
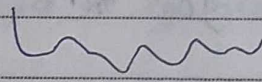


## # Gradient Descent.

  $\rightarrow$  convex

  $\rightarrow$  non-convex

Refer ML notes - repetitive.

## # Derivatives

$\rightarrow$  explained how  $y$  changes with  $x$   
and how we track the change using slope.

## # More Derivative examples.

$e^{h h h}$

weird.

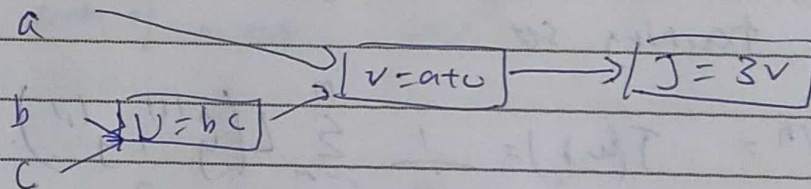
## # Computation Graph.

computing a f<sup>n</sup> consists of multiple steps  
lets say

$$J(a, b, c) = 3(a + \underbrace{bc}_v)$$

$v = bc$   
 $v = a + v$   
 $J = 3v$

Computation graph of above



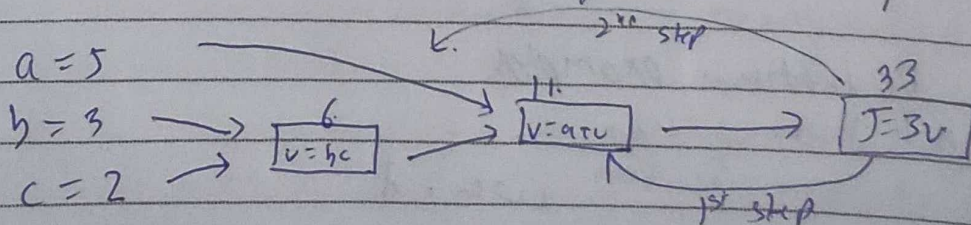
this graph is useful when you want to OPTIMIZE one of the output variable say v or J

when we go from left to right → we can calculate value of J

To compute derivatives → we go from right to left

## # Derivatives with a computation graph

\* One step of backward propagation on a computation graph yields derivative of an final output variable





1<sup>st</sup> step  $\rightarrow$  we want to know how does  $J$  behave when we tweak values of  $v$

$J = 3v$	$f(a) = 3a$
$v = 11 \rightarrow 11.001$	$\frac{df(a)}{da} = 3$
$J = 33 \rightarrow 33.003$	$\therefore \frac{dJ}{dv} = 3$

i.e. when we change values of  $v$ ,  $J$  changes itself 3 times those values.

2<sup>nd</sup> step  $\rightarrow$  now, how does  $J$  behave, when we change values of  $a$ ?

$a = 5 \rightarrow 5.001$	$\rightarrow$ we conclude $J$ changes 3 times informally: $\frac{dJ}{da} = 3$
$v = 11 \rightarrow 11.001$	
$J = 33 \rightarrow 33.003$	

gist is  $\rightarrow$  changing  $a \rightarrow$  changes  $v$  by some percent  
 $\downarrow$   
 $\frac{dv}{da} = 1$   $\downarrow$  changes  $J$  3 times

formally:

$$\frac{dJ}{da} = \frac{dJ}{dv} \cdot \frac{dv}{da}$$

$1 \times 3 = 3$   $\rightarrow$  chain rule !!

This is how we <sup>understand</sup> change how changing previous variables, ~~the~~ changes the value of final output variable

\* In NNs, final output variable is our output and we try to understand how changing ~~from~~ previous layer parameters changes our output

3<sup>rd</sup> example

how does  $J$  behave when we change  $b$ ?

changing  $b \rightarrow$  changes  $U \rightarrow$  changes  $U \rightarrow$  changes  $V$

so  $\frac{\partial J}{\partial b} = \frac{\partial J}{\partial U} \frac{\partial U}{\partial V} \frac{\partial V}{\partial b} = 3 \times 2 = 6$

changes  $J$

Similarly

$$\frac{\partial J}{\partial c} = \frac{\partial J}{\partial U} \frac{\partial U}{\partial c} = 9$$