# MPCS 51040 – C Programming Lecture 9 – Sorting & Searching, Parallel Programming

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# Searching Definitions

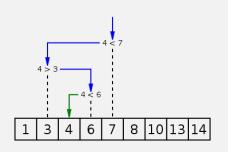


#### Definition

searching Locating an element in a data set linear search Search all elements of the set until found;  $\mathcal{O}(n)$  binary search (on sorted sets) use the fact that the data is sorted to search in  $\mathcal{O}(\log n)$ .



## Searching Binary Search



- Same principle as search in BST
- ▶ However, in this case, worst case  $\mathcal{O}(\log n)$
- Repeatedly compare the middle element against the element being searched for.
  - ▶ If smaller: repeat for the left half of the data
  - ► If larger: repeat for the right half.
  - ▶ If empty set: not found
  - ► if equal: element found
- Requires already sorted random-accessible collection (such as sorted array)



Write a recursive function implementing binary search in a given array



# Sorting Definitions

#### Definition

Sorting arranging a set of elements in prescribed order.

Comparison-sort Compares elements against each other. Fastest possible is  $O(n \log n)$ 

Linear-time sort Does not compare elements but instead relies on assuming certain properties of the data:  $\mathcal{O}(n)$ ; Example:

▶ Sort elements of set 0,4,2,1,3 when it can be assumed that all elements are present and there are no duplicates

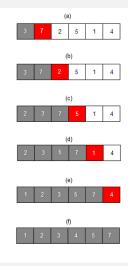
in-place sort The input data to the sort function is modified and no extra (other than  $\mathcal{O}(1)$ ) space is required.

stable sort Maintains the ordering of elements that are already sorted.



#### Insertion Sort

Insertion Sort is an *in-place*, *stable* sorting algorithm which has  $\mathcal{O}(n^2)$  time complexity. When doing incremental inserting in an already sorted set, the time complexity is  $\mathcal{O}(n)$ .



- ▶ In place sort
- ► Complexity:  $\mathcal{O}(n^2)$
- ▶ Very useful when inserting in an already sorted list:  $\mathcal{O}(n)$

#### Algorithm:

- ▶ Start on the left of the array (current position = 0)
- Consider the element at the current position.
- Starting from the beginning of the array, move to the right up to the current position inserting the element as soon as it is smaller than the element at that position.
  - ▶ Copy elements to the right to make space for at that position.
- Increment current position and repeat.



## QuickSort Overview

QuickSort is an *in place*, recursive, (non-stable in default implementation) general sorting algorithm. Given a set of elements (in array or other random access method):

Worst case performance:  $\mathcal{O}(n^2)$ .

Average case performance:  $O(n \log n)$ 

### Steps

To sort an array from index  $i \cdots j$ :

- 1. Pick pivot element at index k,  $i \le k \le j$  (i.e. the pivot is an element of the array)
- Partition; Move all elements smaller or equal to the pivot element to the left of the pivot element. Move all elements larger than the pivot element to the right of the pivot element.
- 3. Recursively apply procedure to the partitions  $i\cdots p-1$  and  $p+1\cdots j$ , where p is the new index of the pivot element. (Note that p is the correct position in of the pivot element in the final sorted array!)



# Quicksort How to partition?

- Pick a pivot element (has to be part of the data)
- Move from the right end of the array towards the left end until an element if found which is less than or equal to the pivot element.
- Move from the left end of the array to the right end until an element is found which is larger than or equal to the pivot element.
- Swap them.
- Continue until both fronts meet.

Note that the pivot element is now in the correct sorted position in the array...



# Sorting QuickSort

The performance of quicksort depends on picking a good pivot value;

- ▶ The log n in  $O(n \log n)$  originates in finding a pivot which results in balanced partitions
- $\triangleright$  Consider what happens if we always pick the smallest or largest element as pivot...(hint:  $\mathcal{O}(n^2)$ )

But how to pick a good pivot without looking at all elements?

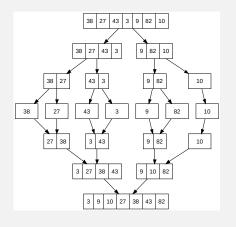
(Would als result in  $\mathcal{O}(n^2)$ )

- ▶ Option: pick a random element from the set.
- ▶ Option: better: pick the middle of element of a selection of 3 randomly chosen elements. (this strongly decreases the changes of picking a 'bad' element)

Quicksort is a popular sorting algorithm because it is very unlikely to show worst case performance.



# MergeSort



MergeSort is an 'out of place', usually stable (depends on implementation), recursive sort algorithm with average case  $\mathcal{O}(n \log n)$  complexity.

- Split the data in two equal sized portions.
- Recursively sort them using merge sort.
- Merge them (in  $\mathcal{O}(n)$ ) time.

Drawback: Merge sort requires O(n) extra space.



# Sorting Counting Sort

Counting sort is a linear sort method and assumes a set of n integers. The largest integer in the set is assumed to be k-1. The complexity of counting sort is  $\mathcal{O}(k+n)$ . Counting sort is *stable*.

- ▶ Allocate an extra array (counts) of size *k* holding integers indicating how many times each element occurs.
- ▶ Go over the set once, using each integer as an index into the count array. For every set element, increment the corresponding count array element.
- ▶ Now for counts, add each element to the next element.
- Scan the input set backwards and for each element, look up the corresponding count in the count array and copy the element to that position in a temporary array. (why scan backwards?)



- ► Sorts data in pieces (digits) one piece at a time (least significant to most significant)
- ▶ Any datatype that can be broken up into 'integer pieces' can be sorted
- Need a stable sort for sorting the digits. Why?

Note: not limited to sorting numbers; As long as we can break up the sort key into similar sized items which have numerical represention, we can use radix sort.

Complexity:  $\mathcal{O}(pn+pk)$ , with p the number of positions (digits) in the input data, n the number of input items, k the radix.



## Parallel Programming?

C is an imperative programming language: we provide the compiler with *statements* to tell it what to do. Statements are executed in a well-defined order (compiler can optimize but needs to preserve the illusion of that sequential ordering).

### Sequential

Within a single scope (function), statements are executed sequentially.

Parallel Computing Many calculations (operations) are performed *simultaneously*.

Parallel Programming Programming a parallel computer.

Almost all current systems are parallel computing systems: most processors are parallel, at various levels (explicitly: multiple hardware threads(cores) or implicitly (superscalar processor, i.e. multiple instructions concurrently).



## Parallel Computing

#### Definition

Parallel computing: performing many calculations (instructions) simultaneously.

#### Parallelism?

Many forms exist:

- bit-level parallelism
- instruction-level parallelism
- data parallelism
- task parallelism

Most forms require explicit programmer effort (except for maybe bit-level and instruction-level parallelism).

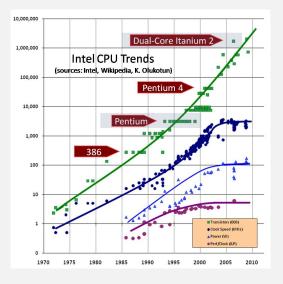
Programming for parallel systems requires additional consideration and skills:

- finding and exploiting parallelism
- synchronizing where needed (but not more)



## Parallel Programming

If it's harder, why bother?



Why bother with parallel computing?

- Achieving single-threaded gains is more and more difficult
  - Clock frequency difficult to increase (without significant overhead/tradeoff)
  - Complexity already high: branch prediction, out-of-order execution, speculative execution, . . .
- Power usage/efficiency is becoming more important (e.g. intel turboboost)

Easier and more efficient to increase parallelism (multiple cores)



Usually requires software changes!



## Parallel Programming

Some definitions

#### Definition

Analyizing execution efficiency:

serial No parallelism (one after another)

speedup  $S(p) = \frac{T_1}{T_p}$ , where  $T_1$  is the time for the *serial* program, and  $T_p$  is the time needed to execute the parallel program using p cores.

linear speedup  $S(x) \approx x$ 

superlinear speedup If S(x) > x

Processes and Threads

process A program being executed. The process owns the address space (memory), resources (open files etc.), . . .

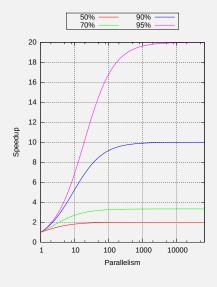
thread A single execution context executing program code. A process has at least one thread.

thread-safe A thread-safe function can be called concurrently from multiple threads and continue to function correctly.



#### Amdahl's Law

#### **Analyzing Performance Potential**



Amdahl's law describes, for a fixed size problem, the maximal potential speedup that can be expected:

 $S(x) = \frac{1}{1-p+\frac{p}{x}}$ , with p the percentage of the task that benefits from parallelization and x the number of cores used to solve the problem.

In other words, given unlimited parallel processing power, the part which can be parallelized completes in near-zero time, meaning the *serial* time will dominate the overall time.

#### Notes:

- ightharpoonup Assumes serial part remains the same with changing x
- ► Note logscale (and diminishing returns!)
- Gustafson's law: similar but for increasing problem sizes

$$S(x) = 1 - p + sp$$



# Flynn's Taxonomy

SIMD Single Instruction Multiple Data (stream)

MIMD Multiple Instruction Multiple Data

SISD Single Instruction Single Data

MISD Multiple Instruction Single Data

These are on the *CPU instruction level*. A similar classification can be made at the program (language) level.

SPMD Single Program Multiple Data

MPMD Multiple Program Multiple Data



## Parallel Programming

Many ways of classifying parallel programming models:

#### Based on execution model:

SPMD Single Program Multiple Data

SPSD Single Program Single Data

MPSD Multiple Program Single Data

MPMD Multiple Program Multiple Data

(you might also see 'Instruction' instead of 'Program')

#### Based on communication model:

- Shared memory example: OpenMP
- Distributed memory (message passing)
   example: MPI, go



## Parallel Programming & The C language

### Support for concurrency in C11:

- ▶ C11 adds *optional* support for multi-threaded parallel programming.
- Very few compilers support it.
- ▶ Includes defining the **memory model** in the presence of threads.

However, C was used for multi-threaded programming long before C11. For example, POSIX Threads (see pthread.h). The required memory model was assumed.

The C11 thread support functions are heavily modeled on posix threads. For now, recommended to use the posix threads functions due to more widespread availability and due to the optional nature of the C11 standard functions.



## C11 and Parallel Programming

C11 describes a header (threads.h) which provides functions for creating, destroying and synchronizing threads.

Thread support is *optional* in C11, and most compilers do not currently provide C11 thread functionality.

▶ This is mostly since there have been non-C11 standard specified methods of using threads. For example: POSIX threads (pthreads) described by POSIX.1c standard are available on most common platforms (including Windows, Linux, OS X, Solaris, OpenBSD)

We will be using pthreads (pthreads.h)



Review 'man pthreads', in particular the section 'Thread-safe functions'.



### POSIX Threads

```
void * PrintHello(void *threadid)
2
3
       long tid;
       tid = (long)threadid;
        printf("Hello World! It's me,"
               "thread #%ld!\n", tid);
       pthread exit(NULL);
9
    int main(int argc, char *argv[])
10
11
       pthread t threads [NUM THREADS];
12
       int rc;
13
       long t;
14
       for (t=0;t<NUM THREADS;t++)
15
16
         rc = pthread create(&threads[t],
17
         NULL, PrintHello, (void *)t);
18
19
       // need to join before exiting ...
20
```

- Explicitly create and destroy threads.
- Synchronization through mutex, barrier, condition variables.
- Communication via Shared memory threads can access each others variables.
- Low level interface.
- Supports both MPMD and SPMD.



See pthread.c example program



## OpenMP

```
int i, chunk;
    float a[N], b[N], c[N];
    /* Some initializations */
    for (i=0; i < N; i++)
       a[i] = b[i] = i * 1.0;
    chunk = CHUNKSIZE;
    #pragma omp parallel shared(a,b,c,chunk) private(i)
10
11
       #pragma omp for schedule(dynamic, chunk) nowait
12
       for (i=0; i < N; i++)
13
         c[i] = a[i] + b[i];
14
       /* end of parallel region */
```

- ► Higher level interface
- Maps best to shared memory architectures
- Implicit synchronization
- Designed for data parallel processing (SPMD).
- Implemented by compiler, designed to be ignored by compilers that don't support it.



See openmp.c example program.



### **MPI**

```
// Get the number of processes
   int world size;
    MPI Comm size (MPI COMM WORLD, &world size);
    // Get the rank of the process
   int world rank;
    MPI Comm rank (MPI COMM WORLD, &world rank);
    // Print off a hello world message
    printf("Hello world from processor %s, rank %d"
9
               " out of %d processors\n",
               processor name, world rank, world size);
10
11
    // Finalize the MPI environment.
12
    MPI Finalize();
```

- Commonly used for large supercomputers (distributed memory hw is easier to scale)
- Communication through explicit messages (send/recv) or explicit operations (RMA)
   Distributed memory programming – you can only directly access your own memory
- Usually SPMD.



See mpi.c example program.



## OpenCL/CUDA

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```
void saxpy(int n, float a, float *x, float *y)
    { int i = blockIdx.x*blockDim.x + threadIdx.x;
      if (i < n) y[i] = a*x[i] + y[i];
    int main (void)
8
      int N = 1 < < 20:
10
      float *x, *y, *d x, *d y;
11
      x = (float*)malloc(N*sizeof(float));
12
      y = (float *) malloc(N* size of (float));
13
14
      cudaMalloc(&d x, N*sizeof(float));
      cudaMalloc(&d y, N*sizeof(float));
15
16
17
      cudaMemcpy(d x, x, N*sizeof(float), cudaMemcpyHostToDevice);
18
      cudaMemcpy(dy, y, N*sizeof(float), cudaMemcpyHostToDevice);
19
20
      // Perform SAXPY on 1M elements
      saxpy <<<(N+255)/256, 256>>>(N, 2.0f, d x, d y);
21
```

- ► Similar to OpenMP compiler assisted.
- Explicit management of accelerator(GPU) and host memory (slowly disappearing).
- Designed for SPMD (data parallel).



cudaMemcpy(y, d y, N\*sizeof(float), cudaMemcpyDeviceToHost);

See cuda.c example program.



# Thread Creation/Destruction



Linking with pthreads, creating a thread (pt1.c)



## Threads

#### Thread-safe functions (2)

```
void * found:
   bool find node(node t * node, void * d)
3
      if (!node)
          return false:
      if (node->data==d)
7
          found=node:
          return true;
10
      else if (find node(node->left, d))
11
12
          return true;
13
14
      else
15
         return find node(node->right, d));
16
17
   int pseudorandom()
2
       static _assert (sizeof(int)>=4,
3
         "proper size int");
   //-I-C:-- NA 0147400647
```

For a function to be thread-safe, at the very least, any access to a *shared* resource (memory or other) should be properly synchronized/protected.

Are these examples thread-safe?

Why/Why not?



## Homework 6



HW6 review



# Final Project



 ${\sf Review\ assignment}$ 

