

Assignment 5:

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Task 1:

Level 0:

Root (+ : 115, - : 125) Entropy = - (115/240 * log2(115/240) + 125/240 * log2(125/240)) = 0.9987

pick F1: F1 = 0: (+ : 50, - : 70) Entropy = - (50/120 * log2(50/120) + 70/120 * log2(70/120)) = 0.9799

F1 = 1: (+ : 65, - : 55) Entropy = - (65/120 * log2(65/120) + 55/120 * log2(55/120)) = 0.995

IG = 0.9987 - (1/2 * 0.9799 + 1/2 * 0.995) = 0.01125

pick F2: F2 = 0: (+ : 70, - : 50) Entropy = - (70/120 * log2(70/120) + 50/120 * log2(50/120)) = 0.9799

F2 = 1: (+ : 45, - : 75) Entropy = - (45/120 * log2(45/120) + 75/120 * log2(75/120)) = 0.9544

IG = 0.9987 - (1/2 * 0.9799 + 1/2 * 0.9544) = 0.03155

pick F3: F3 = 0: (+ : 15, - : 65) Entropy = - (15/80 * log2(15/80) + 65/80 * log2(65/80)) = 0.6962

F3 = 1: (+ : 30, - : 50) Entropy = - (30/80 * log2(30/80) + 50/80 * log2(50/80)) = 0.9544

F3 = 2: (+ : 70, - : 10) Entropy = - (70/80 * log2(70/80) + 10/80 * log2(10/80)) = 0.5436

IG = 0.9987 - (1/3 * 0.6962 + 1/3 * 0.9544 + 1/3 * 0.5436) = 0.2673

pick F4: F4 = 0: (+ : 50, - : 70) Entropy = - (50/120 * log2(70/120) + 70/120 * log2(50/120)) = 0.9799

F4 = 1: (+ : 70, - : 50) Entropy = - (50/120 * log2(70/120) + 70/120 * log2(50/120)) = 0.9799

IG = 0.9987 - (0.9799) = 0.0188

So we pick F3 as attribute for Root, highest IG.

Level 1:

Now let child with $F3 = 0$ be child 1, same procedure:

child 1: (+ : 15, - : 65) Entropy = - (15/80 * log2(15/80) + 65/80 * log2(65/80)) = 0.6962

pick F1: $F1 = 0$: (+ : 5, - : 35) Entropy = - (5/40 * log2(5/40) + 35/40 * log2(35/40)) = 0.5436

$F1 = 1$: (+ : 10, - : 30) Entropy = - (10/40 * log2(10/40) + 30/40 * log2(30/40)) = 0.8113

$IG = 0.6962 - (1/2 * 0.5436 + 1/2 * 0.8113) = 0.01875$

pick F2: $F2 = 0$: (+ : 15, - : 25) Entropy = - (15/40 * log2(15/40) + 25/40 * log2(25/40)) = 0.9544

$F2 = 1$: (+ : 0, - : 40) Entropy = 0

$IG = 0.6962 - (1/2 * 0 + 1/2 * 0.9544) = 0.219$

pick F4: $F4 = 0$: (+ : 10, - : 30) Entropy = - (10/40 * log2(10/40) + 30/40 * log2(30/40)) = 0.8113

$F4 = 1$: (+ : 5, - : 35) Entropy = - (5/40 * log2(5/40) + 35/40 * log2(35/40)) = 0.5436

$IG = 0.6962 - (1/2 * 0.8113 + 1/2 * 0.5436) = 0.01875$

So for child 1 we pick F2

Now let child with $F3 = 1$ be child 2 same procedure:

child 2: (+ : 30, - : 50) Entropy = - (30/80 * log2(30/80) + 50/80 * log2(50/80)) = 0.9544

pick F1: $F1 = 0$: (+ : 15, - : 25) Entropy = - (15/40 * log2(15/40) + 25/40 * log2(25/40)) = 0.9544

$F1 = 1$: (+ : 15, - : 25) Entropy = - (15/40 * log2(15/40) + 25/40 * log2(25/40)) = 0.9544

$IG = 0.9544 - 0.9544 = 0$

pick F2: $F2 = 0$: (+ : 15, - : 25) Entropy = - (15/40 * log2(15/40) + 25/40 * log2(25/40)) = 0.9544

$F2 = 1$: (+ : 15, - : 25) Entropy = - (15/40 * log2(15/40) + 25/40 * log2(25/40)) = 0.9544

$IG = 0.9544 - 0.9544 = 0$

pick F4: $F4 = 0$: (+ : 10, - : 30) Entropy = - (10/40 * log2(10/40) + 30/40 * log2(30/40)) = 0.8113

$F4 = 1$: (+ : 20, - : 20) Entropy = - (20/40 * log2(20/40) + 20/40 * log2(20/40)) = 1

$IG = 0.9544 - (1/2 * 0.8113 + 1/2 * 1) = 0.04875$

So for child 2 we pick F4

Now child with F3 = 2 be child 3 same procedure:

child 3: (+ : 70, - : 10) Entropy = - (70/80 * log₂(70/80) + 10/80 * log₂(10/80)) = 0.5436

pick F1: F1 = 0: (+ : 30, - : 10) Entropy = - (30/40 * log₂(30/40) + 10/40 * log₂(10/40)) = 0.8113

F1 = 1: (+ : 40, - : 0) Entropy = 0

IG = 0.5436 - (1/2 * 0.8113) = 0.13795

pick F2: F2 = 0: (+ : 40, - : 0) Entropy = 0

F2 = 1: (+ : 30, - : 10) Entropy = - (30/40 * log₂(30/40) + 10/40 * log₂(10/40)) = 0.8113

IG = 0.5436 - (1/2 * 0.8113) = 0.13795

pick F4: F4 = 0: (+ : 30, - : 10) Entropy = - (30/40 * log₂(30/40) + 10/40 * log₂(10/40)) = 0.8113

F4 = 1: (+ : 40, - : 0) Entropy = 0

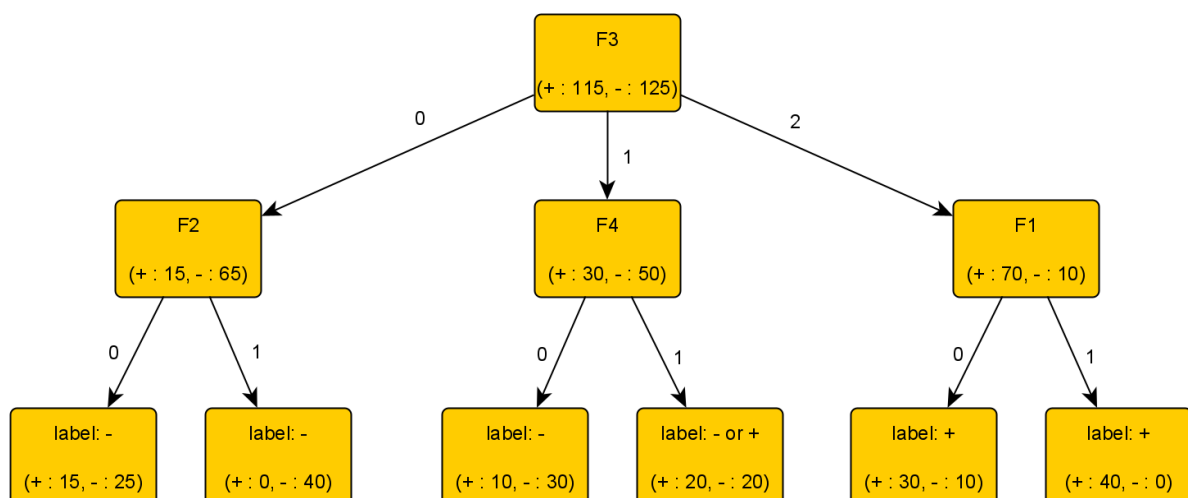
IG = 0.5436 - (1/2 * 0.8113) = 0.13795

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So for child 3 it does not matter, we just pick F1 here

Level 2:

Each of the three nodes from level 1 has two child nodes. Their label and the number of samples for this node can be seen in the Calculations for level 1 and in the picture of the tree. For the right child of node F4 either – or + can be chosen, both choices yield the same prediction error.



Error = ((15 + 10 + 20 + 10)/240) = 55/240 = 11/48 = 0,229. The tree can be simplified to the tree seen below without any impact on the prediction error.

