## Formatting instructions for NIPS 2018

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## **Abstract**

- The abstract paragraph should be indented ½ inch (3 picas) on both the left- and right-hand margins. Use 10 point type, with a vertical spacing (leading) of 11 points. The word **Abstract** must be centered, bold, and in point size 12. Two line spaces precede the abstract. The abstract must be limited to one paragraph.
- 5 1 Introduction
- 6 2 Background

## 7 2.1 Markov Decision Processes

- We define a Markov decision process (MDP) as a tuple  $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}, \mathcal{R}, p_0, \gamma \rangle$ , where  $\mathcal{S}$  is the state-space, A is a finite set of actions,  $\mathcal{P}(\cdot|s,a)$  is the distribution of the next state s' given that action a is taken in state s,  $\mathcal{R}: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$  is the reward function,  $p_0$  is the initial-state 10 distribution, and  $\gamma \in [0,1)$  is the discount factor. We assume the reward function to be uniformly bounded by a constant  $R_{max} > 0$ . A deterministic policy  $\pi : \mathcal{S} \to \mathcal{A}$  is a mapping from states to actions. At the beginning of each episode of interaction, the initial state  $s_0$  is drawn from  $p_0$ . 13 Then, the agent takes the action  $a_0 = \pi(s_0)$ , receives a reward  $\mathcal{R}(s_0, a_0)$ , transitions to the next 14 state  $s_1 \sim \mathcal{P}(\cdot|s_0, a_0)$ , and the process is repeated. The goal is to find the policy maximizing the 15 long-term return over a possibly infinite horizon:  $\max_{\pi} J(\pi) \triangleq \mathbb{E}[\sum_{t=0}^{\infty} \gamma^t r_t \mid \mathcal{M}, \pi]$ . To this end, 17 we define the optimal value function  $Q^*(s,a)$  as the expected return obtained by taking action a in state s and following an optimal policy thereafter. Then, an optimal policy  $\pi^*$  is a policy that 18 is greedy with respect to the optimal value function, i.e.,  $\pi^*(s) = \operatorname{argmax}_a Q^*(s, a)$  for all states 19 s. It can be shown (e.g., [1]) that  $Q^*$  is the unique fixed-point of the optimal Bellman operator T20 defined by  $TQ(s, a) = \mathcal{R}(s, a) + \gamma \mathbb{E}_{\mathcal{P}}[\max_{a'} Q(s', a')]$  for any value function Q. From now on, we 21 adopt the term Q-function to denote any plausible value function, i.e., any function  $Q: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$ 22 uniformly bounded by  $\frac{R_{max}}{1-\gamma}$ . 23
- We define the Bellman residual of a Q-function Q as  $B(Q) \triangleq TQ Q$ . Notice that a Q-function Q is optimal if, and only if, B(Q)(s,a) = 0 for all s,a. Furthermore, if we assume the existence of a distribution  $\mu$  over  $\mathcal{S} \times \mathcal{A}$ , the expected Bellman error of Q is defined as the expected Bellman residual of Q under  $\mu$ .

- 28 2.2 Variational Inference
- 29 3 Variational Transfer Learning
- 30 3.1 Algorithm
- 3.2 Gaussian Variational Transfer
- 32 3.3 Mixture of Gaussian Variational Transfer
- 33 4 Related Works
- 5 Experiments
- 35 5.1 Gridworld
- 36 5.2 Classic Control
- 37 5.3 Maze Navigation
- 6 Conclusion
- 39 References
- 40 [1] Martin L. Puterman. Markov Decision Processes: Discrete Stochastic Dynamic Programming. John Wiley
  41 & Sons, Inc., New York, NY, USA, 1994.