

## Crout Factorization

- 1) Ask the user for a matrix A. Needs to be a squared matrix.
- 2) Ask the user for vector b and make sure that is the same length as matrix A, and ask for a whole number n.
- 3) Next, we create 2 more matrices, we call them L and U. Matrices L and U need to have the following characteristics
  - a) Have the same size as matrix A
  - b) L will have the same elements that are below the diagonal in A but with the opposite sign. The diagonal in L will be the same as A, and all other elements will be 0.
  - c) U will have the same elements in A that are above the diagonal with opposite signs, and will have the same elements in the diagonal as A and the rest of the elements will be 0.
- 4) Time for a cycle
  - a) For  $k = 1 < n$ , with 1 step ( $k++$ )
    - (i)  $sum1 = 0$
    - (ii) For  $p = 1 < k-1$ , with 1 step ( $p++$ )
    - (iii)  $sum1 = sum1 + L_{kp} * U_{kp}$
    - (iv)  $L_{kk} = \sqrt{a_{kk} + sum1}$
    - (v) For  $i = k+1 < n$ , with 1 step ( $i++$ )
    - (vi)  $sum2 = 0$ 
      - (1) For  $r = 1 < k-1$ , with 1 step ( $r++$ )
      - (2)  $sum2 = sum2 + L_{ir} * U_{rk}$
    - (vii)  $L_{ik} = (a_{ik} - sum2)$
  - b) For  $j = k+1 < n$ , with 1 step ( $j++$ )
    - (i)  $sum3 = 0$ 
      - (1) For  $s = 1 < j-1$ , with 1 step ( $s++$ )
        - (A)  $sum3 = sum3 + L_{ks} * U_{sj}$
        - (B)  $U_{kj} = (a_{kj} - sum3) / L_{kk}$
- 5)  $z =$  progressive substitution (1,b)  $x =$  regressive substitution (u,z)
- 6) Regressive Replacement
  - a) Para  $i = n < 1$ , with 1 step ( $i++$ )

- (i)  $\text{sum} = 0$
- (1) for  $j = i + 1 < n$  , with 1 step (j++)
- (A)  $\text{sum} = \text{sum} + a_{ij} * x_{ij}$
- (2)  $x_i = (a_{in+1} - \text{sum}) / a_{ii}$

7) Progressive replacement

- a) Para  $i = 1 < n$  , with 1 step (i++)
- (i)  $\text{sum} = 0$
- (1) for  $j = i + 1 < n$  , with 1 step (j++)
- (A)  $\text{sum} = \text{sum} + a_{ij} * x_{ij}$
- (2)  $x_i = (a_{in+1} - \text{sum}) / a_{ii}$