COMP9334 Capacity Planning for Computer Systems and Networks

Week 1: Revision problem set

COMP9334

Question 1

- An important part of performance analysis is to model the workload. In this question, you will look at a very simple model and we will generalise it to a very well known model in performance analysis in the lecture in Week 2.
- Consider a user who may send HTTP requests to a web server. In the time interval $[k \ \delta, \ (k+1) \ \delta)$ where k is a nonnegative integer, there is a probability of p that this user will send an HTTP request to a web server and there is a probability of (1-p) that this user will not send. Assuming that the probability the user sends (or not send) in each time interval is independent. Assuming that the current time is $10 \ \delta$, what is the probability that this user will not send an HTTP request to the web server before $30 \ \delta$?

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Question 2

- This is a revision question on probability distribution which you should be able to solve if you have the pre-requisites.
- Consider a continuous probability distribution with sample space is [1,∞) and probability density function
 - $f(x) = a / x^3 \text{ for } x \ge 1$
- What is the value of a in order that f(x) be a valid probability density function?
- What is the probability the probability that a number drawn from this distribution is exactly 10?
- Given this probability density function, what is the probability that a number drawn from this distribution has a value greater than 10?

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Question 1 - Answers

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Prob (the user will not send before 30\delta) = Prob (the user will not send in [10\delta,11\delta)) x Prob (the user will not send in [11\delta,12\delta)) x .... Prob (the user will not send in [29\delta,30\delta)) (note: the probability to send is independent for each time) = (1-p)^20
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Question 2 – Answers (Page 1)

 In order that the probability density function be valid, the probability that the number is drawn between [1,∞) is 1.

$$\int_{1}^{\infty} \frac{a}{x^3} = 1 \Rightarrow \left[\frac{ax^{-2}}{-2} \right]_{1}^{\infty} = 1 \Rightarrow \frac{a}{2} = 1 \Rightarrow a = 2$$

- Probability that a number drawn is exactly 10 is zero
 - Explanation: The numbers that can come from this distribution is in the range [1,∞) and there are infinite numbers, hence the probability of getting just one number (in this case 10), is zero.

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Question 2 – Answers (Page 2)

Probability that a number drawn is greater than 10 =

$$\int_{10}^{\infty} \frac{2}{x^3} = \left[\frac{2x^{-2}}{-2} \right]_{10}^{\infty} = 0.01$$

 Note: The probability distribution that you've worked with is called a Pareto distribution. It has what is known as a heavy tail properties. This probability distribution appears very often in modern computer performance analysis.

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