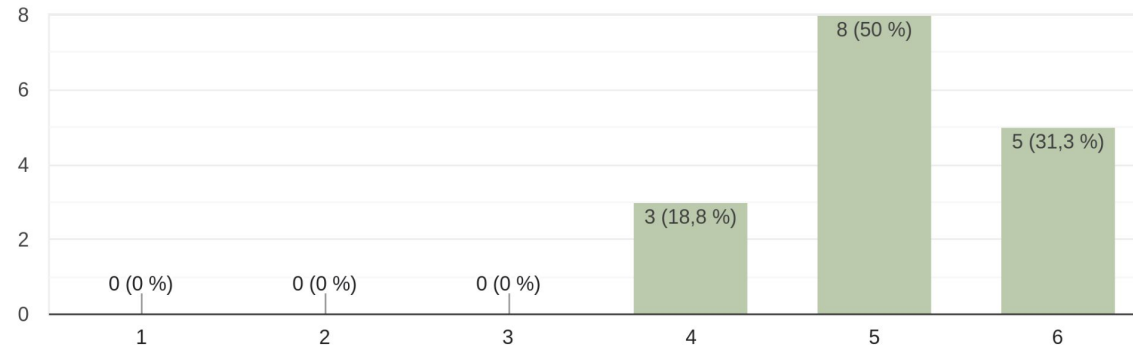


Feedback of Lecture 5

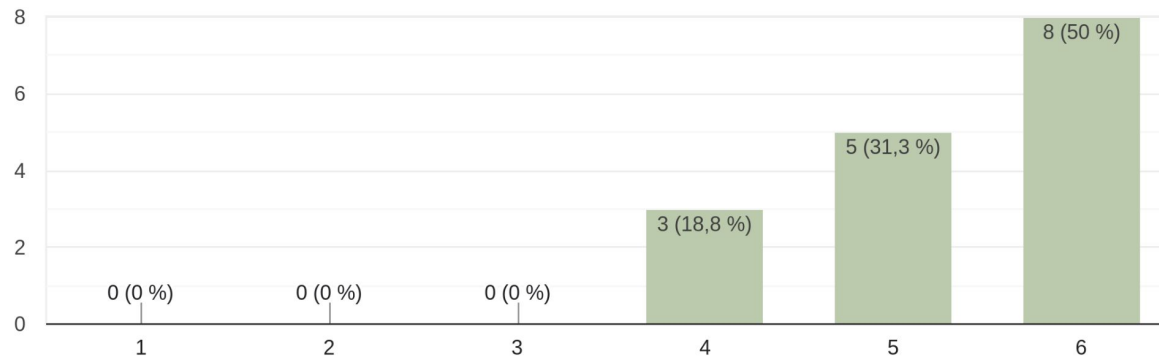
How was your overall impression of the fifth lecture?

16 Antworten



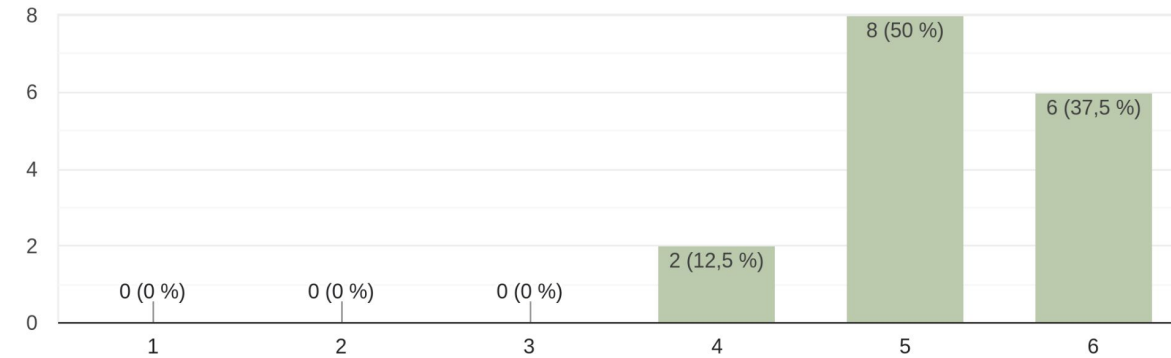
How well could you understand and follow David (the lecturer)?

16 Antworten



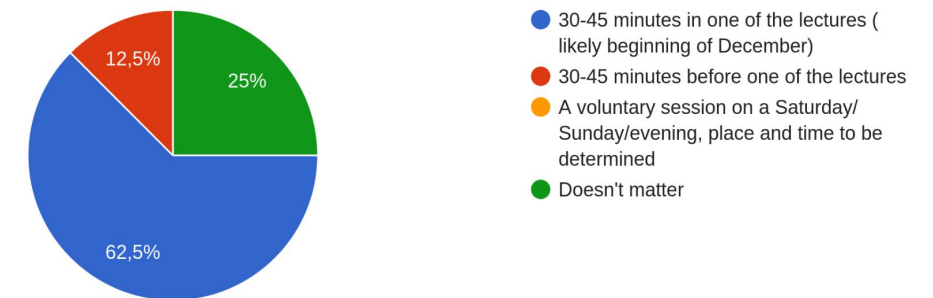
How did you experience the interactions between your peers and David, and among the peers?

16 Antworten



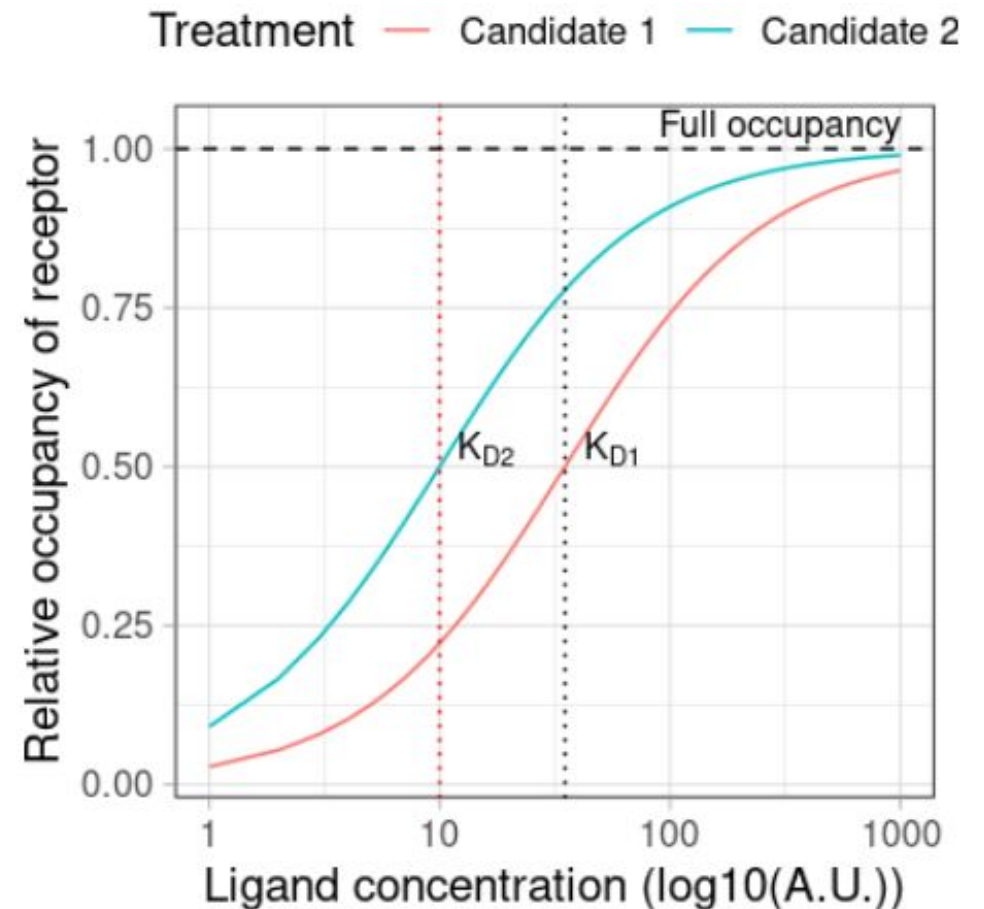
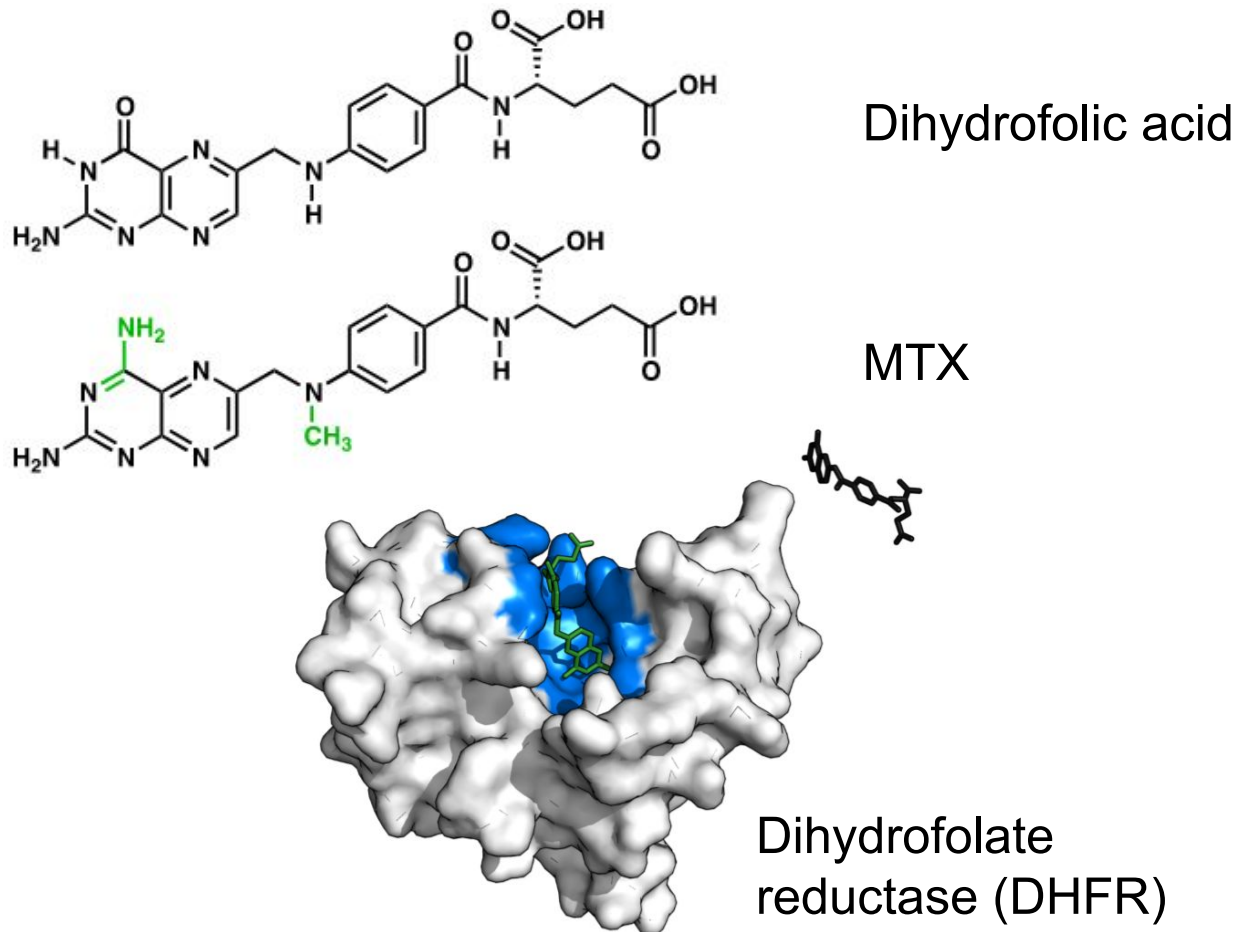
About the possible Ask Me Anything session, what's your most preferred option

16 Antworten



- More time for slides and questions
- Teach math slowly with chalk and board
- How attendance is graded?

AMIDD Lecture 6: Statistical models and causal inference



Dr. Jitao David Zhang, Computational Biologist

¹ Pharmaceutical Sciences, Pharma Research and Early Development, Roche Innovation Center Basel, F. Hoffmann-La Roche

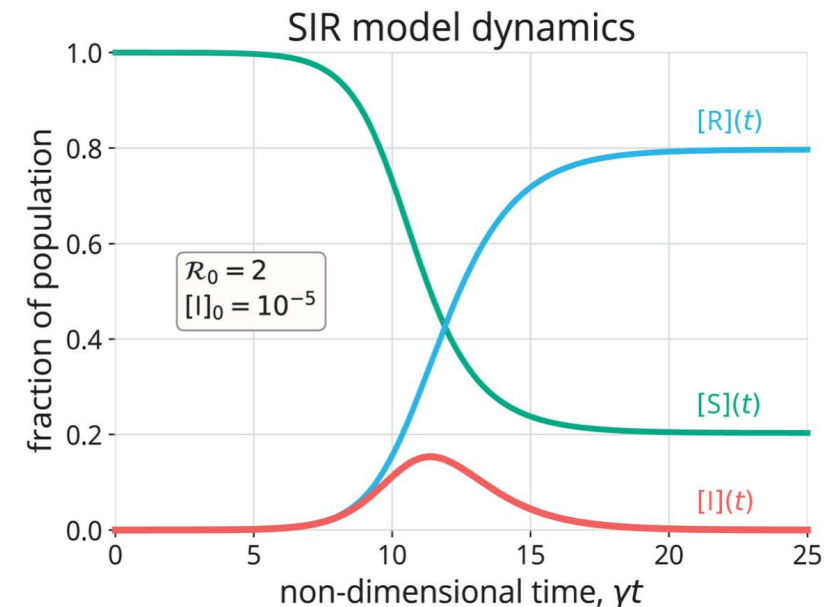
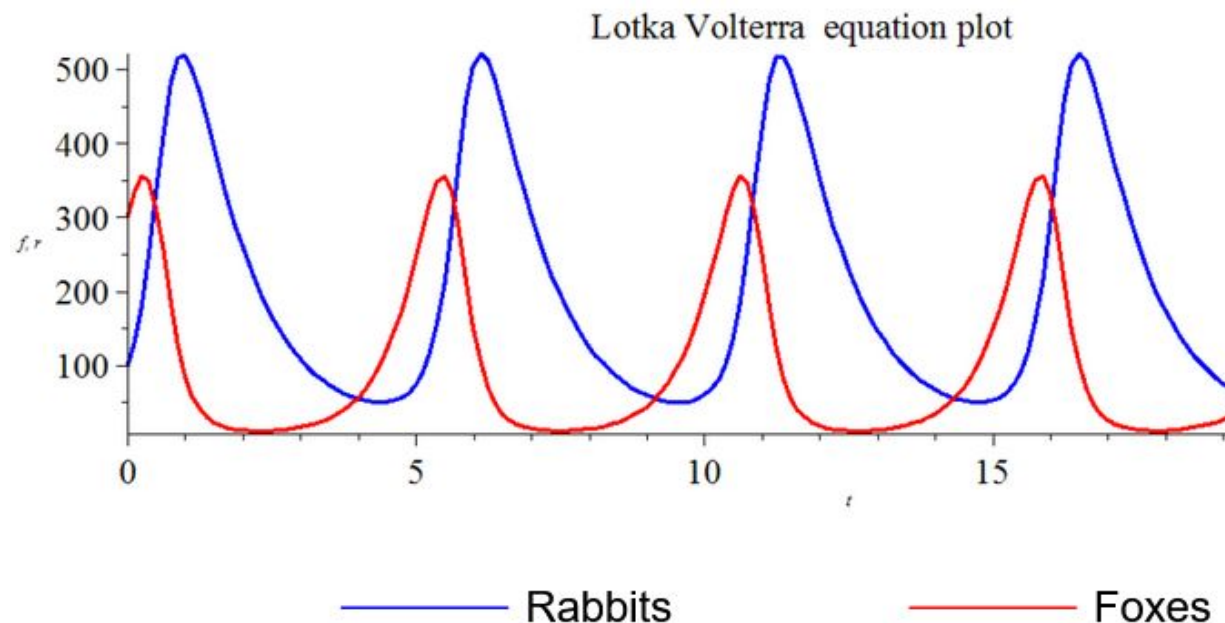
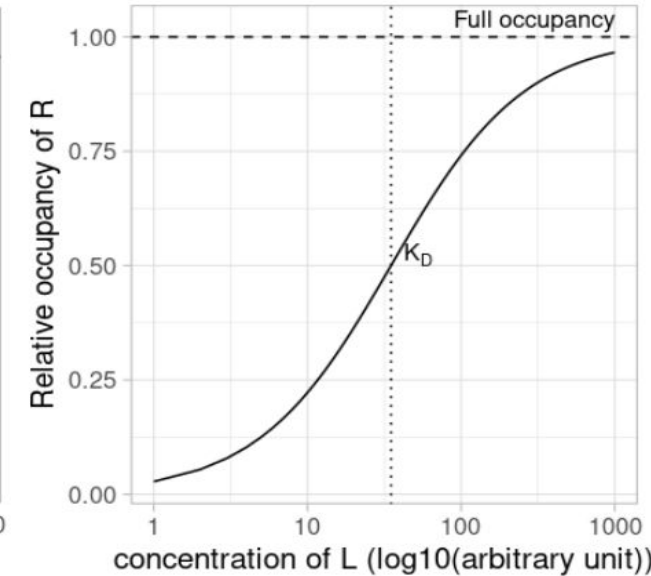
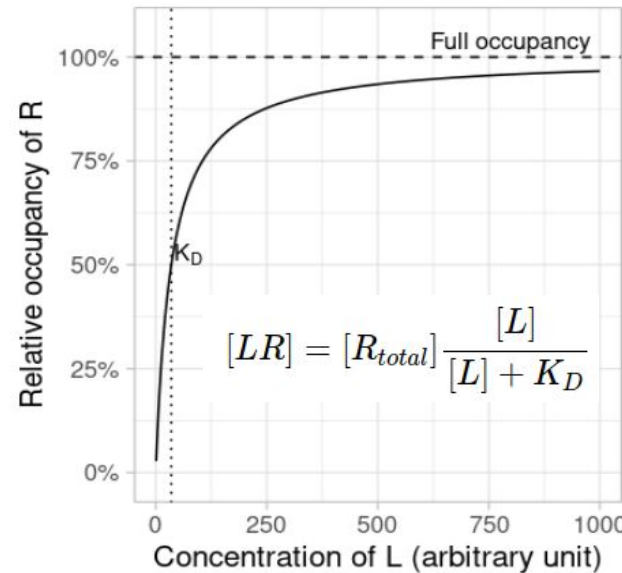
² Department of Mathematics and Informatics, University of Basel

Recap of mechanistic modeling with compartment models

Top right: **Hill-Langmuir function** of target occupancy at equilibrium.

Bottom left: **Lotka-Volterra model** of bait-prey relationships.

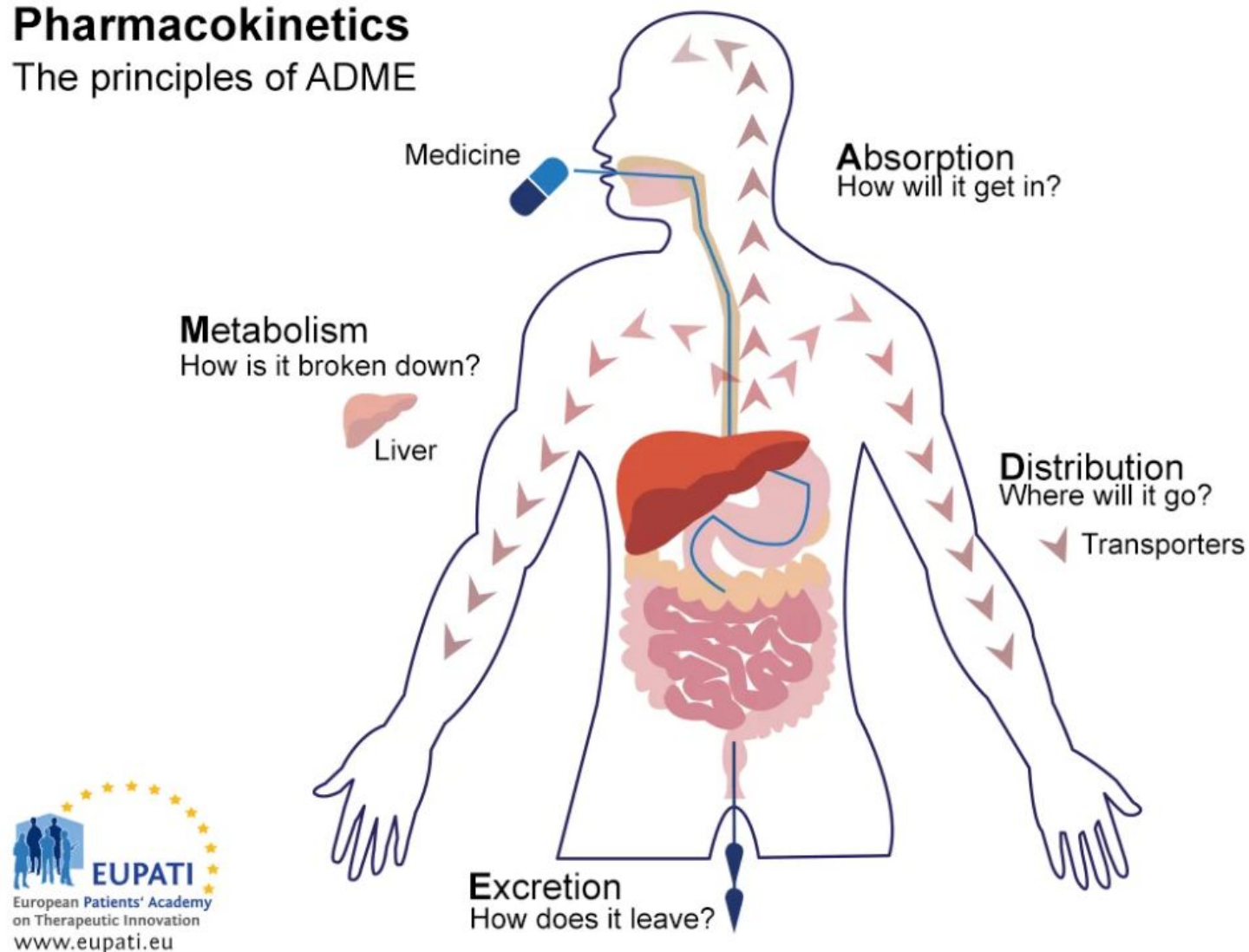
Bottom right: **Susceptible-Infectious-Removed (SIR) model** of transmissible diseases in a defined population.



ODE-based models are powerful tools to model ADME/PK profiles of drugs

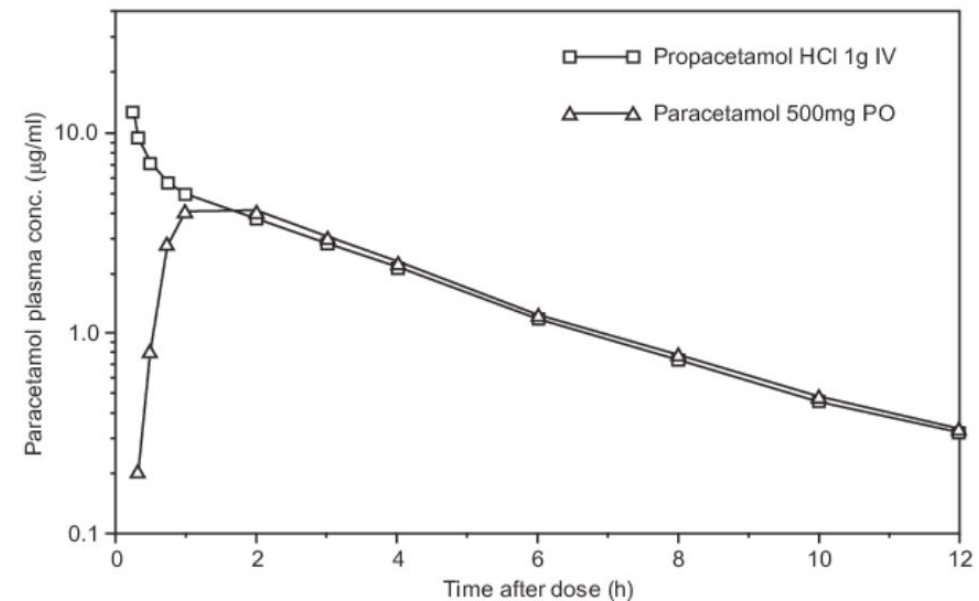
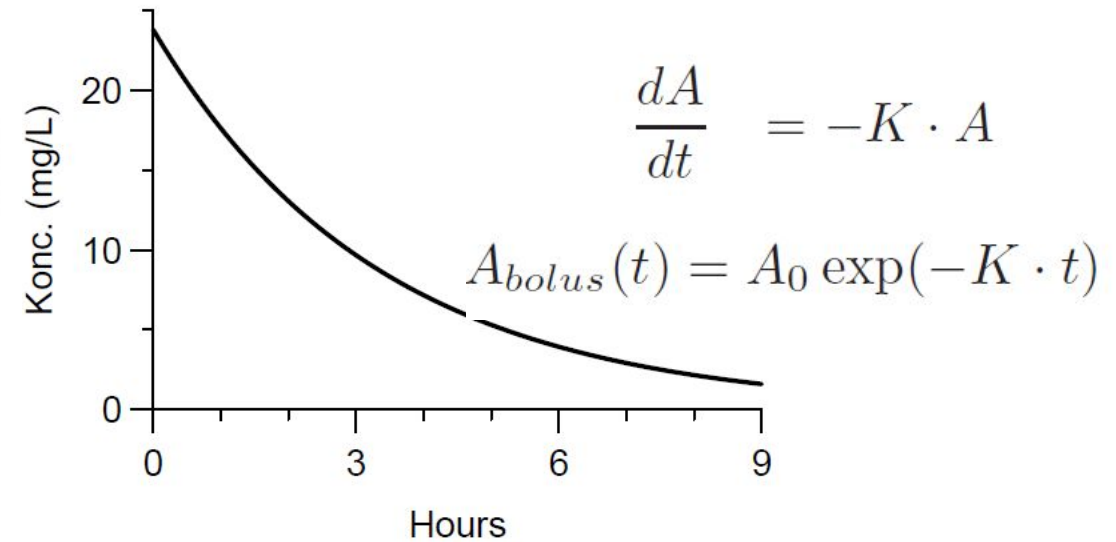
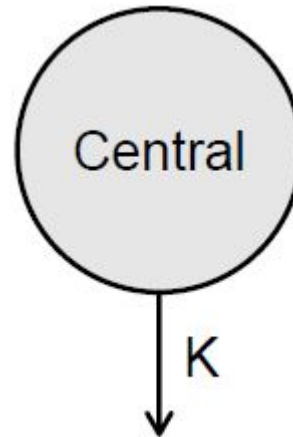
Pharmacokinetics

The principles of ADME



ODE-based mechanistic models are often used in pharmacokinetic modelling

- Pharmacokinetics (PK) describes how the drug is absorbed, distributed, metabolised, and excreted by the body.
- A basic mathematical model of PK is a compartment model, i.e. one or more ordinary differential equations that describe the relationship between drug concentration and time. The simplest model is the decay model of bolus (injection).
 - A_0 : initial concentration
 - $A(t)$: drug concentration at time t
 - K : rate of clearance
- A real-world example: PK of propacetamol, a pro-drug of paracetamol, delivered via IV.



Quantitative Structure-Activity Relationships (QSARs) as an example of statistical modelling

QSAR is a statistical modelling of correlation between biological activity and physicochemical properties, or $\Delta\phi=f(\Delta S)$, where ϕ indicates a biological activity and S indicates a chemical structure (1868-1869).

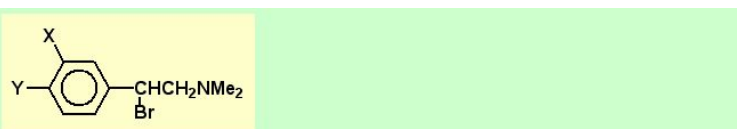
Molecular Descriptors (MD)

Compounds (C)		Target property	MD ₁	MD ₂	...	MD _M
	C ₁	y ₁	x _{1,1}	x _{1,2}	...	x _{1,M}
	C ₂	y ₂	x _{2,1}
	C ₃	y ₃
	C ₄	y ₄

	C _N	y _N	x _{N,1}	x _{N,2}	...	x _{N,M}

The basic form of a QSAR model: find a function f that predicts y from x , $y \sim f(x)$

An example: **The Free-Wilson analysis**. The assumption: the biological activity for a set of analogues could be described by the contributions that substituents or structural elements make to the activity of a parent structure.



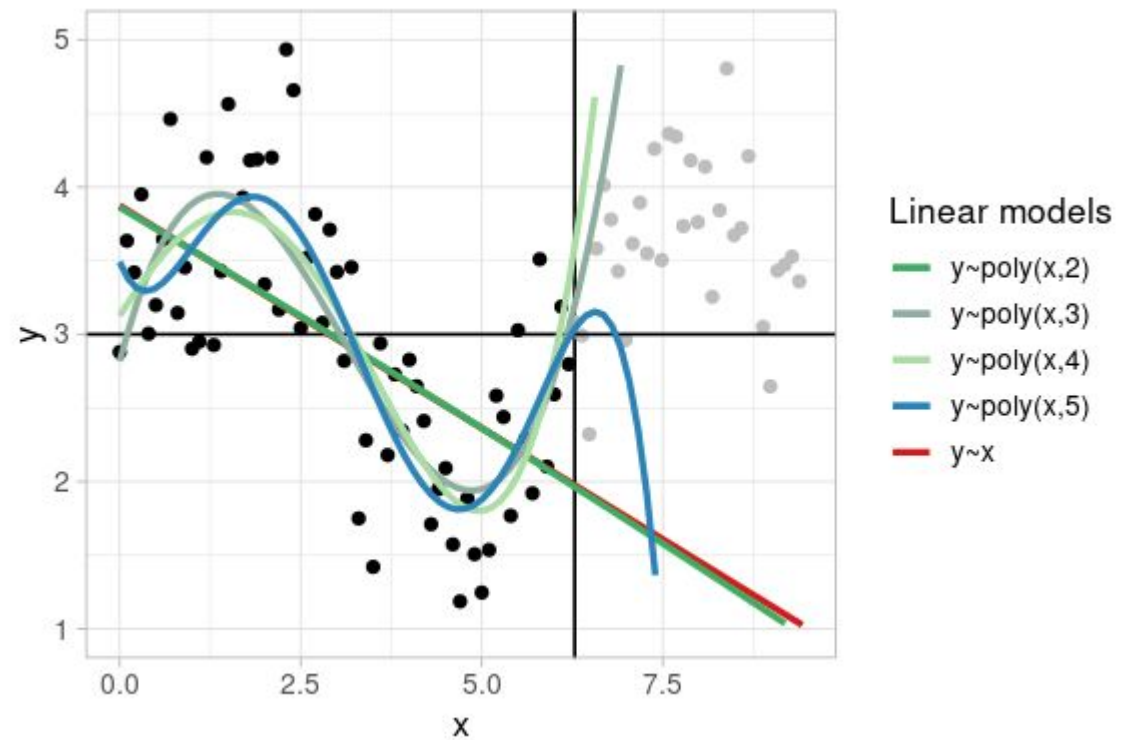
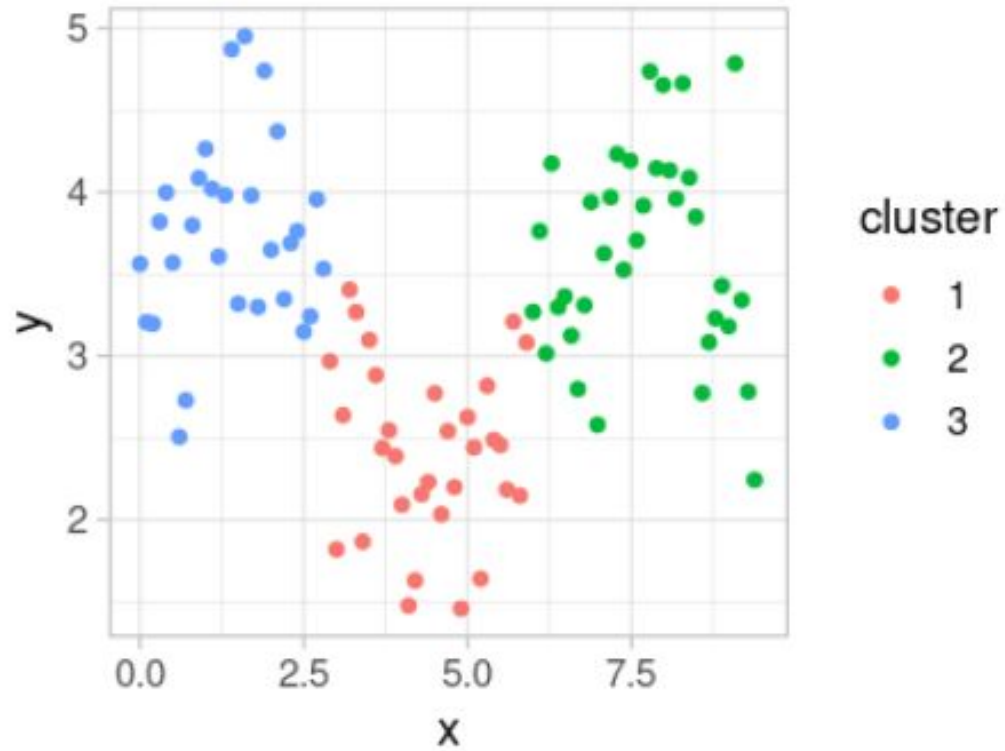
meta	para	meta-					para-					log 1/C	log 1/C
(X)	(Y)	F	Cl	Br	I	Me	F	Cl	Br	I	Me	obsd.	calc.a)
H	H											7.46	7.82
H	F						1					8.16	8.16
H	Cl							1				8.68	8.59
H	Br								1			8.89	8.84
H	I									1		9.25	9.25
H	Me										1	9.30	9.08
F	H	1										7.52	7.52
Cl	H		1									8.16	8.03
Br	H			1								8.30	8.26
I	H				1							8.40	8.40
Me	H					1						8.46	8.28
Cl	F		1				1					8.19	8.37
Br	F			1				1				8.57	8.60
Me	F					1	1						
Cl	Cl		1					1					
Br	Cl			1					1				
Me	Cl					1				1			
Cl	Br		1										
Br	Br			1									
Me	Br					1							
Me	Me					1							
Br	Me			1									

Multivariate regression analysis

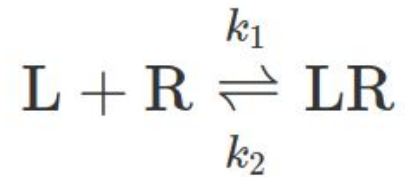
$$\log(1/ED_{50}) = -0.301[m-F] + 0.27[m-Cl] + 0.434[m-Br] + 0.579[m-I] + 0.454[m-Me] + 0.340[p-F] + 0.768[p-Cl] + 1.020[p-Br] + 1.429[p-I] + 1.256[p-Me] + 7.821$$

$n = 22, r^2 = 0.94, s = 0.194, F = 17.0$

Unsupervised versus supervised models

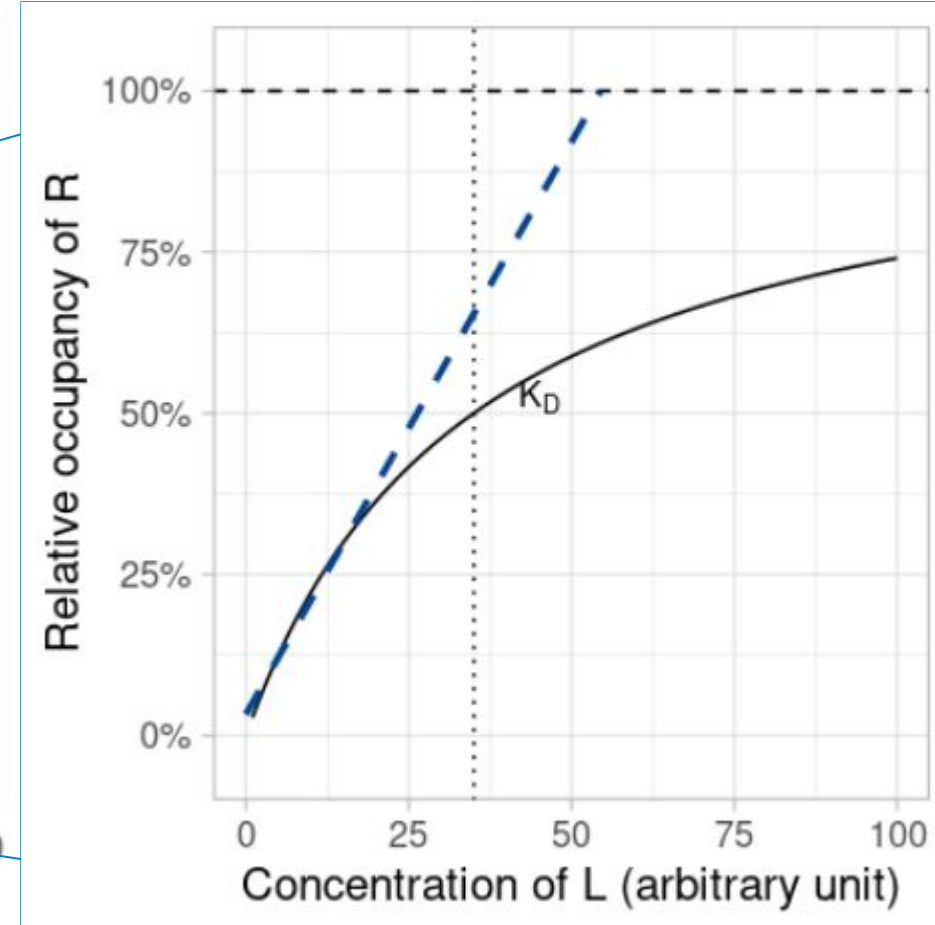
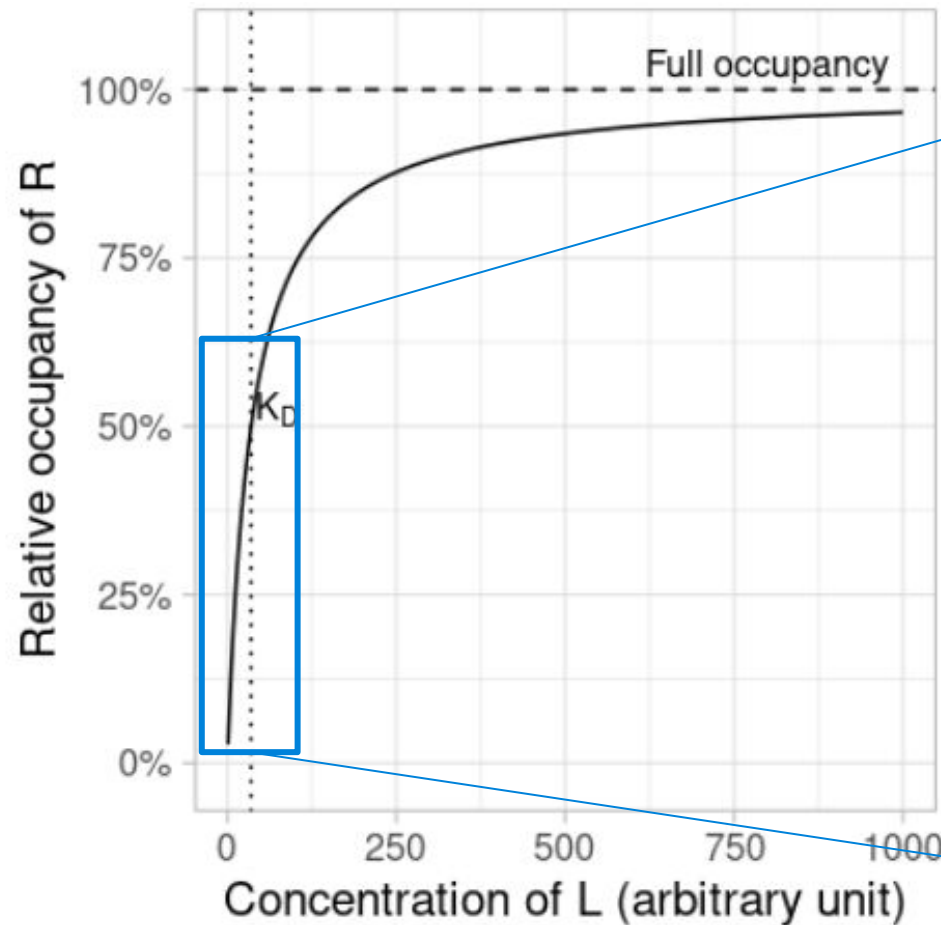


Linear model can be used to model local effects of non-linear models



$$K_D \equiv k_2/k_1$$

$$[LR] = [R_{total}] \frac{[L]}{[L] + K_D}$$

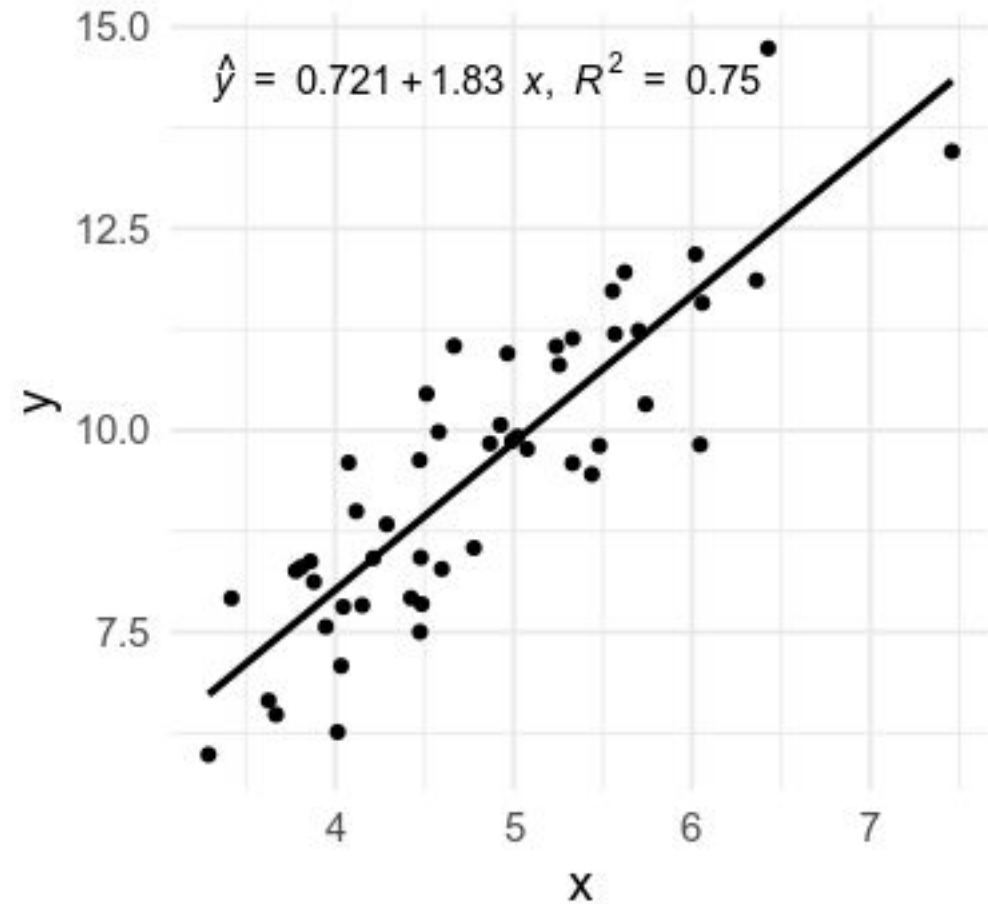


The simplest linear model has three components: the intercept, the slope, and a measure of fit

In this example, the coefficient of determination (R^2) is used as the measure.

R^2 measures the relative fit of the linear model with regard to a baseline model, where the mean value of y is used as a fit.

	x	y
1	4.926791	10.067779
2	4.479734	8.424283
3	4.289686	8.835629
4	4.474023	9.630499
5	4.214551	8.416680
6	6.057431	11.578080
7	4.597903	8.283025
8	5.021571	9.922731
9	3.627323	6.651222
10	5.622794	11.959972
11	5.555025	11.727815
12	4.966007	10.951562
13	5.076791	9.768299

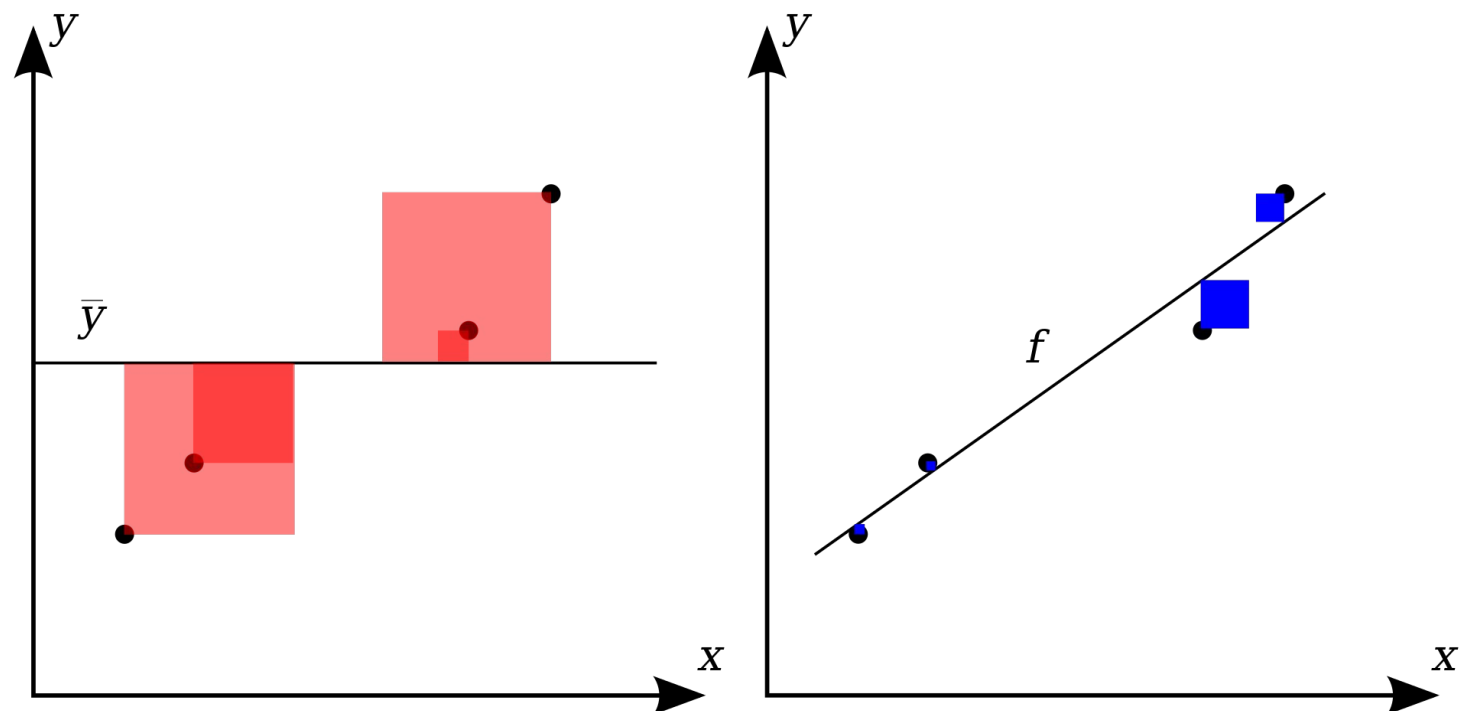


A visual explanation of R^2

The better the linear regression (right) fits the data in comparison to the average (left), the closer the value of R^2 is to 1.

The areas of the blue squares represent the squared residuals with respect to the linear regression. The areas of the red squares represent the squared residuals with respect to the average.

R^2 is defined as $1 - (\text{blue area}) / (\text{red area})$.

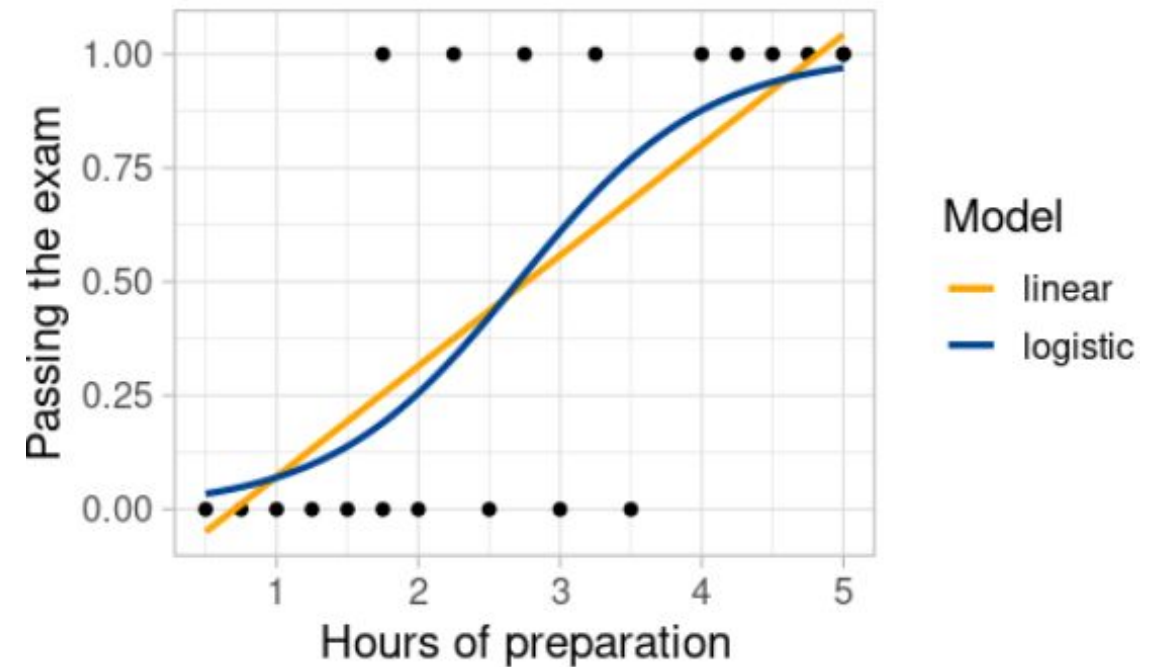


Question: can R^2 be negative?

Work by Orzetto, CC-SA 3.0, from [Wikimedia](https://commons.wikimedia.org/wiki/File:R2_visualization.png)

Logistic regression is an example of *generalized* linear model, which allows dependent variable defined other than real numbers

- Dependent variable of a linear regression model is defined on \mathbb{R} .
- *Generalized* linear models allow the dependent variable to be defined on other domains than real numbers, for instance binary (0/1), counts (non-negative integers), etc.
- Logistic regression maps input real numbers to the range between 0 and 1 in two steps: (1) building a simple linear regression, (2) applying the *logistic function* to map the intermediate dependent variable to the desired domain (0,1).



Data come from [Wikipedia's item on logistic regression](#)

$$t = \alpha + \beta x \qquad y = \frac{1}{1 + e^{-t}}$$

Multiple regression with regularization

- We may have multiple independent variables. For instance, in the example on the right side, we want to predict *which topics contribute to passing the exam*. In such cases, we apply *multiple regression*.
- In multiple regressions, we often wish for a sparse solution: i.e. we wish to know the few most important features that contribute to the prediction. A technique to achieve this is *regularization*.
- Regularization penalizes large coefficients. It effectively push coefficients towards zero. For instance, the equation below shows the *error function of ridge regression*.

$$\tilde{E}(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^N \{y(x_n, \mathbf{w}) - t_n\}^2 + \frac{\lambda}{2} \|\mathbf{w}\|^2$$

	ω_1	ω_2	ω_3	ω_4	ω_5	ω_6	ω_7	ω_8
g_1	1		1	1				1
g_2								
g_3		1			1	1	1	1
g_4	1							1
g_5								1
g_6	1						1	
g_7		1	1	1				1
g_8	1				1			
g_9						1	1	1

	β_{ω_1}
>0	β_{ω_2}
>0	β_{ω_3}
>0	β_{ω_4}
	β_{ω_5}
>0	β_{ω_6}
	β_{ω_7}
	β_{ω_8}

$f(\mathbf{Y})$: a binary label to indicate whether someone pass an exam

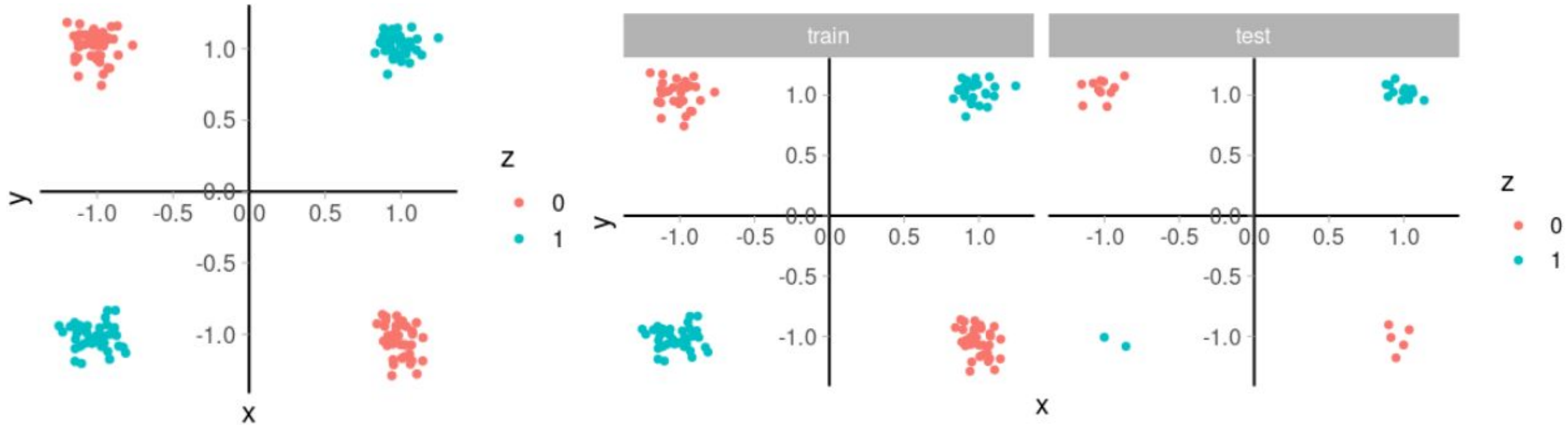
g_1 - g_9 : students

ω_1 - ω_8 : topics

β_{ω_1} - β_{ω_8} : coefficients of topics

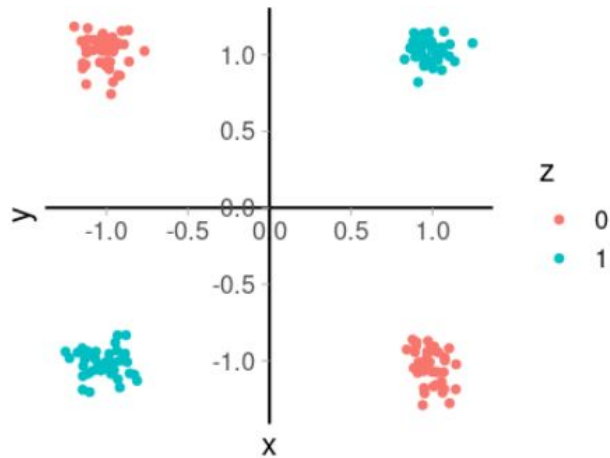
Equation: Bishop, Christopher M. [Pattern Recognition and Machine Learning](#), page 10

We next address two problems: (1) unknown performance of model when new data are met, and (2) non-linearity



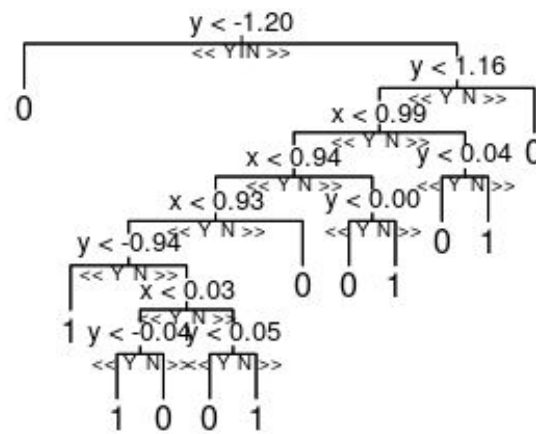
- Left: a simple example of non-linearity: linear models cannot predict z well based on values of x and y . We need something else.
- Right: a model is usually trained in some data, and the performance is assessed in unseen test data.

We can use random forest to model non-linearity

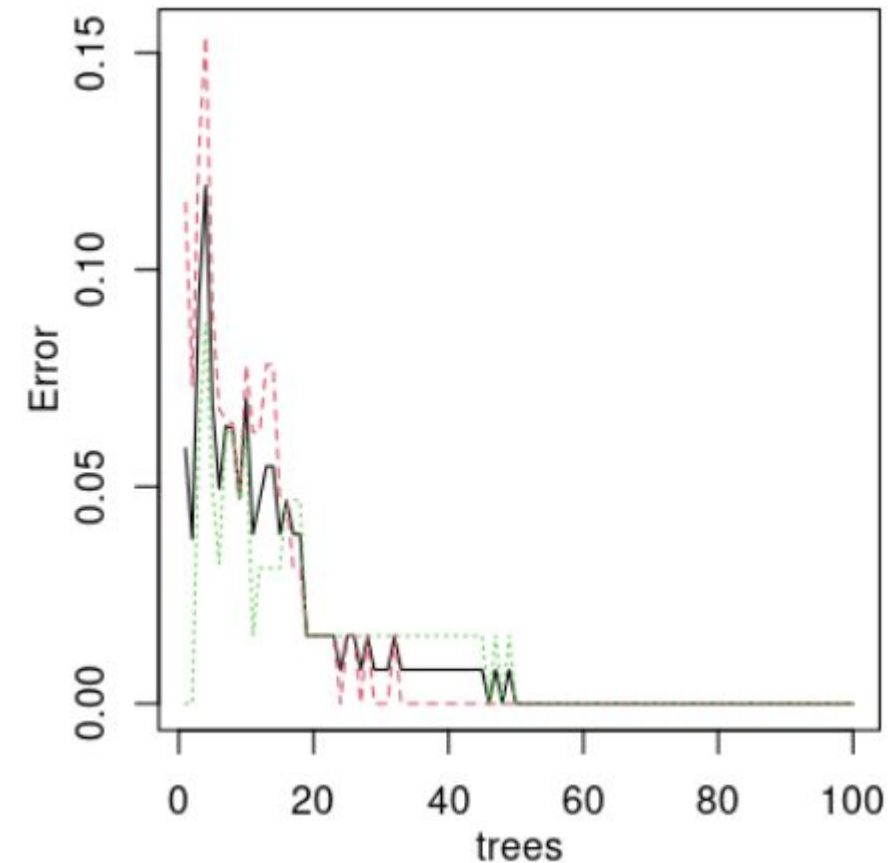
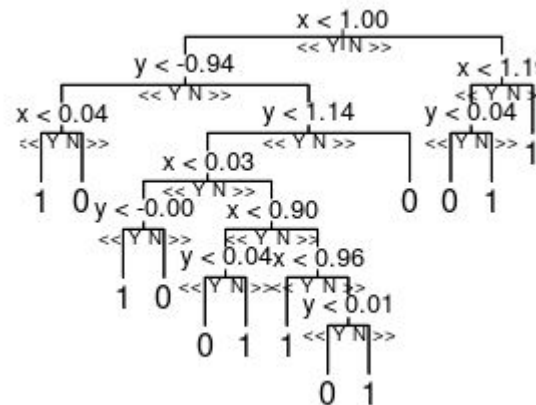


- Random forest is a collection of *decision trees*. Each tree partitions the input data to make predictions.
- Random forest is an example of *ensemble methods*: each tree has weak performance, however the consensus can perform surprisingly well.

Tree #1

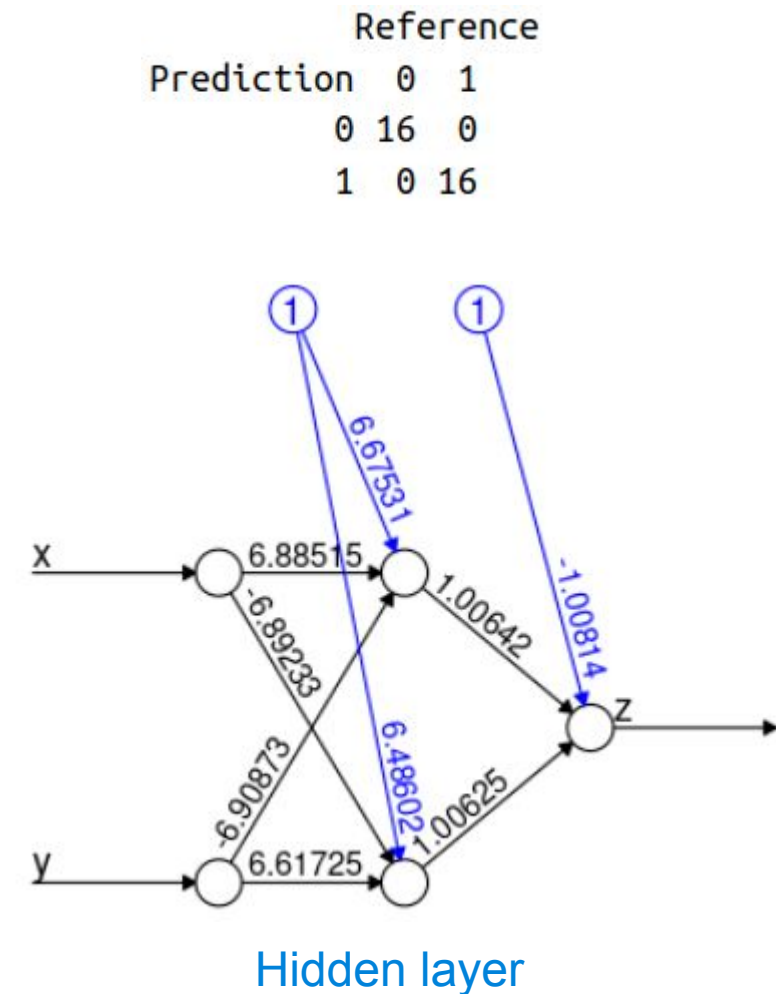


Tree #20



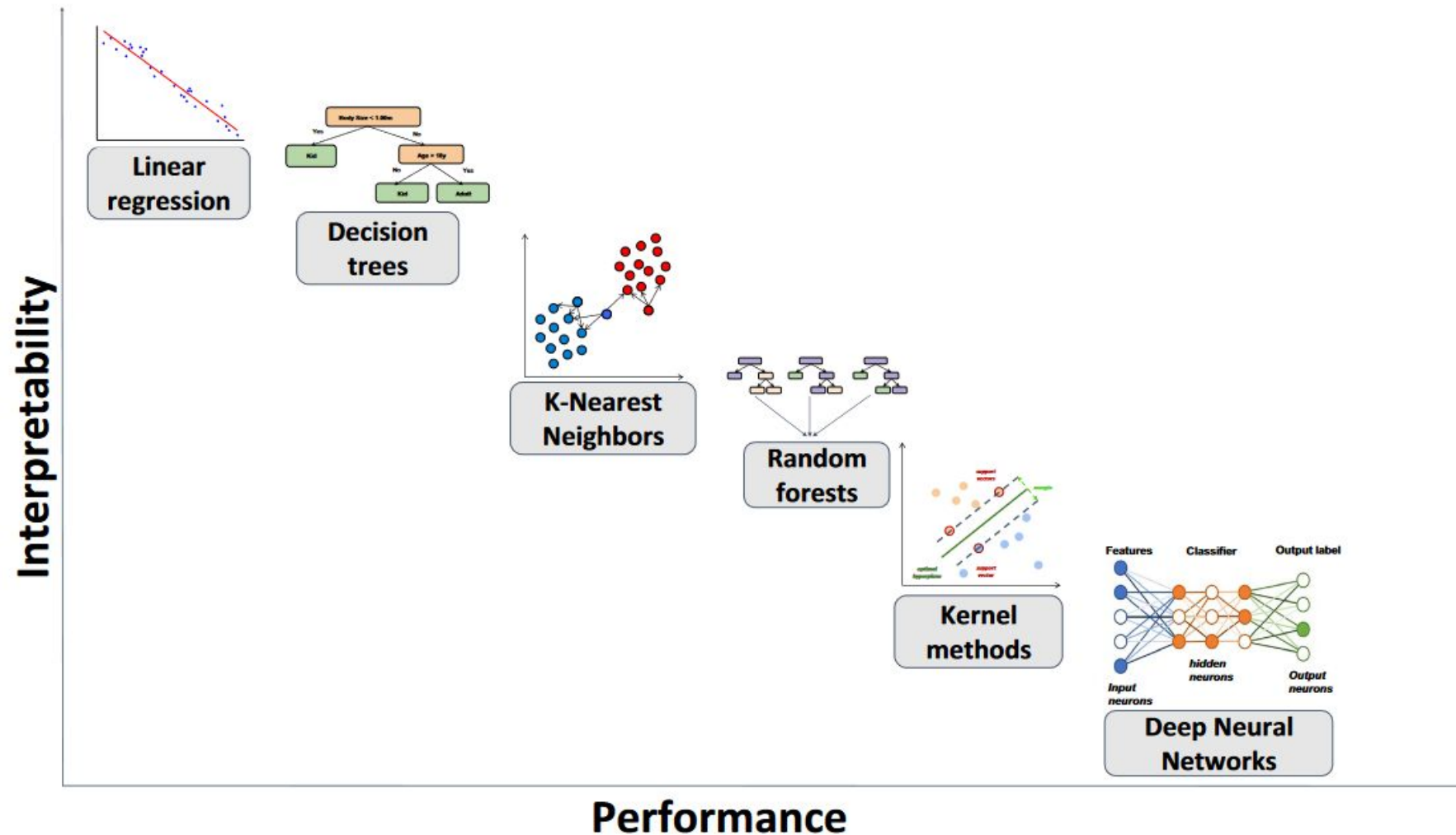
Neural network can be used to model non-linearity, too

- Neural network models non-linearity by applying multiple linear combinations subsequently in the forward propagation.
- Once the architecture (# hidden layers, # nodes, etc.) is fixed, weights of edges neural network are initialized with random numbers, and then optimized by iterative forward and reverse propagation to minimize the error.
- Right figure: the trained neural network with the example data. Blue nodes indicate intercepts.



Error: 0.000172 Steps: 1085

Generally, well-performing models tend to be less interpretable

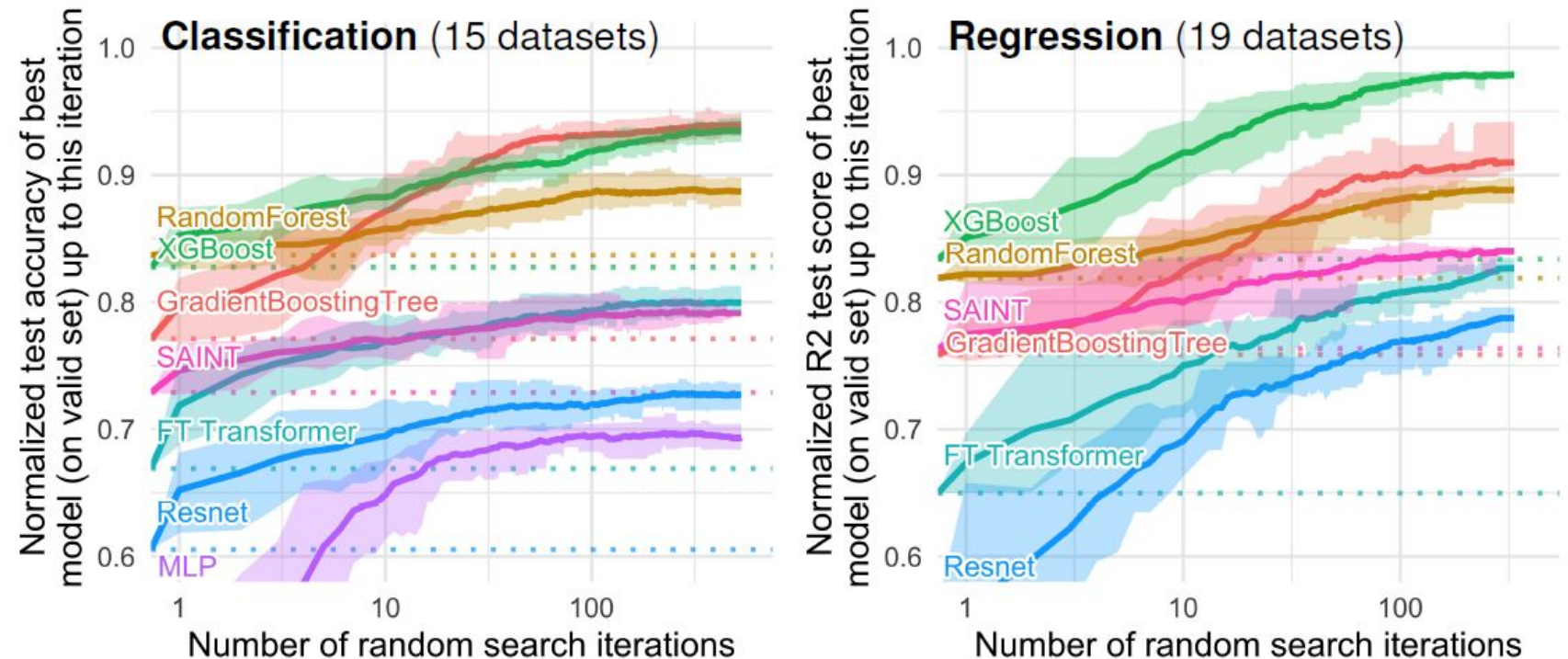


For tabular data: tree-based methods are well interpretable and generally outperform deep learning... until TabPFN (2022-25)

The authors collected 45 tabular datasets from varied domains.

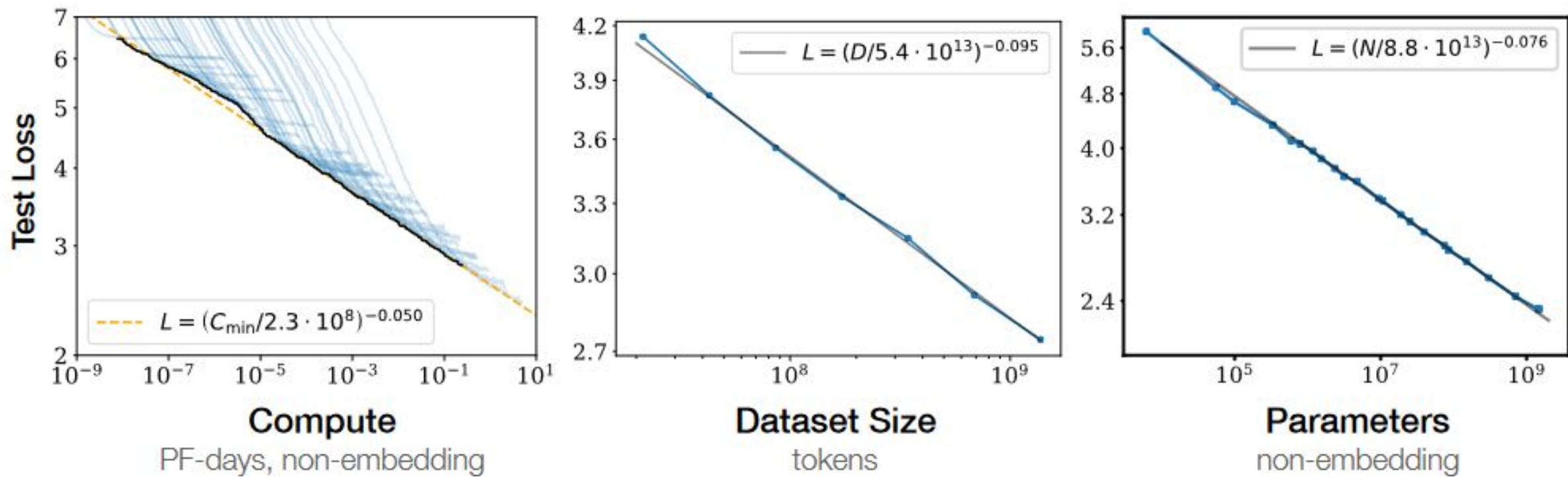
They found that tree-based models remain state-of-the-art on medium-sized data (~10k samples), even without considering the speed.

Conclusion: when working with tabular data, consider tree-based methods, ... or TabPFN (next lecture)



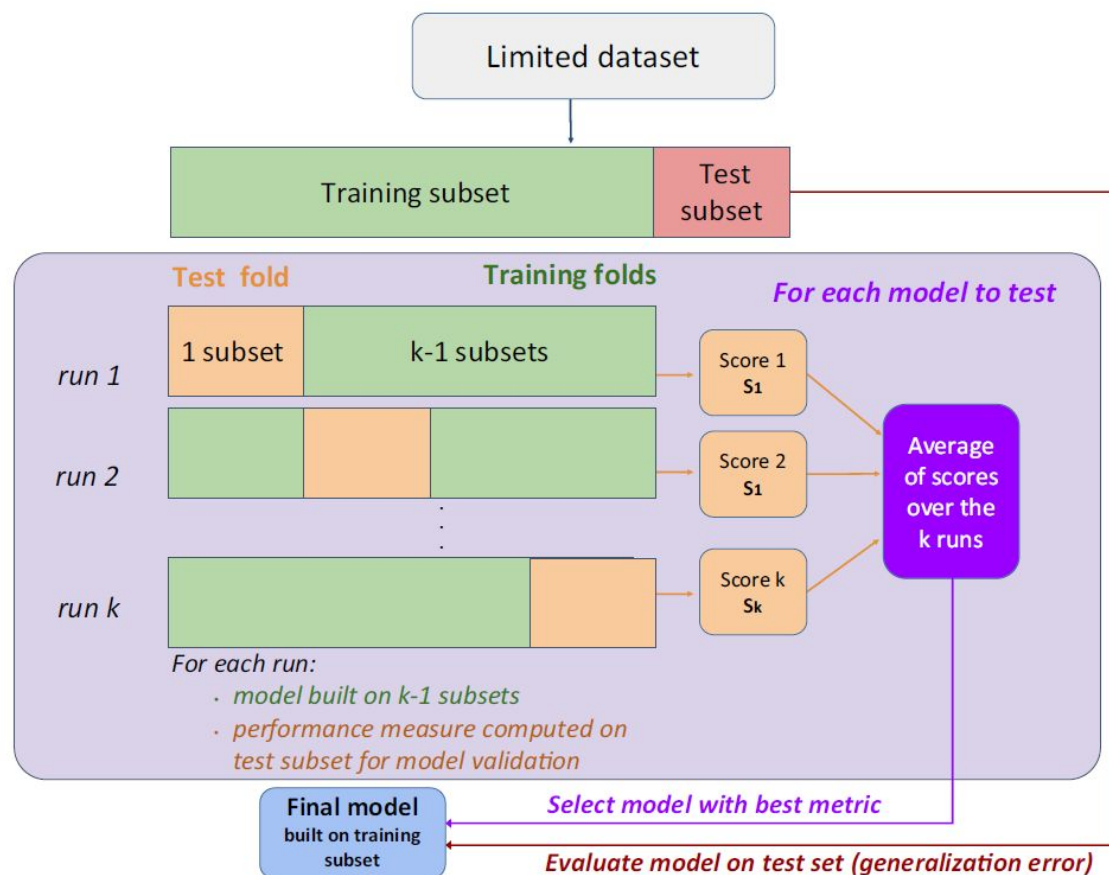
Grinsztajn, Léo, Edouard Oyallon, and Gaël Varoquaux. "Why Do Tree-Based Models Still Outperform Deep Learning on Tabular Data?" arXiv, July 18, 2022. <https://doi.org/10.48550/arXiv.2207.08815>.
 GitHub repository: <https://github.com/LeoGrin/tabular-benchmark>

Performance neural networks improve as data amount, computational power, and model size increases

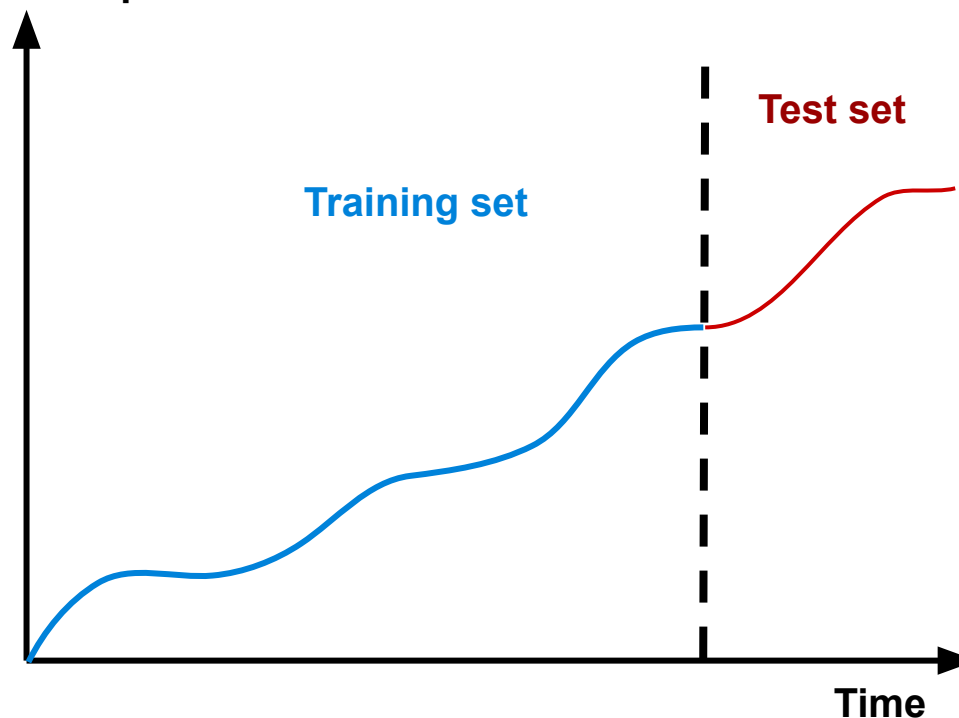


Language modeling performance improves smoothly as we increase the model size, dataset size, and amount of compute used for training. PF-days: Peta-FLOPs. From: Kaplan, J. et al. [Scaling Laws for Neural Language Models](#) (2020).

Watchout 1: Temporal validation is essential for drug discovery



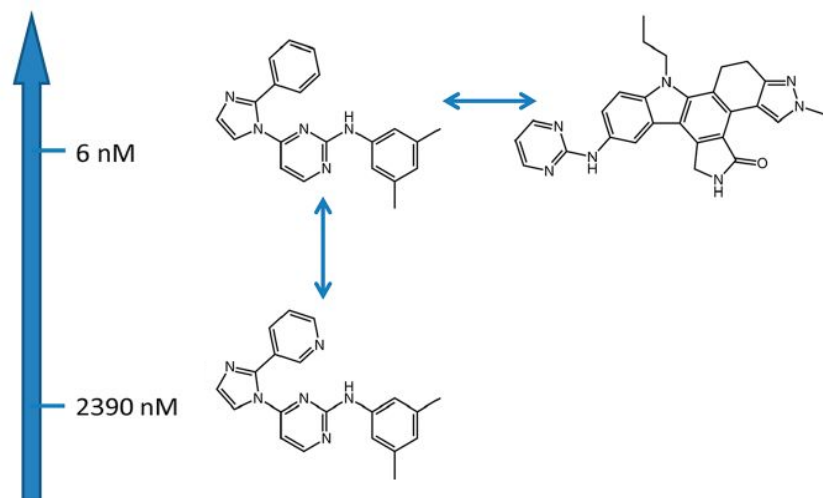
Cumulative count of compounds



(Left) To assess the generalization ability of a supervised learning algorithm, data are separated into a training subset used for building the model and a test subset used to assess the generalization error.

(Right) Temporal validation is especially important for drug discovery, because chemical structures used in the training set may differ substantially from those that will be tested.

Watchout 2: Molecular similarity does not equal biological similarity



Watch out biological activity cliffs:
Structural similarity does not imply similar activity. Top: three vascular endothelial growth factor receptor 2 (VEGFR2) ligands that represent different similarity–activity relationships.

a	1	2	3	4	5
A					
B					
C					
D					
E					

A1: 2D fingerprints
B1: Mechanisms of action
C1: Small molecule roles
D1: Transcription
E1: Therapeutic areas

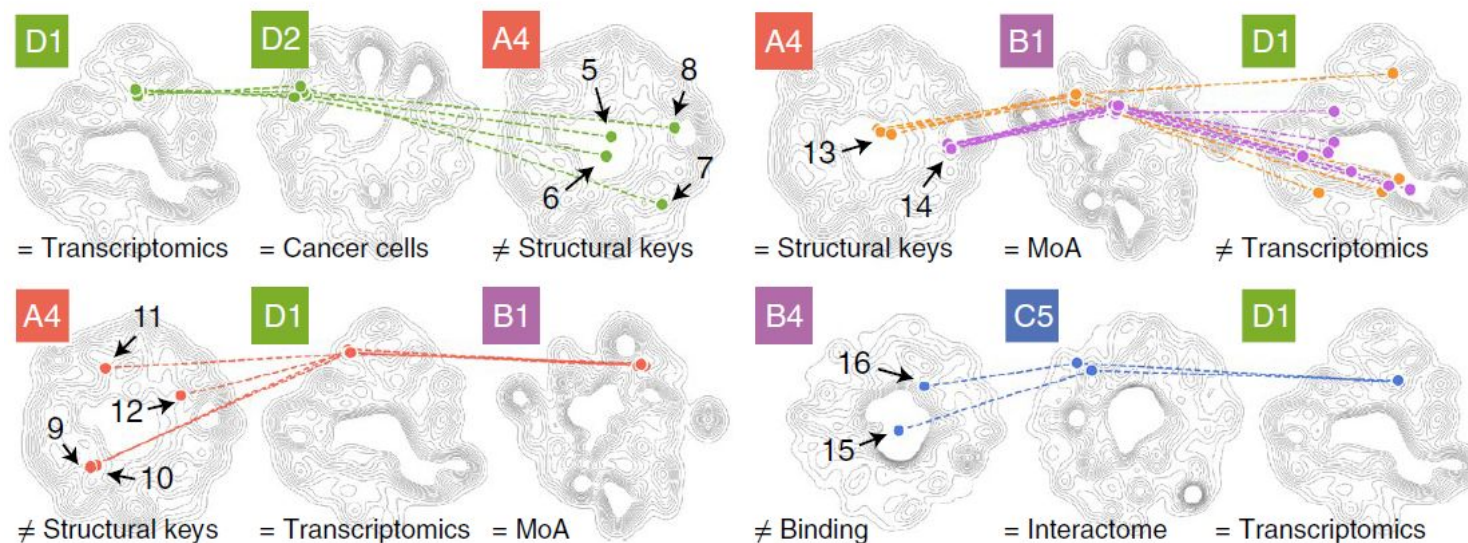
A2: 3D fingerprints
B2: Metabolic genes
C2: Small molecule pathways
D2: Cancer cell lines
E2: Indications

A3: Scaffolds
B3: Crystals
C3: Signaling pathways
D3: Chemical genetics
E3: Side effects

A4: Structural keys
B4: Binding
C4: Biological processes
D4: Morphology
E4: Diseases & toxicology

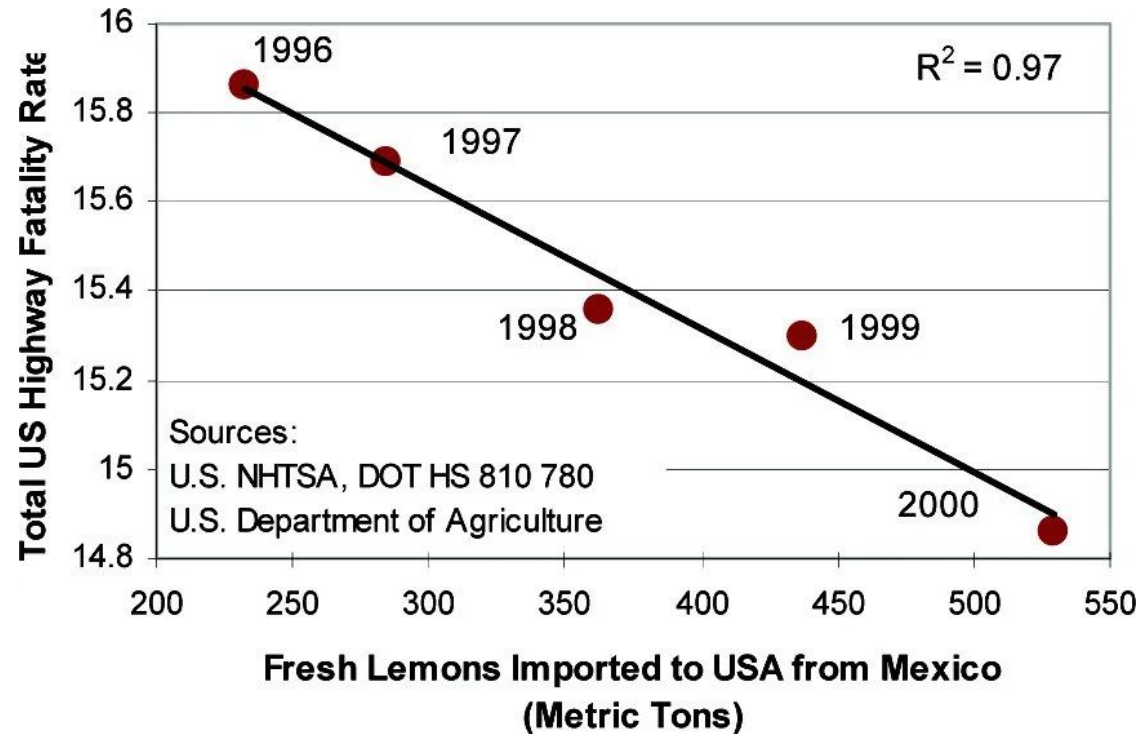
A5: Physicochemistry
B5: HTS bioassays
C5: Interactome
D5: Cell bioassays
E5: Drug–drug interactions

A: Chemistry
B: Targets
C: Biological network
D: Cells
E: Clinical readout



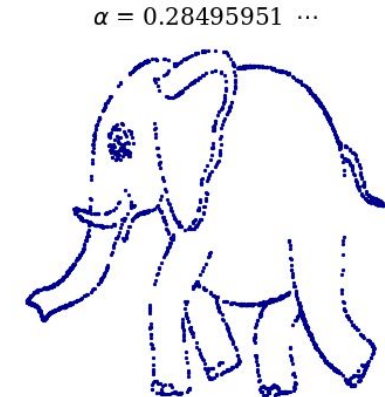
Duran-Frigola, Miquel, Eduardo Pauls, Oriol Guitart-Pla, Martino Bertoni, Víctor Alcalde, David Amat, Teresa Juan-Blanco, and Patrick Aloy. 2020. [“Extending the Small-Molecule Similarity Principle to All Levels of Biology with the Chemical Checker.”](#) Nature Biotechnology, May, 1–10.

Watchout 3: Do we need correlation or causation?



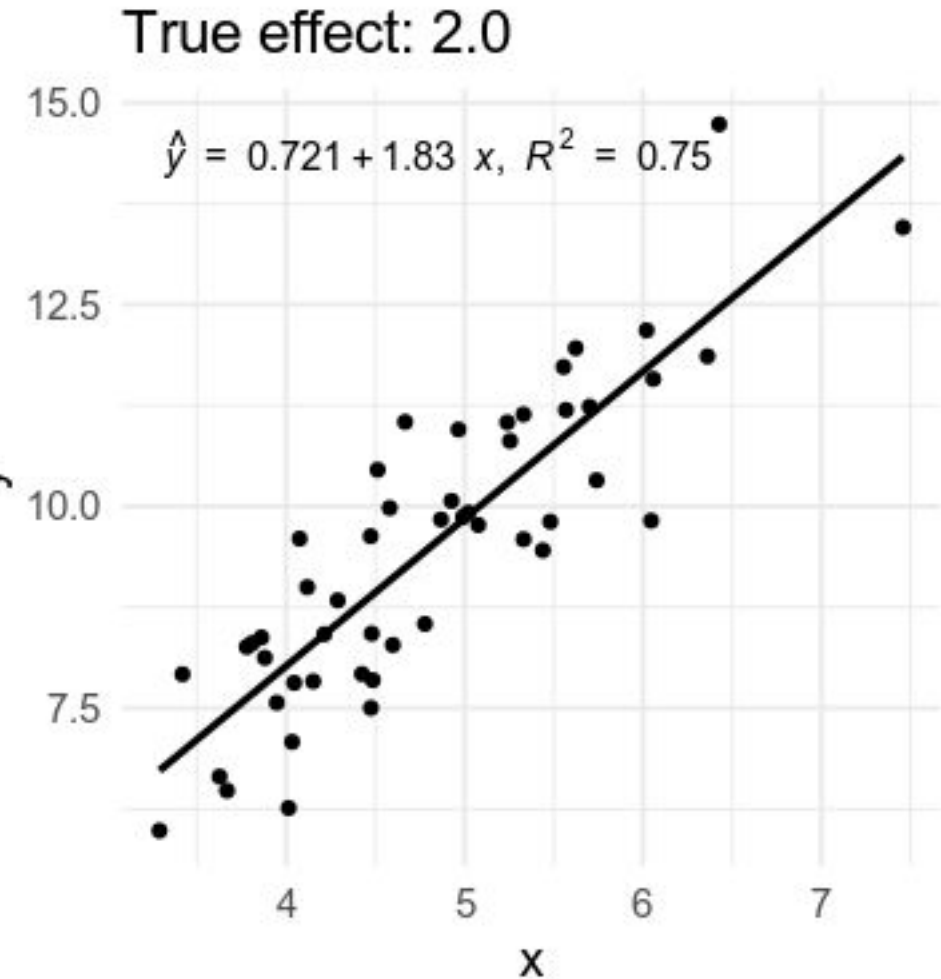
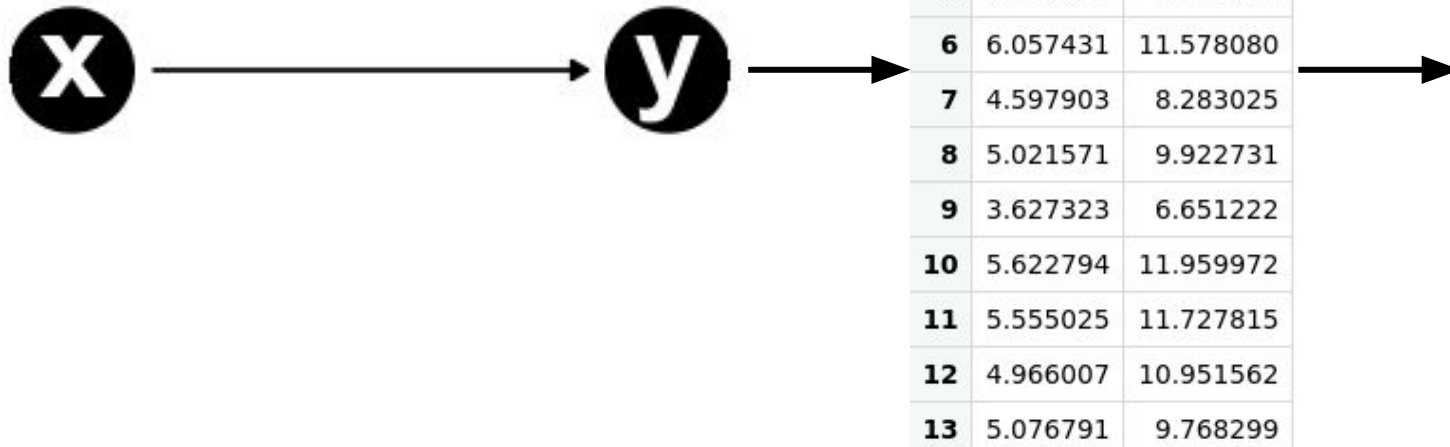
Johnson, Stephen R. "The Trouble with QSAR (or How I Learned To Stop Worrying and Embrace Fallacy)." *Journal of Chemical Information and Modeling* 48, no. 1 (January 1, 2008): 25–26.
<https://doi.org/10.1021/ci700332k>

$$f_{\alpha}(x) = \sin^2 \left(2^{x\tau} \arcsin \sqrt{\alpha} \right)$$



Boué, Laurent. "Real Numbers, Data Science and Chaos: How to Fit Any Dataset with a Single Parameter." *ArXiv:1904.12320 [Cs, Stat]*, April 28, 2019. <http://arxiv.org/abs/1904.12320>. [GitHub Repo](#).
Also see: [Drawing an elephant with four complex parameters](#)

Generative models shed light on correlation and causality



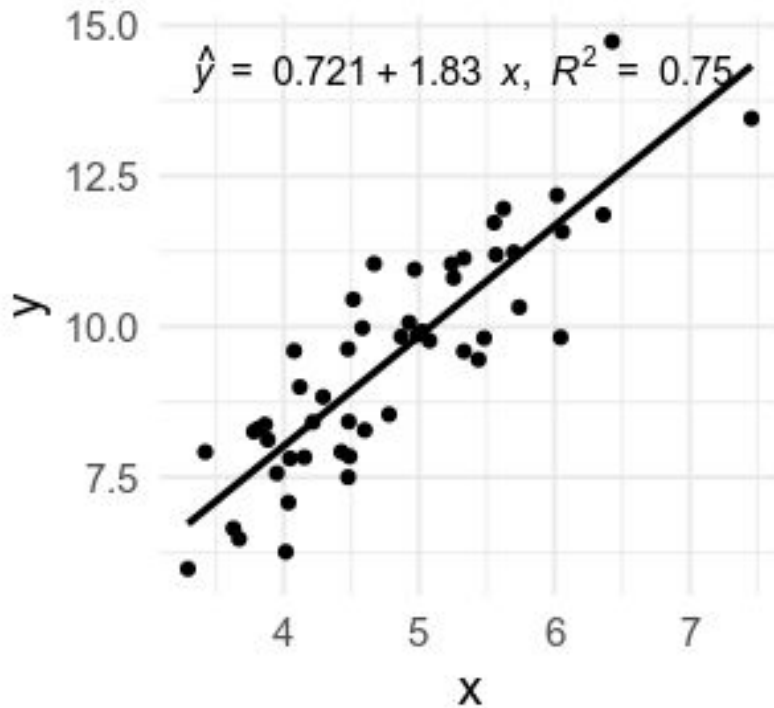
Assumptions of the **generative model**:

1. X is a random variable;
2. Every unit change of X induces a change of 2 units in Y .

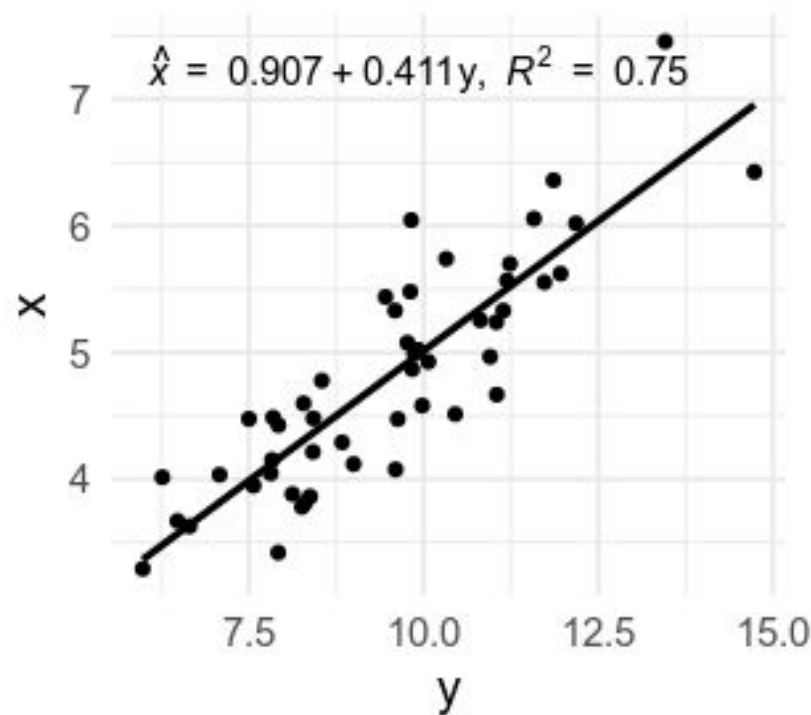
Correlation is caused by causation or confounding



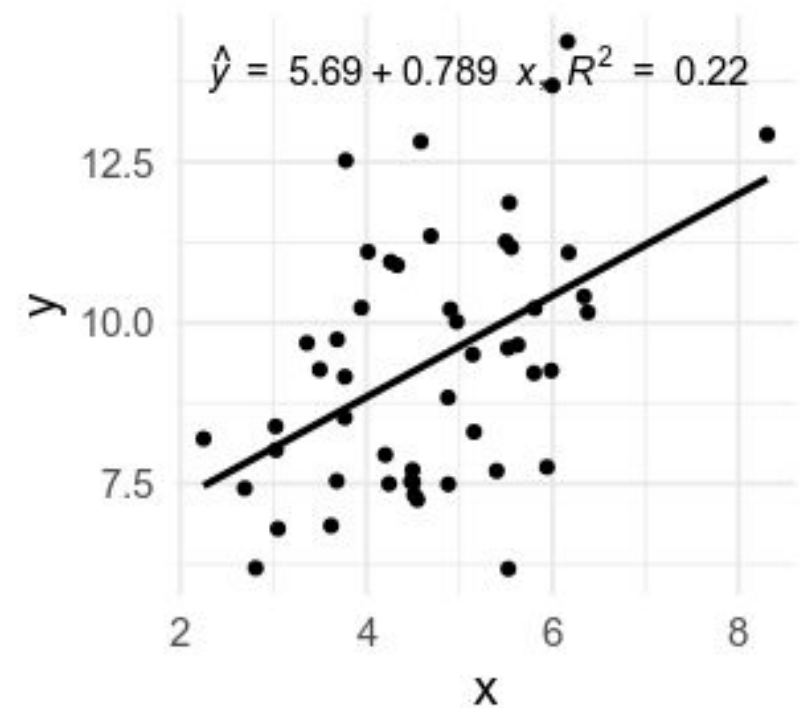
True effect: 2.0



The reverse fit

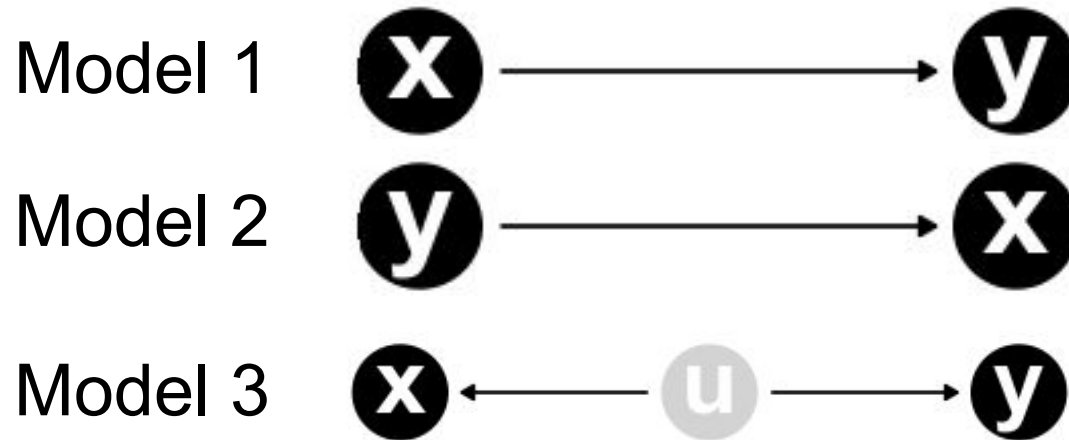


True effect: 0.0



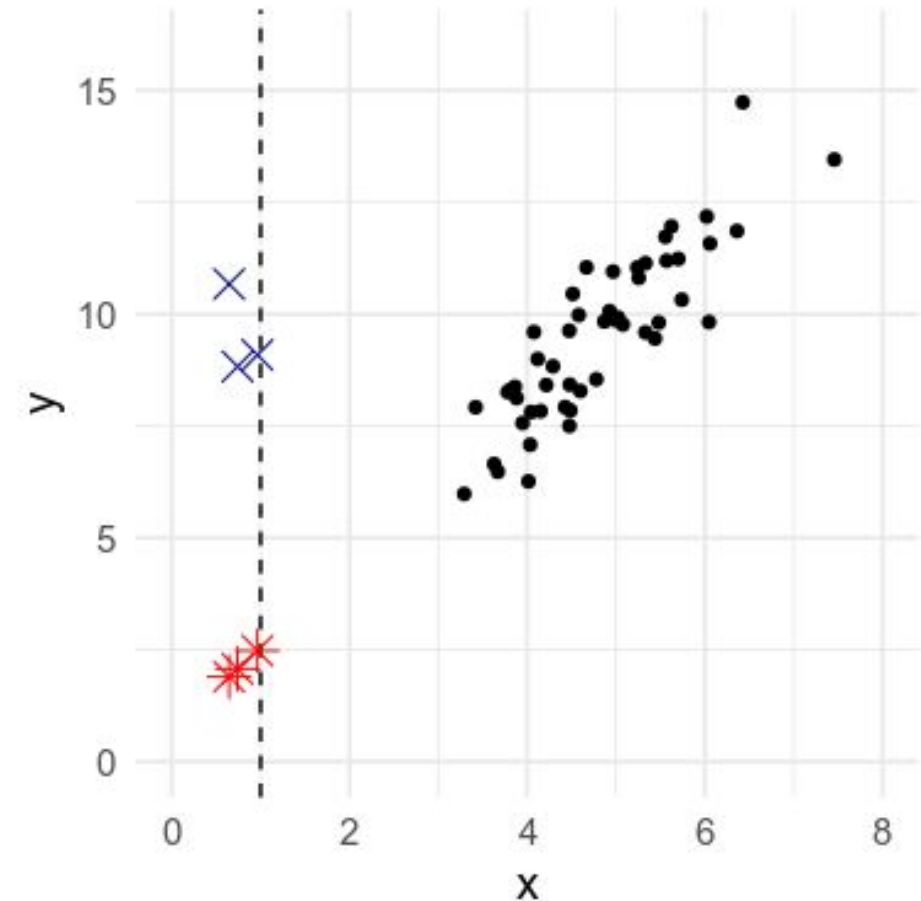
Statistical models alone cannot derive causality from correlation

We learn causality by (1) listing models explicitly and (2) manipulating a variable and observe the outcomes



Assume that the data is generated by either Model 1, or Model 2, or Model 3. And assume that we can manipulate the value of X by setting it to 1.0 (the dash line).

Question: which outcomes (red stars or blue crosses) would support which models? Why?



Conclusions

1. Statistical and machine learning (ML) models can model linear and nonlinear relationships between variables.
2. Applying statistical and ML models in drug discovery needs to consider the facts that we always work on something new, structure similarity does not warrant activity similarity, and correlation is not causation.
3. Correlation can be caused by (1) causation, (2) confounding, (3) coincidence, (4) conspiracy, (5) collider, and (6) chronology.

Relationship between Gaussian, Poisson, and exponential distributions

Histogram of #events in each time unit: Poisson distribution

H

Histogram of time intervals between events: Exponential distribution



Histogram of #events in large time intervals: Gaussian distribution

Each triangle indicates an event that happens continuously and independently from each other at a constant average rate λ . A process in which events occur so is known as a *Poisson point process*. *Histogram* in this plot means the probability histogram: the x axis contains count of the observed events, and the y axis contains count of the observed events divided by the total events.

Importantly, exponential distribution displays the property of *memoryless*. In the context of bolus PK, the *proportion* of drug degraded per time unit k is independent of previous degradation processes.