

RSA(2019/1/23)作业writeup

RSA实践

在一次RSA密钥对生成中, 假设 $p=473398607161$, $q=4511491$, $e=17$
求解出 d 将得到的 d 提交

```
#RSA实践
#三种解法
'''
第一种gmpy2解法
mpz:Multiple-precision Integers (多精度型整数)
gmpy2.invert():求模逆
'''
import gmpy2
p=gmpy2.mpz(473398607161)
q=gmpy2.mpz(4511491)
e=gmpy2.mpz(17)
fn=(p-1)*(q-1)
d=gmpy2.invert(e, fn)
print("d is:")
print(d)

'''
直接用扩展欧几里得法
'''
def computeD(fn, e):
    (x, y, r) = ext_euclid(fn, e)
    #y maybe < 0, so convert it
    if y < 0:
        return fn + y
    return y

def ext_euclid(a, b):
    if b == 0:
        return (1, 0, a)
    else:
        x, y, q = ext_euclid(b, a % b)
        # q = gcd(a, b) = gcd(b, a%b)
        x, y = y, (x - (a // b) * y) # '/'代表整除, 可以用python演示一下.
        return (x, y, q)

p = 473398607161
```

```

q = 4511491
e = 17

n = p * q
print("n: " + str(n))
fn = (p - 1) * (q - 1)
print("f(n):" + str(fn))
d = computeD(fn, e)
print(d)

'''
用工具解密——RSAtools
ps:用这个工具记得将e转化为hex形式
'''

```

RSA

点击下载所需文件，解压得到



flag.enc



public.pem

方法一：openssl应用

根据之前讲的，在命令行里输入：`openssl rsa -pubin -text -modulus -in public.pem`

得到公钥里面信息：

```

deer@deer-PC:~/Desktop/RSA$ openssl rsa -pubin -text -modulus -in public.pem
Public-Key: (256 bit)
Modulus:
 00:a4:1b:00:de:fd:37:8b:73:95:b4:a2:eb:1e:c9:
 6f:56:a6:1c:d9:c3:b5:a0:a7:35:28:5c:1e:eb:2f:
 b8:17:a7
Exponent: 65537 (0x10001)
Modulus=00a41b00defd378b7395b4e2eb1ec9bf56a61cd9c3b5a0a735285c1eeb2fb817a7
writing RSA key
-----BEGIN PUBLIC KEY-----
MDwwOTYtZkZlIhvcNAQEBBQADKwAwKAIhAKQQt79N4tz1bTt6x7JvIawdRn0t aCn
MShSHuzvJenAgMBAAE=
-----END PUBLIC KEY-----

```

注意，这里的modulus和RSAtools一样是n，即

```

n
=0xA41006DEFD378B7395B4E2EB1EC9BF56A61CD9C3B5A0A73528521EEB2FB817A7

```

```
p = 258631601377848992211685134376492365269
```

```
q = 286924040788547268861394901519826758027
```

```
e = 65537
```

通过我们今天讲的也就是RSA实践中给出的三种方法（任选一种）解出：

```
d =
```

```
230717693751110404252872446253287976152957728141801093667842499764982154  
94337
```

用RSAtool生成秘钥：

```
python rsatool.py -f PEM -o private.pem -n
```

```
7420762414294524226305703528711098396764602005730782870958796964670136176  
4263 -d  
230717693751110404252872446253287976152957728141801093667842499764982154  
94337
```

得到秘钥文件,private.pem

```
deer@deer-PC:~/Desktop/RSA$ openssl rsautl -decrypt -in flag.enc -inkey private.pem  
ISG{256bit_is_weak}deer@deer-PC: ~/Desktop/RSA$
```

得到flag: ISG{256bit_is_weak}

方法二：rsa模块的应用（就是小写的rsa）

获得n,p,q,e,d的方法如上：

```
n =  
0xA41006DEFD378B7395B4E2EB1EC9BF56A61CD9C3B5A0A73528521EEB2F  
B817A7  
p = 258631601377848992211685134376492365269  
q = 286924040788547268861394901519826758027  
e = 65537  
d =  
2307176937511104042528724462532879761529577281418010936678424997  
6498215494337
```

rsa模块里面可以利用PrivateKey函数构建出私钥，同时用decrypt进行解密

```
#-*-coding:utf-8-*-
```

```

import rsa
'''
rsa是一个python模板, python2.7-python3.6均支持
'''

n=74207624142945242263057035287110983967646020057307828709587969
646701361764263
e=65537
d=23071769375111040425287244625328797615295772814180109366784249
976498215494337
p=258631601377848992211685134376492365269
q=286924040788547268861394901519826758027

prikey = rsa.PrivateKey(n,e,d,p,q)

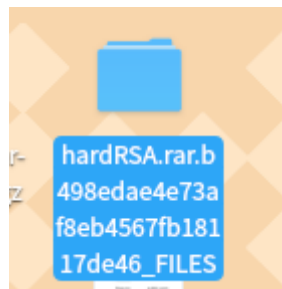
#print(prikey)

t =
rsa.decrypt(b'\x49\xB9\x6E\xDB\xE3\x96\x1F\x58\xD5\x29\x07\x4B\xD8\x9
3\xD6\xE0\x36\xCE\xAF\x2B\x6D\x21\x4B\x47\x0F\xDC\x0D\x48\x72\x3D\x
x6A\x40', prikey)
print(t)

```

Fake_rsa

这题的原题的HardRSA



下载文件本来是这个样子, 在linux里面可以直接解压, 但是在windows里面不行, 可以将.rar后面的后缀删掉, 就可以解压



flag.enc



pubkey.pem

得到以上文件。

用 `openssl rsa -pubin -text -modulus -in pubkey.pem`



```
e = 2
n =
8792434826413240687527614051449993714505089366560259299241817164
7042491658461
```

还是用yafu进行分解：

```
p = 319576316814478949870590164193048041239
q = 275127860351348928173285174381581152299
```

由于e = 2，所以很容易想到rabin算法

```
#!/usr/env/python
#-*-coding:utf-8-*-
import gmpy
import libnum
n=87924348264132406875276140514499937145050893665602592992418171
647042491658461
p=319576316814478949870590164193048041239
q=275127860351348928173285174381581152299
e=2
c=0x39de036de3132757e819f769ead64bb487ee3f47e67843afb73748fd9e979b
e0
mp=pow(c,(p+1)/4,p)
mq=pow(c,(q+1)/4,q)
yp=gmpy.invert(p,q)
yq=gmpy.invert(q,p)
r=(yp*p*mq+yq*q*mp)%n
rr=n-r
s=(yp*p*mq-yq*q*mp)%n
ss=n-s
print (libnum.n2s(r))
print (libnum.n2s(rr))
print (libnum.n2s(s))
print (libnum.n2s(ss))
```

