

```
Colourings[MD[], m_Integer] :=
```

```
Length /@ (Sort[Length /@ (List @@ PermutationCycles@#) [[1]] & //  
    GroupBy[Permutations@Range@m, #] & // Values);
```

```
Colourings[k_MD, m_Integer] := Colourings[k, m] =
```

```
Block[{e = EdgeSequence@k, s, v, w = List @@@ List @@ ToPD@k}, s = SortBy[  
    If[Order[Position[Join @@ e, #[[1]], Position[Join @@ e, #[[3]]] == 1, #, Reverse@#] & /@  
        (w //. (Max@# → Min@# & /@ w[[;;, {3, 5}]])) [[;;, 2 ;; 4],  
    Max@Table[Position[Join @@ e, #[[j]], {j, 2}] &];  
(*In s, the third values are to be derived from the first two.*)  
Total /@ Table[If[ValidColouring[w, e[[1]], s, g], 1, 0],  
    {p, (Length /@ (List @@ PermutationCycles@#) [[1]] // Sort) & //  
        GroupBy[Permutations@Range@m, #] & // Values}, {g, Tuples[p, Length@e[[1]]] }]];
```