## 1

## NCERT Analog Assignment

## EE23BTECH11007 - Aneesh Kadiyala\*

**Question 11.14.17:** A simple pendulum of length  $\ell$  and having a bob of mass M is suspended in a car. The car is moving in a circular track of radius R with a uniform speed  $\nu$ . If the pendulum makes small oscillations in a radial direction about its equilibrium position, what will be its time period? **Solution:** 

TABLE 0 Parameters

Parameter	Description
v	Speed
R	Radius of circular track
M	Mass of bob
g	Acceleration due to gravity
$a_c$	Centrifugal acceleration
$g_e$	Effective gravitational acceleration $\sqrt{g^2 + a^2}$

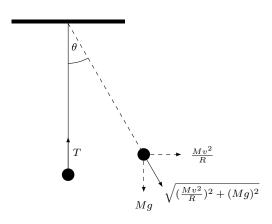


Fig. 0. Free Body Diagram

From the figure, restoring force:

$$F_r = -\left(\sqrt{\left(\frac{Mv^2}{R}\right)^2 + (Mg)^2}\right) \sin\theta(t)$$
 (1)

For small oscillations,  $\theta(t) \ll 1$ .

$$\implies \sin \theta(t) \approx \theta(t)$$
 (2)

$$\implies F_r \approx -\left(\sqrt{\left(\frac{Mv^2}{R}\right)^2 + (Mg)^2}\right)\theta(t) \quad (3)$$

$$\implies a = -\left(\sqrt{\left(\frac{v^2}{R}\right)^2 + g^2}\right)\theta(t) \tag{4}$$

$$l\frac{d^{2}\theta(t)}{dt^{2}} = -\left(\sqrt{\left(\frac{v^{2}}{R}\right)^{2} + g^{2}}\right)\theta(t)$$
 (5)

$$\frac{d^2\theta(t)}{dt^2} = \frac{-1}{\ell} \left( \sqrt{\left(\frac{v^2}{R}\right)^2 + g^2} \right) \theta(t)$$
 (6)

(7)

Taking Laplace transform:

$$s^{2}\theta(s) = \frac{-1}{\ell} \left( \sqrt{\left(\frac{v^{2}}{R}\right)^{2} + g^{2}} \right) \theta(s)$$
 (8)

(9)