

```

Colourings[MDT[], m_Integer] :=
Length /@ (Sort[Length /@
              (List @@ PermutationCycles@#) [[1]] &
            // GroupBy[Permutations@Range@m, #] &
            // Values]);

Colourings[k_MDT, m_Integer] :=
Colourings[k, m] =
Block[{e = EdgeSequence@k, s,
       v, w = List @@@ List @@ ToPD@k},
  s = SortBy[If[Order[Position[Join @@ e, #[[1]],
                          Position[Join @@ e, #[[3]]] == 1,
                          #, Reverse@#] & /@
              (w /. (Max@# -> Min@# & /@
                    w[[;;, {3, 5}])][[;;, 2 ;; 4]],
              Max@Table[Position[Join @@ e, #[[j]],
                              {j, 2}]] &];
  (*In s, the third values are to be
   derived from the first two.*)
  Total /@ Table[If[ValidColouring[
                    w, e[[1]], s, g], 1, 0],
                {p, (Length /@ (List @@
                                PermutationCycles@#) [[1]]
                                // Sort) &
                // GroupBy[Permutations@Range@m, #] &
                // Values}],
                {g, Tuples[p, Length@e[[1]]]}];

```