

3D Terrain with Level of Detail

Written report for the module BTI3041 – Project 2 by

Amar Tabakovic

Bern University of Applied Sciences Engineering and Information Technology Computer Perception & Virtual Reality Lab

> Supervisor Prof. Marcus Hudritsch

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Abstract

Rendering terrains is a central task for video games, geographic information systems and simulators, but also computationally expensive. Optimizations, one of which is the level of detail (LOD), are necessary in order to ensure appropriate performances. This project aims to give an overview of the topic of terrain rendering. As part of this project, a demo terrain renderer (ATLOD) was implemented in C++ and OpenGL. ATLOD currently supports naive brute-force rendering, GeoMipMapping, TODO.

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Introduction

In the field of 3D computer graphics, rendering is one of the central tasks. Many practical applications of 3D computer graphics make use of terrains, such as flight simulators, open-world video games, and Geographic Information Systems (GIS) [1, p. 185]. At the same time, rendering large and constantly visible objects, such as the terrain, is computationally expensive and optimizations are necessary in order to avoid performance deficiencies.

One area which offers potential for optimizations is the *level of detail (LOD)* of objects. The concept of LOD is based on the idea that the farther away an object is, the fewer details are going to be visible to the human eye.

The problem of rendering terrains spawned numerous algorithms and approaches specifically for this purpose.

1.1 Goals of this Project

The main goal of this project is to gain an overview over the field of terrain LOD, in theory as well as in practice. This includes introducing the basics of terrain programming, analyzing and comparing existing approaches and algorithms, and researching what approaches are used in the real world. For this purpose, a terrain demo application (named ATLOD) is developed in C++ and OpenGL.

1.2 Structure of the Report

This report is structured as follows:

- Chapter 2 gives an overview of work that has already been conducted in the area of terrain LOD and relevant literature for this project.
- Chapter 3 Lists a few real-world examples where terrain LOD is being used, such as game engines or geographic information systems.
- Chapter 4 introduces the reader to various approaches for terrain LOD, beginning with some basic background information on terrain modelling

and LOD approaches in general. Afterwards, a selection of algorithms are presented, including ROAM, GeoMipMapping, Quadtrees, Geometry Clipmaps, CDLOD. The algorithms are presented in a high-level manner and in chronological order of their publication date.

- Chapter 5 describes ATLOD, the demo application for terrain rendering implemented as part of this project. An overview of the functionalities is given and the main approaches and design decisions are discussed. The implemented algorithms are analyzed in depth.
- Chapter 6 TODO
- Chapter 7 TODO

Existing Work and Literature

2.1 Research Articles and Publications

Terrain LOD is a well-researched topic and over the last three decades, numerous approaches have been published. In the following, some of the most important publications are listed in chronological order. The approaches that are described in more detail in chapter "Algorithms and Approaches for Terrain LOD" are highlighted in **bold**:

- "Real-Time, Continuous Level of Detail Rendering of Height Fields" [2] by Lindstrom *et al.* in 1996.
- "ROAMing Terrain: Real-time Optimally Adapting Meshes" [3] by Duchaineau *et al.* in 1997.
- "Real-Time Generation of Continuous Levels of Detail for Height Fields" [4] by Röttger *et al.* in 1998.
- "Fast Terrain Rendering Using Geometrical MipMapping" [5] by de Boer in 2000.
- "Rendering Massive Terrains using Chunked Level of Detail Control" [6] by Ulrich in 2002.
- "Geometry Clipmaps: Terrain Rendering Using Nested Regular Grids" [7] by Hoppe and Losasso in 2004.
- "Continuous Distance-Dependent Level of Detail for Rendering Heightmaps (CDLOD)" [8] by Strugar in 2009.
- "Concurrent Binary Trees (with application to longest edge bisection)" TODO cite by Dupuy in 2020.

2.2 Level of Detail for Computer Graphics

Level of Detail for Computer Graphics by Luebke et al. [1] is a reference book for the topic of LOD published in 2002. The book builds on top of years of research in the area of LOD and provides an overview to many LOD techniques. For this project, chapter 7 "Terrain Level of Detail" of the book is especially relevant, as it dives into the topic of LOD for terrains specifically. It covers basic approaches and techniques for terrain LOD, common problems that can arise during rendering of terrains and some solutions to them, and a catalog of terrain LOD algorithms.

2.3 Focus on 3D Terrain Programing

Focus on 3D Terrain Programming by Trent Polack [9] is a book on terrain programming published in 2002. Part one of the book introduces the reader to the basics of terrains, such as height maps and texturing. Part two then covers some more advanced topics, including a selection of terrain LOD algorithms. The presented LOD algorithms are ROAM [3], Röttger's quadtree-based algorithm [4], and GeoMipMapping [5]. The book also includes demo source code in C++ and OpenGL.

2.4 Virtual Terrain Project

The Virtual Terrain Project [10] was a project run from 2001 to 2013 that consisted of a collection of software, information and resources on terrain modelling and rendering, including a large overview of publications and implementations related to terrain LOD algorithms.

Terrain LOD in Real-world Systems

3.1 Game Engines

3.1.1 Godot

Godot is a cross-platform game engine written in C#, C++ and its own scripting language GDScript. Terrains are supported in form of extensions developed by community members, which can be installed and used in Godot projects by game developers.

One such extension is Terrain3D by Cory Petkovsek [11] written in C++ for Godot 4. The LOD approach used in this extension is based on geometry clipmaps by Hoppe and Losasso [7]. The concrete implementation of the geometry clipmap mesh code was created by Mike J Savage [12].

Another extension for terrains is Godot Heightmap Plugin by Marc Gilleron [13] written in GDScript and C++. The extension uses a quadtree-based approach for terrain LOD.

3.1.2 Unity

Unity is another cross-platform game engine written in C# and C++, and has a built-in terrain system. The core engine source code of Unity is only accessible by owning an enterprise licence, therefore no information is given on which terrain LOD is used for the built-in terrain in Unity.

Nonetheless, there exists an open-source library for hierarchical LOD in Unity called HLODSystem developed by JangKyu Seo at Unity TODO citation . HLODSystem also supports terrains with its TerrainHLOD component, allowing for conversion from an Unity Terrain object to a HLOD mesh with configurable parameters, such as chunk size and border vertex count. HLODSystem allows the developer to specify the mesh simplifier to be used and currently the only supported simplifier is UnityMeshSimplifier, an open-source mesh simplifier de-

veloped by TODO that utilizes the fast quadratic mesh simplification algorithm developed by TODO citation.

In addition to the mentioned open-source libraries, a terrain LOD approach was published by Jonathan Dupuy at Unity.

3.1.3 Unreal Engine

Unreal Engine is another cross-platform game engine written in C++ and features an integrated terrain system called the Landscape system. The technical documentation of Unreal Engine 5 mentions utilising GeoMipMapping for handling LOD for landscapes [14]. GeoMipMapping is a terrain LOD approach developed in 2000 by de Boer [5].

3.1.4 Frostbite

Frostbite is a closed-source game engine developed by DICE and is known for the *Battlefield* series. During the Game Developers Conference 2012, DICE presented the terrain system of *Battlefield 3*, which was developed with their Frostbite 2 engine. They mention a quadtree-based terrain LOD system and describe several optimizations regarding paging and streaming of terrain. TODO cite.

3.2 Geographic Information Systems

TODO: Check out Google maps, Google Earth, other GIS TODO: Maybe look at flight simulators (if information available)

Algorithms and Approaches for Terrain LOD

4.1 Basics of Terrain LOD

4.1.1 Terrain Data Representation

Heightmaps

One way of representing terrains is using *heightmaps*. A heightmap is a $n \times n$ -grid that contains the height value y for each (x, z)-position¹. Positions are always spaced evenly in a grid-like manner, but the distance between any two neighboring positions is variable.

The main advantage of height maps is that they allow for very simple storage and manipulation of height data, e.g. in form of images, where low color values represent low areas of terrain and vice versa for high color values. For a grayscale image, up to 256 height values can be used and for an RGB image, more than 16 million height values are supported. Looking up a height value for a given (x,z)-position is easy as well, which consists of a simple lookup at the given position in the image. Figure 4.1 shows a 2000 × 2000 height map of the mountain Dom in Valais, Switzerland.

 $^{^1\}mathrm{We}$ always denote y for the up direction except if explicitly stated otherwise.



Figure 4.1: 2000×2000 heightmap of the mountain Dom in Valais, Switzerland retrieved from SwissTopo [15].

Triangulated Irregular Networks

An alternative to the heightmap is the *triangulated irregular network (TIN)* data structure. A TIN consists of a collection of 3D vertices, where the arrangement of vertices can be irregular. Figure 4.2 shows an example of a TIN.

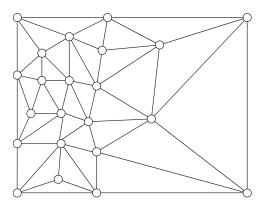


Figure 4.2: Example of a TIN. Note that the left area represents a terrain area with many changes (e.g. mountains, hills, etc.), and the right area represents an area with few changes (e.g. flat areas).

The main advantage of TINs is that fewer polygons need to be used for e.g. smooth terrain areas. Another advantage is that special terrain features can be modelled which are usually difficult to model with heightmaps, such as overhangs, cliffs and caves, The disadvantage of TINs, however, is that the full (x, y, z) coordinates need to be stored, whereas with heightmaps, only the height value y needs to be stored.

4.1.2 Bintrees and Quadtrees

Binary triangle trees (bintrees) and quadtrees are recursive data structures based on triangles and quads respectively. A bintree consists of up to two child triangles, both of which in turn also consist of up to two child triangles each, and so on. Quadtrees are structured similarly, with a quad consisting of up to four child quads, and each child quad consisting of up to four child quads, and so on. Figure 4.3 shows an example of a bintree and a quadtree.

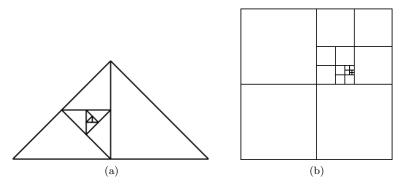


Figure 4.3: Example of a bintree (a) and a quadtree (b).

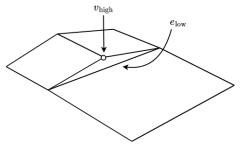
The main advantage of bintrees and quadtrees is that LOD can be modelled very naturally with them. Bintree/quadtree sections with few children correspond to a low LOD and vice versa for bintree/quadtree sections with many children.

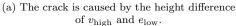
4.1.3 Potential Problems During Terrain Rendering

While terrain LOD algorithms dramatically improve the performance of terrain rendering, there are certain faults that can occur during rendering.

Cracks

Cracks and holes in terrains can appear when a higher LOD terrain section is bordered by a lower LOD terrain section. The main problem is that when a vertex $v_{\rm high}$ of a higher LOD terrain section lies on the edge $e_{\rm low}$ of a lower LOD terrain section and the y coordinate of $v_{\rm high}$ is greater or less than the height of $e_{\rm low}$ at that point, the difference in height causes the crack to appear, as shown in figure 4.4.







(b) The background color is set to red to highlight the cracks.

Figure 4.4: Illustration of a crack (a) and some examples of cracks in a real rendered terrain (b).

Cracks can be solved by either of the following, depending on the capabilities of the LOD approach:

- Removing the vertex in question, cuasing the higher and lower LOD meshes to be connected seamless! (in figure 4.4 vertex v_{high}).
- Inserting an extra vertex at the border edge of the lower LOD mesh [1, p. 194] (in figure 4.4 on top of vertex $v_{\rm high}$). The disadvantage of this is that an extra vertex needs to get created.
- By force splitting the terrain mesh to get a more continuous mesh [1, p. 193].

Popping

The phenomenon of *popping* occurs when the camera is moving and the transition of the terrain's LOD level causes visual pops to appear. Popping decreases the realism of the terrain and should be as minimal as possible. Popping can be reduced by introducing *vertex morphing* [5, 7, 8], i.e. by animating the transition of one LOD level to the next seamlessly through interpolation.

4.2 ROAM

ROAM (short for Real-time Optimally Adapting Meshes) is a terrain LOD algorithm developed by Duchaineau et al. [3] published in 1997. ROAM represents the terrain mesh using bintrees and performs triangle splits and merges for generating and removing detail. The splits and merges happen mainly on the CPU, which makes ROAM a mainly CPU-based approach.

4.2.1 General Idea

The central idea of the algorithm is to use temporal coherence: the mesh from a previous frame \mathbf{T}_{f-1} is used to compute the mesh of the current frame \mathbf{T} , rather than building up the mesh from ground up for each frame. This is done using two priority queues: a split queue \mathcal{Q}_s and a merge queue \mathcal{Q}_m . The split queue contains splittable triangles T and the merge queue contains mergable

triangle pairs (T, T_B) . The elements of the priority queues are ordered by various geometric error metrics, which are explained in the subsection "Error Metrics" of this report. At each frame, the terrain mesh gets split and merged using \mathcal{Q}_s and \mathcal{Q}_m . until either the required size/accuracy is reached or the time runs out. ROAM is designed as a greedy algorithm, meaning it will always performs the most optimal splits/merges for each frame.

4.2.2 Error Metrics

The original ROAM paper mentions various error metrics for the priority queue ordering, which are explained in the following paragraphs.

Wedgies Wedgies are nested bounding volumes around triangles that are computed while building the initial mesh at the beginning of the algorithm. A wedgie is defined to contain the entire x and z extent² of a triangle and the height y including some additional space above and below the highest and lowest points, respectively.

Geometric Screen Distortion Another metric is the distance between where a node is supposed to be on the screen and where the algorithm placed the node. The maximum of all distances is calculated and used as the base priority metric of the algorithm.

4.2.3 Other Optimizations

View-frustum Culling An optimization that is mentioned is view-frustum culling. In each frame, various flags are updated during the recursive traversal of the bintree. These flags indicate whether a wedgie is inside the view-frustum fully, partially, or not at all.

Incremental Triangle Stripping The ROAM paper reports using *incremental triangle stripping* for optimizing the performance of the rendering. This is simply refers to using triangle strips for rendering. which is supported by all major graphics APIs.

4.2.4 Conclusion

The runtime of ROAM is independent of the screen resolution and is proportional to the number of triangle changes per frame.

4.3 GeoMipMapping

Geometrical Mipmapping (GeoMipMapping) is a terrain LOD approach developed by de Boer [5] in the year 2000. It applies the idea of texture mipmapping to terrain rendering.

²The original ROAM paper uses z for the up direction. For the sake of consistency with the rest of this report, we will use y as the up direction here.

4.3.1 General Idea

The central idea of GeoMipMapping is its analogy to texture mipmapping: just like how textures of far away objects are rendered using lower resolution texture mipmaps, terrain areas that are far away from the camera should also be rendered with a lower resolution mesh.

This is achieved by splitting up the terrain into so-called blocks (also called patches) of a fixed width $2^n + 1$ for an arbitrary $n \in \mathbb{N}$. Each block has a LOD level³ $0 \le l \le n$ that changes dynamically at runtime. At load time, every block is computed at every LOD level and subsequently stored, e.g. on an index buffer. Each such representation of a block at a specific LOD level is called a GeoMipMap. For each GeoMipMap, the number of vertices on one side is $2^l + 1$ and the number of quads is 2^{2l} .

For example, the GeoMipMaps of a 5×5 terrain block contain $2^2 + 1 = 5$ vertices on one side at the maximum LOD level 2, $2^1 + 1 = 3$ vertices at LOD level 1 and $2^0 + 1 = 2$ vertices at the minimum LOD level 0. As for the number of quads, at LOD level 2 there are $2^4 = 16$ quads, at LOD level 1 there are $2^2 = 4$ quads and at LOD level 0 there is $2^0 = 1$ quad. Figure 4.5 illustrates the above example.

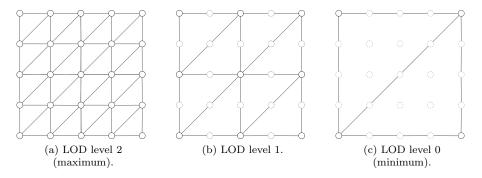


Figure 4.5: Example of each GeoMipMap of a 5×5 block. The omitted vertices of lower LOD GeoMipMaps are marked as dotted circles.

4.3.2 LOD Selection

The LOD for each block is selected at runtime and is based on a

4.3.3 Avoiding Cracks

GeoMipMapping avoids cracks by checking whether the current block has a higher LOD than the bordering block and if this is the case, it omits the vertices that would cause the crack.

In the original GeoMipMapping paper, the vertex omission is performed by rendering the bordering row/column of the current block as triangle fans, as

 $^{^3}$ The original GeoMipMapping paper uses 0 to denote the maximum LOD level and viceversa for the minimum LOD level. In order to avoid any confusion with the term LOD, this report denotes 0 as the minimum LOD level and vice versa for the maximum LOD level.

shown in figure 4.6.

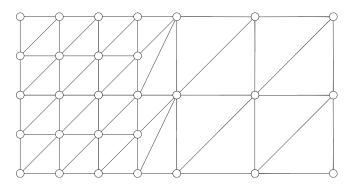


Figure 4.6: Example of GeoMipMapping's crack avoidance between a LOD 2 and a LOD 1 GeoMipMap of two 5×5 blocks as described in the original paper.

An alternative way to render neighboring blocks with different LOD levels is to render the triangle fans from the center point of the 3×3 border subblocks. This approach is somewhat simpler for handling special cases, e.g. when the top and right neighboring blocks have a lower LOD, as shown shown in figure 4.7.

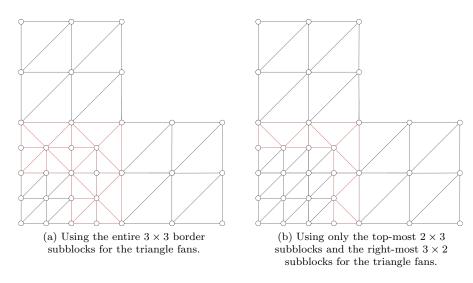


Figure 4.7: Two alternative triangle fan-based methods to avoid cracks between a LOD 2 and two LOD 1 GeoMipMaps of three 5×5 blocks. The border subblocks are marked in red.

Regardless of the rendering approach, a neighborhood structure consisting of the LOD levels of the left, right, top and bottom neighboring blocks needs to be stored per block, so that the algorithm knows how to perform the vertex omission. The LOD levels of each block change continually each frame, which means that the neighborhood structure of each block also gets updated each frame.

4.3.4 Other Optimizations

Vertex Morphing GeoMipMapping can be extended with vertex morphing in order to decrease popping.

View-frustum Culling Blocks that are outside of the view-frustum can be left out completely, thereby dramatically decreasing the number of vertices that need to get rendered. The GeoMipMapping paper mentions using quadtrees to

4.4 Geometry Clipmaps

TODO

ATLOD: A Terrain Level of Detail (Renderer)

This chapter describes ATLOD (short for **A** Terrain Level of **D**etail (Renderer)), the demo terrain rendering application.

5.1 Preliminaries

5.1.1 Used Technologies

ATLOD is written in C++17 and OpenGL 4.2. For compiling build files, CMake (minimum version 3.5) is used. ATLOD uses the following third-party libraries:

- GLM: The *OpenGL Mathematics (GLM)* library provides functionality for the mathematics of graphics programming, such as classes for vectors, matrices and perspective transformations.
- GLEW: The *OpenGL Extension Wranger Library (GLEW)* is an extension loading library for OpenGL.
- GLFW: *GLFW* is a multi-platform library for desktop-based OpenGL applications, offering an API for managing windows, contexts and input handling.
- STB: STB is a collection of header-only libraries developed by Sean Barrett TODO cite. ATLOD uses stb_image.h for loading images of heightmaps and textures.

The source code is hosted on GitHub on the repository AmarTabakovic/3d-terrain-with-lod and is licensed under TODO.

5.1.2 Chosen Algorithms

The chosen algorithms and their reasons for implementing them are the following:

Naive Brute-force Algorithm The naive brute-force algorithm consists of simply reading in all height values from the heightmap as vertices and rendering them directly to the screen. The main reason for implementing the naive brute-force algorithm is to motivate the usage of terrain LOD algorithms by showing the difference in performance compared to the optimized LOD approaches.

GeoMipMapping The main reason for implementing GeoMipMapping is to have at least one CPU-based approach as a reference point for comparison with GPU-based approaches. In addition, GeoMipMapping is considered to be relatively straightforward to implement [9, p. 79].

5.2 Height Data

5.2.1 Data Sources

5.2.2 Supported Formats

The following file formats are supported for loading heightmaps:

- .png and .jpg: Heightmaps can be loaded as PNG and JPG images. This is implemented using stb_image.h.
- .asc: Heightmaps as ASCII grids are supported. Digital elevation data from the Shuttle Radar Topography Mission (SRTM) is delivered in ASCII grid format.
- .xyz: the XYZ format is based on SwissTopo

5.3 Basic Setup and Architecture

5.3.1 Overview

TODO High-level class diagram

- 5.3.2 Shaders
- **5.3.3** Camera
- 5.3.4 Heightmap
- 5.3.5 Terrain

Each terrain LOD algorithm is encapsulated in a class, which inherits from the base terrain class Terrain. The base terrain is structured as shown in listing TODO.

5.4 Naive Brute-force Algorithm

The naive brute-force algorithm, which simply renders every vertex without any LOD considerations, is encapsulated in the class NaiveRenderer.

The method loadBuffers() loads the height data from the heightmap directly into a vertex buffer with the ID terrainVBO and the indices into an index (i.e. element) buffer named terrainEBO. The indices are organized such that they can be rendered as triangle strips with GL_TRIANGLE_STRIPS. Each row is separated using a special marker index named RESTART, which is set to the maximum possible GLuint value and is used for the GL_PRIMITIVE_RESTART mode, allowing for the entire terrain to be rendered in a single glDrawElements() call. This draw call happens every frame in the method render(). Figure 5.1 shows the organization of indices for rendering the terrain as triangle strips.

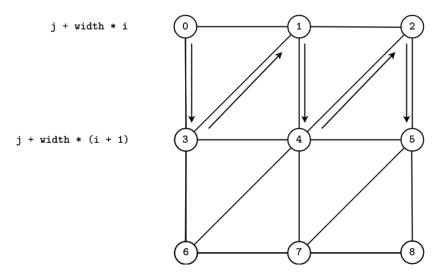


Figure 5.1: Example of a terrain layout for triangle strips. The looping index i goes from 0 to the terrain height and j from 0 to the terrain width. The final indices to be rendered are 0,3,1,4,2,5,RESTART,3,6,4,7,5,8,RESTART.

5.5 GeoMipMapping

ATLOD's GeoMipMapping implementation is encapsulated in the class GeoMipMapping.

5.5.1 Data Structures

5.5.2 Vertex and Index Organisation

Vertices are loaded into the vertex buffer with the method loadBuffers().

5.5.3 Avoiding Pops

Results

6.1 Experimental Setup

For testing out the algorithms, I used a MacBook etc. TODO

Discussion and Conclusion

- 7.1 Further Work
- 7.2 Reflexion

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