

Lecture 4: Dynamic Programming

Cheatsheet

Use this algorithm when:

- You can brute force this problem with a recursive method.
 - It's very common to use DP for problems where you need to make many decisions, or count many things.
- 1) Run a brute force by hand on a small, but not tiny input (could be the sample)
 - 2) See if you did "duplicate work"
 - 3) If you did duplicate work, it is very likely dp

Steps to using the algorithm:

Thinking about the problem:

- 1) Figure out the state
 - a) This is often the hardest step.
 - b) It's often helpful to process the input in a certain order (SORT in some order) and make your index your state.
 - c) If you're working on a decision problem, each decision is a transition, and the intermediate points between each decision is your state.
- 2) Figure out the base case and answer state
- 3) Figure out the transitions
 - a) If there are decisions, each decision is a transition

Implementation:

- 4) Create an array (or map if needed) where the index of the array is the state
- 5) Set the base cases
- 6) Find an order to look at the states in based on the transitions. Loop in that order and do the transitions
- 7) Print out the answer state

How to calculate the runtime:

(# of states) * (# of transitions) * (any extra runtime, ie if you are using a set, this will be $\log(n)$)