

A. Dijkstra shortest path algorithm using Prim's Algorithm in $O(V^2)$:

Dijkstra's algorithm is very similar to [Prim's algorithm for minimum spanning tree](#).

Like Prim's MST, generate a SPT (shortest path tree) with a given source as a root. Maintain two sets, one set contains vertices included in the shortest-path tree, other set includes vertices not yet included in the shortest-path tree. At every step of the algorithm, find a vertex that is in the other set (set not yet included) and has a minimum distance from the source.

Follow the steps below to solve the problem:

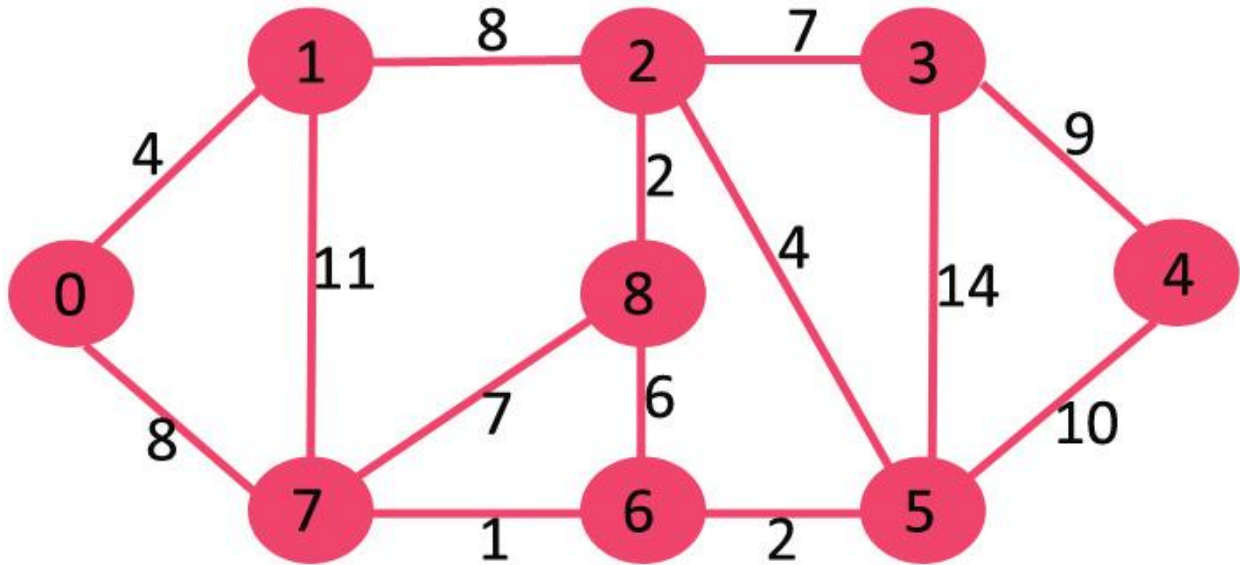
- Create a set **sptSet** (shortest path tree set) that keeps track of vertices included in the shortest path tree, i.e., whose minimum distance from the source is calculated and finalized. Initially, this set is empty.
- Assign a distance value to all vertices in the input graph. Initialize all distance values as **INFINITE**. Assign the distance value as 0 for the source vertex so that it is picked first.
- While **sptSet** doesn't include all vertices
 - Pick a vertex **u** that is not there in **sptSet** and has a minimum distance value.
 - Include **u** to **sptSet**.
 - Then update the distance value of all adjacent vertices of **u**.
 - To update the distance values, iterate through all adjacent vertices.
 - For every adjacent vertex **v**, if the sum of the distance value of **u** (from source) and weight of edge **u-v**, is less than the distance value of **v**, then update the distance value of **v**.

Note: We use a boolean array **sptSet[]** to represent the set of vertices included in SPT. If a value **sptSet[v]** is true, then vertex **v** is included in SPT, otherwise not. Array **dist[]** is used to store the shortest distance values of all vertices.

Below is the illustration of the above approach:

Illustration:

To understand the Dijkstra's Algorithm lets take a graph and find the shortest path from source to all nodes.
Consider below graph and **src = 0**



Step 1:

- The set **sptSet** is initially empty and distances assigned to vertices are $\{0, \text{INF}, \text{INF}, \text{INF}, \text{INF}, \text{INF}, \text{INF}, \text{INF}\}$ where **INF** indicates infinite.
- Now pick the vertex with a minimum distance value. The vertex 0 is picked, include it in sptSet. So sptSet becomes $\{0\}$. After including 0 to sptSet, update di