

1. 1E-1

(a)

$$f'(x) = 10x^9 + 15x^2 + 6x^2$$

(b)

$$f'(x) = 0$$

(c)

$$f'(x) = \frac{1}{2}$$

(d)

$$\begin{aligned} f(x) &= x^8 + x^6 + x^5 + x^3 \\ f'(x) &= 8x^7 + 6x^4 + 5x^4 + 3x^2 \end{aligned}$$

2. 1E-2

(a)

$$f(x) = \frac{a}{2}x^2 + bx$$

(b)

$$f(x) = \frac{1}{7}x^7 + \frac{5}{6}x^6 + x^4$$

(c)

$$\begin{aligned} f'(x) &= x^6 + 2x^3 + 1 \\ f(x) &= \frac{1}{7}x^7 + \frac{1}{2}x^4 + x \end{aligned}$$

3. 1E-3

$$y' = 3x^2 + 2x - 1$$

$3x^2 + 2x - 1 = 0$  at  $x = \frac{1}{3}$  or  $x = -1$ , so the point is  $(\frac{1}{3}, \frac{49}{27})$  or  $(-1, 3)$

4. 1E-4

(a)  $f(x)$  continuous at  $x = 0$ ,

$$f'(x) = \begin{cases} 2ax + b & \leq 0 \\ 25x^4 + 12x^3 + 14x + 8 & > 0 \end{cases}$$

left limit = right limit at  $x = 0$  so that  $b = 8$ .  $a$  can be any value.

(b)

$$f'(a) = 4a + 5$$

5. 1E-5

(a)

$$f'(x) = \frac{1}{(1+x)^2}$$

(b)

$$f'(x) = \frac{-x^2 - 2ax + 1}{(x^2 + 1)^2}$$

(c)

$$f'(x) = \frac{-x^2 - 4x - 1}{(x^2 - 1)^2}$$

(d)

$$f'(x) = \frac{3x^5 - x^4}{x^2}$$