${\bf Free Products Comparison Magma}$

September 15, 2018

Group: $C_2 * C_3$

Searching up to index: 2500

How many normal groups are found : 527

Total Time (in s) in GAP: 100.8 Total Time (in s) in MAGMA: 387.5

| Function | $Count_GAP$ | $Count_MAGMA$ | $Time_GAP$ | Time_MAGMA |
|-----------------------------|--------------|----------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 100.8 | 387.5 |
| FindPQuotients | 247 | 247 | 77.1 | 134.5 |
| FindTQuotients | 1 | 1 | 16.2 | 0.6 |
| FindIntersections | 246 | 246 | 7.5 | 252.4 |
| AddGroup | 724 | 604 | 14.7 | 356.1 |
| MustCheckP | 1706 | 994 | 0.0 | 0.0 |
| FindPModules | 932 | 285 | 77.0 | 134.5 |
| SMTX_BasesMaximalSubmodules | 272 | 266 | 12.9 | 0.6 |
| PullBackH | 404 | 383 | 12.7 | 3.7 |

Group: $C_2 * C_4$

Searching up to index : 500

How many normal groups are found: 688

Total Time (in s) in GAP: 44.0 Total Time (in s) in MAGMA: 129.4

| Function | $Count_GAP$ | $Count_MAGMA$ | $Time_GAP$ | Time_MAGMA |
|----------------|--------------|----------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 44.0 | 129.4 |
| FindPQuotients | 305 | 305 | 36.3 | 65.7 |
| FindTQuotients | 1 | 1 | 0.2 | 0.2 |

| FindIntersections | 304 | 304 | 7.5 | 63.5 |
|-----------------------------|------|-----|------|------|
| AddGroup | 903 | 852 | 13.6 | 97.0 |
| MustCheckP | 1182 | 955 | 0.0 | 0.1 |
| FindPModules | 596 | 381 | 36.3 | 65.6 |
| SMTX_BasesMaximalSubmodules | 331 | 331 | 6.6 | 0.4 |
| PullBackH | 599 | 474 | 4.3 | 0.9 |

Group: $C_2 * C_5$

Searching up to index : 2000

How many normal groups are found : 205

Total Time (in s) in GAP: 61.4 Total Time (in s) in MAGMA: 25.2

| Function | Count_GAP | Count_MAGMA | $Time_GAP$ | Time_MAGMA |
|-----------------------------|-----------|-------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 61.4 | 25.2 |
| FindPQuotients | 88 | 88 | 53.5 | 22.6 |
| FindTQuotients | 1 | 1 | 6.6 | 0.3 |
| FindIntersections | 87 | 87 | 1.1 | 2.3 |
| AddGroup | 344 | 225 | 5.4 | 5.9 |
| MustCheckP | 894 | 349 | 0.0 | 0.0 |
| FindPModules | 592 | 96 | 53.5 | 22.6 |
| SMTX_BasesMaximalSubmodules | 96 | 86 | 10.9 | 0.5 |
| PullBackH | 173 | 157 | 13.6 | 1.4 |

Group: $C_2 * C_6$

Searching up to index : 500

How many normal groups are found : 862

Total Time (in s) in GAP: 56.9 Total Time (in s) in MAGMA: 151.7

| Function | $Count_GAP$ | $Count_MAGMA$ | $Time_GAP$ | Time_MAGMA |
|-------------------|--------------|----------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 56.9 | 151.7 |
| FindPQuotients | 363 | 363 | 47.9 | 76.6 |
| FindTQuotients | 1 | 1 | 0.6 | 0.2 |
| FindIntersections | 362 | 362 | 8.3 | 74.9 |

| AddGroup | 1145 | 1077 | 15.3 | 109.8 |
|-----------------------------|------|------|------|-------|
| MustCheckP | 1344 | 1090 | 0.0 | 0.1 |
| FindPModules | 683 | 456 | 47.9 | 76.5 |
| SMTX_BasesMaximalSubmodules | 398 | 397 | 8.1 | 0.5 |
| PullBackH | 770 | 620 | 7.2 | 1.4 |

Group: $C_2 * C_7$

Searching up to index : 1000

How many normal groups are found : 63

Total Time (in s) in GAP: 7.7 Total Time (in s) in MAGMA: 4.1

| Function | $Count_GAP$ | Count_MAGMA | $Time_GAP$ | $Time_MAGMA$ |
|-----------------------------|--------------|-------------|-------------|---------------|
| LowIndexNormal | 1 | 1 | 7.7 | 4.1 |
| FindPQuotients | 26 | 26 | 7.1 | 3.8 |
| FindTQuotients | 1 | 1 | 0.5 | 0.2 |
| FindIntersections | 25 | 25 | 0.0 | 0.1 |
| AddGroup | 79 | 69 | 0.4 | 0.6 |
| MustCheckP | 385 | 92 | 0.0 | 0.0 |
| FindPModules | 299 | 35 | 7.1 | 3.8 |
| SMTX_BasesMaximalSubmodules | 29 | 29 | 1.1 | 0.0 |
| PullBackH | 55 | 52 | 1.7 | 0.3 |

Group: $C_2 * C_8$

Searching up to index: 500

How many normal groups are found : 1187

Total Time (in s) in GAP: 149.8 Total Time (in s) in MAGMA: 299.6

| Function | $Count_GAP$ | $Count_MAGMA$ | $Time_GAP$ | $Time_MAGMA$ |
|-------------------|--------------|----------------|-------------|---------------|
| LowIndexNormal | 1 | 1 | 149.8 | 299.6 |
| FindPQuotients | 466 | 466 | 135.2 | 177.0 |
| FindTQuotients | 1 | 1 | 0.6 | 0.2 |
| FindIntersections | 465 | 465 | 13.8 | 122.4 |
| AddGroup | 1761 | 1688 | 32.5 | 223.1 |

| MustCheckP | 1581 | 1337 | 0.0 | 0.0 |
|-----------------------------|------|------|-------|-------|
| FindPModules | 868 | 648 | 135.2 | 176.9 |
| SMTX_BasesMaximalSubmodules | 505 | 505 | 20.2 | 1.1 |
| PullBackH | 1353 | 1228 | 23.5 | 2.7 |

Group : $C_2 * C_9$

Searching up to index: 1000

How many normal groups are found : 358

Total Time (in s) in GAP: 47.1 Total Time (in s) in MAGMA: 41.1

| Function | Count_GAP | Count_MAGMA | $Time_GAP$ | Time_MAGMA |
|-----------------------------|-----------|-------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 47.1 | 41.1 |
| FindPQuotients | 184 | 184 | 39.0 | 29.0 |
| FindTQuotients | 1 | 1 | 5.2 | 0.2 |
| FindIntersections | 183 | 183 | 2.9 | 11.9 |
| AddGroup | 490 | 445 | 7.2 | 21.8 |
| MustCheckP | 916 | 563 | 0.0 | 0.0 |
| FindPModules | 485 | 186 | 38.9 | 28.9 |
| SMTX_BasesMaximalSubmodules | 168 | 167 | 5.5 | 0.3 |
| PullBackH | 339 | 328 | 8.2 | 1.3 |

Group : $C_2 * C_{10}$

Searching up to index : 500

How many normal groups are found: 469

Total Time (in s) in GAP: 30.9 Total Time (in s) in MAGMA: 68.4

| Function | $Count_GAP$ | Count_MAGMA | $Time_GAP$ | Time_MAGMA |
|-------------------|--------------|-------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 30.9 | 68.4 |
| FindPQuotients | 227 | 227 | 25.1 | 33.1 |
| FindTQuotients | 1 | 1 | 0.1 | 0.2 |
| FindIntersections | 226 | 226 | 5.6 | 35.1 |
| AddGroup | 567 | 551 | 9.8 | 48.8 |
| MustCheckP | 951 | 732 | 0.0 | 0.0 |

| FindPModules | 458 | 257 | 25.0 | 33.1 |
|-----------------------------|-----|-----|------|------|
| SMTX_BasesMaximalSubmodules | 236 | 236 | 3.6 | 0.2 |
| PullBackH | 367 | 223 | 3.8 | 0.4 |

Group : $C_2 * C_{11}$

Searching up to index : 1000

How many normal groups are found : $21\,$

Total Time (in s) in GAP: 8.8 Total Time (in s) in MAGMA: 1.0

| Function | Count_GAP | Count_MAGMA | $Time_GAP$ | Time_MAGMA |
|-----------------------------|-----------|-------------|-------------|------------|
| LowIndexNormal | 1 | 1 | 8.8 | 1.0 |
| FindPQuotients | 6 | 6 | 1.1 | 0.8 |
| FindTQuotients | 1 | 1 | 7.6 | 0.2 |
| FindIntersections | 5 | 5 | 0.0 | 0.0 |
| AddGroup | 28 | 21 | 0.1 | 0.0 |
| MustCheckP | 317 | 34 | 0.0 | 0.0 |
| FindPModules | 271 | 9 | 1.1 | 0.8 |
| SMTX_BasesMaximalSubmodules | 7 | 7 | 0.0 | 0.0 |
| PullBackH | 16 | 14 | 0.0 | 0.0 |

Group : $C_2 * C_{12}$

Searching up to index : 150

How many normal groups are found: 355

Total Time (in s) in GAP: 8.9 Total Time (in s) in MAGMA: 23.7

| Function | $Count_GAP$ | $Count_MAGMA$ | $Time_GAP$ | $Time_MAGMA$ |
|-------------------|--------------|----------------|-------------|---------------|
| LowIndexNormal | 1 | 1 | 8.9 | 23.7 |
| FindPQuotients | 152 | 152 | 8.1 | 20.4 |
| FindTQuotients | 1 | 1 | 0.0 | 0.1 |
| FindIntersections | 151 | 151 | 0.7 | 3.1 |
| AddGroup | 476 | 473 | 1.7 | 5.6 |
| MustCheckP | 494 | 423 | 0.0 | 0.0 |
| FindPModules | 308 | 237 | 8.1 | 20.4 |

| SMTX_BasesMaximalSubmodules | 181 | 181 | 1.5 | 0.2 |
|-----------------------------|-----|-----|-----|-----|
| PullBackH | 378 | 339 | 0.7 | 0.3 |