```
\mathtt{ToPD@k\_MD}:=\mathtt{ToPD@k}=\mathtt{Block}ig[\{\mathtt{a}=\mathtt{Abs}/\mathtt{@k},\mathtt{n}=\mathtt{Length@k},\mathtt{o},\mathtt{r}\}, o = Ordering@a;
     Do[If[PlanarGraphQ@
                     Graph [Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\}\} \bigcup Join@@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, 3\}\}\} \bigcup Join@Table [Array[\{v, \#-1\} \leftrightarrow \{v, \#\} \&, 3] \bigcup \{\{v, 0\} \leftrightarrow \{v, \#\} \&, 3\}\}
                                               \left(\left\{\left\{v, \#[1]\right\}\right\} \leftrightarrow \left\{\#[2], \#[1]\right\} + \left(1 - c[v] c[\#[2]]\right) / 2\right\}, \left\{v, 3 - \#[1]\right\} \leftrightarrow \left\{\#[2], \#[1]\right\} + \left(1 - c[v] c[\#[2]]\right) / 2\right\}
                                                                                  (1+c[v]c[\#[2]])/2 & /@ (\{\#,o[Mod[v-\#/2,n,1]]\} & /@ {0,2})),
                                    \{v, n\}], (*The crossing assignment c is a valid assignment.*)r = c;
                Break[]], {c, Tuples[{1, -1}, n]}];
      PD @@ (X<sub>##</sub> & @@@ Array[{2 # - 1, 2 a [#]], 2 #, Mod[2 a [#]] + 1, 2 n, 1]}[
                                         If[Sign@k[#] == 1, ;; , {2, 3, 4, 1}]][If[r[#] == 1, ;; , {1, 4, 3, 2}]] &, n])];
```