00000000e+00j,
                -4.08248290e-01+0.00000000e+00j],
               [-4.47213595e-01+0.00000000e+00]
                -2.88675135e-01-1.72755506e-09j,
                -2.88675135e-01+1.72755506e-09j,
                 7.07106781e-01+0.00000000e+00j,
                -4.08248290e-01+0.00000000e+00j]],
              [[-8.51802044e-02+0.00000000e+00],
                 6.77798642e-01+0.00000000e+00j,
                 6.94530680e-02+0.00000000e+00j,
                -3.91484356e-01+0.00000000e+00j,
                -1.09858325e-01+0.00000000e+00j],
               [-2.38253717e-01+0.00000000e+00]
                 3.63488728e-01+0.00000000e+00j,
                 4.40322277e-01+0.00000000e+00j,
                 2.90591999e-01+0.00000000e+00j,
                -3.33805478e-02+0.00000000e+00j],
               [-3.91327229e-01+0.00000000e+00j,
                 4.91788140e-02+0.00000000e+00j,
                -5.72004887e-01+0.00000000e+00j,
                 1.85712658e-02+0.00000000e+00j,
                 6.33521649e-01+0.00000000e+00j],
               [-5.44400741e-01+0.00000000e+00j,
                -2.65131100e-01+0.00000000e+00j,
                -4.54769328e-01+0.00000000e+00j,
                 6.57018896e-01+0.00000000e+00j,
                -7.27468356e-01+0.00000000e+00j],
               [-6.97474253e-01+0.00000000e+00j,
                -5.79441014e-01+0.00000000e+00j,
                 5.16998870e-01+0.00000000e+00j,
                -5.74697805e-01+0.00000000e+00j,
                 2.37185580e-01+0.00000000e+00j]]])
[229]: from scipy.sparse.linalg import eigs
      D, V = eigs(np.eye(5), k=3)
      D
[229]: array([1.+0.j, 1.+0.j, 1.+0.j])
```

[-4.47213595e-01+0.00000000e+00j,

```
[230]: V
[230]: array([[ 0.73493183+0.j, 0.29509892+0.j, 0.27007783+0.j],
              [-0.25460993+0.j, 0.34494288+0.j, -0.33995228+0.j],
              [0.34159688+0.j, -0.37974661+0.j, -0.81110163+0.j],
              [0.52749507+0.j, 0.13582134+0.j, -0.0330806 +0.j],
              [0.01046501+0.j, -0.79452886+0.j, 0.39052559+0.j]]
[215]: Q,R = np.linalg.qr(a)
[215]: array([[-4.47213595e-01, 8.94427191e-01, -4.01682464e-17,
               0.00000000e+00, 0.0000000e+00],
              [-4.47213595e-01, -2.23606798e-01, 8.66025404e-01,
               0.00000000e+00, 2.14690125e-18],
              [-4.47213595e-01, -2.23606798e-01, -2.88675135e-01,
               8.16496581e-01, -8.68448956e-17],
              [-4.47213595e-01, -2.23606798e-01, -2.88675135e-01,
              -4.08248290e-01, -7.07106781e-01],
              [-4.47213595e-01, -2.23606798e-01, -2.88675135e-01,
              -4.08248290e-01, 7.07106781e-01]])
[216]: R
[216]: array([[-6.70820393e+00, -6.70820393e+00, -6.70820393e+00,
              -6.70820393e+00, -6.70820393e+00],
              [0.00000000e+00, -1.44688132e-15, -1.44688132e-15,
              -1.44688132e-15, -1.44688132e-15],
              [ 0.00000000e+00, 0.0000000e+00, -1.26263380e-32,
              -1.26263380e-32, -1.26263380e-32],
              [ 0.0000000e+00, 0.0000000e+00, 0.0000000e+00,
               6.52838235e-49, 6.52838235e-49],
              [ 0.0000000e+00, 0.0000000e+00, 0.0000000e+00,
               0.00000000e+00, -9.51666664e-66]])
[232]: from scipy.linalg import lu
      P,L,U = lu(a)
      Ρ
[232]: array([[1., 0., 0., 0., 0.],
              [0., 1., 0., 0., 0.],
              [0., 0., 1., 0., 0.],
              [0., 0., 0., 1., 0.],
              [0., 0., 0., 0., 1.]]
[233]: L
```

```
[233]: array([[1., 0., 0., 0., 0.],
              [1., 1., 0., 0., 0.],
              [1., 0., 1., 0., 0.],
              [1., 0., 0., 1., 0.],
              [1., 0., 0., 0., 1.]]
[234]: U
[234]: array([[3., 3., 3., 3., 3.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]])
[235]: np.fft.fft(a)
[235]: array([[15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
              [15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j,
                                                    0.+0.j],
              [15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j,
                                                   0.+0.j],
              [15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
              [15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]
[236]: np.fft.ifft(a)
[236]: array([[3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
              [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
              [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j],
              [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]
              [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]]
[250]: a = np.random.rand(5,5)
[251]: np.sort(a)
[251]: array([[0.13382594, 0.38810458, 0.62843572, 0.70302585, 0.81114902],
              [0.03135856, 0.36136427, 0.54705689, 0.59120535, 0.73782371],
              [0.19279555, 0.64519405, 0.67682124, 0.72091305, 0.96818829],
              [0.10955931, 0.59617498, 0.60177775, 0.8718779, 0.95801931],
              [0.09933875, 0.20403836, 0.21766352, 0.3926468, 0.48003049]])
[255]: np.sort(a, axis=1)
[255]: array([[0.13382594, 0.38810458, 0.62843572, 0.70302585, 0.81114902],
              [0.03135856, 0.36136427, 0.54705689, 0.59120535, 0.73782371],
              [0.19279555, 0.64519405, 0.67682124, 0.72091305, 0.96818829],
              [0.10955931, 0.59617498, 0.60177775, 0.8718779, 0.95801931],
              [0.09933875, 0.20403836, 0.21766352, 0.3926468 , 0.48003049]])
```

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[256]: I = np.argsort(a[:, 0]); b = a[I,:]
[256]: array([[0.10955931, 0.59617498, 0.60177775, 0.95801931, 0.8718779],
              [0.21766352, 0.09933875, 0.20403836, 0.3926468, 0.48003049],
              [0.54705689, 0.36136427, 0.73782371, 0.03135856, 0.59120535],
              [0.70302585, 0.81114902, 0.38810458, 0.13382594, 0.62843572],
              [0.96818829, 0.72091305, 0.19279555, 0.64519405, 0.67682124]])
[271]: np.linalg.lstsq(a, b, rcond=None)
[271]: (array([[-0.02470314, -0.99426878, 0.24219306, -1.14861772, -0.45412453],
               [-1.57705109, -0.14924059, 0.45581515, -0.19976327, -0.1638319],
               [-1.46953047, -1.97687497, -0.39631202, -2.63141169, -1.54497317],
               [-0.27431161, -1.07540872, 0.03782807, -2.75632378, -1.24713453],
               [3.20349588, 3.7034493, 0.33499671, 5.27929192, 3.32657953]]),
       array([], dtype=float64),
       array([2.65088822, 0.8711694, 0.63173817, 0.3178289, 0.11755287]))
[268]: from scipy import signal
      signal.resample(a, int(np.ceil(len(a)/3)))
[268]: array([[0.5360673, 0.47297501, 0.43944106, 0.01933851, 0.53229089],
              [0.48213024, 0.56260103, 0.41037492, 0.84507935, 0.76705739]])
[269]: np.unique(a)
[269]: array([0.03135856, 0.09933875, 0.10955931, 0.13382594, 0.19279555,
             0.20403836, 0.21766352, 0.36136427, 0.38810458, 0.3926468,
             0.48003049, 0.54705689, 0.59120535, 0.59617498, 0.60177775,
             0.62843572, 0.64519405, 0.67682124, 0.70302585, 0.72091305,
             0.73782371, 0.81114902, 0.8718779 , 0.95801931, 0.96818829])
[270]: a.squeeze()
[270]: array([[0.70302585, 0.81114902, 0.38810458, 0.13382594, 0.62843572],
              [0.54705689, 0.36136427, 0.73782371, 0.03135856, 0.59120535],
              [0.96818829, 0.72091305, 0.19279555, 0.64519405, 0.67682124],
              [0.10955931, 0.59617498, 0.60177775, 0.95801931, 0.8718779],
              [0.21766352, 0.09933875, 0.20403836, 0.3926468 , 0.48003049]])
```