

Insert Dissertation Title Here

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School of Computing Final Year Research Project

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Abstract

No more than 300 words summarizing this dissertation.

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Introduction

1.1 Overview

Stock markets are often thought to be irrational or in some cases random, which suggests that markets are not made based on fundamental factors alone. In a 1996 speech, former Federal Reserve chair, Alan Greenspan questioned "... how do we know when irrational exuberance has unduly escalated asset values ..." (Greenspan, 1996), suggesting that there may be psychological factors that affect markets such as positive feedback loops.

This project intends to identify if a stock market index's price can be predicted ahead of time, and which factors contribute the most to an accurate prediction. The intended audience for such a project can vary from the institutional to the retail investor to identify opportunities in the market by using only publicly available data rather than proprietary information.

1.2 Aims

This project aims to produce an artificial intelligence model that attempts to predict the following day's price of a stock market index. This will allow the project to research if a stock market index's price can be predicted from the day prior; the factors which affect a stock market index's price and which factors are most important in predicting a stock market index's price.

1.3 Objectives

The objectives are as follows:

- Identifying key factors that can affect stock market performance.
- Collecting above mentioned factors, where the historical data is publicly available and free to use (either public domain, non-commercial licenses, etc).
- Transforming collected data into normalised, or otherwise modified, data that can easily be used to identify patterns, either by humans or by computational neural networks.
- Identifying and applying correct techniques to train a computational neural network (or other suitable technology) to understand which factors are most important when predicting stock market performance.
- Filtering through training data to ensure there are no biases in play.
- Ensuring that the network will be efficient enough to be trained on hardware that is available today, and if possible on consumer hardware such as Nvidia RTX 3000 series GPUs.
- Understanding outputs of the computational neural networks and presenting the output data learned in a way that is clear.
- Interpreting overall results to identify if it is possible to predict a stock market's index direction and/or price for any given day
- Evaluating the results to identify accuracy, limitations and biases

1.4 Constraints

- May be difficult / expensive to get historical data
- May be difficult / expensive to get reliable data
- Access to currently publicly available data may be removed, or otherwise unavailable
- May not have the correct technical skills to sufficiently carry out the projects
- May not have sufficient time to carry out the full objectives of the project
- Hardware available may not be feasible to run / train complex neural networks on

Even if the project was successful for now, it may not be suitable for these reasons:

- May not work in extreme market events
- May not work if new market measures are placed
- May not work if new economic measures are placed
- Access to reliable data may be restricted, removed or otherwise unavailable in the future

Literature Review

Keywords. artificial intelligence, stock market

2.1 Introduction

As the world advances in technology, an increasing number of decisions are dependent on computational models; including financial decisions. This includes, but is not limited to, decisions for money management, risk management, economics, and investing. This literature review will discuss: the feasibility of predicting stock market prices; different artificial intelligence research methods used in financial modelling, particular those that relate to investing and stock market indices; and the different input features used in these models.

2.2 Feasibility of predicting stock market index prices

2.2.1 Efficient Market Hypothesis

Over the year, many people have attempted to predict stock markets in order to profit from price movements as they occur. However, some have theorised that it is not possible to accurately predict prices due to the there being an innumerable number of factors that can affect a stock market, and these factors would already be a function of the current market's price, therefore make it impossible to forecast the price. (Bachelor, 1900, p. 1) This is the basis of the Efficient Market Hypothesis, where an asset price fully reflects the information that is available at any given time.

2.2.2 Empirical evidence of market (in)efficiencies

A 1973 book explains the term 'random walk' as "A random walk is one in which future steps or directions cannot be predicted on the basis of past actions", and continues to describe how when applied to the stock market that "short-run changes in stock prices are unpredictable. [and] Investment advisory services, earnings forecasts, and complicated chart patterns are useless" (Malkiel, 1973, p. 24). A reflection paper by the same author 30 years on, attempts to validate that the efficient market hypothesis still holds true in the 21st century by comparing actively managed funds to tracker funds: suggesting that markets are likely efficient, due to the fact that most actively managed funds are outperformed by a index tracker fund that follows the S&P 500 index; the data presented suggests that most experts (68% to 90% over various time periods) cannot outperform the index whether it be from a one year, three year, five year, ten year or twenty year holding period leading up to 31st December, 2003 (Malkiel, 2005). The author suggests that if markets were inefficient, fund managers should easily be able to outperform the index.

In order to prove, or disprove, the Efficient Market Hypothesis, many studies have been carried out with varying results. In this literature review we will focus on the US markets and the different results the studies have found. Using data from 1964 to 2003 for the US stock market, one study has found markets to be efficient using a threshold autoregressive model and a unit root process (Narayan, 2006). Another empirical look into equity premium prediction, that looks specifically at the US S&P 500 index, using various regression models with additional variables described such as dividends, earnings price ratio, book value, net issuing activity and more has concluded that "the equity premium has not been predictable" (Goval & Welch, 2004, abstract) which would agree with the efficient market hypothesis.

However, other recent studies have suggested the efficient market hypothesis may not hold true. A paper that looks into returns of the US Dow Jones Industrial Average (DJIA) index from 1928 to 2012 showed that while for autocorrelation tests on daily and weekly intervals suggest market efficiency, the same cannot be said for monthly and annual intervals (although the degree of correlation is low). Furthermore, the paper posits that autocorrelation tests are not sufficient to determine dependencies, and puts forwards another type of test called 'run tests' to show that markets are also inefficient in daily and weekly intervals (Sewell, 2012). Another paper that analyses data from 1999 to 2007 of various markets, including the US as well as other developed and developing countries, using a unit root process has stated that their findings show that "real stock price indices are stationary processes that are inconsistent with the efficient market hypothesis" (Lee et al., 2010, p. 1).

2.3 Types of artificial intelligence methods used

2.3.1 Description of artificial intelligence methods

Various artificial intelligence methods have been utilised in order to predict daily direction as well as price of stock markets, the following are described here:

- Multilayer Perceptrons (MLPs)
- Convolutional Neural Networks (CNNs)
- Support Vector Machines (SVMs)
- Long Short Term Memory (LSTM)
- Hybrid approaches

Multilayer Perceptrons (MLPs)

Multilayer Perceptrons (MLPs - Figure 2.1) are a class of artificial neural networks. They contain multiple layers of perceptrons, including an input layer, one or many hidden layers and an output layer. They are feed-forward networks meaning that data is only passed to the next layer and does not move backwards. It is an example of a supervised neural network as labelled data is used in training.

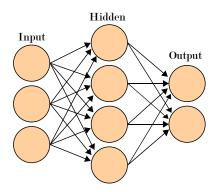


Figure 2.1: Diagram of a Multilayer Perceptron; adapted from Artificial neural network.svg, Wikimedia, Cburnett

Convolutional Neural Networks (CNNs)

Convolutional Neural Networks (CNNs - Figure 2.2) are a class of artificial neural networks. They contain multiple layers; including an input layer, one or many convolutional and pooling layers, and an output layer. The convolutional and pooling layers are inspired by biological processes; each layer extracts and summarises certain features and convolves the input and passes to the next layer. The pooling layers are using to reduce the spatial size of the data by combining outputs in order to optimise the network for performance.

They are feed-forward networks meaning that data is only passed to the next layer and does not move backwards. It is an example of a supervised neural network as labelled data is used in training.

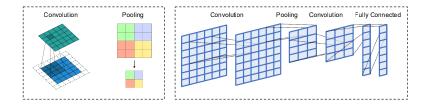


Figure 2.2: Diagram of a Convolutional Neural Network; (Maier et al., 2019)

Support Vector Machines (SVM)

Support Vector Machines (SVMs - Figure 2.3) are a class of machine learning models that are used in classification of data. In this model, the training data is used in order to identify a decision boundary, known as a hyperplane that separates the classifications of data. It is an example of a supervised machine learning model as labelled data is used in training.

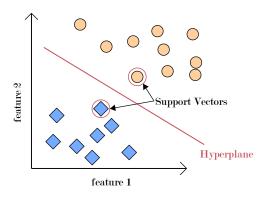


Figure 2.3: Diagram of a Support Vector Machine

Long Short Term Memory (LSTM)

Long Short Term Memory (LSTM - Figure 2.4) is a class of artificial neural networks. They are recurrent networks meaning that data is not necessarily fed-forward as they allow for loops within the network. LSTMs contain cells with 'gates' that allow them to keep context and control the flow of data, as well as make decisions to keep or discard data in order to make predictions. It is an example of a supervised neural network as labelled data is used in training.

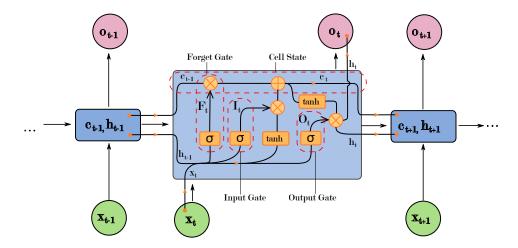


Figure 2.4: Diagram of a Long Short Term Memory Unitadapted from Long Short-Term Memory.svg, Wikimedia, fdeloche

Hybrid Approaches

Hybrid approaches can be utilised in order to overcome shortcomings in certain models. A hybrid approach can utilise any number of different models; for example a CNN-LSTM hybrid model will use CNN and LSTM layers as a CNN may be a good model for classification problems, an LSTM is better suited to time series data.

2.3.2 Artificial intelligence methods used in previous studies

Different studies have utilised different artificial intelligence models to predict the price of stock market indices, with varying degrees of accuracy.

One study using multilayer perceptrons (MLP) to predict the daily direction of an exchange traded fund (ETF) that tracks the US S&P 500 stock market index suggests that the model has an accuracy of up to 60% (Zhong & Enke, 2019). Whereas another study has suggested they can predict the price, not just direction, of the same stock market index with an accuracy of 76% using support vector machines (SVMs) and reinforcement learning

(Shen et al., 2012). As there is a difference of 16%+ in of accuracy in the same stock market index (S&P 500), and the higher accuracy model suggests that support vector machines may provide an improvement over feed-forward neural networks such as MLPs. Another study comparing the performance of MLPs and SVMs agrees that SVMs are superior as, even though both models were able to predict the direction of the S&P 500 index, the MLP model had a maximum error difference of 15% over a 45 day period, whilst the SVM model had a maximum error difference of 6% in their test cases(Sheta et al., 2015). This is further supported by another study comparing various artificial intelligence methods on the Indian Nifty50 index with the SVM model outperforming a back-propagation neural network model, which is somewhat similar to the MLP model, by 5.51% (Kumar & Thenmozhi, 2006).

Further studies have been done on using hybrid approaches to predict stock markets. One study using an approach with a convolutional neural network (CNN) and three long short-term memory (LSTM) networks found that the accuracy of predicting weekly directions of the S&P 500 index was 66.6%, which was greater than with SVMs or CNNs alone, with those models achieving 62.0% and 59.3% respectively (Hao & Gao, 2020). Another study agrees with these findings, with their results also suggesting a model built with CNNs and bi-directional LSTMs are able to outperform SVMs (Eapen et al., 2019). However, the same cannot be said for all types of hybrid neural network models; one study comparing MLPs and hybrid networks on the US Nasdaq index has found that the MLP performs better, albeit slightly with a difference of 0.26% in mean absolute deviation, than an approach with a hybrid model of MLP and Generalized Auto-Regressive Conditional Heteroskedasticity (GARCH) (Guresen et al., 2011).

2.4 Input features for intelligence methods

The studies mentioned in the previous section use different input features for their studies; where the amount of input features ranges from just a single type of input to many various macro-economic factors. One of the hybrid approaches has only stated using the 'daily closing price dataset of the S&P 500 index' in their CNN-LSTM model (Hao & Gao, 2020). Another study using the hybrid approach slightly expands on this by using additional factors related to the index: the opening and closing prices of the S&P 500 index, the low and high prices of the day, and the trading volume. However, these studies have not considered any macro-economic factors. One study expands on this further by also including other indexes across the world as inputs, as well as various currency rates in addition to commodities such as oil and metals (Shen et al., 2012). Other studies expand on this further, for example one study with 27 input features also includes US Treasury yield rates and bond yields (Sheta et al., 2015) and another looks into additional factors for a total of 60 input features including certificate of deposit rates, and term and default spreads (Zhong & Enke, 2019) - though the latter study explains that with principal component analysis, the model peaked in terms of accuracy with 31 input features.

2.5 Conclusion

To conclude, there are differing opinions on whether or not markets are efficient, and therefore whether or not they are predictable. Some economists use the fact that experienced fund managers are rarely able to beat the market as proof that markets are efficient, and there are studies that agree with this hypothesis. However, there are also other studies that disagree presenting their findings that show there is some evidence of market inefficiencies in either the short term or long term.

Regardless of markets being efficient or not, numerous artificial intelligence methods – including MLPs, SVMs, CNNs as well as hybrid approaches using CNNs and LSTMs – have been employed to varying degrees of success. While some studies look at predicting just the direction, and others attempt to predict the price, most have claimed to be able to do so with above 50%

accuracy. From the studies researched here, it can be assumed that in general hybrid approaches involving CNNs and LSTMs outperform SVMs, which outperform MLPs.

These studies use a diverse set of input features in order to build their models, with some using features only directly related to the index and some using extended datasets including inputs from macroeconomic sources in order to build models that take account external factors that may affect the index's price, though there is evidence to suggest that not all of the input features are required to build a good model to predict the price of an index.

Research Questions

3.1 Predicting a stock market index's direction

Question Is it possible to accurately predict a stock market index's (S&P 500) direction for the following day with the CNN-LSTM model?

Sub Questions

- If so, what is the accuracy of the model?
- If not, what limitations affected the model to cause it to be inaccurate?
- Can the findings of this question be used to prove/disprove the efficient market hypothesis?

Importance The findings from this research question will have significant impact in making investment and trading decisions for participants of the market, potentially giving indicators of when to buy / sell into the stock market in order to outperform the market. Furthermore, depending on the accuracy of the model, it may be able to be used as evidence for or against the efficient market hypothesis.

3.2 Predicting a stock market index's price

This question assumes that it is at least somewhat possible to accurately predict the stock market index's direction based on literature review and other studies.

Question Is it possible to accurately predict a stock market index's (S&P 500) price for the following day with the CNN-LSTM model?

Sub Questions

- If so, what is the accuracy of the model?
 - How close is it to the true values?
 - Are there any significant outliers?
 - * If so, what are potential causes?
- If not, what limitations affected the model to cause it to be inaccurate?

Importance The findings from this research question will have significant impact in making investment and trading decisions for participants of the market, potentially giving indicators of when to buy / sell into the stock market in order to outperform the market. Furthermore, depending on the accuracy of the model, it may be able to be used as evidence for or against the efficient market hypothesis.

3.3 History of training data

This question assumes that it is at least somewhat possible to accurately predict the stock market index's direction/price based on literature review and other studies.

Question How do different lengths of time as history in the training data affect the model?

Sub Questions

• What is the ideal length of time to be used in the training data?

• What are potential reasons for this length of time being the most useful?

Importance The findings from this research question will allow optimal algorithms / models to be created in order to avoid wasting computational time that may cause the model to not improve, or even decrease in accuracy. Furthermore, this will be of help to participants of the market to make better informed manual decisions by understanding which time horizons to look at.

3.4 Most important input features

This question assumes that it is at least somewhat possible to accurately predict the stock market index's direction/price based on literature review and other studies.

Question What are the most important input features that affect the model? **Sub Questions**

- How much do each of these input features contribute to the model?
- Do any of the input features identified have negligible impact to the model?
- What are the potential reasons these features do / do not impact the model?

Importance The findings from this research question will allow optimal algorithms / models to be created in order to avoid wasting computational time that may cause the model to not improve, or even decrease in accuracy. Furthermore, this will be of help to participants of the market to make better informed manual decisions by understanding which factors to look at.

Research Design

4.1 Research method

The research methodology is one based on the literature review (chapter 2); the research already carried out in other studies informed the the decision making process behind the requirements of the supporting artefact. Various artificial intelligence models have been analysed and critiqued; as well as the input features used within these models.

These aspects combined are used to inform the variables - such as model used, input features (and their time horizons) - to experiment with to better understand which variables are most important and have the ability to provide the most accurate results.

4.2 Research process

4.2.1 Comparison of AI models in previous studies

From the literature review, various AI models were identified. These include Multilayer Perceptrons (MLPs), Convolutional Neural Networks (CNNs), Support Vector Machines (SVMs), Long Short Term Memory (LSTM) and

hybrid approaches. From this, we can understand which models can have greater accuracy. The review has found a hybrid approach has the greatest accuracy. CNNs and SVMs have a similar degree of accuracy and generally outperform MLPs.

Artificial Intelligence Model	Ease of Implementation	Accuracy of Output
Multilayer Perceptrons	5	3
Convolutional Neural Networks	3	4
Support Vector Machines	3	4
Hybrid (CNN + LSTM)	2	5

Table 4.1: Table rating different AI models on a scale of 1 to 5 based on ease of implementation as well as accuracy

4.2.2 Comparison of input features used in previous studies

Currently, based on the studies in the literature review, it is difficult to suggest which input features are most important for an accurate output. This is due to the studies using more complex datasets as input features generally use a different research model

This is one of the primary research questions identified, and this project intends to answer this question. The previous studies use the following input features; a subset of the features will be used and compared within this project.

- Daily Closing Price
- Low Price
- High Price
- Volume
- Currency Rates

- Commodities (e.g. Oil)
- Treasury Rates
- Stock indices of other countries
- Individual Stocks
- Certificate of Deposits
- Term spreads

4.3 Research outcomes

As CNN+LSTM hybrid approaches have already been proven in previous studies to be an accurate research model, this model should be used within the artefact of this project. However, the effect of different input features on a single research model has not been well identified. This will be a primary area of focus for the supporting artefact to look into. Ideally, this will allow the supporting artefact to have greater than 65% accuracy in predicting the daily price direction.

4.4 Requirements of the artefact

4.4.1 Functional requirements

Based on the literature review, the most accurate models for predictting stock prices had an accuracy of approximately 60% (Zhong & Enke, 2019). While there is an example of a study shown with a greater accuracy of 76% (Shen et al., 2012), another similar study places the accuracy of the model at 59.3% - albeit for weekly predictions rather than daily (Hao & Gao, 2020); thus 60% is considered the current baseline.

Also, due to the fact that this research project attempts to identify the most important input features, as well as the sequence length, they are key requirements of this project.

Predicting the exact return (daily relative price change) per day is an optional requirement due to two reasons: it does not significantly help market participants compared to knowing the direction alone; and it may be more cumbersome / time-consuming for a relatively low significant output for end users.

Necessary requirements

- Predict daily price direction with 65%+ accuracy
- Identify which input features are most important
- Identify what sequence length (number of days of history of each input feature) is optimal
- Display charts of the various models' accuracies to allow user to visualise and compare each model

Optional requirements

Based on the literature review, a study suggested it had been able to accurately predict prices with a mean absolute deviation of 2.516% on the testing data set when compared to the true price.

 \bullet Predict daily price return with a mean absolute deviation of 2.5% or lower

4.4.2 Non-functional requirements

The performance artefact is not time critical due to there being a large time period 17 hours and 30 minutes between market close (4:00 PM ET) and market open (9:30 AM ET) of stock exchanges in the USA; however this may not be ideal for users thus the following non-functional requirements have been identified.

- The artefact should take less than 5 minutes to run per model chosen (on modern GPUs)
- ullet The artefact should allow the user to choose which input features to include with less than 1 click per feature + 1 for entering selection window
- The artefact should allow the user to choose the sequence lengths to include with less than 1 click per sequence length + 1 for entering selection window

Artefact Design

5.1 Development decisions

5.1.1 Software development life cycle

The Agile software development life cycle will be utilised in this project; and this project will be separated into various iterations of design, development, and testing

5.1.2 Software languages / platforms / environments

Python Tensorflow Jupyter Notebook

- 5.2 Data collection
- 5.3 Assumptions made
- 5.4 Data normalisation
- 5.5 Iteration 1
- 5.5.1 Artificial intelligence model used
- 5.5.2 Sequence length used
- 5.5.3 Input features
- 5.5.4 Accuracy of iteration 1
- 5.5.5 Limitations of iteration 1

Results

Evaluation

Project Management

Conclusion

Future Work

References

- Bachelor, L. (1900). Speculation theory. 3rd series, 17, 21–86. https://doi.org/10.24033/asens.476
- Eapen, J., Bein, D., & Verma, A. (2019). Novel deep learning model with cnn and bi-directional lstm for improved stock market index prediction. 2019 IEEE 9th Annual Computing and Communication Workshop and Conference (CCWC), 0264–0270. https://doi.org/10.1109/CCWC.2019.8666592
- Goval, A., & Welch, I. (2004). A comprehensive look at the empirical performance of equity premium prediction. *NBER Working Paper Series*, 10483. https://doi.org/10.3386/w10483
- Greenspan, A. (1996). The challenge of central banking in a democratic society [Remarks by Chairman Alan Greenspan at the Annual Dinner and Francis Boyer Lecture of The American Enterprise Institute for Public Policy Research, Washington, D.C. [Accessed: 2021 10 29]]. http://www.federalreserve.gov/boarddocs/speeches/1996/19961205.htm
- Guresen, E., Kayakutlu, G., & Daim, T. U. (2011). Using artificial neural network models in stock market index prediction. *Expert Systems with Applications*, 38(8), 10389–10397. https://doi.org/https://doi.org/10.1016/j.eswa.2011.02.068
- Hao, Y., & Gao, Q. (2020). Predicting the trend of stock market index using the hybrid neural network based on multiple time scale feature learning. Applied Sciences, 10(11), 3961. https://doi.org/10.3390/app10113961

- Kumar, M., & Thenmozhi, M. (2006). Forecasting stock index movement: A comparison of support vector machines and random forest. *Indian institute of capital markets 9th capital markets conference paper*.
- Lee, C.-C., Lee, J.-D., & Lee, C.-C. (2010). Stock prices and the efficient market hypothesis: Evidence from a panel stationary test with structural breaks. *Japan and the World Economy*, 22(1), 49–58. https://doi.org/https://doi.org/10.1016/j.japwor.2009.04.002
- Maier, A., Syben, C., Lasser, T., & Riess, C. (2019). A gentle introduction to deep learning in medical image processing. *Zeitschrift für Medizinische Physik*, 29(2), 86–101. https://doi.org/10.1016/j.zemedi.2018.12.003
- Malkiel, B. G. (2005). Reflections on the efficient market hypothesis: 30 years later. Financial Review, 40(1), 1–9. https://doi.org/https://doi.org/10.1111/j.0732-8516.2005.00090.x
- Malkiel, B. G. (1973). A random walk down wall street: The time-tested strategy for successful investing. W.W. Norton; Company.
- Narayan, P. K. (2006). The behaviour of us stock prices: Evidence from a threshold autoregressive model. *Mathematics and computers in simulation*, 71(2), 103–108.
- Sewell, M. V. (2012). The efficient market hypothesis: Empirical evidence.

 International Journal of Statistics and Probability, 1(2). https://doi.
 org/10.5539/ijsp.v1n2p164
- Shen, S., Jiang, H., & Zhang, T. (2012). Stock market forecasting using machine learning algorithms. Retrieved December 8, 2021, from http://cs229.stanford.edu/proj2012/ShenJiangZhang-StockMarketForecastingusingMachineLearnpdf
- Sheta, A., Ahmed, S., & Faris, H. (2015). A comparison between regression, artificial neural networks and support vector machines for predicting stock market index. *International Journal of Advanced Research in Artificial Intelligence*, 4, 55–63. https://doi.org/10.14569/IJARAI. 2015.040710

Zhong, X., & Enke, D. (2019). Predicting the daily return direction of the stock market using hybrid machine learning algorithms. Financial Innovation, 5. https://doi.org/10.1186/s40854-019-0138-0

Appendix A

First Appendix