

GATE: ST - 32.2023

EE23BTECH11007 - Aneesg Kadiyala*

Question 10.5.2.19: Subba Rao started work in 1995 at an annual salary of Rs. 5000 and received an increment of Rs. 200 each year. In which year did his income reach Rs. 7000?

Solution:

Let Subba Rao's initial salary $a_0 = \text{Rs. } 5000$

Let Subba Rao's increment $d = \text{Rs. } 200$

Subba Rao's salary after n years $= a_n = a_0 + (n-1)d$

$$7000 = 5000 + (n-1)(200)$$

$$2000 = (n-1)(200)$$

$$n = 11$$

\Rightarrow Subba Rao's income reaches Rs. 7000 eleven years after he started working.

Therefore, Subba Rao's income reached Rs. 7000 in the year 2006.

Question 11.9.3.30: The number of bacteria in a certain culture doubles every hour. If there were 30 bacteria present in the culture originally, how many bacteria will be present at the end of 2^{nd} hour 4^{th} hour and n^{th} hour?

Solution:

Let number of bacteria initially be $a_0 = 30$

Let number of bacteria at the end of n^{th} hour be a_n .

Since number of bacteria doubles every hour,

$$a_n = 2a_{n-1}$$

$$a_n = 2(2a_{n-2})$$

...

$$a_n = 2^n a_0 = 2^n(30)$$

$$\Rightarrow a_2 = 2^2(30) = 120 \text{ and } a_4 = 2^4(30) = 480$$

Therefore, number of bacteria at the end of the 2^{nd} hour is 120, 4^{th} hour is 480, and n^{th} hour is $30(2^n)$.