

# Homework 3

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## 1 Introduction

The Monte Carlo analysis is a board class of computer algorithms that rely on repeated random sampling to obtain numerical results. What Granger and Newbold did to replicate this Monte Carlo scheme was that they did a spurious regression, Granger and Newbold regressed two different random walks together and put them through a loop where there is around 100 simulations to see the percentage of times that  $H_0$  ( $H_0$  = no relationship) is rejected. They showed that out of 100 simulations of random walks, it showed there to be a high amount of times that  $H_0$  was reject showing that there is a relationship, but there was a low  $R^2$  meaning that the has a weak correlation of the linear relationship between the two random walks . In the first test there was 76 times out of 100 simulations that the  $H_0$  was rejected but there was a 0.26  $R^2$ . The  $H_0$  shows that there is a relationship 76 out of the 100 times but our  $R^2$  tells us that we have no very weak relationship. (If  $R^2$  is higher than 0.7 then it is considered a strong relationship).

## 2 Replication and Results

After doing a single sample regression analysis of independent random walks our  $R^2$  shows there is a low value of 0.18, which means there is a low correlation between the two independent random walks. I then did same exact regression, trying to replicate the Granger and Newbold analysis. I set my seed (beginning point) as 2000, I will have  $n=100$  as the sample size and we are going to repeat the experiment  $r=100$  times. Then I compare with the critical value at 5%, how much of those experiment times is higher than the critical value. This will tell us how many times  $H_0$  will be rejected. The results is that we have a  $R^2$  of 0.58 which tell us that we have a weak value and the data is not at all close to the fitted line. Also though code it shows 0.001 mean with a max of 1.000 telling me that majority or the  $R^2$  is not greater than 0.05, which tells me there is not a relationship. But it also shows that we rejected the  $H_0$  777 times out of the 1000 times of the repeated

experiment showing that there is a relationship between the two independent walks. From doing this I have similar results as Granger and Newbold as they also had a low  $R^2$  but had a high percentage of their  $H_0$  being rejected.

Table 1: My Results vs Granger and Newbold's Results

Results	My Results	Granger and Newbold Levels (M=1)
Average $R^2$	0.58	0.26
Percent of time $H_0$ is rejected	77.7	76

### 3 Discussion and Conclusion

The results of my replication shows very similar results to the Granger and Newbold analysis where we both get very high percentages of rejecting the null hypothesis ( $H_0$ ) which proves that there is a relationship but we also get a very low valued  $R^2$  which proves there to be very little linear relationship between the two variables. This is does not make sense to me seeing as one thing shows that there is a relationship but another saying that there is not a relationship between the two random walks. This tells me that this series in this experiment is strongly auto-correlated, even though there should not be a relationship there is some how a relationship after repeating the experiment several times.

# Monte Carlo Progam

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#Monte Carlo Simulation

library(tidyverse)

## — Attaching packages — tidyverse 1.3.0 —

## ✓ ggplot2 3.3.2 ✓ purrr 0.3.4  
## ✓ tibble 3.0.6 ✓ dplyr 1.0.3  
## ✓ tidyr 1.1.2 ✓ stringr 1.4.0  
## ✓ readr 1.3.1 ✓ forcats 0.5.0

## — Conflicts — tidyverse\_conflicts() —  
## x dplyr::filter() masks stats::filter()  
## x dplyr::lag() masks stats::lag()

library(stargazer)

##  
## Please cite as:

## Hlavac, Marek (2018). stargazer: Well-Formatted Regression and Summary Statistics Tables.

## R package version 5.2.2. <https://CRAN.R-project.org/package=stargazer>

library(urca)

u1 <- rnorm(5000,0,1)  
u2 <- rnorm(5000,0,2)  
v1 <- u1  
v2 <- u2

t<-(1:5000)

#Random Walk 1  
for (i in 2:5000) v1[i]<-v1[i-1]+u1[i]

#Random Walk 2

for (i in 2:5000) v2[i]<-v2[i-1]+u2[i]

ggplot()+  
geom\_line(aes(x=t,y=v1,col="white"))+  
geom\_line(aes(x=t,y=v2,col="pink"))+  
theme\_dark()+  
geom\_vline(xintercept = 500,color="yellow")



# Random Walk 1 and Random Walk 2 Regression (w1~w2)  
reg1<-lm(v1~v2)

# Stargazer Regression Result  
stargazer(reg1, report="vcs", type="text",  
omit.stat = c("ser", "f"),  
ci=TRUE, omit.table.layout = "n")

##  
## =====  
## Dependent variable:  
## -----  
## v1  
## -----  
## v2 0.378  
## (0.360, 0.397)  
##  
## Constant -50.446  
## (-51.499, -49.393)  
##  
## -----  
## Observations 5,000  
## R2 0.246  
## Adjusted R2 0.246  
## =====

summary(reg1)

##  
## Call:  
## lm(formula = v1 ~ v2)  
##  
## Residuals:  
## Min 1Q Median 3Q Max  
## -123.318 -17.888 -4.814 30.353 70.851  
##  
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)  
## (Intercept) -50.446087 0.537132 -93.92 <2e-16 \*\*\*  
## v2 0.378368 0.009364 40.41 <2e-16 \*\*\*  
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 37.71 on 4998 degrees of freedom  
## Multiple R-squared: 0.2462, Adjusted R-squared: 0.2461  
## F-statistic: 1633 on 1 and 4998 DF, p-value: < 2.2e-16

sum= summary(reg1)  
#Generating f-stats  
fstat<-sum\$fstatistic  
fstat # value, numf, dendf find from fstats

## value numdf dendf  
## 1632.79 1.00 4998.00

# f-stats only for value  
fstat<-sum\$fstatistic["value"]  
fstat

## value  
## 1632.79

fstat<-sum\$r.squared  
fstat # R^2

## [1] 0.2462437

fstat<-sum\$adj.r.squared  
fstat # adjusted R^2

## [1] 0.2460929

#Clears environment so that previous code does not conflict with new code  
rm(list=ls())

# Taken From Applied Econometrics  
#Econ 508 - Fall 2014  
#from UIUC  
#Monte Carlo  
set.seed(2000)  
r <- 1000  
n <- 100  
A <- array(0,c(1,1000))  
rsq<-numeric(r) # a spot to save R-squared

#The Loop  
for(i in 1:r){  
u<-rnorm(n)  
v<-rnorm(n)  
y<-rep(0,n)  
x<-rep(0,n)  
for(j in 2:n){  
x[j] <- x[j-1] + u[j]  
y[j] <- y[j-1] + v[j]  
}  
A[1,i] <- round(summary(lm(y~x))\$coef["x","t value"],2)  
}  
  
#Generate the number of rejections out of 100 simulations  
B<-as.matrix(abs(A)>abs(qt(0.05,n-1)))  
apply(B,1,sum)

## [1] 777

reg2<-lm(y~x)  
rsq[j]<-summary(reg2)\$r.squared

# The result  
reg2<-lm(y~x)  
stargazer(reg2, report="vcs", type="text",  
omit.stat = c("ser", "f"),  
ci=TRUE, omit.table.layout = "n")

##  
## =====  
## Dependent variable:  
## -----  
## y  
## -----  
## x 1.393  
## (1.159, 1.628)  
##  
## Constant 0.638  
## (-0.395, 1.671)  
##  
## -----  
## Observations 100  
## R2 0.580  
## Adjusted R2 0.576  
## =====

#Summary of the regression and fstats  
sum=summary(reg2)

#Generate Fstats  
fstat<-sum\$fstatistic  
fstat # value, numf, dendf find from fstats

## value numdf dendf  
## 135.6108 1.0000 98.0000

rej<-ifelse(rsq >= 0.05,1,0)# If R^2 is greater or = 0.05 (True of False)  
summary(rej)

## Min. 1st Qu. Median Mean 3rd Qu. Max.  
## 0.000 0.000 0.000 0.001 0.000 1.000