

# Assignment

- Chapter 3: 37 pages
  - My lectures are going much faster than the reading assignments
  - You will need Ch 3 for Assignment 2
- Start Chapter 4
  - Shorter, but probably more confusing

# Clickers

- If any of these are yours, write down your name and the clicker ID on a sheet of paper:
- #01C18B4B
- #0CB07CC0
- #18C2B16B
- #19CB6FBD
- #25D2F700



# Homework

How is the homework going?

- A) I've turned it in
- B) I'm nearly done
- C) I've barely started
- D) I haven't started
- E) None of the above (you should probably tell me what you mean)



# Homework

Was the homework...

- A) Too short
- B) Pretty much OK
- C) Too long
- D) I haven't done enough to know for sure
- E) None of the above



# Class so far

Anonymous

Are the tutorials useful?

- A) Yes, they're the best part of class
- B) Yes, but lectures are more useful
- C) No, but lectures are useful
- D) No, and the lectures aren't very useful either
- E) None of the above

# A little more about data types

- You can “cast” a variable or number to a different type

```
IDL> help,1S,fix(1)
<Expression>      INT      =      1
<Expression>      INT      =      1
IDL> help,1L,long(1)
<Expression>      LONG     =      1
<Expression>      LONG     =      1
IDL> help,1S,fix(1)
<Expression>      INT      =      1
<Expression>      INT      =      1
IDL> help,1B,byte(1)
<Expression>      BYTE     =      1
<Expression>      BYTE     =      1
```

This is a silly name. It exists for historical reasons, or at least I assume it does.

# Rounding #'s

```
IDL> help,round(5.5),floor(5.5),ceil(5.5)
<Expression>      LONG      =      6
<Expression>      LONG      =      5
<Expression>      LONG      =      6
```

# Details of size

- Returns: [# of dimensions, size of each dimension, type code, number of elements]

```
IDL> print,size(1)
```

0

2

1

0 dimensions: scalar (no size of dimension)	Type Code 2: integer	Number of elements: 1
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# Details of size

- Returns: [# of dimensions, size of each dimension, type code, number of elements]

```
IDL> print,size([1])
```

1

1

2

1

1 dimension

Size of dimension 1: 1    Type Code 2: integer    Number of elements: 1



# Size

What will `size([1,2,3,4])` return?

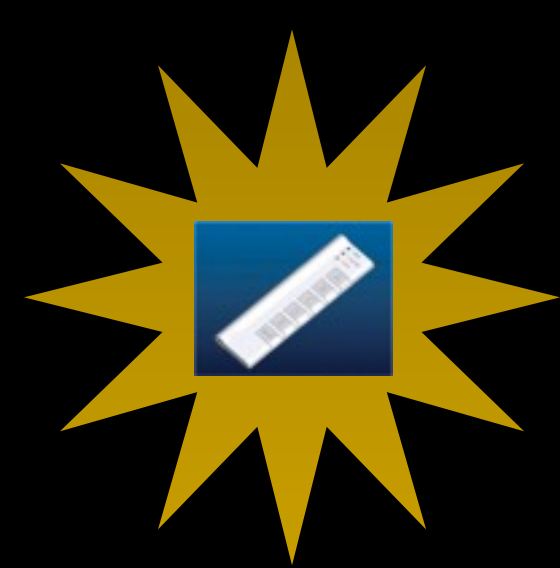
A) `[0, 2, 1]`

B) `[1, 4, 2, 1]`

C) `[1, 4, 2, 4]`

D) `[4, 4, 2, 4]`

E) None of the above / I don't know



# Size

What will `size([1.,2.,3.])` return?

A) `[0, 2, 3]`

B) `[1, 3, 2, 1]`

C) `[1, 3, 2, 3]`

D) `[3, 3, 2, 3]`

E) None of the above / I don't know

# shifting

```
IDL> print,indgen(5)
```

0	1	2	3	4
---	---	---	---	---

```
IDL> print,shift(indgen(5),2)
```

3	4	0	1	2
---	---	---	---	---

```
IDL> print,shift(indgen(5),3)
```

2	3	4	0	1
---	---	---	---	---

# Clipping

- If you want, e.g., all positive numbers in an array, do “`arr > 0`” (sets negative numbers = 0)

```
IDL> x = randomn(seed,5)
```

```
IDL> print,x
```

-2.09936	-0.983745	0.437967	-0.211478	0.360088
----------	-----------	----------	-----------	----------

```
IDL> print,x>0
```

0.00000	0.00000	0.437967	0.00000	0.360088
---------	---------	----------	---------	----------

# Array Scaling

- What do you do if you want an array going from -2 to 2 with 10 elements?
  - first, `findgen(10)` gets you 10 elements from 0-9
  - second, divide by 9 to get your array going from 0 to 1
  - third, multiply by the range `end-start = 2 - (-2) = 4`
  - finally, subtract 2

# Array Scaling

- What do you do if you want an array going from -2 to 2 with 10 elements?

```
IDL> print,findgen(10)/9*4-2
```

-2.00000	-1.55556	-1.11111	-0.666667	-0.222222
0.222222	0.666667	1.11111	1.55556	2.00000

```
IDL> print,-2 + (4./9.) * findgen(10)
```

-2.00000	-1.55556	-1.11111	-0.666667	-0.222222
0.222222	0.666667	1.11111	1.55556	2.00000

```
IDL> xmin=-2
```

```
IDL> xmax=2
```

```
IDL> xrange=xmax-xmin
```

```
IDL> npoints=10
```

```
IDL> print,xmin+(float(xrange)/(npoints-1))*findgen(npoints)
```

-2.00000	-1.55556	-1.11111	-0.666667	-0.222222
0.222222	0.666667	1.11111	1.55556	2.00000

# Array Scaling

- What do you do if you want an array going from -2 to 2 with 10 elements?

Probably the best way:

```
IDL> zero_to_one = findgen(npoints)/(npoints-1)
IDL> xmin=-2
IDL> xmax=2
IDL> xrange=xmax-xmin
IDL> print,xmin+xrange*zero_to_one
```

-2.00000	-1.55556	-1.11111	-0.666667	-0.222222
0.222222	0.666667	1.11111	1.55556	2.00000

Don't do this:

```
IDL> print,-2+0.4444444444*findgen(10)
```

-2.00000	-1.55556	-1.11111	-0.666667	-0.222222
0.222222	0.666667	1.11111	1.55556	2.00000



# Array Scaling

- What do you do if you want an array going from -2 to 2 with 10 elements?

python and matlab have the  
convenience function

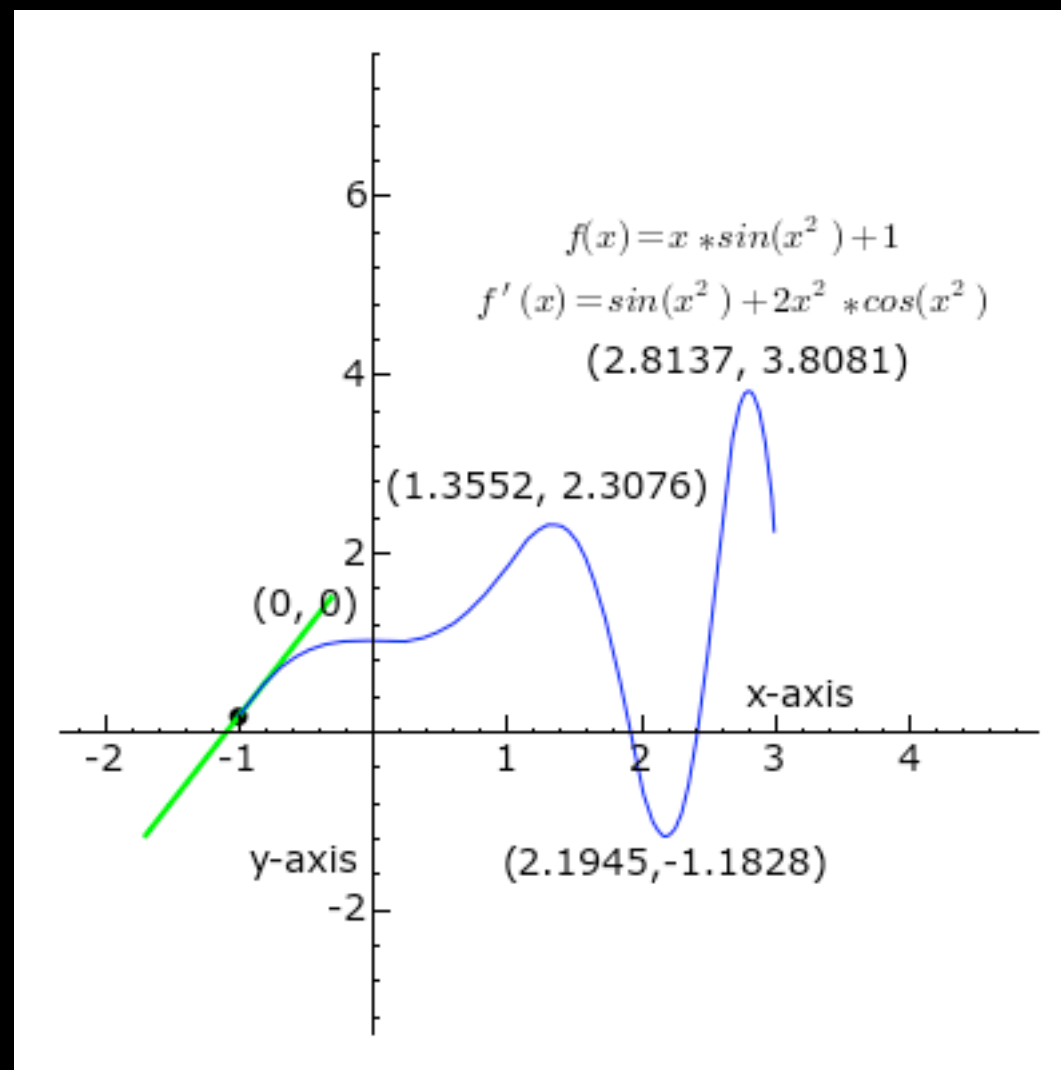
“linspace”:

```
linspace(-2,2,10)
```

We'll make one in IDL soon

# Mathematical Applications

- Finite-Difference Method for derivatives
- Derivatives represent the local slope



# Finite Difference

- For this discussion, we have an  $x$  array and a  $y$  array, where  $y=f(x)$ , but we don't need to know anything else about  $y$ .
- But we'll use  $y=\sin(x)$



# Calc Review

What is  $\frac{d}{dx} \sin(x)$ ?

A)  $\arcsin(x)$

B)  $\cos(x)$

C)  $-\cos(x)$

D)  $\operatorname{cosecant}(x)$

E) None of the above / I don't know

# Setup...

```
IDL> xmin=0
IDL> xmax=!pi/2.
IDL> xrange=xmax-xmin
IDL> npoints=5
IDL> zero_to_one = findgen(npoints)/(npoints-1)
IDL> x = xmin+xrange*zero_to_one
IDL> y = sin(x)
```

# Finite Difference

- We want to know what the derivative,  $dy/dx$ , is
- We can use the `shift` function to determine `dx` and `dy`

```
IDL> dx = x - shift(x,1)
IDL> dy = y - shift(y,1)
IDL> print,dx
-1.57080      0.392699      0.392699      0.392699      0.392699
IDL> print,dy
-1.00000      0.786520      0.130484      0.0633972     0.0195988
```

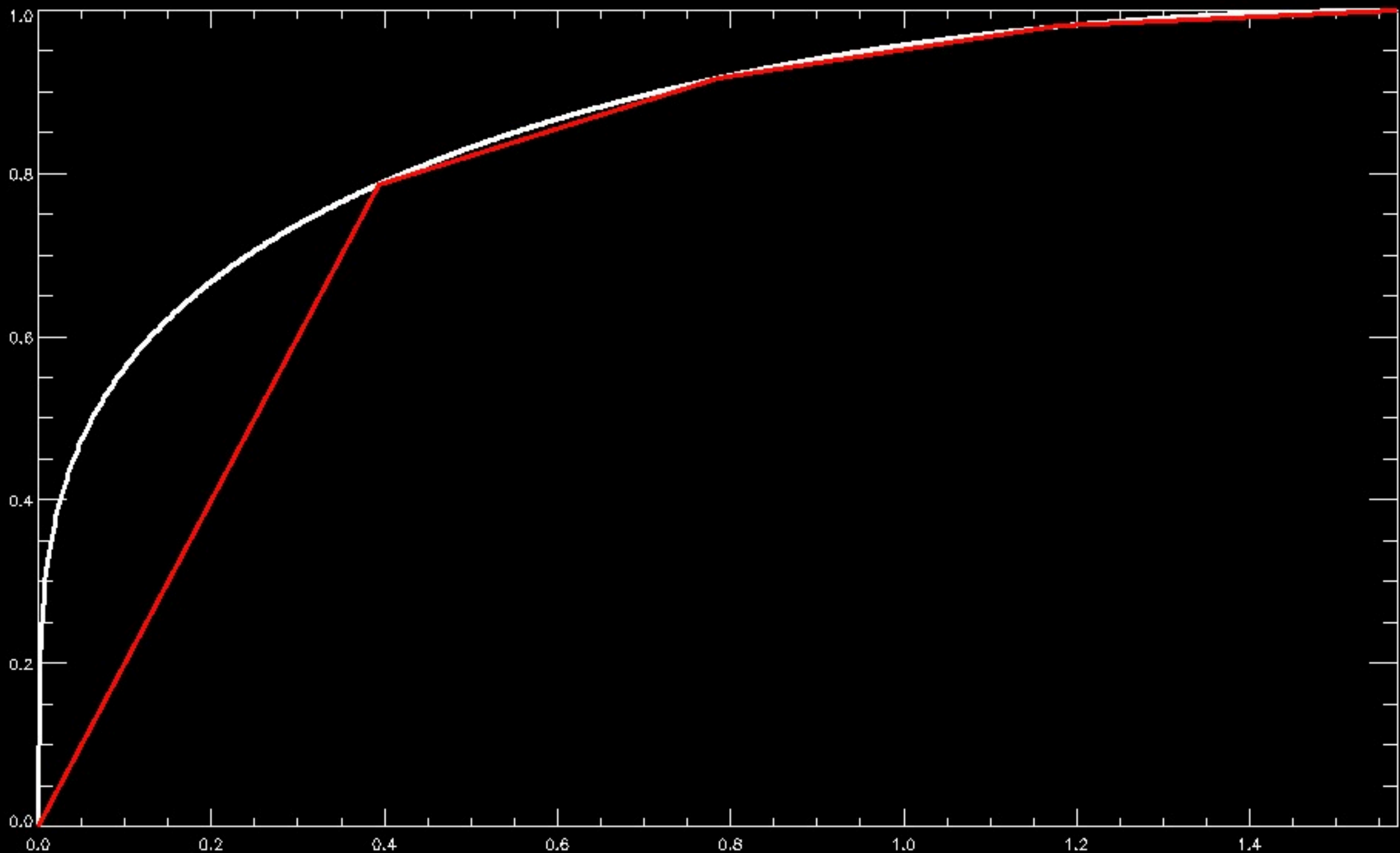
# Finite Difference

- We want to know what the derivative,  $dy/dx$ , is
- We can use the `shift` function to determine  $dx$  and  $dy$

But this is wrong! We can only have 4 delta-x and delta-y measurements for 5 points

```
IDL> dx = x - shift(x,1)
IDL> dy = y - shift(y,1)
IDL> print,dx
-1.57080      0.392699      0.392699      0.392699      0.392699
IDL> print,dy
-1.00000      0.786520      0.130484      0.0633972     0.0195988
```

# Why's it wrong?



```
IDL> xhi = xmin+xrange*findgen(1000)/999
IDL> yhi = sin(xhi)^0.25
IDL> plot,xhi,yhi,/xs,thick=3
IDL> oplot,x,y,color='0000FF'x,thick=3
```



# Finite Difference

- Can also use the “backwards difference” method
- same problem

```
IDL> dx = x - shift(x,-1)
```

```
IDL> dy = y - shift(y,-1)
```

```
IDL> print,dx
```

-0.392699	-0.392699	-0.392699	-0.392699	1.57080
-----------	-----------	-----------	-----------	---------

```
IDL> print,dy
```

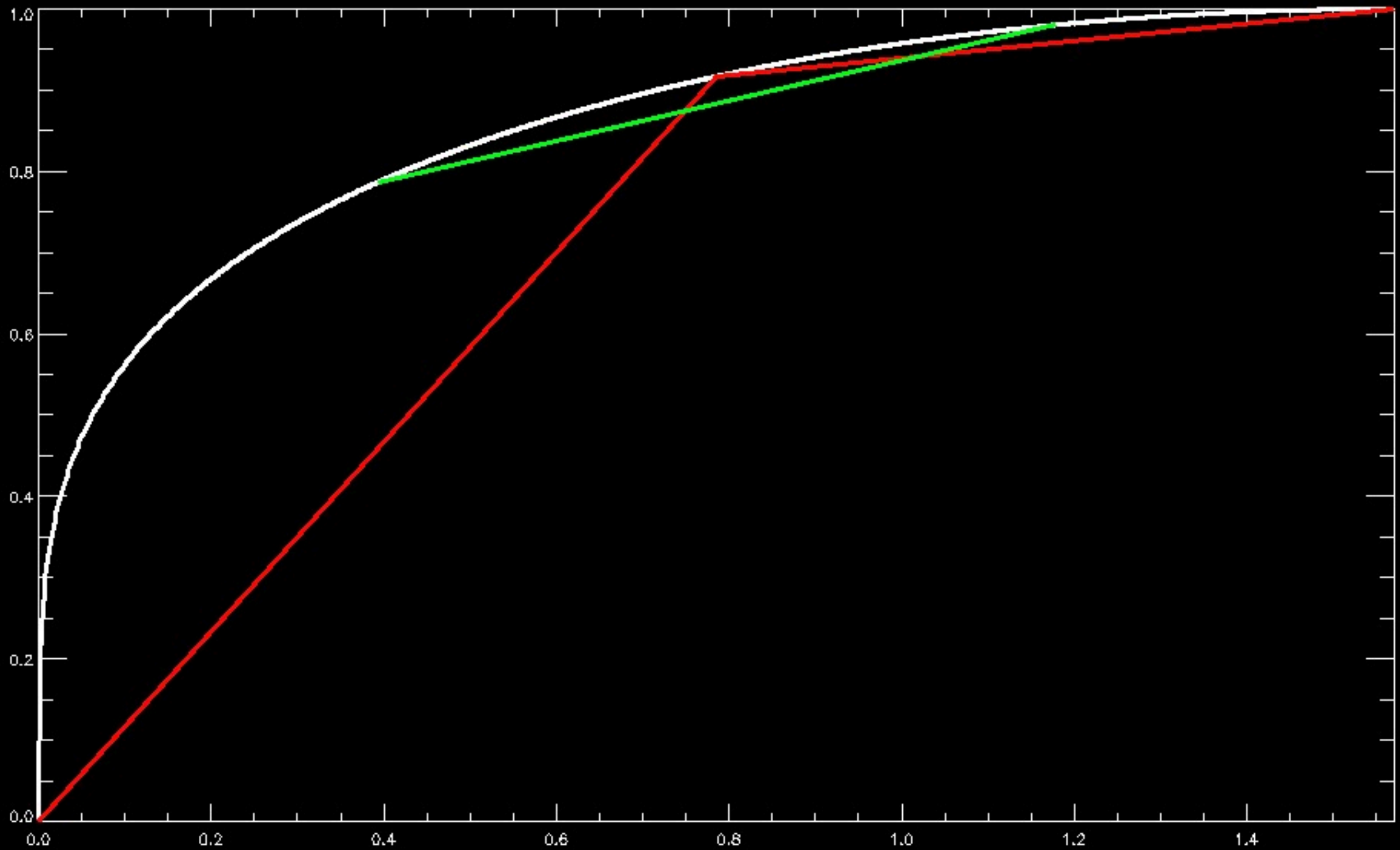
-0.786520	-0.130484	-0.0633972	-0.0195988	1.00000
-----------	-----------	------------	------------	---------

# Finite Difference

- Instead, the central difference is better
- but you lose the end points

```
IDL> d2x = shift(x,1) - shift(x,-1)
IDL> d2y = shift(y,1) - shift(y,-1)
IDL> print,d2x
    1.17810    -0.785398    -0.785398    -0.785398    1.17810
IDL> print,d2y
    0.213480    -0.917004    -0.193881    -0.0829960    0.980401
```

# Central Difference



# Central Difference

- Use the central difference to get all points where it's valid
- Then use forward-difference for the last and backward-difference for the first
  - this actually doesn't do a great job unless you have lots of points

# The code (for reference)

```
IDL> dxf = x - shift(x,1)
IDL> dyf = y - shift(y,1)
IDL>
IDL> dxb = x - shift(x,-1)
IDL> dyb = y - shift(y,-1)
IDL>
IDL> d2x = shift(x,1) - shift(x,-1)
IDL> d2y = shift(y,1) - shift(y,-1)
IDL> print,d2x
      1.17810      -0.785398      -0.785398      -0.785398      1.17810
IDL> print,d2y
      0.213480      -0.917004      -0.193881      -0.0829960      0.980401
IDL>
IDL> dx = d2x
IDL> dx[0] = dxb[0]
IDL> dx[-1] = dxf[-1]
IDL> dy = d2y
IDL> dy[0] = dyb[0]
IDL> dy[-1] = dyf[-1]
IDL> print,dy/dx
      2.00286      1.16757      0.246857      0.105674      0.0499079
```

# Second Derivative

- A good approximation for the second derivative is:

$$(d^2y/d^2x)_i = (y[i-1] - 2*y[i] + y[i+1]) / dx^2$$

$$d2x/d2y = (shift(y,1) - 2*y + shift(y,-1)) / dx^2$$

The text has some more detail



# Derivatives

What is the derivative of  $x^2$  evaluated at  $x=3$ ?

A) 6

B) 9

C) 2

D) 0

E) None of the above / I don't know



# Derivatives

What is the *second* derivative of  $x^2$  evaluated at  $x=3$ ?

A) 6

B) 9

C) 2

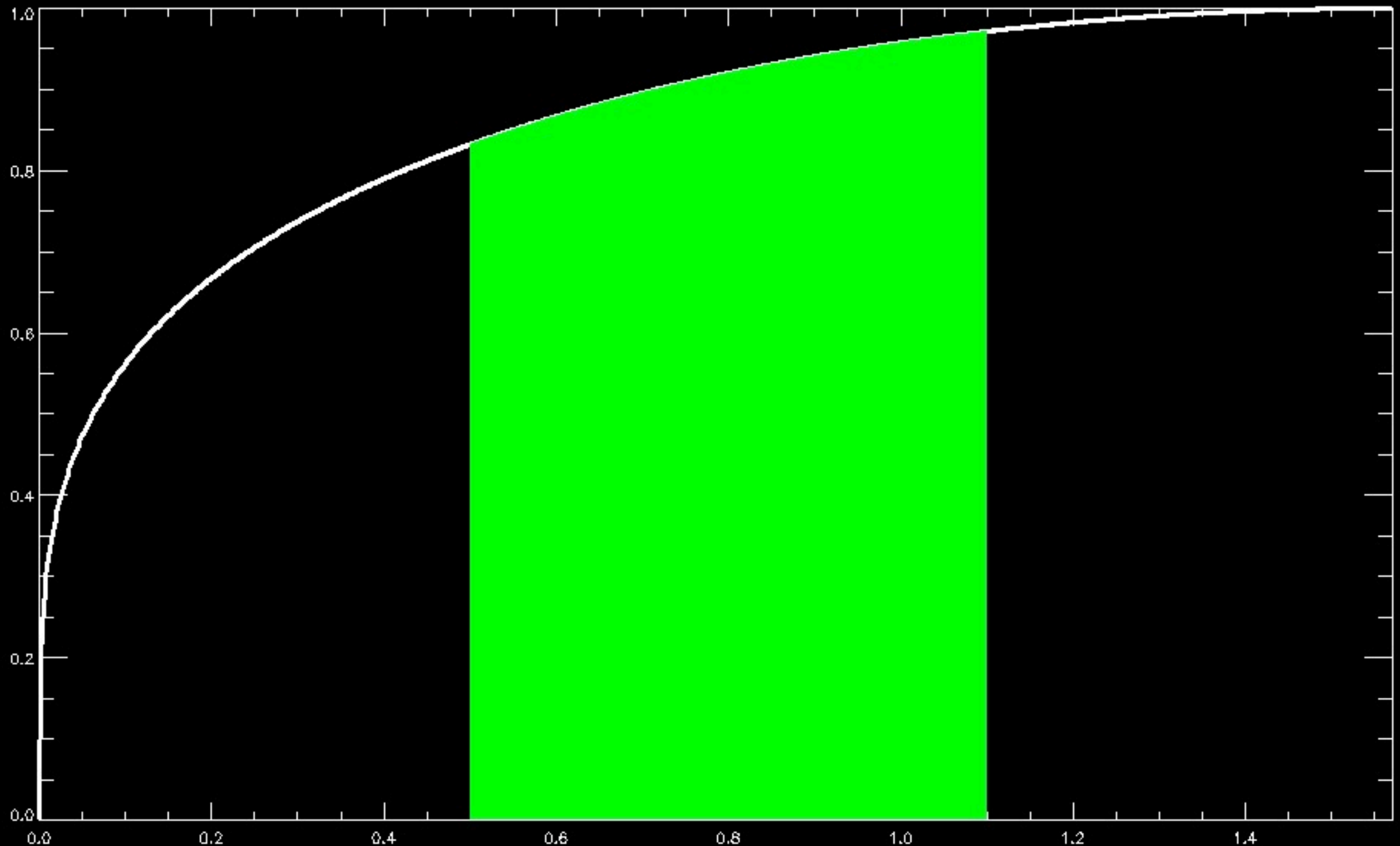
D) 0

E) None of the above / I don't know



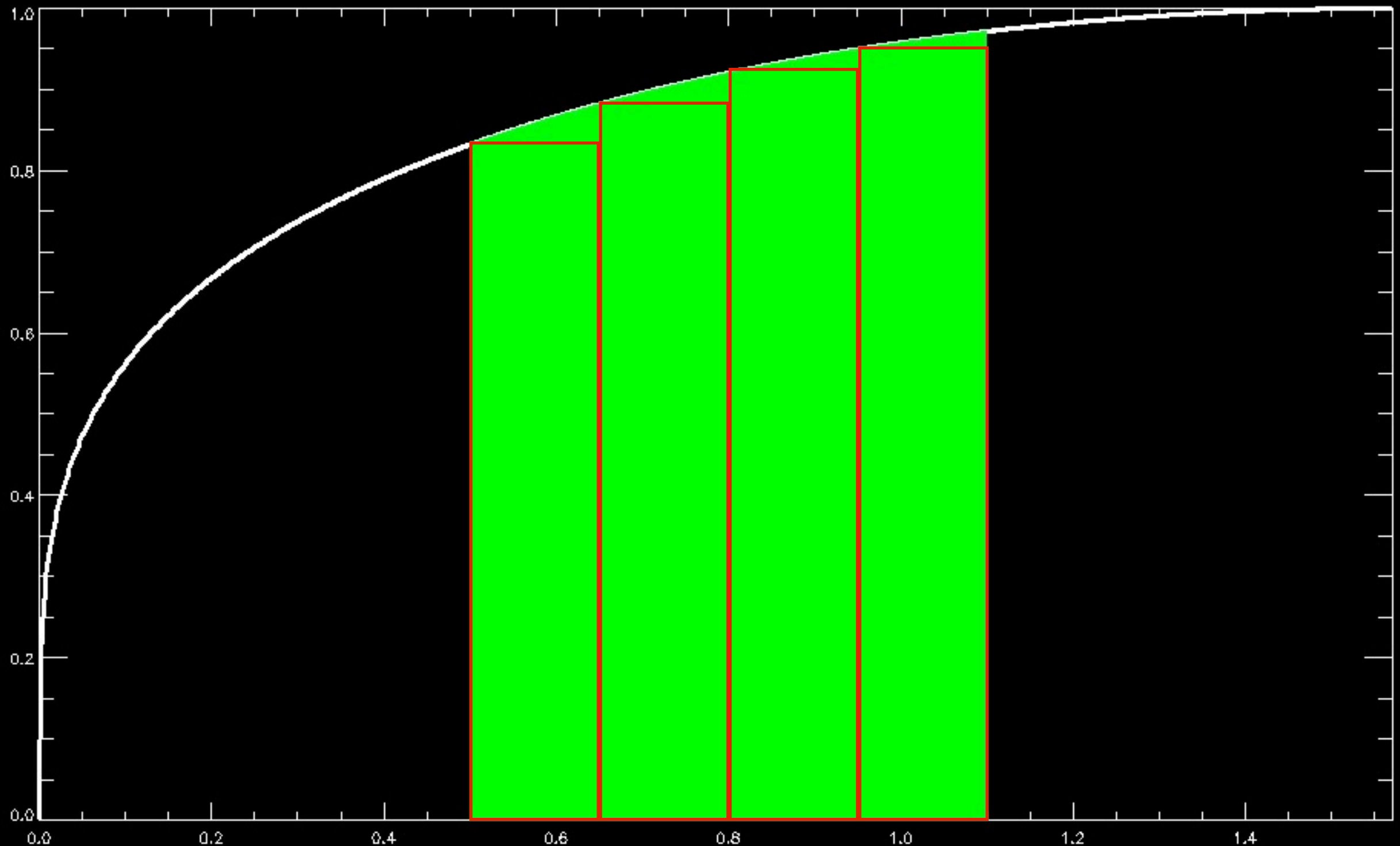
# Integration

- Area under a curve



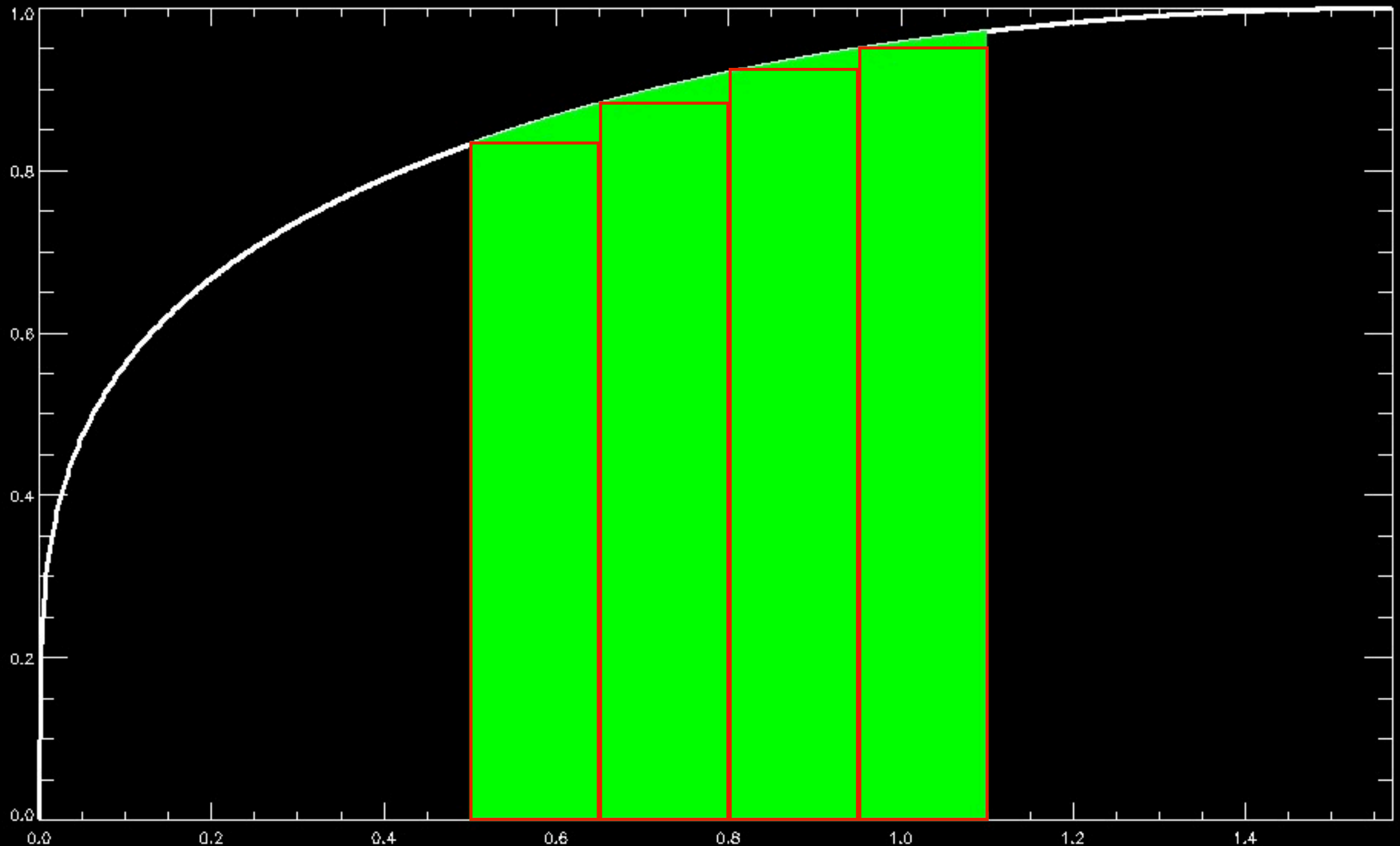
# Integration

- Can approximate with rectangles



# Integration

- Each rectangle has area  $dx * y$



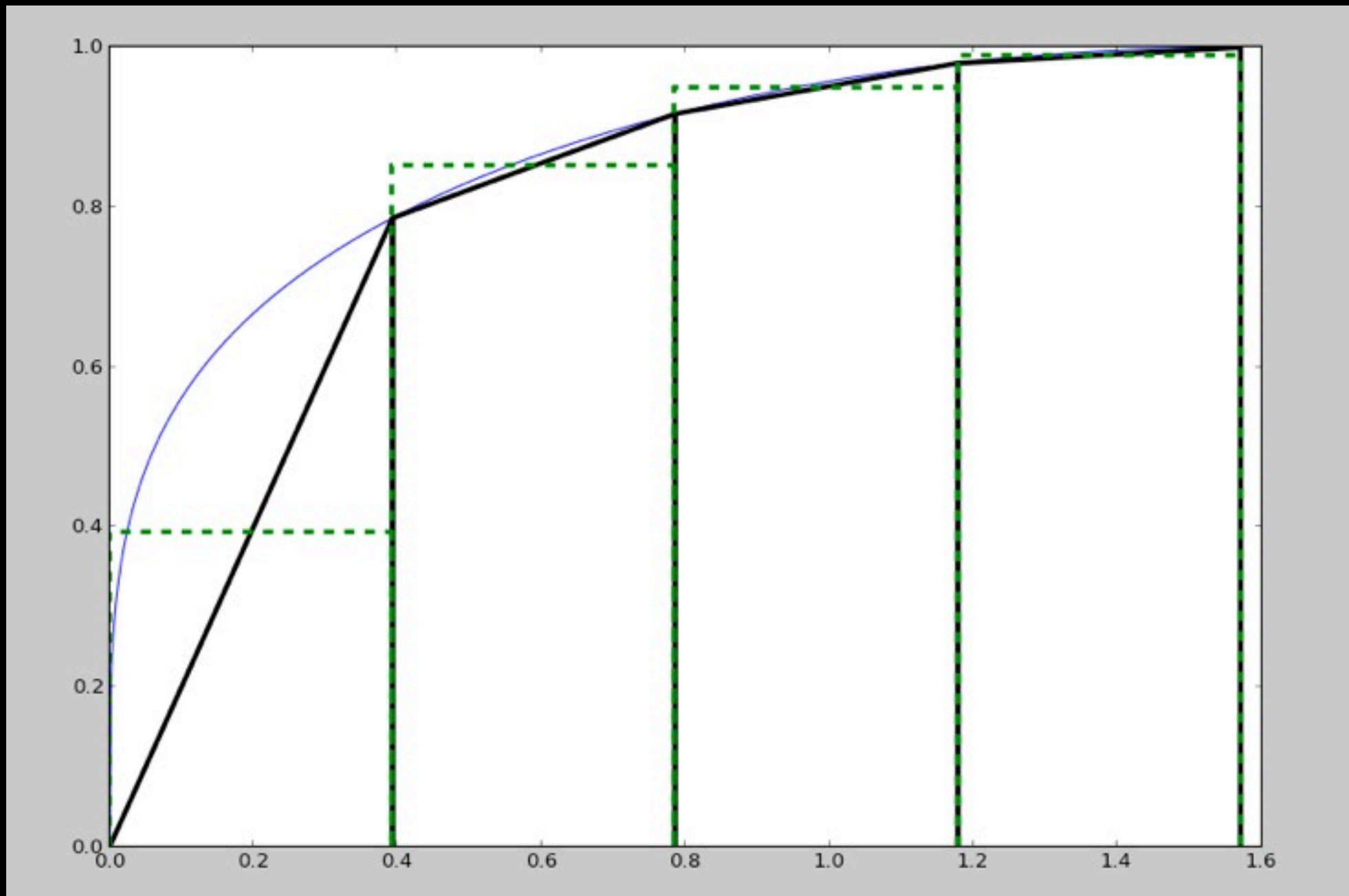
# IDL integration

```
IDL> integral_y = total( y * dx )
```

- but this isn't very accurate for a small number of points

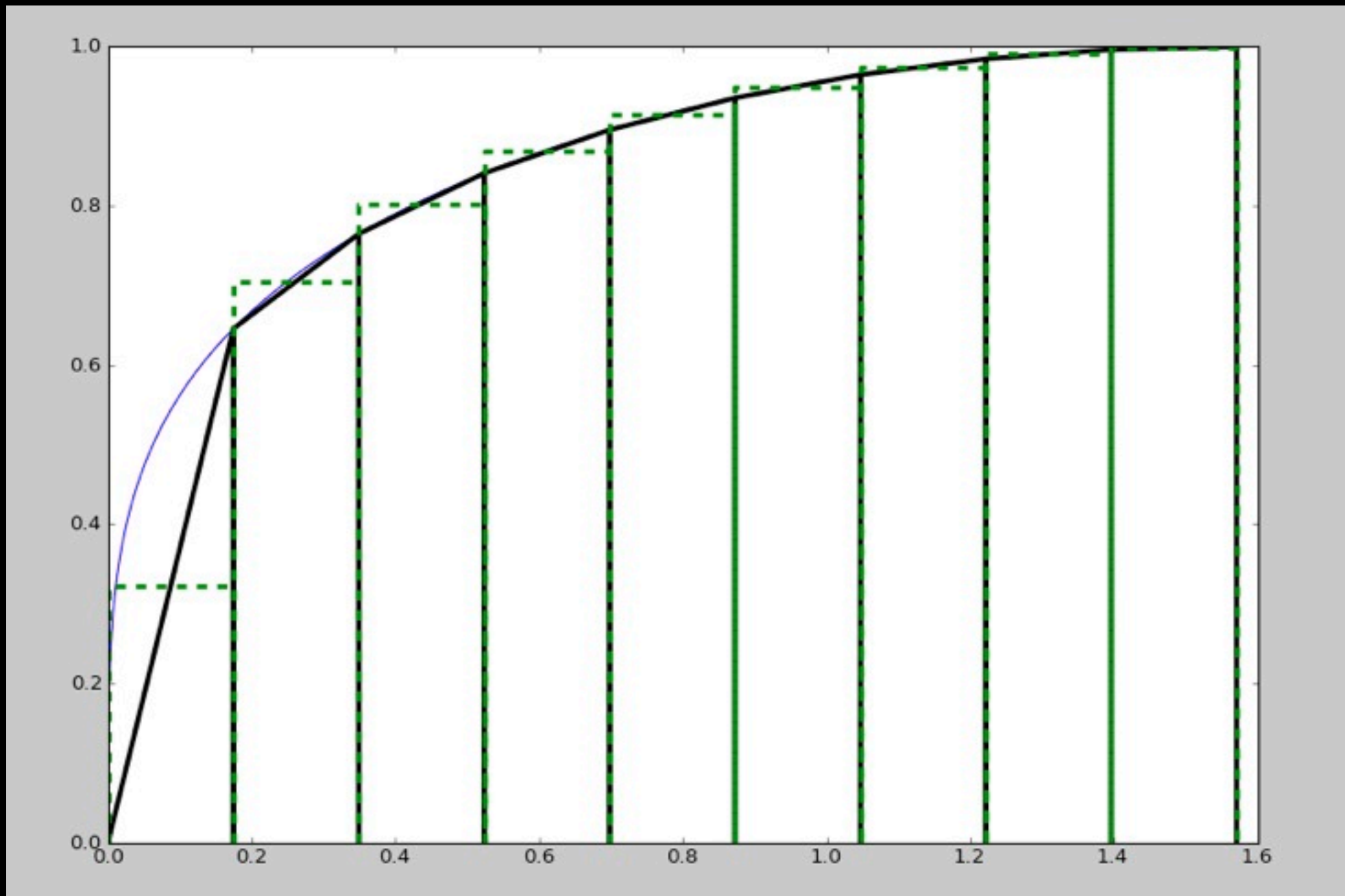
# Integration: Trapezoid Rule

- Mathematical trick to drastically improve accuracy



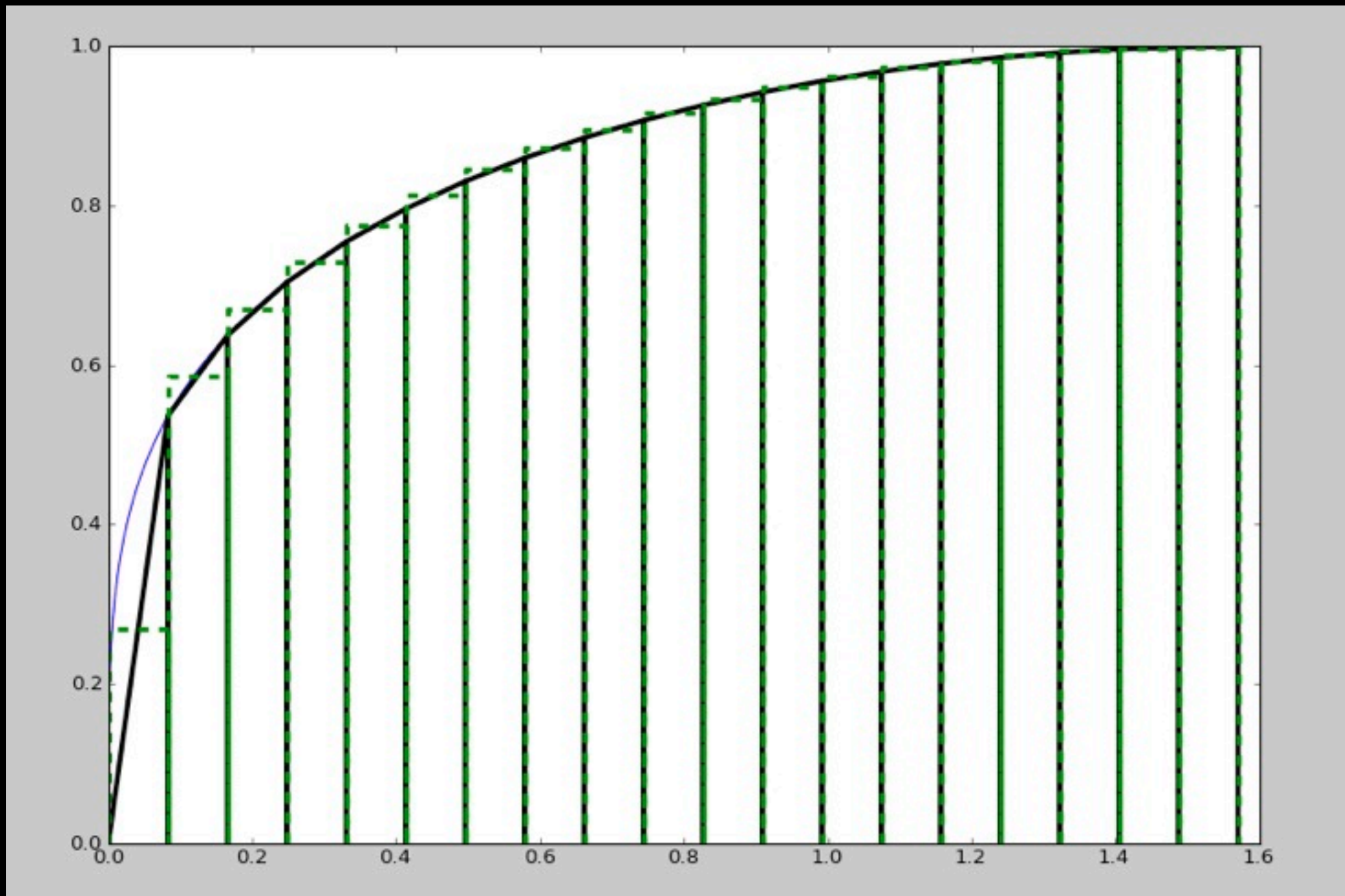
# Integration: Trapezoid Rule

- Mathematical trick to drastically improve accuracy



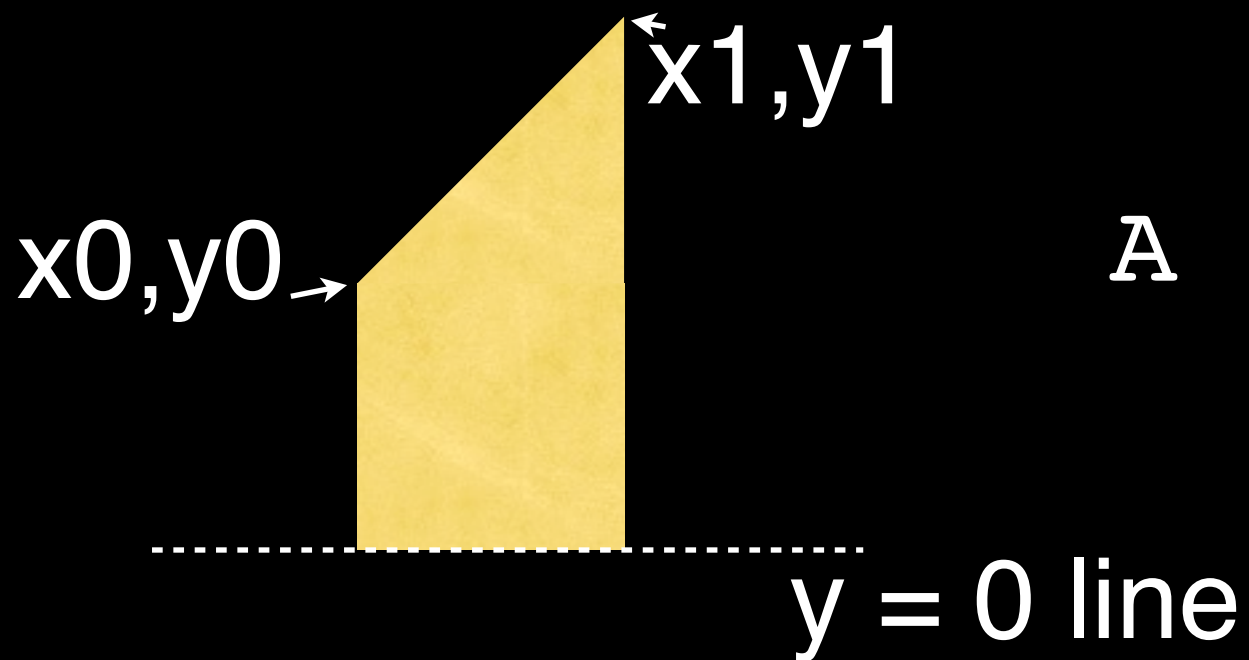
# Integration: Trapezoid Rule

- Mathematical trick to drastically improve accuracy



# Trapezoid Rule

- The area of a trapezoid is just the area of a triangle plus the area of a rectangle (because it's a “right trapezoid”)
- The upper edge of the triangle is defined by two points on the curve

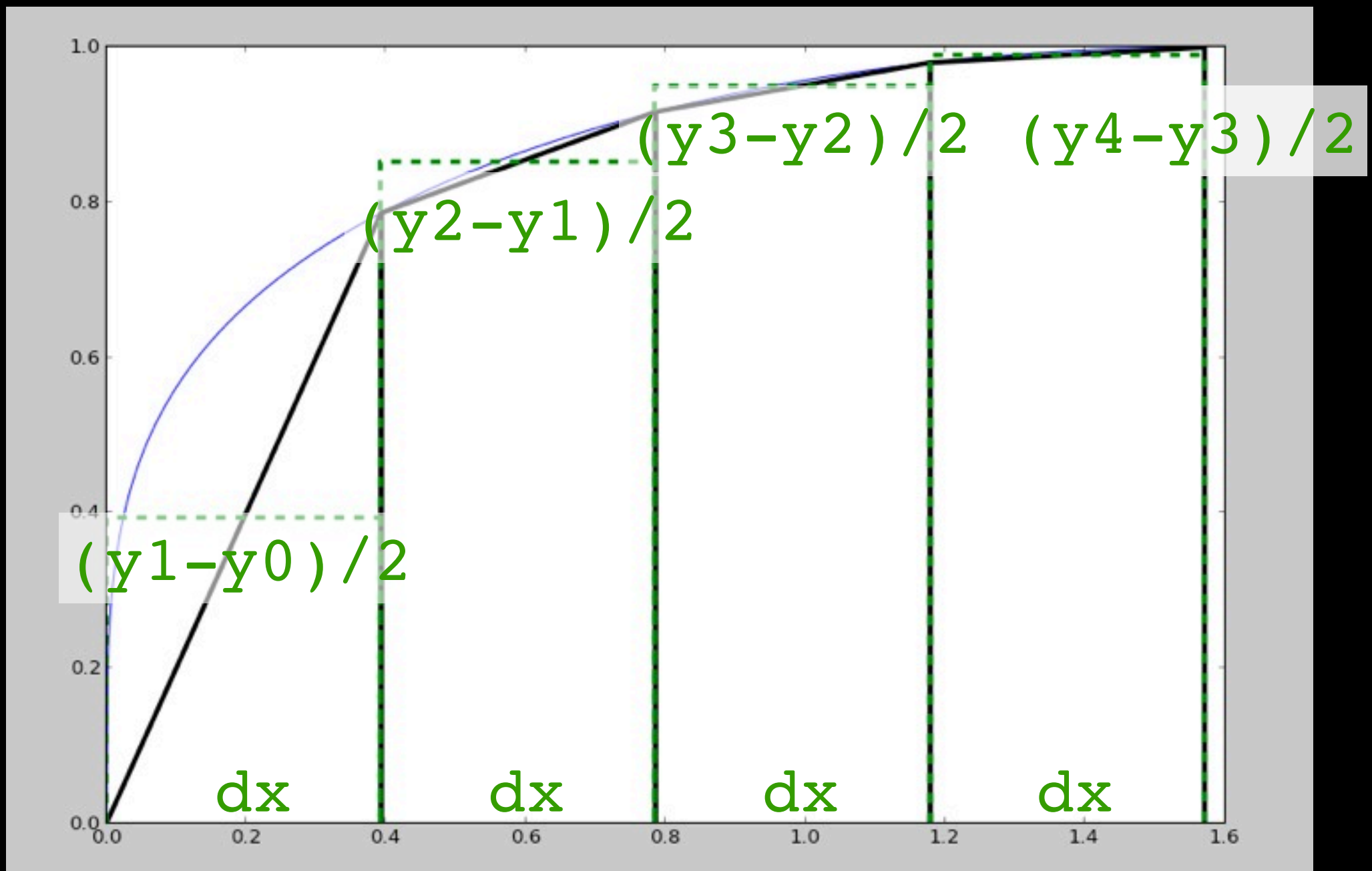


$$A = (x_1 - x_0) * (y_1 - y_0) / 2 + (x_1 - x_0) * y_0$$



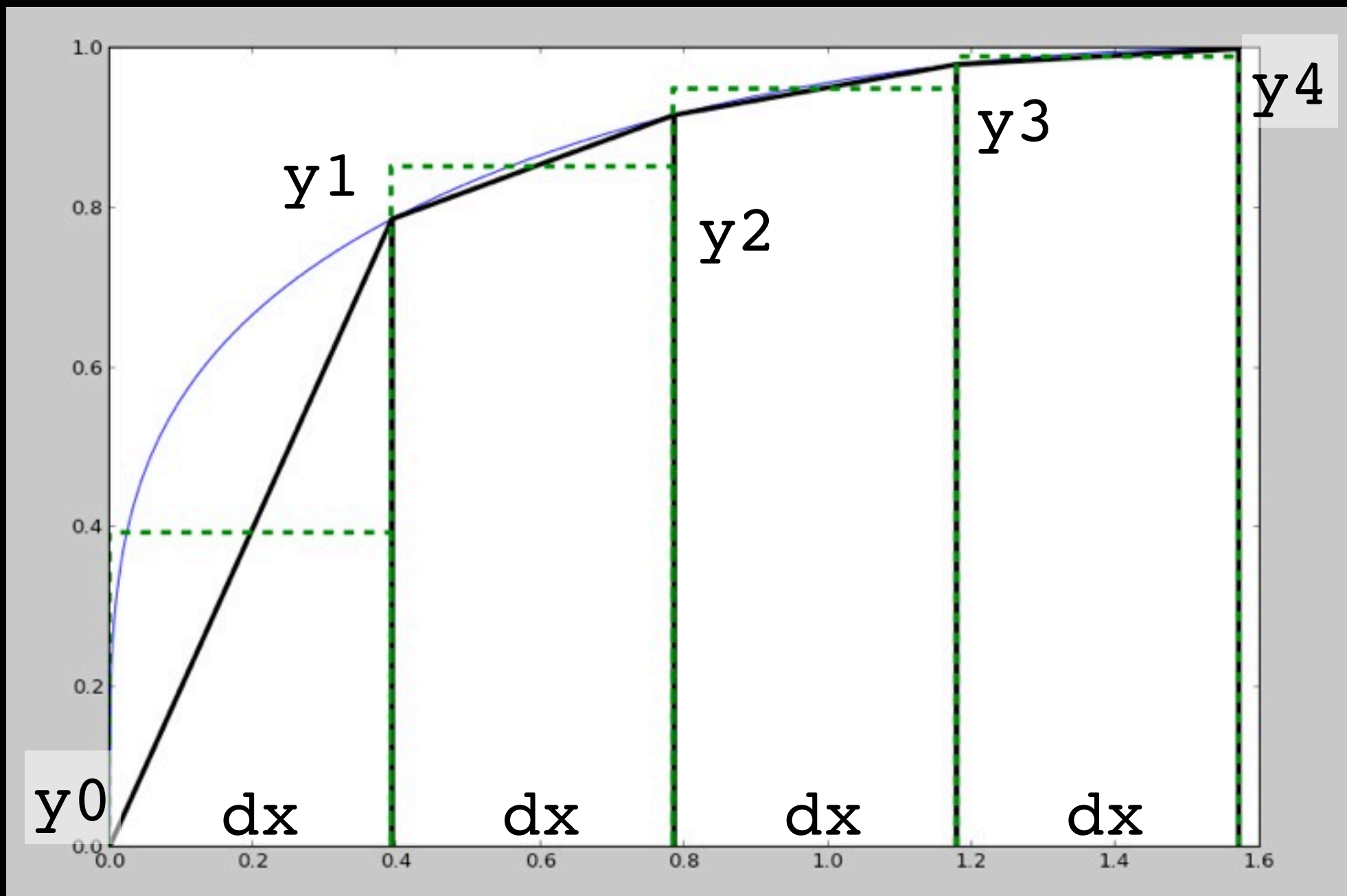
# Integration

- Numbers you use for the “box” method



# Integration: Trapezoid Rule

- The Trapezoid method



# Two methods

- Box:

$$(y[1:*] + y[0:-2]) / 2. * (x[1:*] - x[0:-2])$$

- Trapezoid:

$$(y[0:-2] + (y[1:*] - y[0:-2])) * (x[1:*] - x[0:-2]) / 2$$

- There's an even better method called "Simpson's rule": IDL  
function `qsimp`

- You could also do this using `shift`

- I like the indexing approach because you know which elements you've lost