GuessTuples Project

Andrew J. Wren

28 April 2021

Abstract

Notes on GuessTuples project

1 Configuring the nets

1.1 Alice

One per bit. The input array to guess is $\mathbf{x} = (x_j)_{j=0,...,N_{\text{elements}}}$. There should be N_{code} outputs taking values $\mathbf{y} = (y_j)_{j=0,...,N_{\text{code}}}$.

Normalise all the rewards so that for each bit j, $r_{j,\prime} + (N_{\rm code} - 1) r_{j,\prime} = 0$. In other words

$$r_{jk} \leftarrow r_{jk} - \frac{r_{j\prime} + (N_{\text{code}} - 1) \, r_{j\prime}}{N_{\text{code}}}.\tag{1}$$

The Q estimate is then taken to be

$$Q(\mathbf{x}) = \sum_{j} b_{j} y_{j} \equiv \sum_{j} |y_{j}|, \qquad (2)$$

where

$$b_j = \operatorname{sgn}(y_j) \tag{3}$$

is the prediction for the machine value of the *j*th bit. The loss function is

$$L = |Q(\mathbf{x}) - r|^2. \tag{4}$$

Alternative approaches include:

- 1. Two outputs for each bit showing the reward for each of 0 and 1. May reflect negative rewards better?
- 2. Combine the rewards from the bits (with either one or two outputs per bit) by something other than addition e.g. multiplication or via an NN. *The NN option seems quite interesting. Interesting to use* pytorch's *gradients for that.*
- 3. **One per code.** One output for each possible code. *Might work but* $2^{N_{code}}$ *is quite large... not impossibly so if* $N_{code} = 8$.

- 4. Inspired by Ref. [1], feed x into Alice's 'first' net, to get output y, and all possible codes c into her 'second' net, both net's having the same target dimensionality (a hyperparameter). Then the code to use is the one c(x) closest to the output of the first net, with the Q being given by the inner product $Q = \langle y, c(x) \rangle$. Ref. [2] might provide an alternative, actor–critic, approach on a similar theme. The main case above is, in effect, an embedding of x into the target space (of dimensionality N_{code}) which then compares with the natural embedding of c by, in effect, the inner product.
- 5. Ref. [3] suggest sequentialising, which points to a variant of our main approach which does each bit in succession and feeding those results into successive Alice–nets so the Q-estimate for later bits takes account of earlier bits / estimates, with the $N_{\rm code}$ th estimate providing a final code c and Q-estimate for that code.
- 6. Move away from typical Q-learning. Instead Alice's output is the code c and then when Bob makes his choice x_{pred} (see below) run that choice through a copy of Alice, to get c_{Bob} and then the loss function is

$$L = -r(\boldsymbol{c}, \boldsymbol{c}_{\text{Bob}}). \tag{5}$$

1.2 **Bob**

One per bit aka Simple. Bob receives a matrix, $\mathbf{X} = (X_i) = (X_{ij})$ for $0 \le i < N_{\text{select}}$, $0 \le j < N_{\text{elements}}$, and a code $\mathbf{c} = (c_k)_{k=0,\dots,N_{\text{code}}}$. Why not makes his outputs be Q-estimates $\mathbf{z} = (z_i)_{i=0,\dots,N_{\text{select}}}$. Bob's prediction is then $\mathbf{x}_{\text{pred}} = \mathbf{X}_{i_{\text{pred}}}$ where

$$i_{\text{pred}} = \operatorname{argmax}_{i}(z_{i}).$$
 (6)

The loss function is

$$L = \left| z_{i_{\text{pred}}} - r \right|^2. \tag{7}$$

How do we enforce covariance with respect to the order of (X_i) ?

- 1. Covariance will occur naturally and quickly without any specific intervention. *To be determined*.
- 2. Covariance can be enforced through choosing a set $\{\sigma\}\subseteq S_{n_{\text{code}}}$, which could be generated element—by—element by composing randomly—selected basis transpositions $(j \ j+1)$, and then adding to the loss a term

$$\mu \sum_{\sigma} \left| z - \sigma^{-1} \left[z(\sigma[\mathbf{X}]) \right] \right|^2 \tag{8}$$

for some fixed hyperparameter $\mu > 0$. Note this the term is still run backward through the original $x \mapsto z$ net configuration only. How effective would that be? How big does $\{\sigma\}$ have to be? And how much time would the permutation and the additions forward passes cost?

- 3. Enforce covariance via direct identification of weights in Bob's net. *How?*
- 4. Something related to set transformers. ?
- 5. Adopt a different basic set—up where each (X_i) is fed through the net separately, alongside the code c, resulting in a Q-estimate z_i . Then find the loss function as in Eq. 7. Seems the most straightforward?

None of these quite amount to Bob seeks to reproduce the Alice's code vocabulary. However Bob could additionally set up a net in the same basic configuration as Alice's (he doesn't know the weights of course) and train *that* net jointly with his main net.

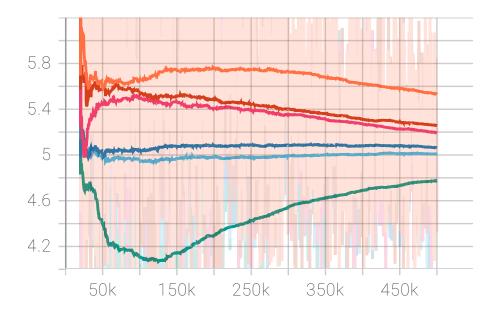


Figure 1: The best results — from /runs/Apr27_23-01-58_andrew-XPS-15-9570. The lines show the square root of the mean square losses with (a) lr=0.3 Alice (orange), Bob (dark blue); (b) lr=0.1 Alice (brick red), Bob (cyan); (c) lr=0.01 Alice (pink), Bob (green). The plot is from TensorFlow and uses smoothing of 0.999.

2 Results

2.1 Original strategies

Figure 1 is representative of the better results for the original strategies, **one per bit** — in other words, not very good. Increasing from h.GAMESIZE = 1 to h.GAMESIZE = 32 gives no better results.

References

- [1] J. He, J. Chen, X. He, J. Gao, L. Li, L. Deng et al., *Deep reinforcement learning with a natural language action space*, arXiv preprint arXiv:1511.04636 (2015).
- [2] G. Dulac-Arnold, R. Evans, H. van Hasselt, P. Sunehag, T. Lillicrap, J. Hunt et al., *Deep reinforcement learning in large discrete action spaces*, arXiv preprint arXiv:1512.07679 (2015).
- [3] S. J. Majeed and M. Hutter, Exact reduction of huge action spaces in general reinforcement learning, arXiv preprint arXiv:2012.10200 (2020).

¹The plot is taken from TensorBoard which gives an .svg file, then converted to .pdf by rsvg-convert -f pdf -o <fig-file-name>.pdf "Sqrt losses.svg".