Package 'PF'

July 17, 2024

```
Type Package
Title Prevented fraction
Version 9.6.8
Date 2024-06-06
Description Functions related to PF (prevented fraction). Calculate incidence
      density ratio, confidence interval, and Rao-Scott weights of PF by multiple
      methods. See http://goo.gl/eJ6Rxi for definition of PF.
      No endorsement, claim, or warranty is implied for this package. It is made
      available for investigational or pedagogical use only. See
      https://www.aphis.usda.gov/animal_health/vet_biologics/publications/STATWI0007.pdf
      for futher details.
License file LICENSE
URL https://github.com/ABS-dev/PF/
BugReports https://github.com/ABS-dev/PF/issues/
LazyLoad true
LazyData true
Depends R (>= 4.2)
Imports methods,
      plyr,
      dplyr,
      tidyr
Suggests magrittr,
      testthat,
      knitr,
      rmarkdown,
      R.rsp
Collate 'aaa.r'
      'aab.r'
      'aac.r'
      'class.r'
      'generics.r'
      'PF.r'
      'PF-package.r'
      'IDRlsi.r'
      'IDRsc.r'
```

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'RRlsi.r'
'RRmh.r'
'RRmpWald.r'
'RRor.r'
'RRotsst.r'
'RRsc.r'
'RRStr.r'
'RRtosst.r'
'rsbWt.r'
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Encoding UTF-8
Roxygen list(markdown = TRUE)
RoxygenNote 7.3.2
VignetteBuilder R.rsp

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.rr.score.asymp

Internal function.

Description

Internal function.

Usage

```
.rr.score.asymp(y, alpha = 0.05, iter.max = 18, converge = 1e-04, mn = FALSE)
```

Arguments

y data alpha alpha

iter.max maximum number of iterations

converge convergence criterion

mn boolean whether to calculate MN or use default value of 1.0

Examples

```
.rr.score.asymp(c(0, 18, 16, 19), mn = FALSE) .rr.score.asymp(c(0, 18, 16, 19), mn = TRUE)
```

bird

bird dataset

Description

bird dataset

Format

a data.frame with 6 observations of the following 4 variables, no NAs

- y: number positive
- n: total number in group tx x all
- tx: treatment "vac" or "con"
- all: all?

References

we need some references

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birdm

birdm dataset

Description

birdm dataset

Format

a data.frame with 6 observations of the following 4 variables, no NAs

- y: number positive
- n: total number in group tx x all
- tx: treatment "vac" or "con"
- all: all?

References

we need some references

IDRlsi

IDR likelihood support interval.

Description

Estimates likelihood support interval for the incidence density ratio or prevented fraction based on it.

Usage

```
IDRlsi(
  y = NULL,
  formula = NULL,
  data = NULL,
  alpha = 0.05,
  k = 8,
  use.alpha = FALSE,
  pf = TRUE,
  converge = 1e-08,
  rnd = 3,
  start = NULL,
  trace.it = FALSE,
  iter.max = 24,
  compare = c("con", "vac")
)
```

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Arguments

y Data vector c(y1, n1, y2, n2) where y are the positives, n are the total, and group

1 is compared to group 2 (control or reference).

formula Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the

group size, x is a factor with two levels of treatment.

data data.frame containing variables of the formula.

alpha Complement of the confidence level.

k Likelihood ratio criterion.

use.alpha Base choice of k on its relationship to alpha?

pf Estimate *IDR* or its complement *PF*?

converge Convergence criterion

rnd Number of digits for rounding. Affects display only, not estimates.

start describe here.

trace.it Verbose tracking of the iterations? iter.max Maximum number of iterations

compare Text vector stating the factor levels: compare[1] is the vaccinate group to which

compare[2] (control or reference) is compared.

Details

Estimates likelihood support interval for the incidence density ratio based on orthogonal factoring of reparameterized likelihood. The incidence density is the number of cases per subject-time; its distribution is assumed Poisson.

Likelihood support intervals are usually formed based on the desired likelihood ratio, often 1 / 8 or 1 / 32. Under some conditions the log likelihood ratio may follow the chi square distribution. If so, then $\alpha=1-F(2log(k),1)$, where F is a chi-square CDF. if use.alpha = TRUE``RRsc() will make the conversion from α to k.

The data may also be a matrix, in which case y would be entered as matrix(c(y1, n1 - y1, y2, n2 - y2), 2, 2, byrow = TRUE).

Value

A rrsi object with the following elements.

- estimate: vector with point and interval estimate
- estimator: either PF or IDR
- y: data.frame with "y1", "n1", "y2", "n2" values.
- k: Likelihood ratio criterion
- rnd: how many digits to round the display
- alpha: complement of confidence level

Author(s)

PF-package

References

Royall R. Statistical Evidence: A Likelihood Paradigm. Chapman & Hall, Boca Raton, 1997. Section 7.2.

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See Also

IDRsc

```
\ensuremath{\mathtt{\#}} Both examples represent the same observation, with data entry by vector
# and matrix notation.
y_vector <- c(26, 204, 10, 205)
IDRlsi(y_vector, pf = FALSE)
# 1 / 8 likelihood support interval for IDR
# corresponds to 95.858% confidence
# (under certain assumptions)
# IDR
# IDR LL UL
# 2.61 1.26 5.88
y_{matrix} \leftarrow matrix(c(26, 178, 10, 195), 2, 2, byrow = TRUE)
y_matrix
# [, 1] [, 2]
# [1, ] 26 178
# [2, ] 10 195
IDRlsi(y_matrix, pf = FALSE)
\# 1 / 8 likelihood support interval for IDR
# corresponds to 95.858% confidence
# (under certain assumptions)
# IDR
# IDR LL UL
# 2.61 1.26 5.88
data1 \leftarrow data.frame(group = rep(c("treated", "control"), each = 5),
             n = c(rep(41, 4), 40, rep(41, 5)),
             y = c(4, 5, 7, 6, 4, 1, 3, 3, 2, 1),
             cage = rep(paste("cage", 1:5), 2))
IDRlsi(data = data1, formula = cbind(y, n) \sim group,
               compare = c("treated", "control"), pf = FALSE)
# 1 / 8 likelihood support interval for IDR
# corresponds to 95.858% confidence
# (under certain assumptions)
# IDR
# IDR LL UL
# 2.61 1.26 5.88
require(dplyr)
data2 <- data1 |>
  group_by(group) |>
```

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IDRsc

IDR confidence interval.

Description

Estimates confidence interval for the incidence density ratio or prevented fraction based on it.

Usage

```
IDRsc(
  y = NULL,
  data = NULL,
  formula = NULL,
  compare = c("con", "vac"),
  alpha = 0.05,
  pf = TRUE,
  rnd = 3
)
```

Arguments

у	Data vector $c(y1, n1, y2, n2)$ where y are the positives, n are the total, and group 1 is compared to group 2 (control or reference).
data	data.frame containing variables of formula.
formula	Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the group size, x is a factor with two levels of treatment.
compare	Text vector stating the factor levels: compare[1] is the vaccinate group to which compare[2] (control or reference) is compared.
alpha	Complement of the confidence level.
pf	Estimate <i>IDR</i> , or its complement <i>PF</i> ?
rnd	Number of digits for rounding. Affects display only, not estimates.

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Details

The incidence density is the number of cases per subject-time; its distribution is assumed Poisson. IDRsc estimates a confidence interval for the incidence density ratio using Siev's formula based on

the Poisson score statistic.
$$IDR = \widehat{IDR} \left\{ 1 + \left(\frac{1}{y_1} + \frac{1}{y_2} \right) \frac{z_{\alpha/2}^2}{2} \pm \frac{z_{\alpha/2}^2}{2y_1y_2} \sqrt{y_{\bullet} \left(y_{\bullet} z_{\alpha/2}^2 + 4y_1y_2 \right)} \right\}$$

The data may also be a matrix. In that case y would be entered as

$$matrix(c(y1, n1 - y1, y2, n2 - y2), 2, 2, byrow = TRUE).$$

Value

A rr1 object with the following elements.

- estimate: vector with point and interval estimate
- estimator: either PF or IDR
- y: data vector
- · rnd: how many digits to round the display
- alpha: complement of confidence level

Author(s)

PF-package

References

Siev D, 1994. Estimating vaccine efficacy in prospective studies. *Preventive Veterinary Medicine* 20:279-296, Appendix 1.

Graham PL, Mengersen K, Morton AP, 2003. Confidence limits for the ratio of two rates based on likelihood scores:non-iterative method *Statistics in Medicine* 22:2071-2083.

Siev D, 2004. Letter to the editor. *Statistics in Medicine* 23:693. (Typographical error in formula: replace the two final minus signs with subscript dots.)

See Also

IDRlsi

```
# All examples represent the same observation, with data entry by vector,
# matrix, and formula+data notation.

y_vector <- c(26, 204, 10, 205)
IDRsc(y_vector, pf = FALSE)

# IDR
# 95% interval estimates

# IDR LL UL
# 2.61 1.28 5.34

y_matrix <- matrix(c(26, 178, 10, 195), 2, 2, byrow = TRUE)
y_matrix
# [, 1] [, 2]</pre>
```

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```
#[1,] 26 178
# [2, ] 10 195
IDRsc(y_matrix, pf = FALSE)
# IDR
# 95% interval estimates
# IDR LL UL
# 2.61 1.28 5.34
require(dplyr)
data1 <- data.frame(group = rep(c("treated", "control"), each = 5),</pre>
           n = c(rep(41, 4), 40, rep(41, 5)),
           y = c(4, 5, 7, 6, 4, 1, 3, 3, 2, 1),
           cage = rep(paste("cage", 1:5), 2))
data2 <- data1 |>
 group_by(group) |>
  summarize(sum_y = sum(y),
 sum_n = sum(n)
IDRsc(data = data2, formula = cbind(sum_y, sum_n) ~ group,
   compare = c("treated", "control"), pf = FALSE)
# IDR
# 95% interval estimates
# IDR LL UL
# 2.61 1.28 5.34
```

New

New dataset

Description

New dataset

Format

a data frame with 52 observations of the following 3 variables, no NAs

- cage: cage ID. 1 26
- tx: treatment. one of "con" or "vac"
- pos: numeric indicator of positive response. 0 = FALSE or 1 = TRUE

References

We need some references

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pf-class

Data class pf

Description

data class pf

Fields

- estimator: either "PF" or "IDR"
- rnd: how many digits to round display
- alpha: complement of c.i.

Author(s)

PF-package

See Also

```
rr1, rrsi, rrsc, rrstr
```

phiWt

Binomial dispersion parameter.

Description

MME estimate of dispersion parameter phi.

Usage

```
phiWt(fit, subset.factor = NULL, fit.only = TRUE, show.warns = FALSE)
```

Arguments

fit A glm object.

subset.factor Factor for estimating phi by subset.

fit.only Return only the new fit? If FALSE, also returns the weights and phi estimates.

show.warns Show warnings

Details

Estimates binomial dispersion parameter ϕ by the method of moments. Refits the model, weighting the observations by $1/\phi$. Uses quasibinomial family in glm().

Value

A list with the following elements. fit: the new model fit, updated by the estimated weights weights: vector of weights phi: vector of phi estimates

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Author(s)

PF-package

References

Wedderburn RWM, 1974. Quasi-likelihood functions, generalized linear models, and the Gauss-Newton method. *Biometrika* 61:439-447.

See Also

tauWt, RRor.

Examples

```
birdm.fit <- glm(cbind(y, n - y) ~ tx-1, binomial, birdm)
RRor(phiWt(birdm.fit))
#
# 95% t intervals on 4 df
#
# PF
# PF LL UL
# 0.479 -0.537 0.823
#
# mu.hat LL UL
# txcon 0.768 0.95 0.367
# txvac 0.400 0.78 0.111
#</pre>
```

print.rr1

Print values for PF data obhects.

Description

Print values for PF data obhects.

Usage

```
## S3 method for class 'rr1'
print(x, ...)
## S3 method for class 'rror'
print(x, ...)
## S3 method for class 'rrsi'
print(x, ...)
## S3 method for class 'rrmp'
print(x, ...)
## S3 method for class 'rrsc'
print(x, ...)
## S3 method for class 'rrsc'
print(x, ...)
```

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Arguments

x object of class rr1, rror, rrsi, rrmp, rrstr, rrsc other arguments not used by this method

rat rat dataset

Description

rat dataset

Format

a data.frame with 32 observations of the following 3 variables, no NAs

- y: number positive
- n: total number
- group: treatment group: "control" or "treated"

References

Weil's rat data (Table 1 of Rao and Scott)

rr1-class

Data class rr1

Description

Data class rr1

Fields

• estimate: vector with point and interval estimate

• estimator: either "PF" or "IDR"

- Y: data.frame with restructured input
- rnd: how many digits to round display
- alpha: complement of c.i.

Author(s)

PF-package

See Also

IDRsc, RRotsst, RRtosst

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RRlsi RR likelihood support interval.

Description

likelihood support interval for the risk ratio or prevented fraction by the likelihood profile.

Usage

```
RRlsi(
  y = NULL,
  formula = NULL,
  data = NULL,
  compare = c("vac", "con"),
  alpha = 0.05,
  k = 8,
  use.alpha = FALSE,
  pf = TRUE,
  iter.max = 50,
  converge = 1e-06,
  rnd = 3,
  start = NULL,
  track = FALSE,
  full.track = FALSE
)
```

Arguments

full.track

у	Data vector c(y1, n1, y2, n2) where y are the positives, n are the total, and group 1 is compared to group 2 (control or reference group).
formula	Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the group size, x is a factor with two levels of treatment.
data	data.frame containing variables of formula.
compare	Text vector stating the factor levels: compare[1] is the vaccinate group to which compare[2] (control or reference) is compared.
alpha	Complement of the confidence level (see details).
k	Likelihood ratio criterion.
use.alpha	Base choice of k on its relationship to alpha?
pf	Estimate <i>RR</i> or its complement <i>PF</i> ?
iter.max	Maximum number of iterations
converge	Convergence criterion
rnd	Number of digits for rounding. Affects display onlyRR, not estimates.
start	Optional starting value.
track	Verbose tracking of the iterations?

Verbose tracking of the iterations?

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Details

Estimates a likelihood support interval for RR or PF by the profile likelihood method using the DUD algorithm.

Likelihood support intervals are usually formed based on the desired likelihood ratio, often 1 / 8 or 1 / 32. Under some conditions the log likelihood ratio may follow the chi square distribution. If so, then $\alpha=1-F(2log(k),1)$, where F is a chi-square CDF. if use.alpha = TRUE, RRlsi() will make the conversion from α to k

The data may also be a matrix. In that case Y would be entered as matrix(c(y1, n1-y1, y2, n2-y2), 2, 2, byrow = TRUE).

Value

An object of class rrsi with the following fields: estimate: matrix of point and interval estimates - see details estimator: either "PF" or "RR" y: data.frame with "y1", "n1", "y2", "n2" values. rnd: how many digits to round the display k: likelihood ratio criterion alpha: complement of confidence level

Author(s)

PF-package

References

Royall R. Statistical Evidence: A Likelihood Paradigm. Chapman & Hall, Boca Raton, 1997. Section 7.6

Ralston ML, Jennrich RI, 1978. DUD, A Derivative-Free Algorithm for Nonlinear Least Squares. *Technometrics* 20:7-14.

```
# All examples represent the same observation, with data entry by vector,
# matrix, and formula+data notation.
y_{\text{vector}} <- c(4, 24, 12, 28)
RRlsi(y_vector)
# 1 / 8 likelihood support interval for PF
# corresponds to 95.858% confidence
    (under certain assumptions)
# PF
      PF
             LL
# 0.6111 0.0168 0.8859
y_{matrix} \leftarrow matrix(c(4, 20, 12, 16), 2, 2, byrow = TRUE)
y_matrix
# [, 1] [, 2]
#[1,] 4 20
# [2, ] 12 16
RRlsi(y_matrix)
```

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```
# 1 / 8 likelihood support interval for PF
# corresponds to 95.858% confidence
    (under certain assumptions)
# PF
#
      PF
            LL
                    UL
# 0.6111 0.0168 0.8859
require(dplyr)
data1 <- data.frame(group = rep(c("treated", "control"), each = 2),</pre>
 y = c(1, 3, 7, 5),
 n = c(12, 12, 14, 14),
 cage = rep(paste("cage", 1:2), 2))
data2 <- data1 |>
  group_by(group) |>
  summarize(sum_y = sum(y),
   sum_n = sum(n)
RRlsi(data = data2, formula = cbind(sum_y, sum_n) ~ group,
  compare = c("treated", "control"))
# 1 / 8 likelihood support interval for PF
# corresponds to 95.858% confidence
# (under certain assumptions)
# PF
# PF
        LL
                UL
# 0.6111 0.0168 0.8859
```

RRmh

Mantel-Haenszel method, CI for common RR over strata or clusters with sparse data.

Description

Estimates confidence intervals for the risk ratio or prevented fraction from clustered or stratified data, using a Mantel-Haenszel estimator for sparse data.

Usage

```
RRmh(
  formula = NULL,
  data = NULL,
  compare = c("vac", "con"),
  Y,
  alpha = 0.05,
  pf = TRUE,
  rnd = 3
)
```

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Arguments

formula Formula of the form $cbind(y, n) \sim x + cluster(w)$, where Y is the number positive, n is the group size, x is a factor with two levels of treatment, and w is a factor indicating the clusters. data.frame containing variables for formula data compare Text vector stating the factor levels: compare[1] is the vaccinate group to which compare[2] (control or reference) is compared. Υ Matrix of data, $K \times 4$. Each row is a stratum or cluster. The columns are y1, n1, y2, n2, where the y's are the number of positive in each group, and the n is the total in each group. Group 1 corresponds to vaccinates and group 2 are controls or reference. If data entered by formula and dataframe, Y is generated automatically. alpha Complement of the confidence level.

alpha Complement of the confidence level.

pf Estimate RR or its complement PF?

rnd Number of digits for rounding. Affects display only, not estimates.

Details

Based on the Mantel-Haenszel (1959) procedure for sparse data developed by Greenland and Robins (1985). The confidence limits are based on asymptotic normality of the log(risk ratio). Agresti and Hartzel (2000) favor this procedure for small, sparse data sets, but they warn that it is less efficient than maximum likelihood for large data sets.

Value

An object of class rr1 with the following fields.

- estimate: vector of point and interval estimates: point estimate, lower confidence limit, upper confidence limit
- estimator: either "PF" or "RR"
- y: data.frame of restructured input
- rnd: how many digits to round the display
- alpha: complement of confidence level

Note

If either all y1's or all y2's are zero, a division by zero may occur, and a NaN returned for some values.

Vignette Examples for Stratified Designs forthcoming with more examples.

Call to this function may be one of two formats: (1) specify data and formula or (2) as a matrix Y RRmh(formula, data, compare = c("b", "a"), pf = TRUE, alpha = 0.05, rnd = 3) RRmh(Y, pf = TRUE, alpha = 0.05, rnd = 3)

Author(s)

PF-package

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References

Mantel N, Haenszel W, 1959. Statistical aspects of the analysis of data from retrospective studies of disease. *Journal of the National Cancer Institute* 22:719-748.

Greenland S, Robins JM, 1985. Estimation of a common effect parameter from sparse follow-up data. *Biometrics* 41: 55-68. Errata, 45: 1323-1324.

Agresti A, Hartzel J, 2000. Strategies for comparing treatments on a binary response with multicentre data. *Statistics in Medicine* 19: 1115-1139.

Lachin JM, 2000. *Biostatistical Methods: The Assessment of Relative Risks* (Wiley, New York), Sec. 4.3.1.

See Also

rr1

Examples

```
## Table 1 from Gart (1985)
## as data frame
# tx group "b" is control
RRmh(cbind(y, n) \sim tx + cluster(clus),
     compare = c("a", "b"), pf = FALSE)
# RR
# 95% interval estimates
#
#
  RR LL UL
# 2.67 1.37 5.23
## or as matrix
RRmh(Y = table6, pf = FALSE)
# RR
\# 95% interval estimates
  RR LL UL
# 2.67 1.37 5.23
```

rrmp-class

Data class rrmp

Description

data class rrmp

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Fields

• estimate: vector with point and interval estimate

• estimator: either "PF" or "IDR"

· Y: data vector

• rnd: how many digits to round display

• alpha: complement of c.i.

· compare: text vector, same as input

• multvec: data.frame showing the multinomial representation of the data

Author(s)

PF-package

See Also

RRmpWald

RRmpWald

Wald confidence intervals for RR from matched pairs

Description

Estimates confidence intervals for the risk ratio or prevented fraction from matched pairs.

Usage

```
RRmpWald(
  formula = NULL,
  data = NULL,
  compare = c("vac", "con"),
  affected = 1,
  x,
  alpha = 0.05,
  pf = TRUE,
  tdist = TRUE,
  df = NULL,
  rnd = 3
)
```

Arguments

Formula of the form $y \sim x + cluster(w)$, where y is the indicator for an individual's positive response, x is a factor with two levels of treatment, and w identifies

the pairs.

data data. frame containing variables in formula

compare Text vector stating the factor levels: compare[1] is the vaccinate group to which

compare[2] (control or reference) is compared.

affected Indicator for positive response

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х	Alternative data input. Instead of formula and data frame, data may be input as frequency vector. See example for how to order this vector.
alpha	Complement of the confidence level
pf	Estimate <i>RR</i> or its complement <i>PF</i> ?
tdist	Use t distribution?
df	Degrees of freedom. When NULL, the function will default to ' $df = N$
	• 2', where N is the total number of pairs.
rnd	Number of digits for rounding. Affects display only, not estimates.

Details

Estimates confidence intervals for the risk ratio or prevented fraction from matched pairs. The response is the tetranomial vector c(11, 12, 21, 22), where the first index is the row and the the second index is the column when displayed as a 2x2 table. Wald type confidence intervals are found by applying the delta method to the multinomial variance. This method fails when there are no responders in one of the treatment groups.

Alternative forms of data entry are illustrated by the output, say Y, where c(Y*xtable) = Y*freqvec = Y*multvec*Freq.

If RR = 0 (PF = 1), the function will return degenerate interval.

Value

A rrmp object with the following fields:

- estimate: vector of point and interval estimates see details
- estimator: either "PF" or "RR"
- compare: text vector, same as input
- alpha: complement of confidence level
- rnd: how many digits to round the display
- multvec: data frame showing the multinomial representation of the data

Note

Experimental functions for estimating profile likelihood intervals are in the CVBmisc package.

```
Call to this function may be one of two formats: (1) specify data and formula or (2) as a vector \mathbf{x}
```

```
RRmpWald(formula, data, compare = c("vac", "con"), affected = 1, alpha = 0.05, pf = TRUE, tdist = TRUE, df = NULL, rnd = 3)
```

```
RRmpWald(x, compare = c("vac", "con"), affected = 1, alpha = 0, 05, pf = TRUE, tdist = TRUE, df = NULL, rnd = 3)
```

Author(s)

PF-package

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Examples

```
RRmpWald(pos \sim tx + cluster(cage), New, compare = c("vac", "con"))
# PF
# 95% interval estimates
#
#
    PF
          LL
               UL
# 0.550 0.183 0.752
require(magrittr)
thistable <- New |>
 tidyr::spread(tx, pos) |>
 dplyr::mutate(vac = factor(vac, levels = 1:0),
   con = factor(con, levels = 1:0)) |>
 with(table(vac, con))
thistable
    con
# vac 1 0
  1 7 2
# 0 13 4
as.vector(thistable)
#[1] 7 13 2 4
RRmpWald(x = as.vector(thistable))
# PF
# 95% interval estimates
    PF
        LL
# 0.550 0.183 0.752
```

RRor

RR estimate from logistic regression.

Description

Model based interval estimate of the risk ratio or prevented fraction from a logistic regression model.

Usage

```
RRor(
   fit = NULL,
   beta.hat = NULL,
   var.beta.hat = NULL,
   degf = NULL,
   which = c(1, 2),
   pf = TRUE,
   norm = FALSE,
   alpha = 0.05,
   rnd = 3
)
```

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Arguments

fit A glm object.

beta.hat Parameters estimates from a logistic regression with no intercept.

var.beta.hat Variance-covariance matrix from a logistic regression with no intercept.

degf Degrees of freedom.

which Numeric vector indicating which parameters to compare, so that RR = compare[2]

/compare[1]

pf Estimate *RR* or its complement *PF*?

norm Estimate confidence interval using quantiles of Guassian rather

than t distribution quantiles?

alpha Complement of the confidence level.

rnd Number of digits for rounding. Affects display only, not estimates.

Details

Estimates confidence intervals using the delta method on parameters from a generalized linear model with logit link.

 $RR = \mu_2/\mu_1$, where μ_i are the estimated probabilities from the model.

Value

A rror object with the following fields.

- estimate: vector with point and interval estimate
- estimator: either PF or RR
- mu: matrix with rows giving probability estimates for each of the groups
- rnd: how many digits to round the display
- alpha: complement of confidence level
- norm: logical indicating Gaussian or t-interval
- · degf: degrees of freedom

Note

```
Call to this function may be one of two formats: (1) specify fit or (2) beta.hat, var.beta.hat, degf
```

```
RRor(fit, degf = NULL, pf = TRUE, alpha = 0.05, which = c(1, 2), norm = TRUE, rnd = 3) 
RRor(beta.hat, var.beta.hat, degf, pf = TRUE, alpha = 0.05, which = c(1, 2), norm = TRUE, rnd = 3)
```

Author(s)

PF-package

See Also

rror, phiWt, tauWt StatWI007 for more examples

22 rror-class

Examples

```
bird.fit <- glm(cbind(y, n - y) \sim tx - 1, binomial, bird)
RRor(tauWt(bird.fit))
\# 95% t intervals on 4 df
#
# PF
#
     PF
         LL
                  UL
# 0.500 -0.583 0.842
       mu.hat LL
# txcon 0.733 0.943 0.3121
# txvac 0.367 0.752 0.0997
RRor(phiWt(bird.fit))
# 95% t intervals on 4 df
#
# PF
     PF
#
          LL
                   UL
# 0.500 -0.583 0.842
       mu.hat LL
#
# txcon 0.733 0.943 0.3121
# txvac 0.367 0.752 0.0997
```

rror-class

Data class rror

Description

data class rror

Fields

- estimate: vector with point and interval estimate
- estimator: either "PF" or "IDR"
- · Y: data vector
- rnd: how many digits to round display
- alpha: complement of c.i.
- norm: logical indicating Gaussian or t interval
- degf: degrees of freedom
- mu: matrix with rows giving probability estimates for each of the groups

Author(s)

PF-package

See Also

RRor

RRotsst 23

RRotsst

RR exact CI, OTSST method.

Description

Estimates confidence interval for the risk ratio or prevented fraction, exact method based on the score statistic (inverts one two-sided test).

Usage

```
RRotsst(
  y = NULL,
  data = NULL,
  formula = NULL,
  compare = c("vac", "con"),
  alpha = 0.05,
  pf = TRUE,
  stepstart = 0.1,
  iter.max = 36,
  converge = 1e-06,
  rnd = 3,
  trace.it = FALSE,
  nuisance.points = 120,
  gamma = 1e-06
)
```

evaluation)

Arguments

У	Data vector c(y1, n1, y2, n2) where y are the positives, n are the total, and group 1 is compared to group 2 (control or reference).	
data	data.frame containing variables of the formula.	
formula	Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the group size, x is a factor with two levels of treatment.	
compare	Text vector stating the factor levels: compare[1] is the vaccinate group to which compare[2] (control or reference) is compared.	
alpha	Complement of the confidence level.	
pf	Estimate <i>RR</i> or its complement <i>PF</i> ?	
stepstart	starting interval for step search	
iter.max	Maximum number of iterations	
converge	Convergence criterion	
rnd	Number of digits for rounding. Affects display only, not estimates.	
trace.it	Verbose tracking of the iterations?	
nuisance.points		
	number of points over which to evaluate nuisance parameter	
gamma	parameter for Berger-Boos correction (restricts range of nuisance parameter	

RRotsst RRotsst

Details

Estimates confidence intervals based on the score statistic that are 'exact' in the sense of accounting for discreteness. The score statistic is used to select tail area tables, and the binomial probability is estimated over the tail area by taking the maximum over the nuisance parameter. Algorithm is a simple step search.

```
The data may also be a matrix. In that case Y would be entered as matrix(c(y1, n1 - y1, y2, n2 - y2), 2, 2, byrow = TRUE).
```

Value

An object of class rr1 with the following fields:

- estimate: vector with point and interval estimate
- estimator: either "PF" or "RR"
- y: data.frame with "y1", "n1", "y2", "n2" values.
- rnd: how many digits to round the display
- alpha: complement of confidence level

Author(s)

PF-package

References

Koopman PAR, 1984. Confidence intervals for the ratio of two binomial proportions. *Biometrics* 40:513-517.

Agresti A, Min Y, 2001. On small-sample confidence intervals for parameters in discrete distribution. *Biometrics* 57: 963-971.

Berger RL, Boos DD, 1994. P values maximized over a confidence set for the nuisance parameter. *Journal of the American Statistical Association* 89:214-220.

See Also

RRtosst, rr1.

```
# All examples represent the same observation, with data entry by multiple
# options.

y_vector <- c(4, 24, 12, 28)
RRotsst(y_vector, rnd = 3)

# PF
# 95% interval estimates

# PF LL UL
# 0.6111 0.0148 0.8519

y_matrix <- matrix(c(4, 20, 12, 16), 2, 2, byrow = TRUE)
RRotsst(y_matrix, rnd = 3)</pre>
```

RRsc 25

```
# PF
# 95% interval estimates
         LL
# 0.6111 0.0148 0.8519
require(dplyr)
data1 <- data.frame(group = rep(c("treated", "control"), each = 2),</pre>
 y = c(1, 3, 7, 5),
 n = c(12, 12, 14, 14),
 cage = rep(paste("cage", 1:2), 2))
data2 <- data1 |>
  group_by(group) |>
  summarize(sum_y = sum(y),
   sum_n = sum(n)
RRotsst(data = data2, formula = cbind(sum_y, sum_n) ~ group,
  compare = c("treated", "control"))
# 95% interval estimates
# PF
        LL
# 0.6111 0.0148 0.8519
```

RRsc

RR score based asymptotic CI.

Description

Estimates confidence intervals for the risk ratio or prevented fraction based on the score statistic.

Usage

```
RRsc(
  y = NULL,
  data = NULL,
  formula = NULL,
  compare = c("vac", "con"),
  alpha = 0.05,
  pf = TRUE,
  trace.it = FALSE,
  iter.max = 18,
  converge = 1e-06,
  rnd = 3
)
```

Arguments

Data vector c(y1, n1, y2, n2) where y are the positives, n are the total, and group 1 is compared to group 2 (control or reference group).

data data.frame containing variables of formula.

26 RRsc

formula	Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the group size, x is a factor with two levels of treatment.
compare	Text vector stating the factor levels: compare[1] is the vaccinate group to which compare[2] (control or reference) is compared.
alpha	Complement of the confidence level.
pf	Estimate <i>RR</i> or its complement <i>PF</i> ?
trace.it	Verbose tracking of the iterations?
iter.max	Maximum number of iterations
converge	Convergence criterion
rnd	Number of digits for rounding. Affects display only, not estimates.

Details

Estimates are returned for three estimators based on the score statistic. The score method was introduced by Koopman (1984). Gart and Nam's modification (1988) includes a skewness correction. The method of Miettinen and Nurminen (1985) is a version made slightly more conservative than Koopman's by including a factor of (N-1)/N. The starting estimate for the DUD algorithm is obtained by the modified Katz method (log method with 0.5 added to each cell). Both forms of the Katz estimate may be retrieved from the returned object using RRsc()\$estimate.

The data may also be a matrix. In that case Y would be entered as matrix(c(y1, n1-y1, y2, n2-y2), 2, 2, byrow = TRUE).

Value

A rrsc object with the following fields.

- estimate: matrix of point and interval estimates see details
- estimator: either "PF" or "RR"
- y: data.frame with "y1", "n1", "y2", "n2" values.
- rnd: how many digits to round the display
- alpha: complement of confidence level

Author(s)

PF-package

References

Gart JJ, Nam J, 1988. Approximate interval estimation of the ratio of binomial parameters: a review and corrections for skewness. *Biometrics* 44:323-338.

Koopman PAR, 1984. Confidence intervals for the ratio of two binomial proportions. *Biometrics* 40:513-517.

Miettinen O, Nurminen M, 1985. Comparative analysis of two rates. *Statistics in Medicine* 4:213-226.

Ralston ML, Jennrich RI, 1978. DUD, A Derivative-Free Algorithm for Nonlinear Least Squares. *Technometrics* 20:7-14.

See Also

rrsc

rrsc-class 27

```
# All examples represent the same observation, with data entry by using
# multiple notation options.
y_{\text{vector}} < -c(4, 24, 12, 28)
RRsc(y_vector)
# PF
# 95% interval estimates
# PF
         LL
               UL
# MN method
              0.611 0.0251 0.857
# score method 0.611 0.0328 0.855
# skew corr 0.611 0.0380 0.876
y_{matrix} \leftarrow matrix(c(4, 20, 12, 16), 2, 2, byrow = TRUE)
# [, 1] [, 2]
# [1, ] 4 20
# [2, ] 12 16
RRsc(y_matrix)
# PF
# 95% interval estimates
# PF
         LL
               UL
# MN method 0.611 0.0251 0.857
# score method 0.611 0.0328 0.855
# skew corr 0.611 0.0380 0.876
require(dplyr)
data1 <- data.frame(group = rep(c("treated", "control"), each = 2),</pre>
 y = c(1, 3, 7, 5),
 n = c(12, 12, 14, 14),
 cage = rep(paste("cage", 1:2), 2))
data2 <- data1 |>
  group_by(group) |>
  summarize(sum_y = sum(y),
   sum_n = sum(n)
RRsc(data = data2, formula = cbind(sum_y, sum_n) ~ group,
 compare = c("treated", "control"))
# PF
# 95% interval estimates
# PF
         LL
               UL
              0.611 0.0251 0.857
# MN method
# score method 0.611 0.0328 0.855
# skew corr 0.611 0.0380 0.876
```

28 rrsi-class

Description

data class rrsc

Fields

• estimate: vector with point and interval estimate

• rnd: how many digits to round display

• alpha: complement of c.i.

• estimator: either "PF" or "RR"

• Y: data.frame with restructured input

Author(s)

PF-package

See Also

rrsc

rrsi-class

Data class rrsi

Description

data class rrsi

Fields

- Y: data.frame with restructured input
- k: likelihood ratio criterion
- rnd: digits to round display
- alpha: complement of c.i.
- estimate: vector with point and interval estimate
- estimator: either "PF" or "IDR"

Author(s)

PF-package

See Also

IDRlsi, RRlsi

RRstr 29

RRstr

Gart-Nam method, CI for common RR over strata or clusters.

Description

Estimates confidence intervals for the risk ratio or prevented fraction from clustered or stratified data.

Usage

```
RRstr(
  formula = NULL,
  data = NULL,
  compare = c("vac", "con"),
  Y,
  alpha = 0.05,
  pf = TRUE,
  trace.it = FALSE,
  iter.max = 24,
  converge = 1e-06,
  rnd = 3,
  multiplier = 0.7,
  divider = 1.1
)
```

Arguments

formula	Formula of the form $cbind(y, n) \sim x + cluster(w)$, where y is the number positive, n is the group size, x is a factor with two levels of treatment, and w is a factor indicating the clusters.
data	data.frame containing variables of formula
compare	Text vector stating the factor levels: compare[1] is the control or reference group to which compare[2] is compared
Υ	Matrix of data. Each row is a stratum or cluster. The columns are y2, n2, y1, n1. If data entered by formula and dataframe, Y is generated automatically.
alpha	Size of the homogeneity test and complement of the confidence level.
pf	Estimate RR or its complement PF?
trace.it	verbose tracking of the iterations?
iter.max	Maximum number of iterations
converge	Convergence criterion
rnd	Number of digits for rounding. Affects display only, not estimates.
multiplier	internal control parameter for algorithm
divider	internal control parameter for algorithm

Details

Uses the DUD algorithm to estimate confidence intervals by the method of Gart.

30 RRstr

Value

A rrstr object with the following fields:

- estimate: matrix of point and interval estimates starting value, MLE, and skewness corrected
- hom: list of homogeneity statistic, p-value, and degrees of freedom, or error message if appropriate.
- estimator: either "PF" or "RR"
- y: data.frame of restructured input
- compare: groups compared
- rnd: how many digits to round the display
- alpha: size of test; complement of confidence level

Note

Vignette Examples for Stratified Designs forthcoming with more examples.

```
Call to this function may be one of two formats: (1) specify data and formula or (2) as a matrix Y RRstr(formula, data, compare = c("b", "a"), pf = TRUE, alpha = 0.05, trace.it = FALSE, iter.max = 24, converge = 1e-6, rnd = 3, multiplier = 0.7, divider = 1.1)

RRstr(Y, compare = c("b", "a"), pf = TRUE, alpha = 0.05, trace.it = FALSE, iter.max = 24, converge = 1e-6, rnd = 3, multiplier = 0.7, divider = 1.1)
```

Author(s)

PF-package

References

Gart JJ, 1985. Approximate tests and interval estimation of the common relative risk in the combination of $2x^2$ tables. *Biometrika* 72:673-677.

Gart JJ, Nam J, 1988. Approximate interval estimation of the ratio of binomial parameters: a review and corrections for skewness. *Biometrics* 44:323-338.

Ralston ML, Jennrich RI, 1978. DUD, A Derivative-Free Algorithm for Nonlinear Least Squares. *Technometrics* 20:7-14.

See Also

rrstr

rrstr-class 31

```
# df 3
# p 0.812

# RR estimates

# RR LL UL
# starting 2.66 1.37 5.18
# mle 2.65 1.39 5.03
# skew corr 2.65 1.31 5.08

## or as matrix
RRstr(Y = table6, pf = FALSE)

tst <- data.frame(y = c(0, 2, 0, 4, 0, 3, 0, 7), n = rep(10, 8), tx = rep(c("a", "b"), 4), clus = rep(paste("Row", 1:4, sep = ""), each = 2))</pre>
```

rrstr-class

Data class rrstr

Description

data class rrstr

Fields

- estimate: vector with point and interval estimate
- rnd: how many digits to round display
- alpha: complement of c.i.
- estimator: either "PF" or "RR"
- hom: list of homogeneity statistic, p-value, and degrees of freedom. If Phi == 0 | Phi == 1, homogeneity test is not possible and error message displays
- Y: data.frame of restructured input
- compare: groups compared

Author(s)

PF-package

See Also

rrstr

RRtosst

RRtosst

RR exact CI, TOSST method.

Description

Estimates confidence interval for the risk ratio or prevented fraction; exact method based on the score statistic (inverts two one-sided tests).

Usage

```
RRtosst(
  y = NULL,
  formula = NULL,
  data = NULL,
  compare = c("vac", "con"),
  alpha = 0.05,
  pf = TRUE,
  stepstart = 0.1,
  iter.max = 36,
  converge = 1e-06,
  rnd = 3,
  trace.it = FALSE,
  nuisance.points = 120,
  gamma = 1e-06
)
```

Arguments

У	Data vector $c(y1, n1, y2, n2)$ where y are the positives, n are the total, and group 1 is compared to group 2 (control or reference group).	
formula	Formula of the form $cbind(y, n) \sim x$, where y is the number positive, n is the group size, x is a factor with two levels of treatment.	
data	data.frame containing variables of formula.	
compare	Text vector stating the factor levels: $compare[1]$ is the vaccinate group to which $compare[2]$ (control or reference) is compared.	
alpha	Complement of the confidence level.	
pf	Estimate <i>RR</i> or its complement <i>PF</i> ?	
stepstart	starting interval for step search	
iter.max	Maximum number of iterations	
converge	Convergence criterion	
rnd	Number of digits for rounding. Affects display only, not estimates.	
trace.it	Verbose tracking of the iterations?	
nuisance.points		
	number of points over which to evaluate nuisance parameter	
gamma	parameter for Berger-Boos correction (restricts range of nuisance parameter evaluation)	

RRtosst 33

Details

Estimates confidence intervals based on the score statistic that are 'exact' in the sense of accounting for discreteness. Inverts two one-sided score tests. The score statistic is used to select tail area tables, and the binomial probability is estimated over the tail area by taking the maximum over the nuisance parameter. Algorithm is a simple step search.

The data may also be a matrix. In that case Y would be entered as

```
matrix(c(y1, n1-y1, y2, n2-y2), 2, 2, byrow = TRUE).
```

Value

A rr1 object with the following fields.

- estimate: vector with point and interval estimate
- estimator: either "PF" or "RR"
- y: data.frame with "y1", "n1", "y2", "n2" values.
- rnd: how many digits to round the display
- alpha: complement of confidence level

Author(s)

PF-package

References

Koopman PAR, 1984. Confidence intervals for the ratio of two binomial proportions. *Biometrics* 40:513-517.

Agresti A, Min Y, 2001. On small-sample confidence intervals for parameters in discrete distribution. *Biometrics* 57: 963-971.

Berger RL, Boos DD, 1994. P values maximized over a confidence set for the nuisance parameter. *Journal of the American Statistical Association* 89:214-220.

See Also

RRotsst, rr1

```
# Both examples represent the same observation, with data entry by vector
# and matrix notation.

y_vector <- c(4, 24, 12, 28)
RRtosst(y_vector)

# PF
# 95% interval estimates

# PF LL UL
# 0.611 0.012 0.902

y_matrix <- matrix(c(4, 20, 12, 16), 2, 2, byrow = TRUE)
# [, 1] [, 2]
# [1, ] 4 20</pre>
```

34 rsb

```
# [2, ] 12 16
RRtosst(y_matrix)
# PF
# 95% interval estimates
    PF
        LL
                UL
# 0.611 0.012 0.902
require(dplyr)
data1 <- data.frame(group = rep(c("treated", "control"), each = 2),</pre>
 y = c(1, 3, 7, 5),
 n = c(12, 12, 14, 14),
 cage = rep(paste("cage", 1:2), 2))
data2 <- data1 |>
 group_by(group) |>
  summarize(sum_y = sum(y),
   sum_n = sum(n)
RRtosst(data = data2, formula = cbind(sum_y, sum_n) ~ group,
 compare = c("treated", "control"))
# PF
# 95% interval estimates
    PF
         LL
# 0.611 0.012 0.902
```

rsb

Rao-Scott weights.

Description

Rao-Scott weights.

Usage

```
rsb(y = NULL, n = NULL, formula = NULL, data = NULL, id = NULL)
```

Arguments

У	vector of number positive.
n	vector of total number.
formula	Formula of the form $cbind(y, n) \sim id$, where y is the number positive, n is the total number, id is a factor for estimating the weights by subset.
data	data.frame containing variables of formula.
id	vector of factor for estimating the weights by subset.

Details

Estimates the cluster design effect d_i as the variance inflation due to clustering by the method of Rao and Scott. rsb estimates the d_i for use by rsbWt or other functions.

rsbWt 35

Value

A list with the following elements.

- w: vector of weights
- d: vector of d_i estimates

Author(s)

```
PF-package
```

References

Rao JNK, Scott AJ, 1992. A simple method for the analysis of clustered binary data. *Biometrics* 48:577-585.

See Also

```
rsbWt.
```

Examples

```
# Weil's rat data (Table 1 of Rao and Scott)
rsb(rat$y, rat$n, id = rat$group)$d
# control treated
# 1.232495 3.952861
rsb(data = rat, formula = cbind(y, n) ~ group)$d
# control treated
# 1.232495 3.952861
```

rsbWt

Rao-Scott weighting.

Description

Rao-Scott weighting of clustered binomial observations.

Usage

```
rsbWt(fit = NULL, subset.factor = NULL, fit.only = TRUE)
```

Arguments

```
fit A glm object.
```

subset.factor Factor for estimating the weights by subset.

fit.only Return only the new fit? If FALSE, also returns the weights and phi estimates.

Details

Estimates the cluster design effect d_i as the variance inflation due to clustering by the method of Rao and Scott. Observations are then weighted by the inverse of the d_i .

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Value

A list with the following elements.

- fit: the new model fit, updated by the estimated weights
- weights: vector of weights
- d: vector of d_i estimates

Author(s)

PF-package

References

Rao JNK, Scott AJ, 1992. A simple method for the analysis of clustered binary data. *Biometrics* 48:577-585.

See Also

RRor, rsb.

Examples

```
birdm.fit <- glm(cbind(y, n - y) ~ tx-1, binomial, birdm)
RRor(rsbWt(birdm.fit))
#
# 95% t intervals on 4 df
#
# PF
# PF LL UL
# 0.479 -1.061 0.868
#
# mu.hat LL UL
# txcon 0.768 0.968 0.2659
# txvac 0.400 0.848 0.0737
#</pre>
```

Set1

Set1 dataset

Description

Set1 dataset

Format

a data.frame with 6 observation of the following 4 variables, no NAs

- y: number positive
- n: total number in group tx x clus
- tx: treatment "vac" or "con"
- clus: cluster ID

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References

We need some references

set1

set1 dataset

Description

set1 dataset

Format

a 3 x 4 matrix of data in Set1

References

we need some references!

Table6

Table6 dataset

Description

Table6 dataset

Format

a data.frame with 8 observations of the following 4 variables, no NAs

- y: number positive
- n: total number in group tx x clus
- tx: treatment "a" or "b"
- clus: cluster ID

References

Table 1 from Gart (1985)

table6

table6 dataset

Description

table6 dataset

Format

matrix for of data in Table6

38 tauWt

tauWt

Binomial dispersion: intra-cluster correlation parameter.

Description

MME estimates of binomial dispersion parameter tau (intra-cluster correlation).

Usage

```
tauWt(
  fit,
  subset.factor = NULL,
  fit.only = TRUE,
  iter.max = 12,
  converge = 1e-06,
  trace.it = FALSE
)
```

Arguments

fit A glm object.

subset.factor Factor for estimating tau by subset.

fit.only Return only the final fit? If FALSE, also returns the weights and tau estimates.

iter.max Maximum number of iterations.

converge Convergence criterion: difference between model degrees of freedom and Pearson's chi-square. Default 1e-6.

trace.it Display print statements indicating progress

Details

Estimates binomial dispersion parameter τ by the method of moments. Iteratively refits the model by the Williams procedure, weighting the observations by $1/\phi_{ij}$, where $\phi_{ij}=1+\tau_j(n_{ij}-1)$, j indexes the subsets, and i indexes the observations.

Value

A list with the following elements. fit: the new model fit, updated by the estimated weights weights: vector of weights phi: vector of phi estimates

Author(s)

PF-package

References

Williams DA, 1982. Extra-binomial variation in logistic linear models. *Applied Statistics* 31:144-148.

Wedderburn RWM, 1974. Quasi-likelihood functions, generalized linear models, and the Gauss-Newton method. *Biometrika* 61:439-447.

tauWt 39

See Also

```
phiWt, RRor.
```

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