

《编译原理与设计》

语法分析程序 的设计与实现

实验报告

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1. 实验内容

编写语法分析程序，实现对算术表达式的语法分析。要求所分析的算术表达式由如下的文法产生：

$$E \rightarrow E+T \mid E-T \mid T$$

$$T \rightarrow T * F \mid T / F \mid F$$

$$F \rightarrow (E) \mid \text{num}$$

2. 实验要求

在对输入的算术表达式进行分析的过程中，依次输出所采用的产生式。编写 LL(1)语法分析程序，要求如下：

- (1) 编程实现算法 4.2，为给定文法自动构造预测分析表；
- (2) 编程实现算法 4.1，构造 LL(1)预测分析程序。

3. 开发环境

操作系统：Microsoft Windows 10.0.14393 (x64)

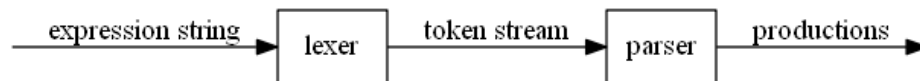
IDE：Microsoft Visual Studio Community 2015

编译器：MSVC++ 14.0

附加库：Boost 1.62.0

4. 设计思路

本语法分析程序首先利用上次实验实现的词法分析程序将输入串转化为 token 流，再在此基础上采用 LL(1)分析方法对输入算术表达式进行分析，并输出分析过程采用的产生式。流程如下：



LL(1)分析的关键在于构造预测分析表，然后使用分析表与一个分析栈进行联合控制，实现对输入符号串的自顶向上分析。构造预测分析表的前序工作依次如下（各部分算法细节详见 [5. 程序实现](#)）：

- (1) [消除文法的左递归](#)；
- (2) [提取文法的左公因子](#)；
- (3) [构造文法的 FIRST 集](#)；
- (4) [构造文法的 FOLLOW 集](#)。

此外，本程序的文法[可配置](#)，可通过修改.ini 文件来完善 C 语言语法规则。

5. 程序实现

源码:

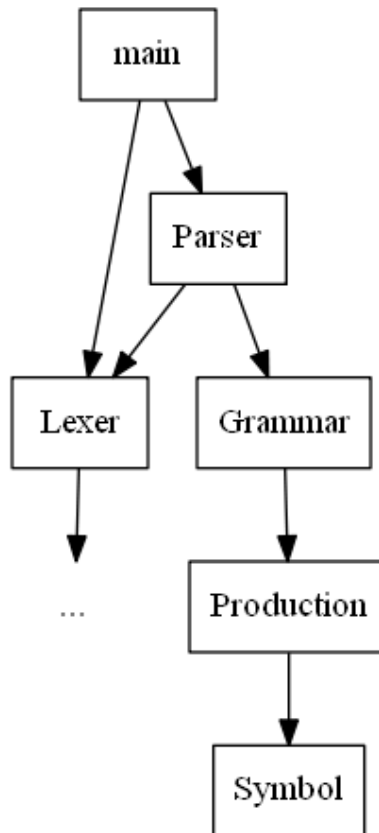
Local: [/src_code](#)

Online: <https://github.com/YangXuanyue/Compiler>

本语法分析程序采用了 C++ 来编写，程序中实现了一个 `Parser` 类作为语法分析器的对外接口，并为其重载了输入流操作符，可与上次实验实现的词法分析类 `Lexer` 连接如下：

```
Lexer lexer('\n'); //以换行符为输入串结尾
Parser parser;
cin >> lexer >> parser;
```

本程序的结构示意图如下所示：



其中 `Lexer` 分支为上次实验实现的词法分析器，其余各模块实现简述如下：

5.1. Symbol

该模块定义了文法符号的存储设计如下：

```
enum SymbolType {
    NONTERMINAL, //string
    TERMINAL //TokenType
};

typedef variant<string, TokenType> Symbol;
```

文法符号有非终结符（nonterminal）与终结符（terminal）两种，考虑到语法分析是在词法分析得到的 token 流上进行的，其文法的终结符即为各类 token，于是在本程序中采用字符串 `std::string` 来存储非终结符，采用 `TokenType` 来存储终结符。为统一，使用 Boost 库的 `boost::variant` 来存放两者，其可视为一个面向对象版本的联合类型 union，文档详见 [Boost.Variant](#)。

5.2. Production

该模块定义了产生式结构体大致如下：

```
struct Production {
    Symbol left;
    deque<Symbol> right;
};
```

其中产生式的左部为一个 `Symbol` 类型的非终结符。考虑到在文法的改造环节如消除左递归、提取左公因子中，需频繁对产生式右部文法符号串的头尾端进行插入删除等操作，为提高效率，采用了对头尾增删操作具有 $\theta(1)$ 时间复杂度的双端队列 `std::deque` 来存放产生式右部的文法符号串。

5.3. Grammar

该模块定义了文法类大致如下：

```

class Grammar {
private:
    //非终结符集与终结符集
    vector<Symbol> nonterminals, terminals;
    //起始符号
    Symbol start_symbol;
    //产生式集
    vector<Production> productions;
    //每个非终结符为左端的产生式序号集
    map<Symbol, set<int>> production_idxes;
    //每个产生式右端文法符号串的FIRST集
    vector<set<Symbol>> first_of_production;
    //FIRST集与FOLLOW集
    map<Symbol, set<Symbol>> first, follow;
    //对每个非终结符是否已构造完FIRST集与FOLLOW集的标志, 方便递归
    map<Symbol, bool> has_constructed_first, has_constructed_follow;
    //判断两个非终结符的FOLLOW集是否互相包含, 避免求FOLLOW集过程出现无限递归
    map<Symbol, map<Symbol, bool>> includes_follow_of;

public:
    Grammar();
    //从配置文件加载文法
    void load_from_ini();
    //消除左递归
    void remove_left_recursion();
    //提取左公因子
    void extract_common_left_factor();
    //对非终结符nonterminal构造FIRST集
    void construct_first(const Symbol& nonterminal);
    //对非终结符nonterminal构造FOLLOW集
    void construct_follow(const Symbol& nonterminal);
};

```

该模块实现了文法的加载、改造与 FIRST 集、FOLLOW 集的构造，此为构造 LL(1)预测分析表的前序工作。具体算法及实现简述如下：

5.3.1. 加载配置文件

本实验仅要求识别简单的算术表达式，而 C 语言的文法远不止于此，为便于后期拓展完善，本程序实现了文法的可配置化，配置文件为 `src_code/Compiler/Parser/Grammar.ini`，通过 `load_from_ini()` 函数读取该配置文件，并依据其格式完成文法的初始化。配置格式如下：

```

nonterminals = {
    E T F ...
}

terminals = {
    + / if for ...
}

start_symbol = {E}

productions = {
    {E -> E+T | E-T | ...}
    ...
}

```

要求:

- (1) 输入的终结符是合法的 C 语言关键字、运算符或诸如 num、id 之类的 token 类型;
- (2) 产生式以 {} 括起, 同一非终结的不同产生式之间以 | 隔开, 由于暂不支持转义, 产生式中不可出现 {、} 或 |, 有待进一步改进。

本实验的文法配置如下:

```

nonterminals = {
    E T F
}

terminals = {
    + - * / ( ) num
}

start_symbol = {E}

productions = {
    {E -> E+T | E-T | T}
    {T -> T*F | T/F | F}
    {F -> (E) | num}
}

```

5.3.2. 消除左递归

若一个文法中存在非终结符 A , 对某个文法符号串 α , 存在推导

$$A \xRightarrow{+} A\alpha,$$

则该文法存在左递归。

若对非终结 A ，有产生式 $A \rightarrow A\alpha \mid \beta$ ，则 A 是直接左递归的。消除直接左递归可对产生式作如下改造：

$$\begin{aligned} A &\rightarrow \beta A' \\ A' &\rightarrow \alpha A' \mid \varepsilon \end{aligned}$$

为消除文法中的所有左递归，需将所有非终结排成一定顺序，依次将 $A_i \rightarrow A_j \beta (i > j)$ 中的 A_j 分别替换为 A_j 的所有产生式，再对 A_i 消除直接左递归。

在递归下降分析方法中，要求文法不能含有左递归，否则将可能出现死循环。而 LL(1) 预测分析消除了递归下降分析的不确定性，也基于文法不能含有左递归的前提条件，否则在构造 FOLLOW 集的过程就会出现死循环。

本程序中消除左递归的算法实现如下：

```
void Grammar::remove_left_recursion() {
    set<Symbol> vis_nonterminals; //已对应产生式消除完左递归的非终结符集
    vector<Symbol> new_nonterminals; //新终结符集
    for (const auto& nonterminal : nonterminals) { //遍历非终结符集
        set<int> new_production_idxes(production_idxes[nonterminal]);
        for (int i : production_idxes[nonterminal]) { //遍历非终结符nonterminal的所有产生式
            Symbol first_symbol(productions[i].right.front()); //产生式第一个符号
            //若first_symbol是一个已消除左递归的非终结符
            if (vis_nonterminals.find(first_symbol) != vis_nonterminals.end()) {
                new_production_idxes.erase(i);
                //将该产生式的第一个符号分别替换为该符号的所有产生式
                productions[i].right.pop_front();
                for (int j : production_idxes[first_symbol]) {
                    new_production_idxes.insert(production_idxes.size());
                    Production new_production(productions[i]);
                    new_production.right.insert(
                        new_production.right.begin(),
                        productions[j].right.begin(),
                        productions[j].right.end()
                    );
                    productions.emplace_back(std::move(new_production));
                }
            }
        }
        production_idxes[nonterminal] = new_production_idxes;
        vector<int> left_recursive_production_idxes; //含左递归的产生式序号集
        for (int i : production_idxes[nonterminal]) { //遍历非终结符nonterminal的产生式
            const Symbol& first_symbol(productions[i].right.front());
            //若出现了左递归，即第一个符号是非terminal
            if (first_symbol == nonterminal) {
```

```

        if (first_symbol == nonterminal) {
            //将该产生式从nonterminal的产生式集中删除
            new_production_idxes.erase(i);
            //再加入left_recursive_production_idxes中
            left_recursive_production_idxes.push_back(i);
        }
    }
    if (left_recursive_production_idxes.size()) { //若含有左递归
        production_idxes[nonterminal] = new_production_idxes;
        Symbol new_nonterminal(boost::get<string>(nonterminal) + "'"); //新非终结符
        new_nonterminals.emplace_back(new_nonterminal);
        //消除nonterminal的直接左递归
        for (int i : production_idxes[nonterminal]) {
            productions[i].right.push_back(new_nonterminal);
        }
        production_idxes[nonterminal] = std::move(new_production_idxes);
        production_idxes[new_nonterminal].insert(productions.size());
        productions.emplace_back(new_nonterminal,
            std::move(deque<Symbol>{EPSILON}));
        for (int i : left_recursive_production_idxes) {
            productions[i].left = new_nonterminal;
            productions[i].right.pop_front();
            productions[i].right.push_back(new_nonterminal);
            production_idxes[new_nonterminal].insert(i);
        }
    }
    vis_nonterminals.insert(nonterminal);
}
for (auto& new_nonterminal : new_nonterminals) {
    nonterminals.emplace_back(std::move(new_nonterminal));
}
}

```

对本实验中文法消除左递归后的输出如下：

```

E -> T E'
T -> F T'
F -> ( E )
F -> num
E' -> + T E'
E' -> - T E'
E' -> epsilon
T' -> * F T'
T' -> / F T'
T' -> epsilon

```

5.3.3. 提取左公因子

若有产生式 $A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$ ，则可提取左公因子将其改造为：

$$\begin{aligned}
 A &\rightarrow \alpha A_1 \\
 A_1 &\rightarrow \beta_1 \mid \beta_2
 \end{aligned}$$

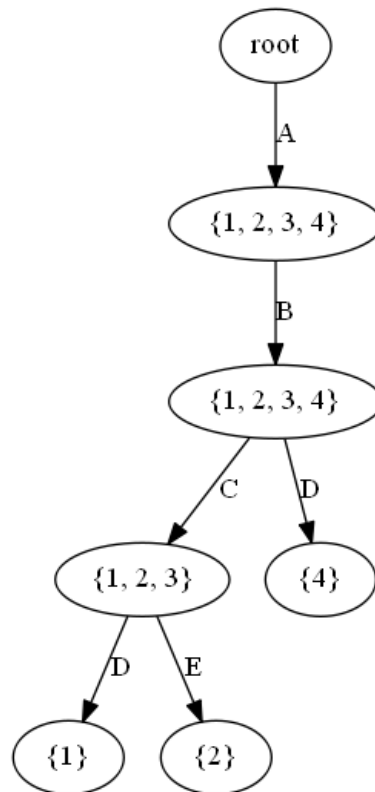
为消除预测分析时的不确定性，需对文法提取左公因子。提取左公因子是一个比较麻烦的问题，因一个非终结符的所有产生式可能含有不同的左公因子，并且对每个产生式都得提取出与其他若干个产生式最

长的左公因子。本程序使用了 [Trie 树](#) 这一数据结构高效地解决了这个问题，算法如下：

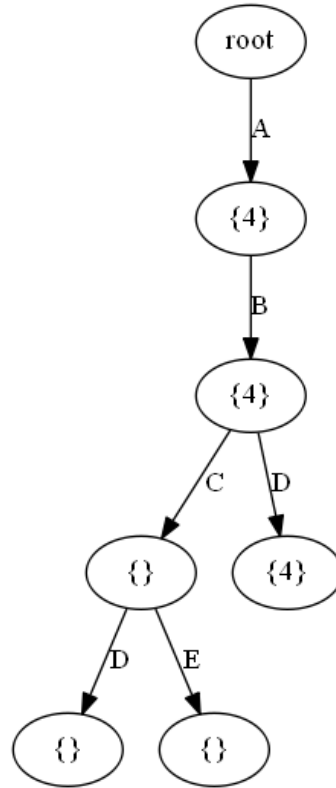
- (1) 将所有产生式的右部都插入 Trie 树中，并在 Trie 树节点中保存所有经过该结点中的产生式序号。以文法

1. $S \rightarrow ABCD$
2. $S \rightarrow ABCE$
3. $S \rightarrow ABC$
4. $S \rightarrow ABD$

为例，插入 Trie 树后如下图：



- (2) 对每一个产生式的右部，在其在 Trie 树上对应根到叶节点的路径中，找到第一个只有该产生式经过的结点，则其父节点中保存的产生式集即为与其有最长左公因子的产生式集。如对 1 号产生式，可查得与其有最长左公因子的产生式集为{1, 2, 3}。
- (3) 将该产生式集中每一个产生式从 Trie 上删除，再对该集提取左公因子。对该例子得到：



并且产生式集 $\{1, 2, 3\}$ 被改造为:

$$S \rightarrow ABCS_1$$

$$S_1 \rightarrow D \mid E \mid \varepsilon$$

(4) 对剩余的未被删除的产生式从步骤(1)开始执行。

本程序中提取左公因子的算法实现如下:

```

void Grammar::extract_common_left_factor() {
    //记录对每个非终结符的产生式已提取了多少个左公因子,
    //其个数作为对应新非终结符后缀
    map<Symbol, int> new_nonterminal_suffixes;
    //一直循环直至所有左公因子被消除
    while (true) {
        bool has_common_left_factor(false);
        //将每个符号映射到一个整数
        map<Symbol, int> symbol_to_idx;
        int cur_idx(0);
        for (const auto& nonterminal : nonterminals) {
            symbol_to_idx[nonterminal] = cur_idx++;
        }
        for (const auto& terminal : terminals) {
            symbol_to_idx[terminal] = cur_idx++;
        }
        Trie<int, -1> trie(MAX_TRIE_SIZE, cur_idx);
        vector<Symbol> new_nonterminals;
    }
}

```

```

//maps each symbol in each production to its idx
//for insertion in trie
vector<vector<int>> int_mapped_productions(productions.size());
for (const auto& nonterminal : nonterminals) {
    trie.clear();
    //对非终结符nonterminal的每个产生式，将其转化为整数映射值数组，插入到trie中
    for (int i : production_idxes[nonterminal]) {
        for (const auto& symbol : productions[i].right) {
            int_mapped_productions[i].push_back(symbol_to_idx[symbol]);
        }
        trie.insert<vector<int>, int>(int_mapped_productions[i], i);
    }
    set<int> remaining_production_idxes(production_idxes[nonterminal]);
    //clf = common left factor
    //in pair<vector<int>, int>:
    //vector<int> contains indexes of productions shared clf
    //int indicates the length of their clf
    vector<pair<set<int>, int>> clf_shared_productions_sets;
    for (int i : production_idxes[nonterminal]) {
        if (remaining_production_idxes.find(i)
            != remaining_production_idxes.end()) {
            int cur(trie.root);
            int clf_len(0);
            //在该产生式对应trie树上路径中找第一个只有其经过的结点
            for (const auto& symbol : productions[i].right) {
                int idx(symbol_to_idx[symbol]);
                int nxt(trie.nodes[cur].next[idx]);
                if (trie.nodes[nxt].vis_vals.size() == 1) {
                    if (trie.nodes[cur].vis_vals.size() > 1) {
                        //trie根节点到其父结点路径长度即为该产生式集的左公因子长度
                        clf_shared_productions_sets.emplace_back(
                            trie.nodes[cur].vis_vals, clf_len
                        );
                    }
                    //将经过其父结点的产生式从trie中删除
                    for (int i : clf_shared_productions_sets.back().first) {
                        remaining_production_idxes.erase(i);
                        trie.erase<vector<int>, int>(int_mapped_productions[i], i);
                    }
                    break;
                }
            }
            cur = nxt;
            ++clf_len;
        }
    }
    if (clf_shared_productions_sets.size()) {
        has_common_left_factor = true;
        production_idxes[nonterminal] = std::move(remaining_production_idxes);
        //int new_nonterminal_suffix(1);
        for (auto& clf_shared_productions : clf_shared_productions_sets) {
            //对每一个含左公因子的产生式集都得增加一个新非终结符
            Symbol new_nonterminal(
                boost::get<string>(nonterminal)
                + "_" + lexical_cast<string>(new_nonterminal_suffixes[nonterminal]++)
            );
            new_nonterminals.emplace_back(new_nonterminal);
            Production new_production(nonterminal);
            int clf_len(clf_shared_productions.second);
            auto clf_shared_production_idxes(
                std::move(clf_shared_productions.first)
            );
            bool has_init_new_production(false);
            //提取左公因子
            for (int i : clf_shared_production_idxes) {
                productions[i].left = new_nonterminal;
                for (int j(0); j < clf_len; ++j) {
                    if (!has_init_new_production) {
                        new_production.right.emplace_back(

```

```

        std::move(productions[i].right.front())
    );
    }
    productions[i].right.pop_front();
}
has_init_new_production = true;
if (productions[i].right.empty()) {
    productions[i].right.emplace_back(EPSILON);
}
production_idxes[new_nonterminal].insert(i);
}
production_idxes[nonterminal].insert(productions.size());
new_production.right.emplace_back(std::move(new_nonterminal));
productions.emplace_back(std::move(new_production));
}
}
//若新左公因子，即有新产生式，需继续循环
if (has_common_left_factor) {
    for (auto& new_nonterminal : new_nonterminals) {
        nonterminals.emplace_back(std::move(new_nonterminal));
    }
} else {
    break;
}
}
}

```

本实验中文法不含左公因子，以上述文法为例，程序输出为：

```

S -> A B S_1
S_0 -> D
S_0 -> E
S_0 -> epsilon
S_1 -> D
S_1 -> C S_0

```

5.3.4. 构造 FIRST 集

对任意文法符号串，其 FIRST 集为其可推导出的开头终结符号集合。

构造任意文法符号 X 的 FIRST 集 $FIRST(X)$ 可遍历 X 的产生式并利用如下规则：

- (1) 若 $X \in V_T$ ，则 $FIRST(X) = \{X\}$;
- (2) 若 $X \in V_N$ ，且有 $X \rightarrow a \dots (a \in V_T \vee a = \varepsilon)$ ，则 $FIRST(X) = FIRST(X) \cup \{a\}$;
- (3) 若有 $X \rightarrow Y_1 Y_2 \dots Y_k Y_{k+1} \dots$ ，且有 $\varepsilon \in FIRST(Y_i) (i = 1, \dots, k)$ ，则 $FIRST(X) = FIRST(X) \cup \{a \in FIRST(Y_i) \mid a \neq \varepsilon\}$;
若 $\forall Y_i, \varepsilon \in FIRST(Y_i)$ ， $FIRST(X) = FIRST(X) \cup \{\varepsilon\}$ 。

该程序中构造 FIRST 集的算法实现如下：

```

//构造非终结符nonterminal的FIRST集
void Grammar::construct_first(const Symbol& nonterminal) {
    for (int i : production_idxes[nonterminal]) { //遍历nonterminal的产生式
        const auto& production(productions[i]);
        bool all_has_epsilon(true); //标记是否产生式所有符号的FIRST集都含epsilon
        for (const auto& symbol : production.right) { //遍历产生式的符号
            //若该符号是终结符, 将其加入该产生式的FIRST集中并退出
            if (symbol.which() == TERMINAL) {
                first_of_production[i].insert(symbol);
                break;
            }
            //若还未构造该符号的FIRST集, 递归构造该符号的FIRST集
            if (!has_constructed_first[symbol]) {
                construct_first(symbol);
            }
            //将该符号的FIRST集加入到该产生式的FIRST集中
            first_of_production[i].insert(
                first[symbol].begin(),
                first[symbol].end()
            );
            //若该符号的FIRST集中含epsilon, 继续遍历, 否则退出
            if (first[symbol].find(EPSILON) == first[symbol].end()) {
                all_has_epsilon = false;
                break;
            } else {
                //去掉epsilon
                first_of_production[i].erase(EPSILON);
            }
        }
    }
    //若都含epsilon加入到, 将epsilon加入到该产生式的FIRST集中
    if (all_has_epsilon) {
        first_of_production[i].insert(EPSILON);
    }
    //将该产生式的FIRST集加入到nonterminal的FIRST集中
    first[nonterminal].insert(
        first_of_production[i].begin(),
        first_of_production[i].end()
    );
}
//标记已构造nonterminal的FIRST集
has_constructed_first[nonterminal] = true;
}

```

对该实验中文法构造 FIRST 集, 输出如下:

```

first[E] = {(, num}
first[T] = {(, num}
first[F] = {(, num}
first[E'] = {+, -, epsilon}
first[T'] = {/, *, epsilon}

```

5.3.5. 构造 FOLLOW 集

对任意非终结符，其 FOLLOW 集是该文法所有句型中紧跟在其后的终结符或结尾符号 end 的集合。

构造任意文法符号 X 的 FOLLOW 集 $FOLLOW(X)$ 可遍历文法所有产生式并利用如下规则：

- (1) 若 X 是起始符号，则 $FOLLOW(X) = FOLLOW(X) \cup \{end\}$;
- (2) 若有 $A \rightarrow \cdots X\beta$ ，则 $FOLLOW(X) = FOLLOW(X) \cup \{a \in FIRST(\beta) \mid a \neq \varepsilon\}$;
- (3) 若有 $A \rightarrow \cdots X$ ，或有 $A \rightarrow \cdots X\beta$ 且 $\varepsilon \in FIRST(\beta)$ ，则 $FOLLOW(X) = FOLLOW(X) \cup FOLLOW(A)$ 。

由于两个非终结符的 FOLLOW 集完全有可能互相包含，此时若在求其中一个的 FOLLOW 直接递归求另一个的 FOLLOW 集，则会出现无穷递归的死循环。为解决这个问题，注意到

$$\left. \begin{array}{l} FOLLOW(A) \subseteq FOLLOW(B) \\ FOLLOW(B) \subseteq FOLLOW(A) \end{array} \right\} \Rightarrow FOLLOW(A) = FOLLOW(B),$$

故本程序利用二维数组 `includes_follow_of` 记录下两个非终结符的 FOLLOW 集的包含关系。以 A, B 为例，若在构造 A 的 FOLLOW 集时需用到 B 的 FOLLOW 集，则 `includes_follow_of[A][B]` 为 true，并递归对 B 构造 FOLLOW 集，此时若又需用到 A 的 FOLLOW 集，则 `includes_follow_of[B][A]` 为 true，但由于 `includes_follow_of[A][B]` 为 true，不会再递归构造 A 的 FOLLOW 集。最后由于 `includes_follow_of[A][B]` 与 `includes_follow_of[B][A]` 都为 true，可判断 $FOLLOW(A) = FOLLOW(B)$ ，将 $FOLLOW(A)$ 与 $FOLLOW(B)$ 的并集赋给彼此即可。

该程序中构造 FOLLOW 集的算法实现如下：

```
//构造非终结符nonterminal的FOLLOW集
void Grammar::construct_follow(const Symbol& nonterminal) {
    //遍历文法所有产生式
    for (const auto& tmp_nonterminal : nonterminals) {
        for (int i : production_idxes[tmp_nonterminal]) {
            const auto& production(productions[i]);
            for (int j(0), k; j < production.right.size(); ++j) {
                if (production.right[j] == nonterminal) { //生成式中出现nonterminal
                    for (k = j + 1; k < production.right.size(); ++k) {
                        const auto& symbol(production.right[k]);
                        if (symbol.which() == TERMINAL) { //终结符直接加入并退出
                            follow[nonterminal].insert(symbol);
                        }
                    }
                }
            }
        }
    }
}
```

```

        break;
    }

    //依次加入后续符号的FIRST集除非该符号的FIRST集不含epsilon
    follow[nonterminal].insert(
        first[symbol].begin(),
        first[symbol].end()
    );
    if (first[symbol].find(EPSILON) == first[symbol].end()) {
        break;
    } else {
        follow[nonterminal].erase(EPSILON);
    }
}
//若无后续符号或后续符号串的FIRST集都含epsilon
if (k == production.right.size()
    && production.left != nonterminal) {
    const auto& another_nonterminal(production.left);
    //标记nonterminal的FOLLOW集包含another_nonterminal的FOLLOW集
    includes_follow_of[nonterminal][another_nonterminal] = true;
    //若未标记another_nonterminal的FOLLOW集包含nonterminal的FOLLOW集
    if (!includes_follow_of[another_nonterminal][nonterminal]) {
        //若还未构造another_nonterminal的FOLLOW集,
        //递归构造another_nonterminal的FOLLOW集
        if (!has_constructed_follow[another_nonterminal]) {
            construct_follow(another_nonterminal);
        }
        //将another_nonterminal的FOLLOW集加入到nonterminal的FOLLOW集
        follow[nonterminal].insert(
            follow[another_nonterminal].begin(),
            follow[another_nonterminal].end()
        );
    }
}
}
}
}
//标记已构造nonterminal的FOLLOW集
has_constructed_follow[nonterminal] = true;
}

```

最后还应处理 FOLLOW 集互相包含的情况：

```

for (const auto& nonterminal : nonterminals) {
    for (const auto& another_nonterminal : nonterminals) {
        if (includes_follow_of[nonterminal][another_nonterminal]
            && includes_follow_of[another_nonterminal][nonterminal]) {
            follow[nonterminal].insert(
                follow[another_nonterminal].begin(),
                follow[another_nonterminal].end()
            );
            follow[another_nonterminal] = follow[nonterminal];
        }
    }
}

```

对该实验中文法构造 FOLLOW 集，输出如下：

```

follow[E] = {}, end}
follow[T] = {+, -, }, end}
follow[F] = {+, -, /, *, }, end}
follow[E'] = {}, end}
follow[T'] = {+, -, }, end}

```

5.4. Parser

该模块定义了语法分析器类大致如下：

```
class Parser {
    //重载流操作符让parser在lexer词法分析的结果上进行语法分析
    friend Parser& operator >> (const Lexer& lexer, Parser& parser);

private:
    Grammar grammar; //文法
    map<Symbol, map<Symbol, int>> parsing_table; //分析表

    void construct_parsing_table(); //构造分析表

public:
    enum {
        SYNCH = -1 //错误处理标志
    };

    Parser() {
        construct_parsing_table();
    }
};
```

5.4.1. 构造预测分析表

预测分析表是预测分析程序工作的依据，其是一个二维表，表项 `parsing_table[nonterminal][terminal]` 是非终结符 `nonterminal` 遇到非终结符 `terminal`（可能为 `end`）时的分析动作指示，如采用某个产生式进行最左推导或错误提示。

构造预测分析表的算法实现如下：

```
void Parser::construct_parsing_table() {
    grammar.remove_left_recursion(); //消除左递归
    grammar.extract_common_left_factor(); //提取左公因子
    grammar.construct_first(); //构造FIRST集
    grammar.construct_follow(); //构造FOLLOW集
    for (const auto& nonterminal : grammar.nonterminals) { //遍历非终结符集
        for (int i : grammar.production_idxes[nonterminal]) { //遍历其产生式集
            bool has_epsilon = false; //标记是否为空产生式
            //对该产生式的FIRST集中的终结符，将该产生式填入对应表项中
            for (const auto& terminal : grammar.first_of_production[i]) {
                if (boost::get<TokenType>(terminal) != EPSILON) {
                    parsing_table[nonterminal][terminal] = i;
                } else {
                    has_epsilon = true;
                }
            }
        }
    }
}
```



```

        //若是空产生式
        if (has_epsilon) {
            //对该非终结符FOLLOW集中的终结符, 将该产生式填入对应表项中
            for (const auto& terminal : grammar.follow[nonterminal]) {
                parsing_table[nonterminal][terminal] = i;
            }
        }
    }
    //对于该非终结符FOLLOW集中的终结符, 若对应表项为空, 填入用于错误处理的同步信息|SYNCH
    for (const auto& terminal : grammar.follow[nonterminal]) {
        if (parsing_table[nonterminal].find(terminal)
            == parsing_table[nonterminal].end()) {
            parsing_table[nonterminal][terminal] = SYNCH;
        }
    }
}
}
}

```

5.4.2. 预测分析程序

本非递归预测分析程序使用了一个输入缓冲区（词法分析得到的 `token_stream`）、一个分析栈（`parsing_stack`）与一张分析表（`parsing_table`），输出为每次最左推导使用的产生式。其中分析栈存放了待扫描 token 流的句型，每次依据栈顶符号与带扫描 token 流的第一个 token（终结符），有分析表得到当前的分析动作（移进扫描指针、使用产生式替换栈顶或给出错误提示）。具体实现如下：

```

Parser& operator >> (const Lexer& lexer, Parser& parser) {
    //经词法分析得到的token流
    const vector<Token>& token_stream(lexer.get_token_stream());
    //分析栈
    stack<Symbol> parsing_stack;
    //左句型
    pair<deque<Symbol>, deque<Symbol>> left_sentencial_form{
        {}, {parser.grammar.get_start_symbol()}
    };
    //将结尾符号与文法起始符号压入分析栈
    parsing_stack.push(END);
    parsing_stack.push(parser.grammar.get_start_symbol());
    const vector<Production>& productions(parser.grammar.get_productions());
    //扫描token流
    for (int i(0); i < token_stream.size(); ) {
        out << "current left sentencial form:\n\t\t\t\t";
        for (const auto& symbol : left_sentencial_form.first) {
            print_symbol(out, symbol);
            out << " ";
        }
        for (const auto& symbol : left_sentencial_form.second) {
            print_symbol(out, symbol);
            out << " ";
        }
        out << endl;
        out << "current token stream:\n\t\t\t\t";
        for (int j(i); j < token_stream.size(); ++j) {
            print_symbol(out, token_stream[j].type);

```

```

        out << " ";
    }
    out << endl;
    out << "output:\n\t\t\t\t\t";
    const auto& token(token_stream[i]);
    //若当前分析栈顶为终结符
    if (parsing_stack.top().which() == TERMINAL) {
        //若该终结符与待输入token流第一个token匹配
        if (boost::get<TokenType>(parsing_stack.top()) == token.type) {
            //指针移进
            ++i;
        } else {
            //否则出现错误, 给出错误信息parsing_stack.top());oken (后续会弹栈)
            out << "error: ";
            print_symbol(out, parsing_stack.top());
            out << " expected\n";
        }
    }
    //弹栈
    parsing_stack.pop();
    //更新当前左句型
    if (left_sentencial_form.second.size()) {
        left_sentencial_form.first.push_back(
            left_sentencial_form.second.front()
        );
        left_sentencial_form.second.pop_front();
    }
} else {
    //栈顶为非终结符, 在分析表中查找对应动作
    auto res(parser.parsing_table[parsing_stack.top()].find(token.type));
    if (res != parser.parsing_table[parsing_stack.top()].end()) {
        //若表项非空白, 弹栈
        Symbol nonterminal(std::move(parsing_stack.top()));
        parsing_stack.pop();
        left_sentencial_form.second.pop_front();
        if (res->second != Parser::SYNCH) {
            //若表项不是同步信息SYNCH,
            //将使用对应产生式压栈, 并更新当前左句型
            const Production& production(productions[res->second]);
            out << production;
            if (!(production.right.front().which() == TERMINAL
                && boost::get<TokenType>(production.right.front())
                == EPSILON)) {
                for (int j(production.right.size() - 1); ~j; --j) {
                    parsing_stack.push(production.right[j]);
                }
                left_sentencial_form.second.insert(
                    left_sentencial_form.second.begin(),
                    production.right.begin(),
                    production.right.end()
                );
            }
        } else {
            //若为SYNCH给出错误提示: 此处需要一个栈顶非终结符能推导出的句子 (已弹栈)
            out << "error: " << nonterminal << " expected\n";
        }
    } else {
        //若表项为空白, 将指针移进并给出错误提示: 此处不需要该token|
        out << "error: ";
        print_symbol(out, Symbol(token_stream[i].type));
        out << " unexpected\n";
        ++i;
    }
}
    }
    out << endl;
}
out << endl;
return parser;
}

```

6. 程序测试

以下为测试样例，分为正确表达式与错误表达式两部分，样例格式如下：

(输入算术表达式)	
current left sentencial form:	(当前左句型)
current token stream:	(当前待扫描 token 流) 注：已经词法分析将符号串转为 token 流
output:	(输出产生式) 或 (错误信息)

6.1. 正确表达式

1
current left sentencial form: E
current token stream: num end
output: E -> T E'
current left sentencial form: T E'
current token stream: num end
output: T -> F T'
current left sentencial form: F T' E'
current token stream: num end
output: F -> num
current left sentencial form: num T' E'
current token stream: num end
output: num end
current left sentencial form: num T' E'
current token stream: end
output: T' -> epsilon
current left sentencial form: num E'

```
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                num
current token stream:
                                end
output:
```

```
1+1
current left sentencial form:
                                E
current token stream:
                                num + num end
output:
                                E -> T E'

current left sentencial form:
                                T E'
current token stream:
                                num + num end
output:
                                T -> F T'

current left sentencial form:
                                F T' E'
current token stream:
                                num + num end
output:
                                F -> num

current left sentencial form:
                                num T' E'
current token stream:
                                num + num end
output:

current left sentencial form:
                                num T' E'
current token stream:
                                + num end
output:
                                T' -> epsilon

current left sentencial form:
                                num E'
current token stream:
                                + num end
output:
                                E' -> + T E'

current left sentencial form:
```

```

current token stream:    num + T E'
                        + num end
output:
current left sentencial form:
                        num + T E'
current token stream:
                        num end
output:
                        T -> F T'

current left sentencial form:
                        num + F T' E'
current token stream:
                        num end
output:
                        F -> num

current left sentencial form:
                        num + num T' E'
current token stream:
                        num end
output:

current left sentencial form:
                        num + num T' E'
current token stream:
                        end
output:
                        T' -> epsilon

current left sentencial form:
                        num + num E'
current token stream:
                        end
output:
                        E' -> epsilon

current left sentencial form:
                        num + num
current token stream:
                        end
output:

```

```

2.3+4.5e6

```

```

current left sentencial form:
                        E
current token stream:
                        num + num end
output:
                        E -> T E'

current left sentencial form:

```

```

current token stream:      T E'
                           num + num end
output:
                           T -> F T'

current left sentencial form:
                           F T' E'
current token stream:
                           num + num end
output:
                           F -> num

current left sentencial form:
                           num T' E'
current token stream:
                           num + num end
output:

current left sentencial form:
                           num T' E'
current token stream:
                           + num end
output:
                           T' -> epsilon

current left sentencial form:
                           num E'
current token stream:
                           + num end
output:
                           E' -> + T E'

current left sentencial form:
                           num + T E'
current token stream:
                           + num end
output:

current left sentencial form:
                           num + T E'
current token stream:
                           num end
output:
                           T -> F T'

current left sentencial form:
                           num + F T' E'
current token stream:
                           num end
output:
                           F -> num

current left sentencial form:
                           num + num T' E'
current token stream:
                           num end

```

```

output:

current left sentencial form:
                        num + num T' E'
current token stream:
                        end
output:
                        T' -> epsilon

current left sentencial form:
                        num + num E'
current token stream:
                        end
output:
                        E' -> epsilon

current left sentencial form:
                        num + num
current token stream:
                        end
output:

```

```

(1 + 3) * (3 / 2 + 4)
current left sentencial form:
                        E
current token stream:
                        ( num + num ) * ( num / num + num ) end
output:
                        E -> T E'

current left sentencial form:
                        T E'
current token stream:
                        ( num + num ) * ( num / num + num ) end
output:
                        T -> F T'

current left sentencial form:
                        F T' E'
current token stream:
                        ( num + num ) * ( num / num + num ) end
output:
                        F -> ( E )

current left sentencial form:
                        ( E ) T' E'
current token stream:
                        ( num + num ) * ( num / num + num ) end
output:

current left sentencial form:
                        ( E ) T' E'
current token stream:
                        num + num ) * ( num / num + num ) end

```

```

output:
                                E -> T E'

current left sentencial form:
                                ( T E' ) T' E'
current token stream:
                                num + num ) * ( num / num + num ) end
output:
                                T -> F T'

current left sentencial form:
                                ( F T' E' ) T' E'
current token stream:
                                num + num ) * ( num / num + num ) end
output:
                                F -> num

current left sentencial form:
                                ( num T' E' ) T' E'
current token stream:
                                num + num ) * ( num / num + num ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( num E' ) T' E'
current token stream:
                                + num ) * ( num / num + num ) end
output:
                                E' -> + T E'

current left sentencial form:
                                ( num + T E' ) T' E'
current token stream:
                                + num ) * ( num / num + num ) end
output:
                                T -> F T'

current left sentencial form:
                                ( num + F T' E' ) T' E'
current token stream:
                                num ) * ( num / num + num ) end
output:
                                F -> num

```



```

current left sentencial form:
    ( num + num T' E' ) T' E'
current token stream:
    num ) * ( num / num + num ) end
output:

current left sentencial form:
    ( num + num T' E' ) T' E'
current token stream:
    ) * ( num / num + num ) end
output:
    T' -> epsilon

current left sentencial form:
    ( num + num E' ) T' E'
current token stream:
    ) * ( num / num + num ) end
output:
    E' -> epsilon

current left sentencial form:
    ( num + num ) T' E'
current token stream:
    ) * ( num / num + num ) end
output:

current left sentencial form:
    ( num + num ) T' E'
current token stream:
    * ( num / num + num ) end
output:
    T' -> * F T'

current left sentencial form:
    ( num + num ) * F T' E'
current token stream:
    * ( num / num + num ) end
output:

current left sentencial form:
    ( num + num ) * F T' E'
current token stream:
    ( num / num + num ) end
output:
    F -> ( E )

current left sentencial form:
    ( num + num ) * ( E ) T' E'
current token stream:
    ( num / num + num ) end
output:

current left sentencial form:
    ( num + num ) * ( E ) T' E'
current token stream:
    num / num + num ) end
output:

```

```

                                E -> T E'

current left sentencial form:
                                ( num + num ) * ( T E' ) T' E'
current token stream:
                                num / num + num ) end
output:
                                T -> F T'

current left sentencial form:
                                ( num + num ) * ( F T' E' ) T' E'
current token stream:
                                num / num + num ) end
output:
                                F -> num

current left sentencial form:
                                ( num + num ) * ( num T' E' ) T' E'
current token stream:
                                num / num + num ) end
output:

current left sentencial form:
                                ( num + num ) * ( num T' E' ) T' E'
current token stream:
                                / num + num ) end
output:
                                T' -> / F T'

current left sentencial form:
                                ( num + num ) * ( num / F T' E' ) T' E'
current token stream:
                                / num + num ) end
output:

current left sentencial form:
                                ( num + num ) * ( num / F T' E' ) T' E'
current token stream:
                                num + num ) end
output:
                                F -> num

current left sentencial form:
                                ( num + num ) * ( num / num T' E' ) T' E'
current token stream:
                                num + num ) end
output:

current left sentencial form:
                                ( num + num ) * ( num / num T' E' ) T' E'
current token stream:
                                + num ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( num + num ) * ( num / num E' ) T' E'

```

```

current token stream:
    + num ) end
output:
    E' -> + T E'

current left sentencial form:
    ( num + num ) * ( num / num + T E' ) T' E'
current token stream:
    + num ) end
output:

current left sentencial form:
    ( num + num ) * ( num / num + T E' ) T' E'
current token stream:
    num ) end
output:
    T -> F T'

current left sentencial form:
    ( num + num ) * ( num / num + F T' E' ) T' E'
current token stream:
    num ) end
output:
    F -> num

current left sentencial form:
    ( num + num ) * ( num / num + num T' E' ) T' E'
current token stream:
    num ) end
output:

current left sentencial form:
    ( num + num ) * ( num / num + num T' E' ) T' E'
current token stream:
    ) end
output:
    T' -> epsilon

current left sentencial form:
    ( num + num ) * ( num / num + num E' ) T' E'
current token stream:
    ) end
output:
    E' -> epsilon

current left sentencial form:
    ( num + num ) * ( num / num + num ) T' E'
current token stream:
    ) end
output:

current left sentencial form:
    ( num + num ) * ( num / num + num ) T' E'
current token stream:
    end
output:
    T' -> epsilon

```

```

current left sentencial form:
    ( num + num ) * ( num / num + num ) E'
current token stream:
    end
output:
    E' -> epsilon

current left sentencial form:
    ( num + num ) * ( num / num + num )
current token stream:
    end
output:

```

```

(3.2 + 6.9)
current left sentencial form:
    E
current token stream:
    ( num + num ) end
output:
    E -> T E'

current left sentencial form:
    T E'
current token stream:
    ( num + num ) end
output:
    T -> F T'

current left sentencial form:
    F T' E'
current token stream:
    ( num + num ) end
output:
    F -> ( E )

current left sentencial form:
    ( E ) T' E'
current token stream:
    ( num + num ) end
output:

current left sentencial form:
    ( E ) T' E'
current token stream:
    num + num ) end
output:
    E -> T E'

current left sentencial form:
    ( T E' ) T' E'
current token stream:
    num + num ) end
output:

```

```

                                T -> F T'

current left sentencial form:
                                ( F T' E' ) T' E'
current token stream:
                                num + num ) end
output:
                                F -> num

current left sentencial form:
                                ( num T' E' ) T' E'
current token stream:
                                num + num ) end
output:

current left sentencial form:
                                ( num T' E' ) T' E'
current token stream:
                                + num ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( num E' ) T' E'
current token stream:
                                + num ) end
output:
                                E' -> + T E'

current left sentencial form:
                                ( num + T E' ) T' E'
current token stream:
                                + num ) end
output:

current left sentencial form:
                                ( num + T E' ) T' E'
current token stream:
                                num ) end
output:
                                T -> F T'

current left sentencial form:
                                ( num + F T' E' ) T' E'
current token stream:
                                num ) end
output:
                                F -> num

current left sentencial form:
                                ( num + num T' E' ) T' E'
current token stream:
                                num ) end
output:

current left sentencial form:
                                ( num + num T' E' ) T' E'

```

```

current token stream:
                                ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( num + num E' ) T' E'
current token stream:
                                ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( num + num ) T' E'
current token stream:
                                ) end
output:

current left sentencial form:
                                ( num + num ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                ( num + num ) E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                ( num + num )
current token stream:
                                end
output:

```

```

((((((4))))))
current left sentencial form:
                                E
current token stream:
                                ( ( ( ( ( num ) ) ) ) ) ) end
output:
                                E -> T E'

current left sentencial form:
                                T E'
current token stream:
                                ( ( ( ( ( num ) ) ) ) ) ) end
output:
                                T -> F T'

current left sentencial form:

```

```

current token stream:      F T' E'
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           F -> ( E )

current left sentencial form:
                           ( E ) T' E'
current token stream:
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           ( ( ( ( ( num ) ) ) ) ) ) end

current left sentencial form:
                           ( E ) T' E'
current token stream:
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           E -> T E'

current left sentencial form:
                           ( T E' ) T' E'
current token stream:
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           T -> F T'

current left sentencial form:
                           ( F T' E' ) T' E'
current token stream:
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           F -> ( E )

current left sentencial form:
                           ( ( E ) T' E' ) T' E'
current token stream:
                           ( ( ( ( ( num ) ) ) ) ) ) end
output:
                           ( ( ( ( ( num ) ) ) ) ) ) end

current left sentencial form:
                           ( ( E ) T' E' ) T' E'
current token stream:
                           ( ( ( ( num ) ) ) ) ) ) end
output:
                           E -> T E'

current left sentencial form:
                           ( ( T E' ) T' E' ) T' E'
current token stream:
                           ( ( ( ( num ) ) ) ) ) ) end
output:
                           T -> F T'

current left sentencial form:
                           ( ( F T' E' ) T' E' ) T' E'
current token stream:
                           ( ( ( ( num ) ) ) ) ) ) end

```

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output:
                                F -> ( E )

current left sentencial form:
                                ( ( ( E ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( ( ( num ) ) ) ) ) end
output:

current left sentencial form:
                                ( ( ( E ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( ( num ) ) ) ) ) end
output:

                                E -> T E'

current left sentencial form:
                                ( ( ( T E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( ( num ) ) ) ) ) end
output:

                                T -> F T'

current left sentencial form:
                                ( ( ( F T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( ( num ) ) ) ) ) end
output:

                                F -> ( E )

current left sentencial form:
                                ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( ( num ) ) ) ) ) end
output:

current left sentencial form:
                                ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( num ) ) ) ) ) end
output:

                                E -> T E'

current left sentencial form:
                                ( ( ( ( T E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( num ) ) ) ) ) end
output:

                                T -> F T'

current left sentencial form:
                                ( ( ( ( F T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ( ( num ) ) ) ) ) end
output:

                                F -> ( E )

```



```

current left sentencial form:
                        ( ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                        ( ( num ) ) ) ) ) end
output:

current left sentencial form:
                        ( ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                        ( num ) ) ) ) ) end
output:
                        E -> T E'

current left sentencial form:
                        ( ( ( ( ( T E' ) T' E' ) T' E' ) T' E' ) T' E' )
T' E'
current token stream:
                        ( num ) ) ) ) ) end
output:
                        T -> F T'

current left sentencial form:
                        ( ( ( ( ( F T' E' ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E'
current token stream:
                        ( num ) ) ) ) ) end
output:
                        F -> ( E )

current left sentencial form:
                        ( ( ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E' )
T' E' ) T' E'
current token stream:
                        ( num ) ) ) ) ) end
output:

current left sentencial form:
                        ( ( ( ( ( ( E ) T' E' ) T' E' ) T' E' ) T' E' )
T' E' ) T' E'
current token stream:
                        num ) ) ) ) ) end
output:
                        E -> T E'

current left sentencial form:
                        ( ( ( ( ( ( T E' ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E' ) T' E'
current token stream:
                        num ) ) ) ) ) end
output:
                        T -> F T'

current left sentencial form:
                        ( ( ( ( ( ( F T' E' ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E' ) T' E'

```

```

current token stream:
    num ) ) ) ) ) end
output:
    F -> num

current left sentencial form:
    ( ( ( ( ( num T' E' ) T' E' ) T' E' ) T' E' )
T' E' ) T' E' ) T' E'
current token stream:
    num ) ) ) ) ) end
output:

current left sentencial form:
    ( ( ( ( ( num T' E' ) T' E' ) T' E' ) T' E' )
T' E' ) T' E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:
    T' -> epsilon

current left sentencial form:
    ( ( ( ( ( num E' ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:
    E' -> epsilon

current left sentencial form:
    ( ( ( ( ( num ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:

current left sentencial form:
    ( ( ( ( ( num ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:
    T' -> epsilon

current left sentencial form:
    ( ( ( ( ( num ) E' ) T' E' ) T' E' ) T' E' )
T' E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:
    E' -> epsilon

current left sentencial form:
    ( ( ( ( ( num ) ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E'
current token stream:
    ) ) ) ) ) end
output:

```

```

current left sentencial form:
                                ( ( ( ( ( num ) ) T' E' ) T' E' ) T' E' ) T'
E' ) T' E'
current token stream:
                                ) ) ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) E' ) T' E' ) T' E' ) T' E' )
T' E'
current token stream:
                                ) ) ) ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                ) ) ) ) end
output:

current left sentencial form:
                                ( ( ( ( ( num ) ) ) T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                ) ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ) ) ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) T' E' ) T' E' ) T' E'
current token stream:
                                ) ) ) end
output:

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) T' E' ) T' E' ) T' E'
current token stream:
                                ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) E' ) T' E' ) T' E'
current token stream:
                                ) ) end
output:

```

```

                                E' -> epsilon
current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) T' E' ) T' E'
current token stream:
                                ) ) end
output:

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) T' E' ) T' E'
current token stream:
                                ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) E' ) T' E'
current token stream:
                                ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) ) T' E'
current token stream:
                                ) end
output:

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) ) E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( ( ( ( num ) ) ) ) ) )
current token stream:
                                end
output:

```

```

((0.2-9) *(5*9/9+(10)))
current left sentencial form:
                                E
current token stream:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) end

```

```

output:
                                E -> T E'

current left sentencial form:
                                T E'
current token stream:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) end
output:
                                T -> F T'

current left sentencial form:
                                F T' E'
current token stream:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) end
output:
                                F -> ( E )

current left sentencial form:
                                ( E ) T' E'
current token stream:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) end
output:

current left sentencial form:
                                ( E ) T' E'
current token stream:
                                ( num - num ) * ( num * num / num + ( num ) ) )
end
output:
                                E -> T E'

current left sentencial form:
                                ( T E' ) T' E'
current token stream:
                                ( num - num ) * ( num * num / num + ( num ) ) )
end
output:
                                T -> F T'

current left sentencial form:
                                ( F T' E' ) T' E'
current token stream:
                                ( num - num ) * ( num * num / num + ( num ) ) )
end
output:
                                F -> ( E )

current left sentencial form:
                                ( ( E ) T' E' ) T' E'
current token stream:
                                ( num - num ) * ( num * num / num + ( num ) ) )
end
output:

```

```

current left sentencial form:
      ( ( E ) T' E' ) T' E'
current token stream:
      num - num ) * ( num * num / num + ( num ) ) )
end
output:
      E -> T E'

current left sentencial form:
      ( ( T E' ) T' E' ) T' E'
current token stream:
      num - num ) * ( num * num / num + ( num ) ) )
end
output:
      T -> F T'

current left sentencial form:
      ( ( F T' E' ) T' E' ) T' E'
current token stream:
      num - num ) * ( num * num / num + ( num ) ) )
end
output:
      F -> num

current left sentencial form:
      ( ( num T' E' ) T' E' ) T' E'
current token stream:
      num - num ) * ( num * num / num + ( num ) ) )
end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num E' ) T' E' ) T' E'
current token stream:
      - num ) * ( num * num / num + ( num ) ) ) end
output:
      E' -> - T E'

current left sentencial form:
      ( ( num - T E' ) T' E' ) T' E'
current token stream:
      - num ) * ( num * num / num + ( num ) ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num - T E' ) T' E' ) T' E'
current token stream:
      num ) * ( num * num / num + ( num ) ) ) end
output:
      T -> F T'

```

```

current left sentencial form:
      ( ( num - F T' E' ) T' E' ) T' E'
current token stream:
      num ) * ( num * num / num + ( num ) ) ) end
output:
      F -> num

current left sentencial form:
      ( ( num - num T' E' ) T' E' ) T' E'
current token stream:
      num ) * ( num * num / num + ( num ) ) ) end
output:

current left sentencial form:
      ( ( num - num T' E' ) T' E' ) T' E'
current token stream:
      ) * ( num * num / num + ( num ) ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num - num E' ) T' E' ) T' E'
current token stream:
      ) * ( num * num / num + ( num ) ) ) end
output:
      E' -> epsilon

current left sentencial form:
      ( ( num - num ) T' E' ) T' E'
current token stream:
      ) * ( num * num / num + ( num ) ) ) end
output:

current left sentencial form:
      ( ( num - num ) T' E' ) T' E'
current token stream:
      * ( num * num / num + ( num ) ) ) end
output:
      T' -> * F T'

current left sentencial form:
      ( ( num - num ) * F T' E' ) T' E'
current token stream:
      * ( num * num / num + ( num ) ) ) end
output:

current left sentencial form:
      ( ( num - num ) * F T' E' ) T' E'
current token stream:
      ( num * num / num + ( num ) ) ) end
output:
      F -> ( E )

current left sentencial form:
      ( ( num - num ) * ( E ) T' E' ) T' E'
current token stream:

```

```

                                ( num * num / num + ( num ) ) ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( E ) T' E' ) T' E'
current token stream:
                                num * num / num + ( num ) ) ) end
output:
                                E -> T E'

current left sentencial form:
                                ( ( num - num ) * ( T E' ) T' E' ) T' E'
current token stream:
                                num * num / num + ( num ) ) ) end
output:
                                T -> F T'

current left sentencial form:
                                ( ( num - num ) * ( F T' E' ) T' E' ) T' E'
current token stream:
                                num * num / num + ( num ) ) ) end
output:
                                F -> num

current left sentencial form:
                                ( ( num - num ) * ( num T' E' ) T' E' ) T' E'
current token stream:
                                num * num / num + ( num ) ) ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( num T' E' ) T' E' ) T' E'
current token stream:
                                * num / num + ( num ) ) ) end
output:
                                T' -> * F T'

current left sentencial form:
                                ( ( num - num ) * ( num * F T' E' ) T' E' ) T'
E'
current token stream:
                                * num / num + ( num ) ) ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( num * F T' E' ) T' E' ) T'
E'
current token stream:
                                num / num + ( num ) ) ) end
output:
                                F -> num

current left sentencial form:
                                ( ( num - num ) * ( num * num T' E' ) T' E' ) T'
E'
current token stream:
                                num / num + ( num ) ) ) end

```



```

output:

current left sentencial form:
      ( ( num - num ) * ( num * num T' E' ) T' E' ) T'
E'
current token stream:
      / num + ( num ) ) ) end
output:
      T' -> / F T'

current left sentencial form:
      ( ( num - num ) * ( num * num / F T' E' ) T'
E' ) T' E'
current token stream:
      / num + ( num ) ) ) end
output:

current left sentencial form:
      ( ( num - num ) * ( num * num / F T' E' ) T'
E' ) T' E'
current token stream:
      num + ( num ) ) ) end
output:
      F -> num

current left sentencial form:
      ( ( num - num ) * ( num * num / num T' E' ) T'
E' ) T' E'
current token stream:
      num + ( num ) ) ) end
output:

current left sentencial form:
      ( ( num - num ) * ( num * num / num T' E' ) T'
E' ) T' E'
current token stream:
      + ( num ) ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num - num ) * ( num * num / num E' ) T' E' )
T' E'
current token stream:
      + ( num ) ) ) end
output:
      E' -> + T E'

current left sentencial form:
      ( ( num - num ) * ( num * num / num + T E' ) T'
E' ) T' E'
current token stream:
      + ( num ) ) ) end
output:

current left sentencial form:

```

```

( ( num - num ) * ( num * num / num + T E' ) T'
E' ) T' E'
current token stream:
( num ) ) ) end
output:
T -> F T'

current left sentencial form:
( ( num - num ) * ( num * num / num + F T' E' )
T' E' ) T' E'
current token stream:
( num ) ) ) end
output:
F -> ( E )

current left sentencial form:
( ( num - num ) * ( num * num / num + ( E ) T'
E' ) T' E' ) T' E'
current token stream:
( num ) ) ) end
output:

current left sentencial form:
( ( num - num ) * ( num * num / num + ( E ) T'
E' ) T' E' ) T' E'
current token stream:
num ) ) ) end
output:
E -> T E'

current left sentencial form:
( ( num - num ) * ( num * num / num + ( T E' )
T' E' ) T' E' ) T' E'
current token stream:
num ) ) ) end
output:
T -> F T'

current left sentencial form:
( ( num - num ) * ( num * num / num + ( F T'
E' ) T' E' ) T' E' ) T' E'
current token stream:
num ) ) ) end
output:
F -> num

current left sentencial form:
( ( num - num ) * ( num * num / num + ( num T'
E' ) T' E' ) T' E' ) T' E'
current token stream:
num ) ) ) end
output:

current left sentencial form:
( ( num - num ) * ( num * num / num + ( num T'
E' ) T' E' ) T' E' ) T' E'
current token stream:

```

```

                                ) ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num E' )
T' E' ) T' E' ) T' E'
current token stream:
                                ) ) ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num ) T'
E' ) T' E' ) T' E'
current token stream:
                                ) ) ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num ) T'
E' ) T' E' ) T' E'
current token stream:
                                ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num )
E' ) T' E' ) T' E'
current token stream:
                                ) ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num ) )
T' E' ) T' E'
current token stream:
                                ) ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num ) )
T' E' ) T' E'
current token stream:
                                ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num + ( num ) )
E' ) T' E'
current token stream:
                                ) end
output:
                                E' -> epsilon

```

```

current left sentencial form:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) T' E'
current token stream:
                                ) end
output:

current left sentencial form:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num +
( num ) ) ) E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num - num ) * ( num * num / num +
( num ) ) )
current token stream:
                                end
output:

```

```

((2*(5 - 9)/8)*(9/(1/(9-9.36e5))))
current left sentencial form:
                                E
current token stream:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
                                E -> T E'

current left sentencial form:
                                T E'
current token stream:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
                                T -> F T'

current left sentencial form:
                                F T' E'
current token stream:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
                                F -> ( E )

```

```

current left sentencial form:
      ( E ) T' E'
current token stream:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:

current left sentencial form:
      ( E ) T' E'
current token stream:
      ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
      E -> T E'

current left sentencial form:
      ( T E' ) T' E'
current token stream:
      ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
      T -> F T'

current left sentencial form:
      ( F T' E' ) T' E'
current token stream:
      ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:
      F -> ( E )

current left sentencial form:
      ( ( E ) T' E' ) T' E'
current token stream:
      ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) end
output:

current left sentencial form:
      ( ( E ) T' E' ) T' E'
current token stream:
      num * ( num - num ) / num ) * ( num / ( num
/ ( num - num ) ) ) ) end
output:
      E -> T E'

current left sentencial form:
      ( ( T E' ) T' E' ) T' E'
current token stream:
      num * ( num - num ) / num ) * ( num / ( num
/ ( num - num ) ) ) ) end
output:
      T -> F T'

current left sentencial form:
      ( ( F T' E' ) T' E' ) T' E'

```

```

current token stream:
    num * ( num - num ) / num ) * ( num / ( num
/ ( num - num ) ) ) ) end
output:
    F -> num

current left sentencial form:
    ( ( num T' E' ) T' E' ) T' E'
current token stream:
    num * ( num - num ) / num ) * ( num / ( num
/ ( num - num ) ) ) ) end
output:

current left sentencial form:
    ( ( num T' E' ) T' E' ) T' E'
current token stream:
    * ( num - num ) / num ) * ( num / ( num /
( num - num ) ) ) ) end
output:
    T' -> * F T'

current left sentencial form:
    ( ( num * F T' E' ) T' E' ) T' E'
current token stream:
    * ( num - num ) / num ) * ( num / ( num /
( num - num ) ) ) ) end
output:

current left sentencial form:
    ( ( num * F T' E' ) T' E' ) T' E'
current token stream:
    ( num - num ) / num ) * ( num / ( num /
( num - num ) ) ) ) end
output:
    F -> ( E )

current left sentencial form:
    ( ( num * ( E ) T' E' ) T' E' ) T' E'
current token stream:
    ( num - num ) / num ) * ( num / ( num /
( num - num ) ) ) ) end
output:

current left sentencial form:
    ( ( num * ( E ) T' E' ) T' E' ) T' E'
current token stream:
    num - num ) / num ) * ( num / ( num / ( num
- num ) ) ) ) end
output:
    E -> T E'

current left sentencial form:
    ( ( num * ( T E' ) T' E' ) T' E' ) T' E'
current token stream:
    num - num ) / num ) * ( num / ( num / ( num
- num ) ) ) ) end
output:

```

```

                                T -> F T'

current left sentencial form:
                                ( ( num * ( F T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num - num ) / num ) * ( num / ( num / ( num
- num ) ) ) ) end
output:
                                F -> num

current left sentencial form:
                                ( ( num * ( num T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                num - num ) / num ) * ( num / ( num / ( num
- num ) ) ) ) end
output:

current left sentencial form:
                                ( ( num * ( num T' E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                - num ) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num * ( num E' ) T' E' ) T' E' ) T' E'
current token stream:
                                - num ) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
                                E' -> - T E'

current left sentencial form:
                                ( ( num * ( num - T E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                - num ) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:

current left sentencial form:
                                ( ( num * ( num - T E' ) T' E' ) T' E' ) T'
E'
current token stream:
                                num ) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
                                T -> F T'

current left sentencial form:
                                ( ( num * ( num - F T' E' ) T' E' ) T' E' )
T' E'
current token stream:

```

```

num ) ) ) ) end
output:
F -> num

current left sentencial form:
( ( num * ( num - num T' E' ) T' E' ) T'
E' ) T' E'
current token stream:
num ) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
current left sentencial form:
( ( num * ( num - num T' E' ) T' E' ) T'
E' ) T' E'
current token stream:
) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
T' -> epsilon

current left sentencial form:
( ( num * ( num - num E' ) T' E' ) T' E' )
T' E'
current token stream:
) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
E' -> epsilon

current left sentencial form:
( ( num * ( num - num ) T' E' ) T' E' ) T'
E'
current token stream:
) / num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
current left sentencial form:
( ( num * ( num - num ) T' E' ) T' E' ) T'
E'
current token stream:
/ num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
T' -> / F T'

current left sentencial form:
( ( num * ( num - num ) / F T' E' ) T' E' )
T' E'
current token stream:
/ num ) * ( num / ( num / ( num -
num ) ) ) ) end
output:
current left sentencial form:

```



```

( ( num * ( num - num ) / F T' E' ) T' E' )
T' E'
current token stream:
num ) * ( num / ( num / ( num - num ) ) ) )
end
output:
F -> num

current left sentencial form:
( ( num * ( num - num ) / num T' E' ) T'
E' ) T' E'
current token stream:
num ) * ( num / ( num / ( num - num ) ) ) )
end
output:

current left sentencial form:
( ( num * ( num - num ) / num T' E' ) T'
E' ) T' E'
current token stream:
) * ( num / ( num / ( num - num ) ) ) ) end
output:
T' -> epsilon

current left sentencial form:
( ( num * ( num - num ) / num E' ) T' E' )
T' E'
current token stream:
) * ( num / ( num / ( num - num ) ) ) ) end
output:
E' -> epsilon

current left sentencial form:
( ( num * ( num - num ) / num ) T' E' ) T'
E'
current token stream:
) * ( num / ( num / ( num - num ) ) ) ) end
output:

current left sentencial form:
( ( num * ( num - num ) / num ) T' E' ) T'
E'
current token stream:
* ( num / ( num / ( num - num ) ) ) ) end
output:
T' -> * F T'

current left sentencial form:
( ( num * ( num - num ) / num ) * F T' E' )
T' E'
current token stream:
* ( num / ( num / ( num - num ) ) ) ) end
output:

current left sentencial form:
( ( num * ( num - num ) / num ) * F T' E' )
T' E'

```

```

current token stream:
      ( num / ( num / ( num - num ) ) ) ) end
output:
      F -> ( E )

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( E ) T'
E' ) T' E'
current token stream:
      ( num / ( num / ( num - num ) ) ) ) end
output:
      ( num / ( num / ( num - num ) ) ) ) end

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( E ) T'
E' ) T' E'
current token stream:
      num / ( num / ( num - num ) ) ) ) end
output:
      E -> T E'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( T E' )
T' E' ) T' E'
current token stream:
      num / ( num / ( num - num ) ) ) ) end
output:
      T -> F T'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( F T'
E' ) T' E' ) T' E'
current token stream:
      num / ( num / ( num - num ) ) ) ) end
output:
      F -> num

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num T'
E' ) T' E' ) T' E'
current token stream:
      num / ( num / ( num - num ) ) ) ) end
output:
      ( num * ( num - num ) / num ) * ( num T'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num T'
E' ) T' E' ) T' E'
current token stream:
      / ( num / ( num - num ) ) ) ) end
output:
      T' -> / F T'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num / F
T' E' ) T' E' ) T' E'
current token stream:
      / ( num / ( num - num ) ) ) ) end
output:

```

```

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num / F
T' E' ) T' E' ) T' E'
current token stream:
                                ( num / ( num - num ) ) ) end
output:
                                F -> ( E )

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( E ) T' E' ) T' E' ) T' E'
current token stream:
                                ( num / ( num - num ) ) ) end
output:

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( E ) T' E' ) T' E' ) T' E'
current token stream:
                                num / ( num - num ) ) ) end
output:
                                E -> T E'

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( T E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num / ( num - num ) ) ) end
output:
                                T -> F T'

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( F T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num / ( num - num ) ) ) end
output:
                                F -> num

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num / ( num - num ) ) ) end
output:

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                / ( num - num ) ) ) end
output:
                                T' -> / F T'

current left sentencial form:

```

```

      ( ( num * ( num - num ) / num ) * ( num /
( num / F T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      / ( num - num ) ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / F T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      ( num - num ) ) ) end
output:
      F -> ( E )

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( E ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      ( num - num ) ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( E ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      num - num ) ) ) end
output:
      E -> T E'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( T E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      num - num ) ) ) end
output:
      T -> F T'

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( F T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      num - num ) ) ) end
output:
      F -> num

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      num - num ) ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      - num ) ) ) end

```

```

output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                - num ) ) ) end

output:
                                E' -> - T E'

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - T E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                - num ) ) ) end

output:

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - T E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num ) ) ) end

output:
                                T -> F T'

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - F T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num ) ) ) end

output:
                                F -> num

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                num ) ) ) end

output:

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num T' E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ) ) ) ) end

output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num E' ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
                                ) ) ) ) end

output:
                                E' -> epsilon

```

```

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      ) ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) T' E' ) T' E' ) T' E' ) T' E'
current token stream:
      ) ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) E' ) T' E' ) T' E' ) T' E'
current token stream:
      ) ) ) end
output:
      E' -> epsilon

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) T' E' ) T' E' ) T' E'
current token stream:
      ) ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) T' E' ) T' E' ) T' E'
current token stream:
      ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) E' ) T' E' ) T' E'
current token stream:
      ) ) end
output:
      E' -> epsilon

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) T' E' ) T' E'
current token stream:
      ) ) end
output:

current left sentencial form:
      ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) T' E' ) T' E'
current token stream:

```

```

                                ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) E' ) T' E'
current token stream:
                                ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) T' E'
current token stream:
                                ) end
output:

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) ) E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num * ( num - num ) / num ) * ( num /
( num / ( num - num ) ) ) )
current token stream:
                                end
output:

```

6.2. 错误表达式

```

((1)
current left sentencial form:
                                E
current token stream:
                                ( ( num ) end
output:
                                E -> T E'

current left sentencial form:

```

```

                                T E'
current token stream:          ( ( num ) end
output:                         T -> F T'

current left sentencial form:
                                F T' E'
current token stream:          ( ( num ) end
output:                         F -> ( E )

current left sentencial form:
                                ( E ) T' E'
current token stream:          ( ( num ) end
output:

current left sentencial form:
                                ( E ) T' E'
current token stream:          ( num ) end
output:                         E -> T E'

current left sentencial form:
                                ( T E' ) T' E'
current token stream:          ( num ) end
output:                         T -> F T'

current left sentencial form:
                                ( F T' E' ) T' E'
current token stream:          ( num ) end
output:                         F -> ( E )

current left sentencial form:
                                ( ( E ) T' E' ) T' E'
current token stream:          ( num ) end
output:

current left sentencial form:
                                ( ( E ) T' E' ) T' E'
current token stream:          num ) end
output:                         E -> T E'

current left sentencial form:
                                ( ( T E' ) T' E' ) T' E'
current token stream:          num ) end

```



```

output:
                                T -> F T'

current left sentencial form:
                                ( ( F T' E' ) T' E' ) T' E'
current token stream:
                                num ) end
output:
                                F -> num

current left sentencial form:
                                ( ( num T' E' ) T' E' ) T' E'
current token stream:
                                num ) end
output:

current left sentencial form:
                                ( ( num T' E' ) T' E' ) T' E'
current token stream:
                                ) end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num E' ) T' E' ) T' E'
current token stream:
                                ) end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num ) T' E' ) T' E'
current token stream:
                                ) end
output:

current left sentencial form:
                                ( ( num ) T' E' ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                ( ( num ) E' ) T' E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                ( ( num ) ) T' E'
current token stream:
                                end
output:
                                error: ) expected

```

```

current left sentencial form:
      ( ( num ) ) T' E'
current token stream:
      end
output:
      T' -> epsilon

current left sentencial form:
      ( ( num ) ) E'
current token stream:
      end
output:
      E' -> epsilon

current left sentencial form:
      ( ( num ) )
current token stream:
      end
output:

```

(1))

```

current left sentencial form:
      E
current token stream:
      ( num ) ) end
output:
      E -> T E'

current left sentencial form:
      T E'
current token stream:
      ( num ) ) end
output:
      T -> F T'

current left sentencial form:
      F T' E'
current token stream:
      ( num ) ) end
output:
      F -> ( E )

current left sentencial form:
      ( E ) T' E'
current token stream:
      ( num ) ) end
output:

current left sentencial form:
      ( E ) T' E'
current token stream:
      num ) ) end
output:
      E -> T E'

```

```

current left sentencial form:
      ( T E' ) T' E'
current token stream:
      num ) ) end
output:
      T -> F T'

current left sentencial form:
      ( F T' E' ) T' E'
current token stream:
      num ) ) end
output:
      F -> num

current left sentencial form:
      ( num T' E' ) T' E'
current token stream:
      num ) ) end
output:

current left sentencial form:
      ( num T' E' ) T' E'
current token stream:
      ) ) end
output:
      T' -> epsilon

current left sentencial form:
      ( num E' ) T' E'
current token stream:
      ) ) end
output:
      E' -> epsilon

current left sentencial form:
      ( num ) T' E'
current token stream:
      ) ) end
output:

current left sentencial form:
      ( num ) T' E'
current token stream:
      ) end
output:
      T' -> epsilon

current left sentencial form:
      ( num ) E'
current token stream:
      ) end
output:
      E' -> epsilon

current left sentencial form:
      ( num )
current token stream:

```

output:) end error: end expected
*1	
current left sentencial form:	E
current token stream:	* num end
output:	error: * unexpected
current left sentencial form:	E
current token stream:	num end
output:	E -> T E'
current left sentencial form:	T E'
current token stream:	num end
output:	T -> F T'
current left sentencial form:	F T' E'
current token stream:	num end
output:	F -> num
current left sentencial form:	num T' E'
current token stream:	num end
output:	
current left sentencial form:	num T' E'
current token stream:	end
output:	T' -> epsilon
current left sentencial form:	num E'
current token stream:	end
output:	E' -> epsilon
current left sentencial form:	num
current token stream:	

output:	end
---------	-----

1+1	
current left sentencial form:	E
current token stream:	* num * + num end
output:	error: * unexpected
current left sentencial form:	E
current token stream:	num * + num end
output:	E -> T E'
current left sentencial form:	T E'
current token stream:	num * + num end
output:	T -> F T'
current left sentencial form:	F T' E'
current token stream:	num * + num end
output:	F -> num
current left sentencial form:	num T' E'
current token stream:	num * + num end
output:	
current left sentencial form:	num T' E'
current token stream:	* + num end
output:	T' -> * F T'
current left sentencial form:	num * F T' E'
current token stream:	* + num end
output:	
current left sentencial form:	num * F T' E'
current token stream:	+ num end

```

output:
                                error: + unexpected

current left sentencial form:
                                num * T' E'
current token stream:
                                + num end
output:
                                T' -> epsilon

current left sentencial form:
                                num * E'
current token stream:
                                + num end
output:
                                E' -> + T E'

current left sentencial form:
                                num * + T E'
current token stream:
                                + num end
output:

current left sentencial form:
                                num * + T E'
current token stream:
                                num end
output:
                                T -> F T'

current left sentencial form:
                                num * + F T' E'
current token stream:
                                num end
output:
                                F -> num

current left sentencial form:
                                num * + num T' E'
current token stream:
                                num end
output:

current left sentencial form:
                                num * + num T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                num * + num E'
current token stream:
                                end
output:
                                E' -> epsilon

```

```

current left sentencial form:
                        num * + num
current token stream:
                        end
output:

```

```
1/(1+
```

```

current left sentencial form:
                        E
current token stream:
                        num / ( num + end
output:
                        E -> T E'

current left sentencial form:
                        T E'
current token stream:
                        num / ( num + end
output:
                        T -> F T'

current left sentencial form:
                        F T' E'
current token stream:
                        num / ( num + end
output:
                        F -> num

current left sentencial form:
                        num T' E'
current token stream:
                        num / ( num + end
output:

current left sentencial form:
                        num T' E'
current token stream:
                        / ( num + end
output:
                        T' -> / F T'

current left sentencial form:
                        num / F T' E'
current token stream:
                        / ( num + end
output:

current left sentencial form:
                        num / F T' E'
current token stream:
                        ( num + end
output:
                        F -> ( E )

current left sentencial form:

```

```

num / ( E ) T' E'
current token stream:
( num + end
output:

current left sentencial form:
num / ( E ) T' E'
current token stream:
num + end
output:
E -> T E'

current left sentencial form:
num / ( T E' ) T' E'
current token stream:
num + end
output:
T -> F T'

current left sentencial form:
num / ( F T' E' ) T' E'
current token stream:
num + end
output:
F -> num

current left sentencial form:
num / ( num T' E' ) T' E'
current token stream:
num + end
output:

current left sentencial form:
num / ( num T' E' ) T' E'
current token stream:
+ end
output:
T' -> epsilon

current left sentencial form:
num / ( num E' ) T' E'
current token stream:
+ end
output:
E' -> + T E'

current left sentencial form:
num / ( num + T E' ) T' E'
current token stream:
+ end
output:

current left sentencial form:
num / ( num + T E' ) T' E'
current token stream:
end
output:

```



```

                                error: T expected

current left sentencial form:
                                num / ( num + E' ) T' E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                num / ( num + ) T' E'
current token stream:
                                end
output:
                                error: ) expected

current left sentencial form:
                                num / ( num + ) T' E'
current token stream:
                                end
output:
                                T' -> epsilon

current left sentencial form:
                                num / ( num + ) E'
current token stream:
                                end
output:
                                E' -> epsilon

current left sentencial form:
                                num / ( num + )
current token stream:
                                end
output:

```

```

1+2*-8
current left sentencial form:
                                E
current token stream:
                                num + num * - num end
output:
                                E -> T E'

current left sentencial form:
                                T E'
current token stream:
                                num + num * - num end
output:
                                T -> F T'

current left sentencial form:
                                F T' E'
current token stream:
                                num + num * - num end

```

```

output:
                                F -> num

current left sentencial form:
                                num T' E'
current token stream:
                                num + num * - num end
output:

current left sentencial form:
                                num T' E'
current token stream:
                                + num * - num end
output:
                                T' -> epsilon

current left sentencial form:
                                num E'
current token stream:
                                + num * - num end
output:
                                E' -> + T E'

current left sentencial form:
                                num + T E'
current token stream:
                                + num * - num end
output:

current left sentencial form:
                                num + T E'
current token stream:
                                num * - num end
output:
                                T -> F T'

current left sentencial form:
                                num + F T' E'
current token stream:
                                num * - num end
output:
                                F -> num

current left sentencial form:
                                num + num T' E'
current token stream:
                                num * - num end
output:

current left sentencial form:
                                num + num T' E'
current token stream:
                                * - num end
output:
                                T' -> * F T'

current left sentencial form:

```

```

current token stream:    num + num * F T' E'
output:                  * - num end

current left sentencial form:
current token stream:    num + num * F T' E'
output:                  - num end
                        error: F expected

current left sentencial form:
current token stream:    num + num * T' E'
output:                  - num end
                        T' -> epsilon

current left sentencial form:
current token stream:    num + num * E'
output:                  - num end
                        E' -> - T E'

current left sentencial form:
current token stream:    num + num * - T E'
output:                  - num end

current left sentencial form:
current token stream:    num + num * - T E'
output:                  num end
                        T -> F T'

current left sentencial form:
current token stream:    num + num * - F T' E'
output:                  num end
                        F -> num

current left sentencial form:
current token stream:    num + num * - num T' E'
output:                  num end

current left sentencial form:
current token stream:    num + num * - num T' E'
output:                  end

```

```
                                T' -> epsilon
current left sentencial form:
                                num + num * - num E'
current token stream:
                                end
output:
                                E' -> epsilon
current left sentencial form:
                                num + num * - num
current token stream:
                                end
output:
```

7. 分析总结

从测试结果可看出，对于正确的表达式，语法分析输出结果也是正确的，而对于错误的表达式，本程序的错误处理措施也能在一定程度上对其进行恢复，当然也具有一定的局限性。

在编译流程中，语法分析是词法分析的后续环节，其分析的基础是词法分析得到的 **token** 流，故在本次试验中也利用了上次词法分析实验的成果，在其基础上加以拓展，延续了其设计思路。

编写语法分析程序的过程中遇到了更大的挑战，如如何表示文法产生式，如何高效且正确地提取左公因子，如何解决求 **FOLLOW** 集过程可能出现的死循环问题，这也相当于是对数据结构、算法及编程能力的一个锻炼。