

EJERCICIOS LIMITES

1. En los ejercicios de a. a d. demostrar que: $\lim_{x \rightarrow a} f(x) = L$

(a) $f(x) = \frac{x^2-4}{x-2}, a = 2, L = 4$

(b) $f(x) = \sqrt{x}, a = 2, L = \sqrt{2}$

(c) $f(x) = \sqrt[3]{x}, a = 3, L = \sqrt[3]{3}$

(d) $f(x) = \frac{1}{x+1}, a = 2, L = \frac{1}{3}$

2. Calcule los siguientes límites, usando teoremas:

(a) $\lim_{h \rightarrow 0} \frac{\sqrt{x+h} - \sqrt{x}}{h}, x > 0$

(b) $\lim_{h \rightarrow 0} \frac{1}{h} \left(\frac{1}{\sqrt{1+h}} - 1 \right)$

(c) $\lim_{h \rightarrow 0} \frac{1}{h} \left(\frac{1}{\sqrt{1+h}} - 1 \right)$

(d) $\lim_{x \rightarrow 2} \frac{x^5-32}{x-2}$

(e) $\lim_{h \rightarrow 0} \frac{(1+h)^{\frac{3}{2}} - 1}{h}$

(f) $\lim_{r \rightarrow 1} \sqrt{\frac{2r^2+3r-1}{r^2+1}}$

(g) $\lim_{x \rightarrow 3} \frac{x^6-729}{x+3}$

(h) $\lim_{x \rightarrow 2^-} \frac{4-x^2}{\sqrt{2+x-x^2}}$

(i) $\lim_{x \rightarrow 0^+} x \sqrt{1 + \frac{1}{x^2}}$

(j) $\lim_{x \rightarrow 0} x \operatorname{sen}\left(\frac{1}{x}\right)$

3. Analizar la continuidad de las siguientes funciones:

(a) $f(x) = \frac{x^2-4}{x^2-8x+12}, \quad 0 < x < 5, x \neq 2, f(2) = 1.$

(b) $f(x) = \frac{x^3-1}{x^2+x-2}, \quad 0 < x < 2, x \neq 1, f(1) = 1$

(c) $f(x) = \begin{cases} x-4, & -1 < x \leq 2 \\ x^2-6, & 2 < x < 5 \end{cases}$

$$(d) \ f(x) = \begin{cases} \frac{x^2-1}{x^4-1}, & -1 < x < 2, x \neq 1 \\ x^2 + 3x - 2, & 2 \leq x < 5 \end{cases}$$

$$(e) \ f(x) = \begin{cases} \frac{x-2}{|x-2|}, & x \neq 2 \\ 0, & x = 2 \end{cases}$$

$$(f) \ f(x) = \begin{cases} \frac{x^2-x-6}{x-3}, & x \neq 3 \\ 5, & x = 3 \end{cases}$$

$$(g) \ f(x) = \begin{cases} \operatorname{sen}\left(\frac{\pi}{x}\right), & -1 < x < 1, x \neq 0 \\ 0, & x = 0 \end{cases}$$