

## Cholesky Factorization

- 1) Ask the user for a matrix A. Needs to be a squared matrix.
- 2) Ask the use for vector b and make sure that is the same length as matrix A, and a whole number n.
- 3) Next, we create 2 more matrices, we call them L and U. Matrices L and U need to have the following characteristics
  - a) Have the same size as matrix A
  - b) L will have the same elements that are below the diagonal in A but with the opposite sign. The diagonal in L will be the same as A, and all other elements will be 0.
  - c) U will have the same elements in A that are above the diagonal with opposite signs, and will have the same elements in the diagonal as A and the rest of the elements will be 0.
- 4) Time for a cycle
  - a) For  $k = 1 < n$ , with 1 step increments ( $k++$ )
    - (i)  $sum1 = 0$ 
      - (1) For  $p = 1 < k-1$ , with 1 step increments ( $p++$ )
        - (A)  $sum1 = sum1 + L_{kp} * U_{kp}$
        - (2)  $L_{kk} = \sqrt{a_{kk} - sum1}$
      - (ii) For  $i = k+1 < n$ , with 1 step increments ( $i++$ )
        - (1)  $sum2 = 0$
        - (2) For  $r = 1 < k-1$ , with 1 step increments ( $r++$ )
          - (A)  $sum2 = sum2 + L_{ir} * U_{rk}$
          - (B)  $L_{ik} = (a_{ik} - sum2) / U_{kk}$
        - (iii) For  $j = k+1 < n$ , with 1 step increments ( $j++$ )
          - (1)  $sum3 = 0$
          - (2) For  $s = 1 < s-1$ , with 1 step increments ( $s++$ )
            - (A)  $sum3 = sum3 + L_{ks} * U_{sj}$
            - (B)  $U_{kj} = (a_{kj} - sum3) / L_{kk}$
    - 5)  $z =$  progressive replacement (1,b)  $x =$  regressive replacement (u,z)
    - 6) Regressive Replacement
      - a) Para  $i = n < 1$ , with 1 step increments ( $i++$ )
        - (i)  $sum = 0$

(1) for  $j = i + 1 < n$  , with 1 step increments ( $j++$ )

(A)  $\text{sum} = \text{sum} + a_{ij} * x_{ij}$

(2)  $x_i = (a_{in+1} - \text{sum}) / a_{ii}$

## 7) Progressive Replacement

a) Para  $i = 1 < n$  , with 1 step increments ( $i++$ )

(i)  $\text{sum} = 0$

(1) for  $j = i + 1 < n$  , with 1 step increments ( $j++$ )

(A)  $\text{sum} = \text{sum} + a_{ij} * x_{ij}$

(2)  $x_i = (a_{in+1} - \text{sum}) / a_{ii}$