${\bf Access\ Jupyter\ notebook\ file\ in\ here,\ best\ run\ using\ jupyter\ notebook\ or\ using\ VSCode}$

$$1. \quad \begin{bmatrix} 0 \\ 1 \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix} \\ \begin{bmatrix} 0 & 1 \\ 0 & 1 \\ 1 & 1 \\ 0 & 1 \end{bmatrix} \\ \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$$

$$Phi = np.array([0],[0],[1],[0])$$

$$2. |\Phi\rangle = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} |\Psi\rangle$$
$$|\Phi\rangle = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$$
$$= \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

$$Phi = np.array([0],[0],[0],[1])$$

$$3. |\Psi\rangle = \left(\begin{pmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix} \right) \otimes \begin{bmatrix} 0 \\ 1 \end{bmatrix} \right) \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$= \begin{pmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} \end{bmatrix} \otimes \begin{bmatrix} 0 \\ 1 \end{bmatrix} \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$= \begin{pmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \otimes \begin{bmatrix} 0 \\ 1 \end{bmatrix} \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$= \begin{pmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \otimes \begin{bmatrix} 0 \\ 1 \end{bmatrix} \\ 0 \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \\ 0 \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\begin{array}{l} {\rm Phi} \, = \, {\rm np.\,array} \, (\,[\,0\,]\,\,,[\,0\,]\,\,,[\,1\,]\,\,,[\,0\,]\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,[\,0\,]\,\,,$$

$$\begin{aligned} 4. \ U &= \left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \otimes \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \right) \otimes \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \\ & \text{Phi} = \underset{}{\text{np.array}} \left(\begin{bmatrix} [0] &, [0] &, [0] &, [1] &, [0] &, [0] \\ [0] &, [0] &, [0] &, [0] &, [0] &, [0] &, [0] \end{bmatrix}, \begin{bmatrix} [0] &, [0] &, [0] \end{bmatrix} \right) , \end{aligned}$$

5. NP-Hard

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